



Theory of Multilayer Coating for proof-of-concept experiments

KEK  High Energy Accelerator Research Organization, Tsukuba, Japan

KUBO, Takayuki

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毅幸

<http://researchmap.jp/kubotaka/>

This work was supported by Japan Society for the Promotion of Science KAKENHI:

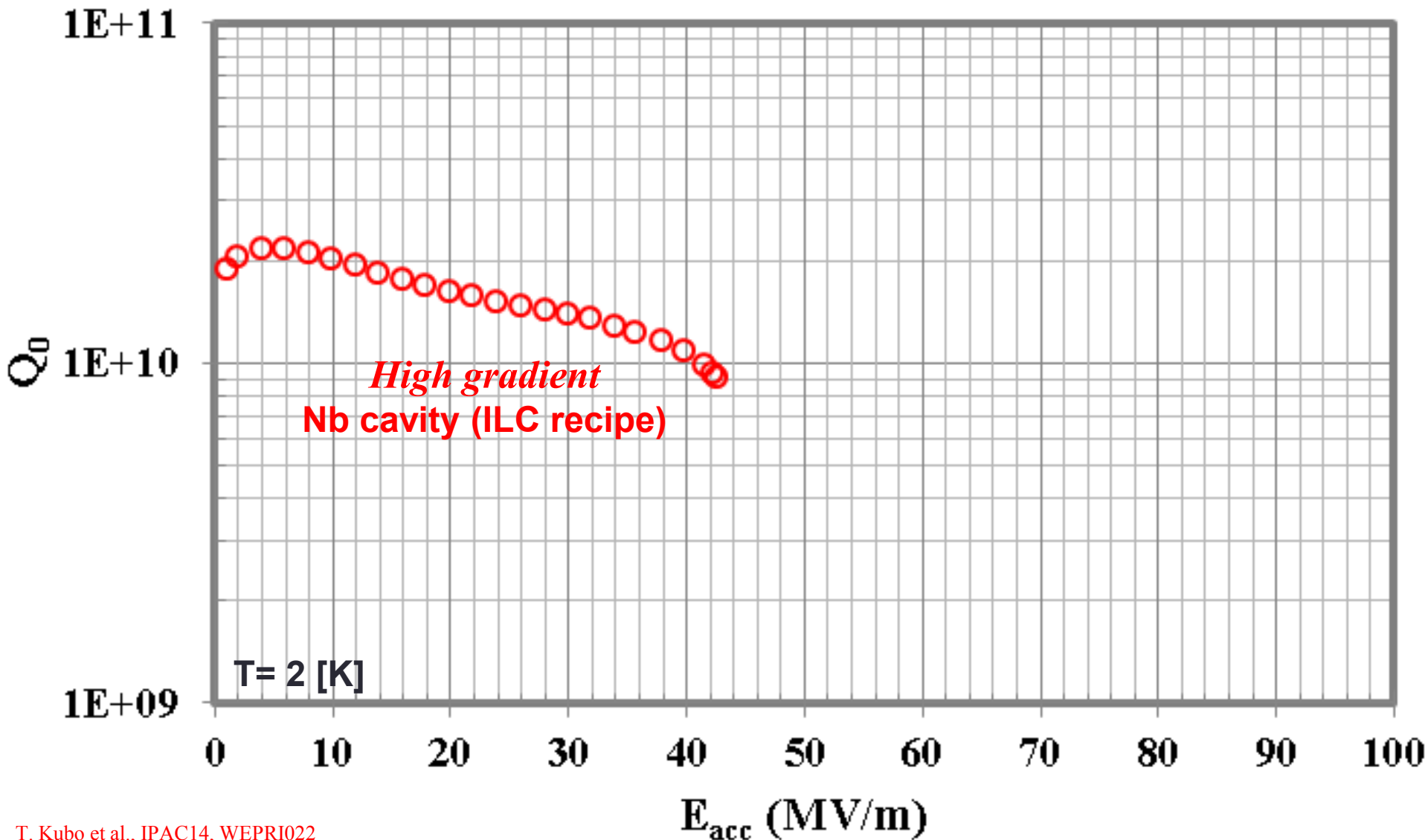
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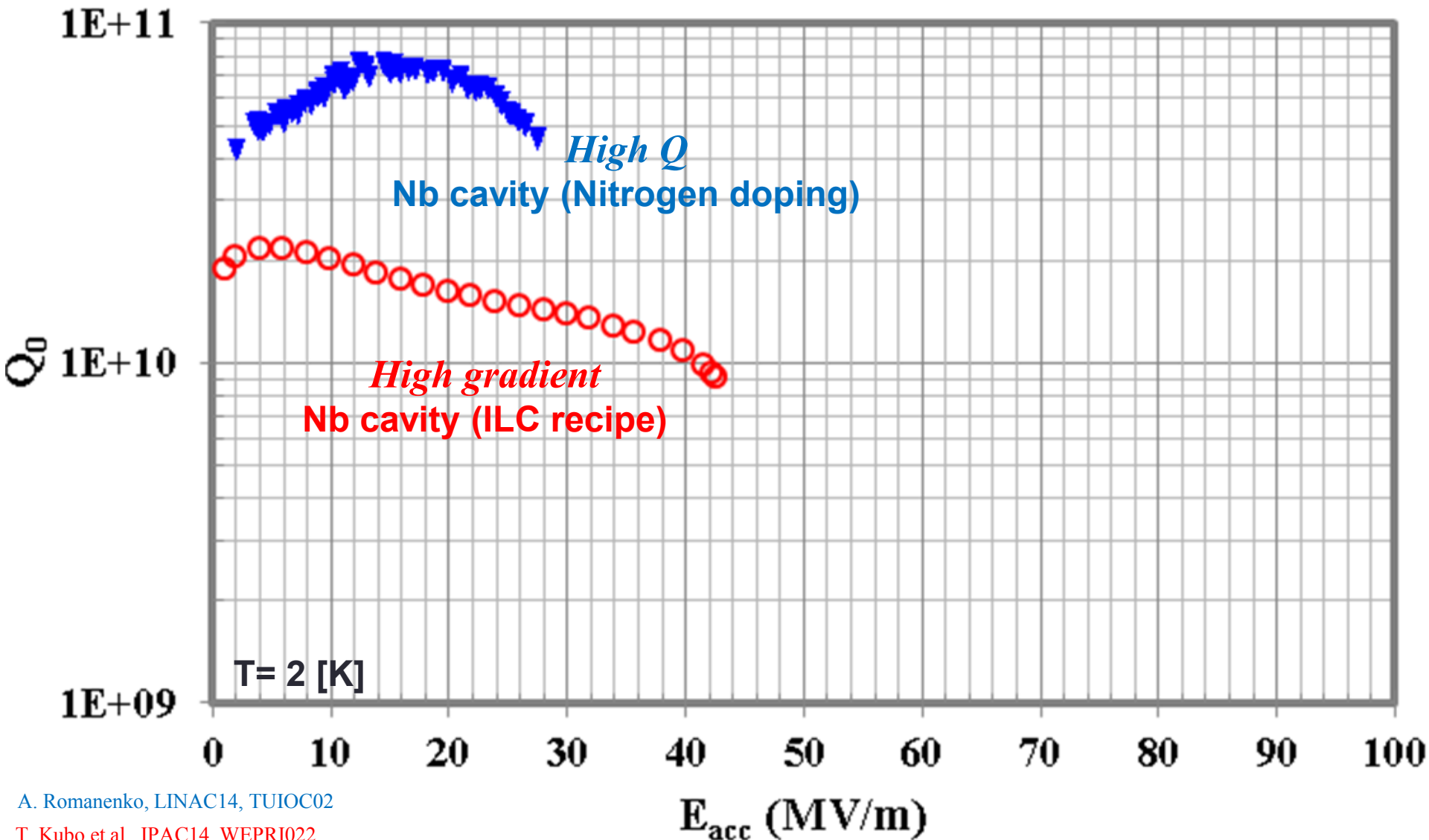


Nb cavity processed by the ILC recipe

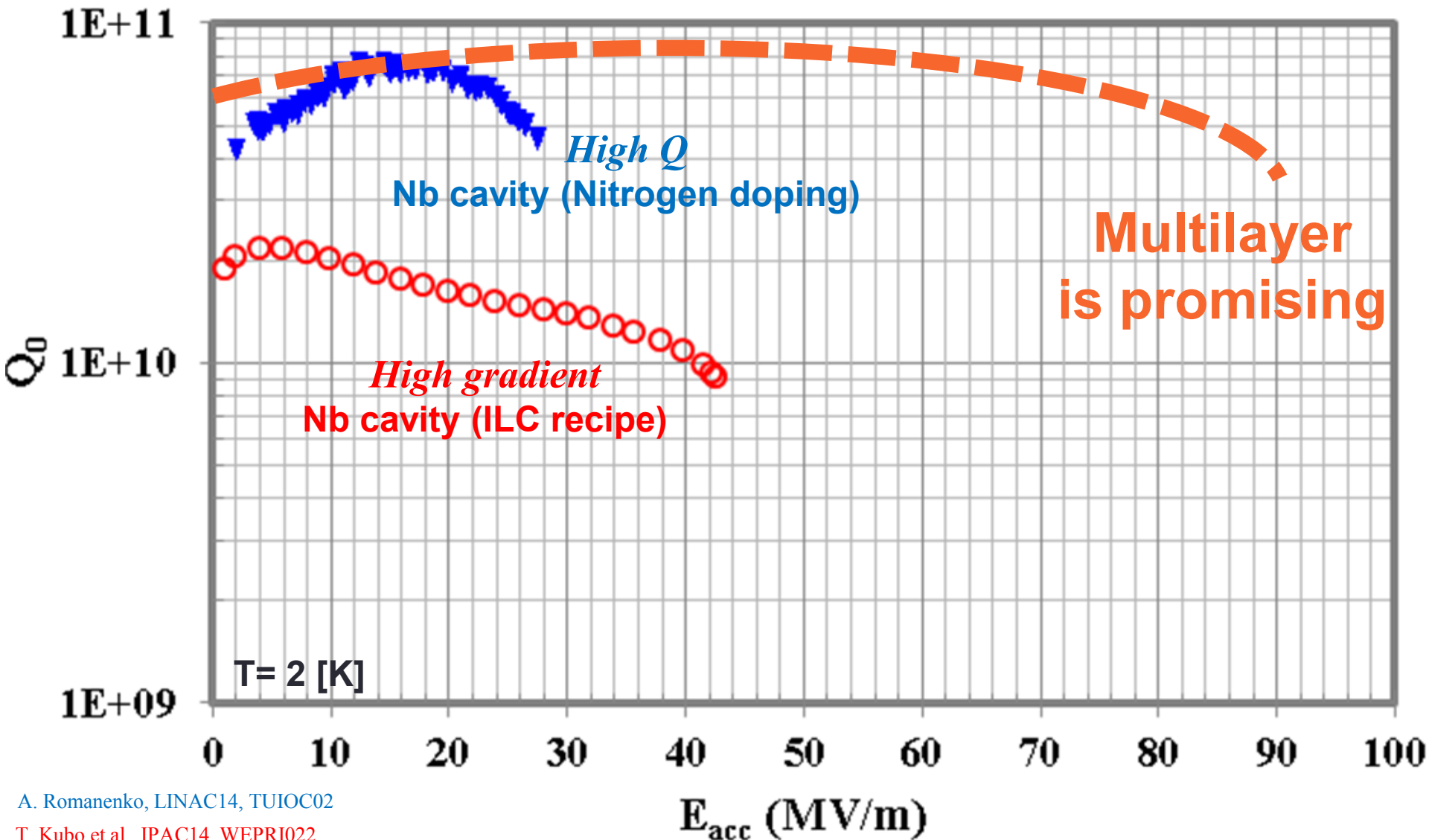


Breakthrough by the nitrogen doping

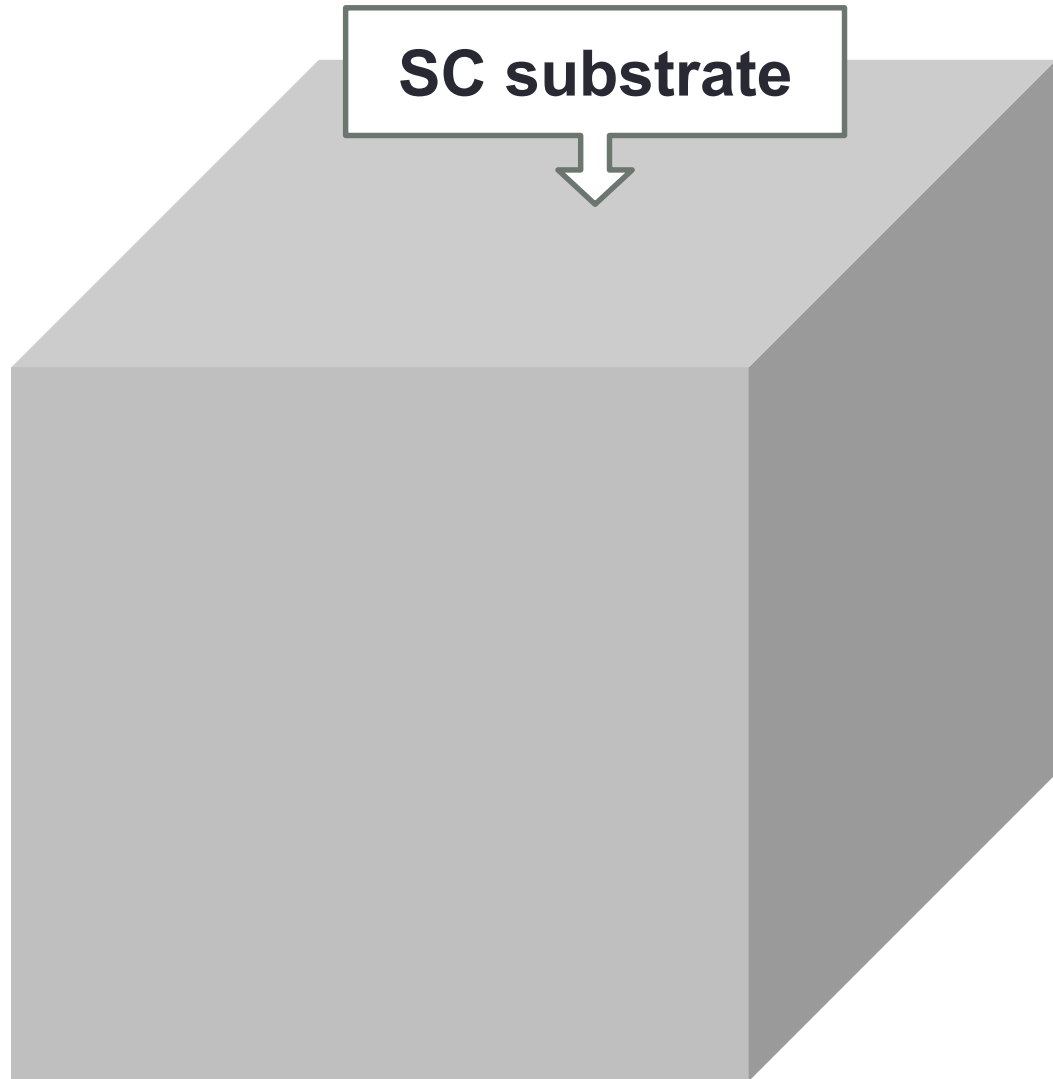
A. Grassellino et al, Supercond. Sci. Technol. **26**, 102001 (2013)



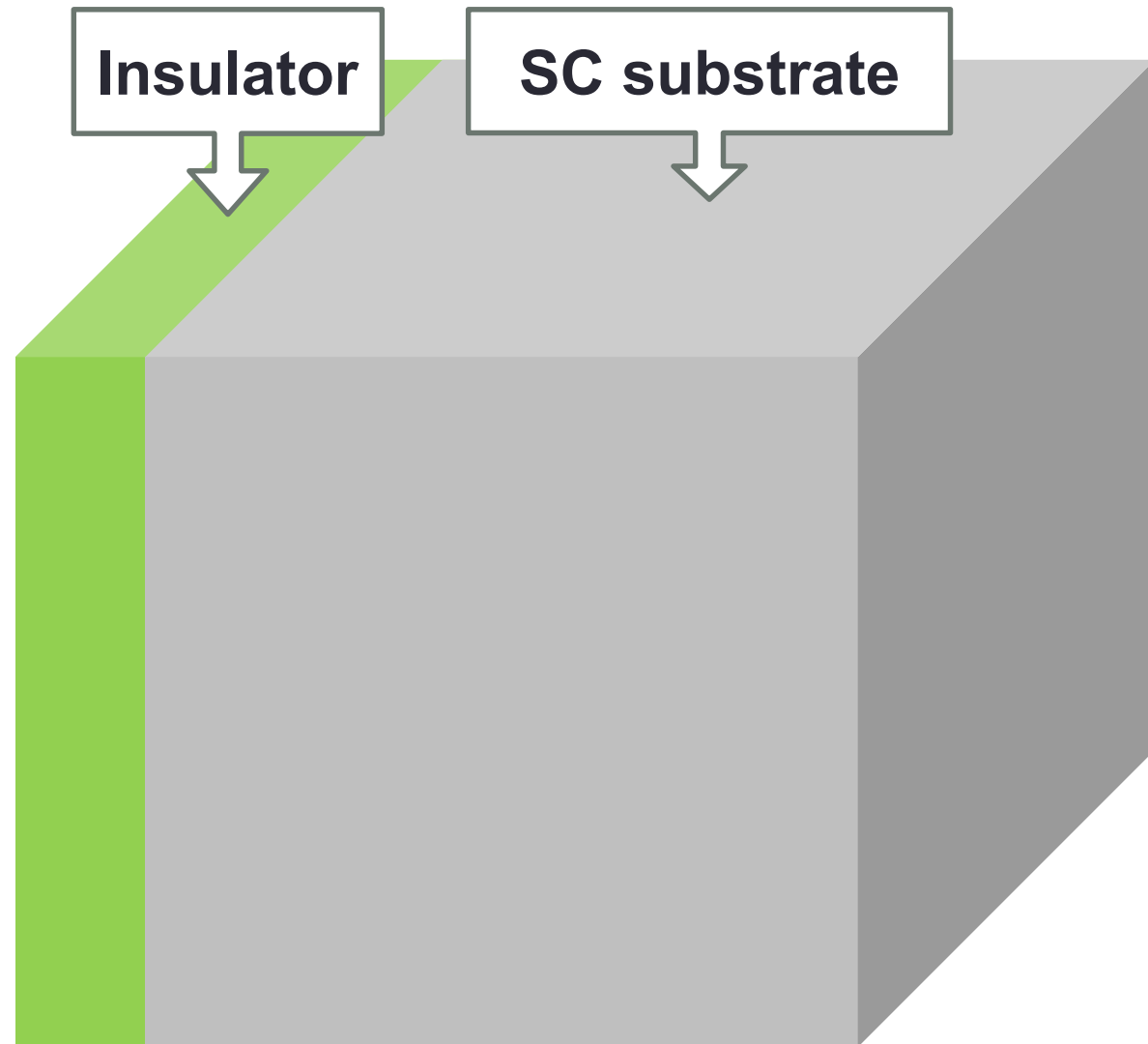
We want to go beyond Nb!



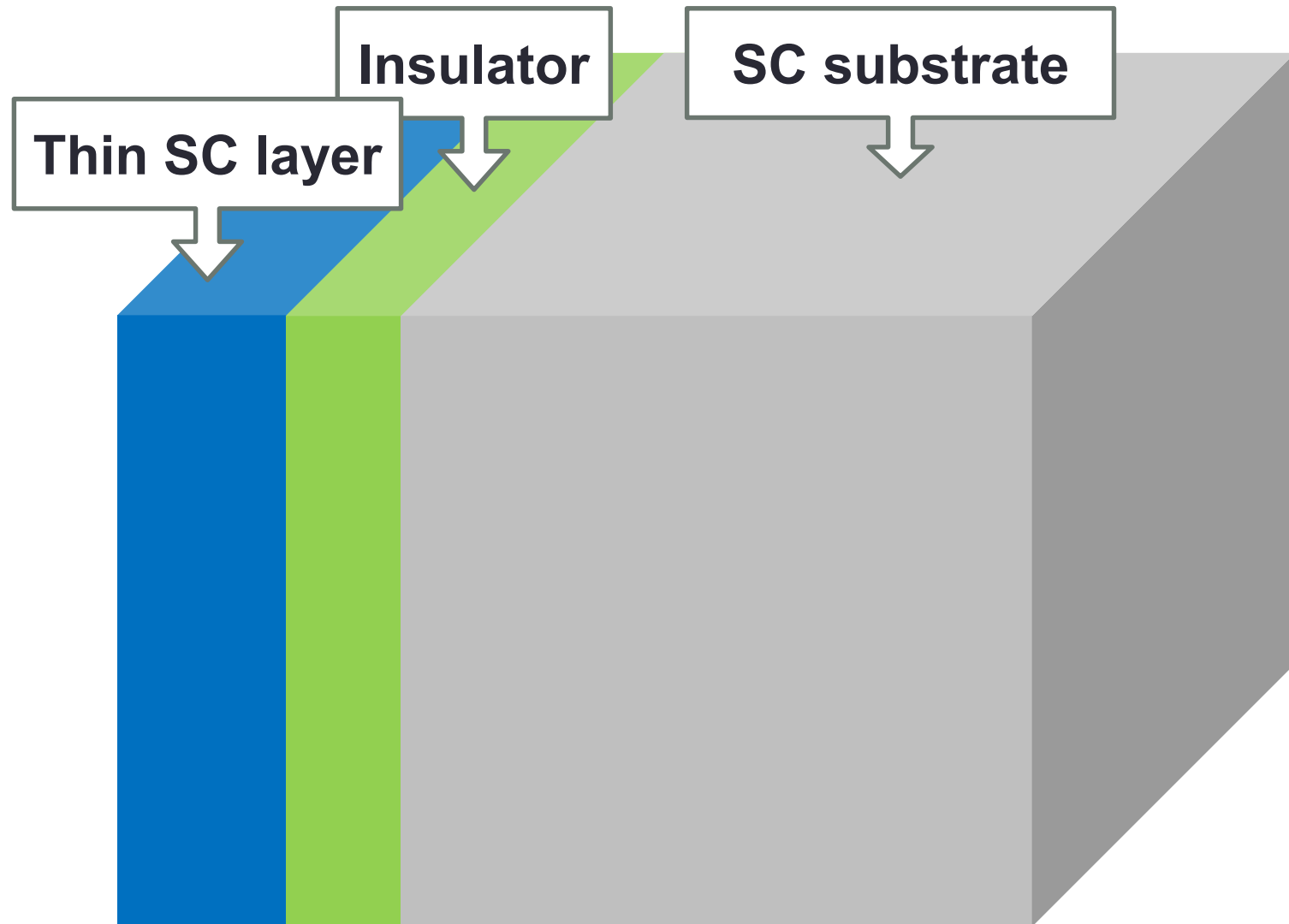
The multilayer coating was proposed by A. Gurevich, [Appl. Phys. Lett. 88, 012511 \(2006\)](#)



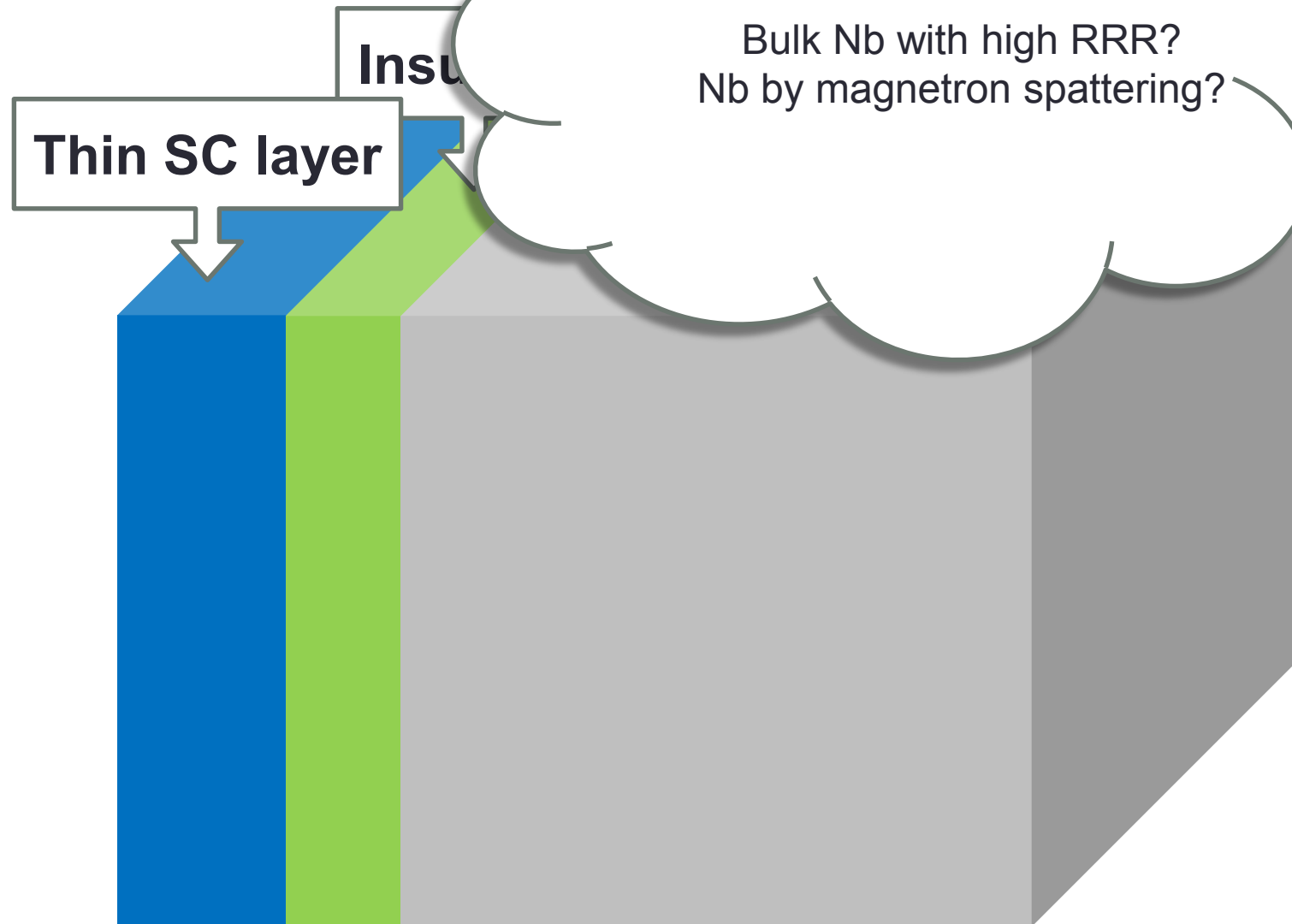
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The multilayer coating is proposed by A



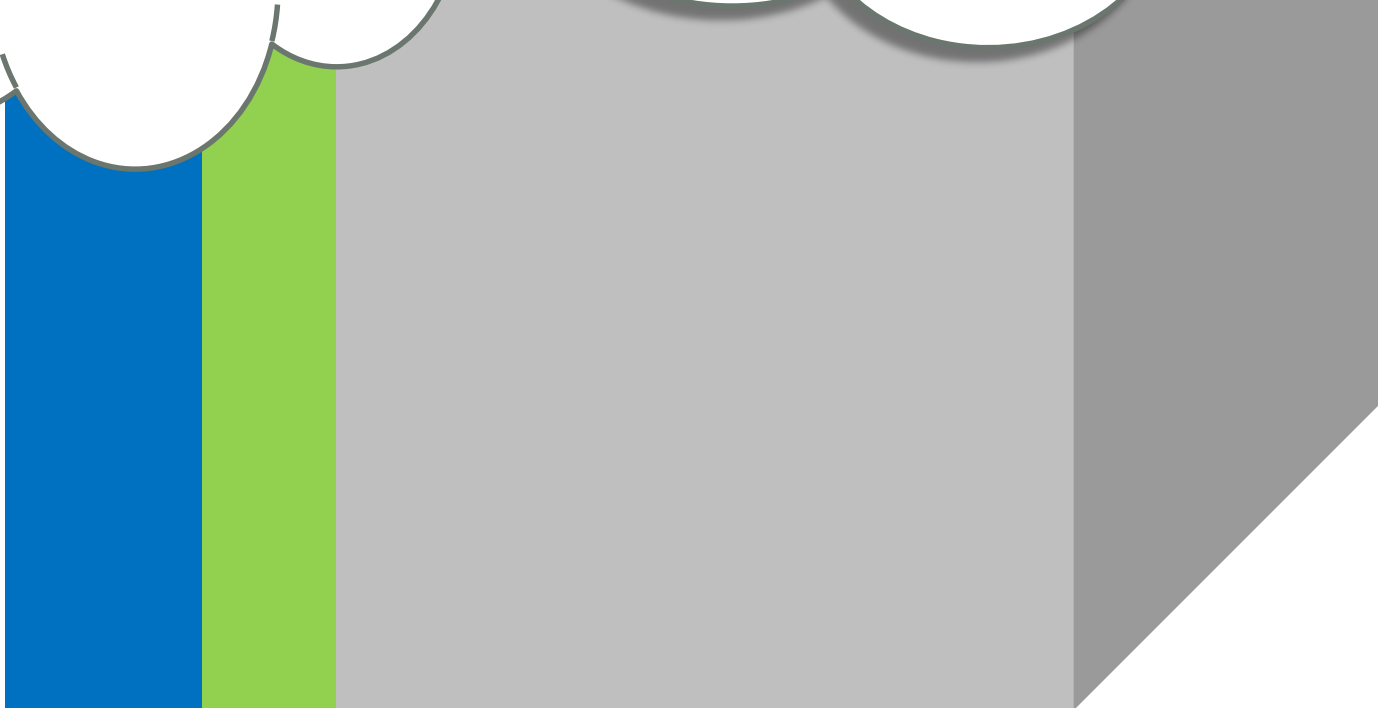
The r

**How to fix
insulator
thickness d_I ?**

10nm?
100nm?

Substrate Material?

Bulk Nb with high RRR?
Nb by magnetron sputtering?



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**How to fix
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Substrate Material?

Bulk Nb with high RRR?
Nb by magnetron sputtering?

**How to fix S layer
thickness d_S ?**

10nm?
100nm?



§ 1

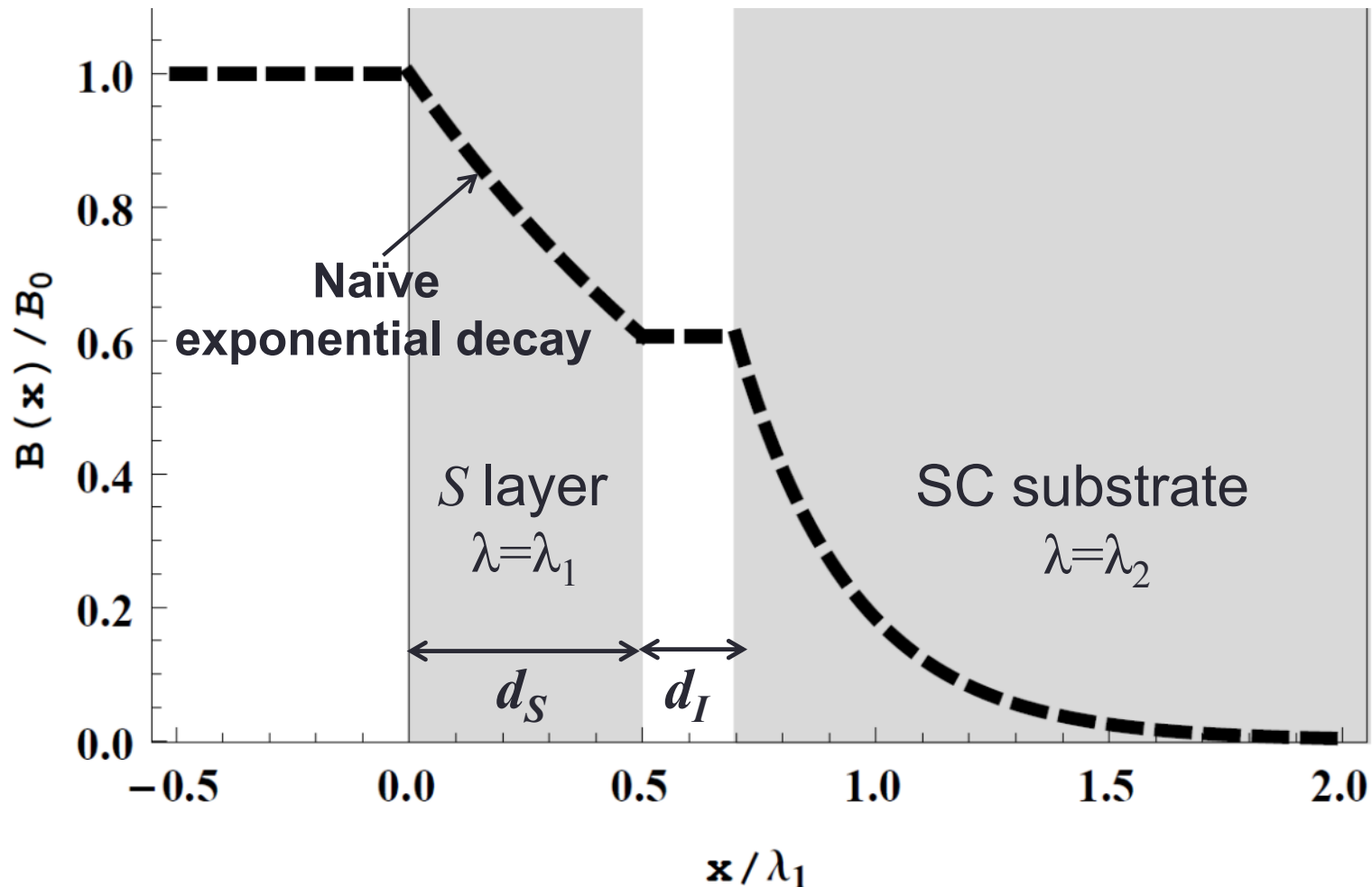
The optimum parameters

1. The magnetic field distribution (and thus the screening current distribution $\mathbf{J} \propto d\mathbf{B}/d\mathbf{x}$) in the S layer is different from the naïve exponential decay.
2. When d_S and d_I are thin enough and $\lambda_1 > \lambda_2$, the screening current in the S layer is suppressed, and the surface field can exceed the superheating field of the S layer.
3. However, an extremely thin d_S can not protect the SC substrate. Thus the S layer must have some thickness to decay the magnetic field and protect the SC substrate. The optimum thickness of d_S exists.

1. **T. Kubo** et al., Appl. Phys. Lett. **104**, 032603 (2014) [submitted to arXiv on April 2013; published on January 2014]
2. **S. Posen** et al., in proceedings of SRF2013, p. 788, WEIOC04 [Sep.2013].
3. **A. Gurevich**, AIP Advances **5**, 017112 (2015) [submitted on Sep.2014; published on Jan.2015]
4. **S. Posen** et al., arXiv:1506.08428v1 [June 2015].

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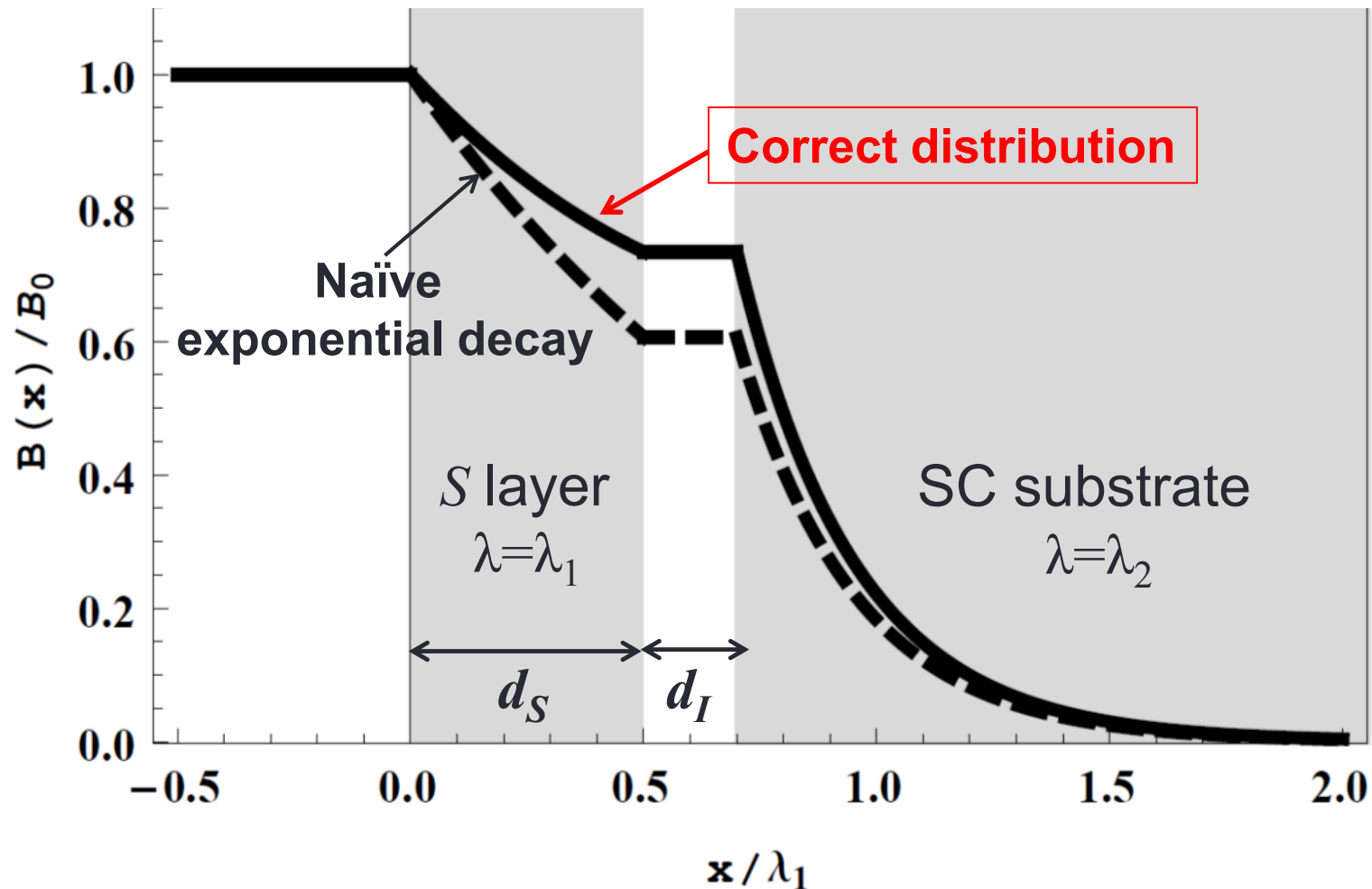
T. Kubo, Y. Iwashita, and T. Saeki, [Appl. Phys. Lett. 104, 032603 \(2014\)](#)

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The derivation processes are explained in detail in [proceedings of IPAC13, p. 2343, WEPWO014](#) [May 2013]

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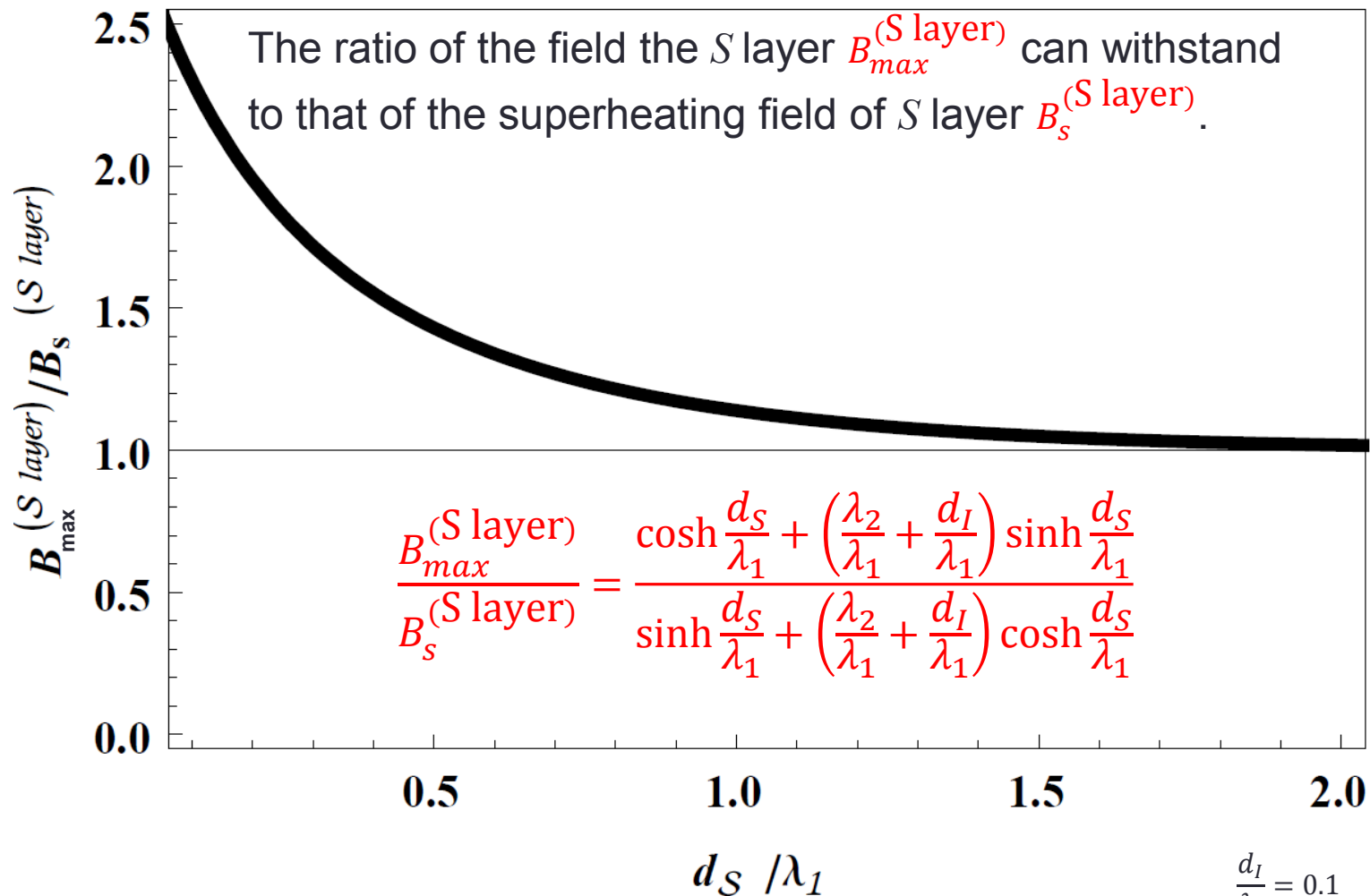


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2. When d_S and d_I are thin enough and $\lambda_1 > \lambda_2$, the screening current in the S layer is suppressed, and the surface field can exceed superheating field of the S layer.



$$\frac{d_I}{\lambda_1} = 0.1 \quad \frac{\lambda_2}{\lambda_1} = 0.25$$

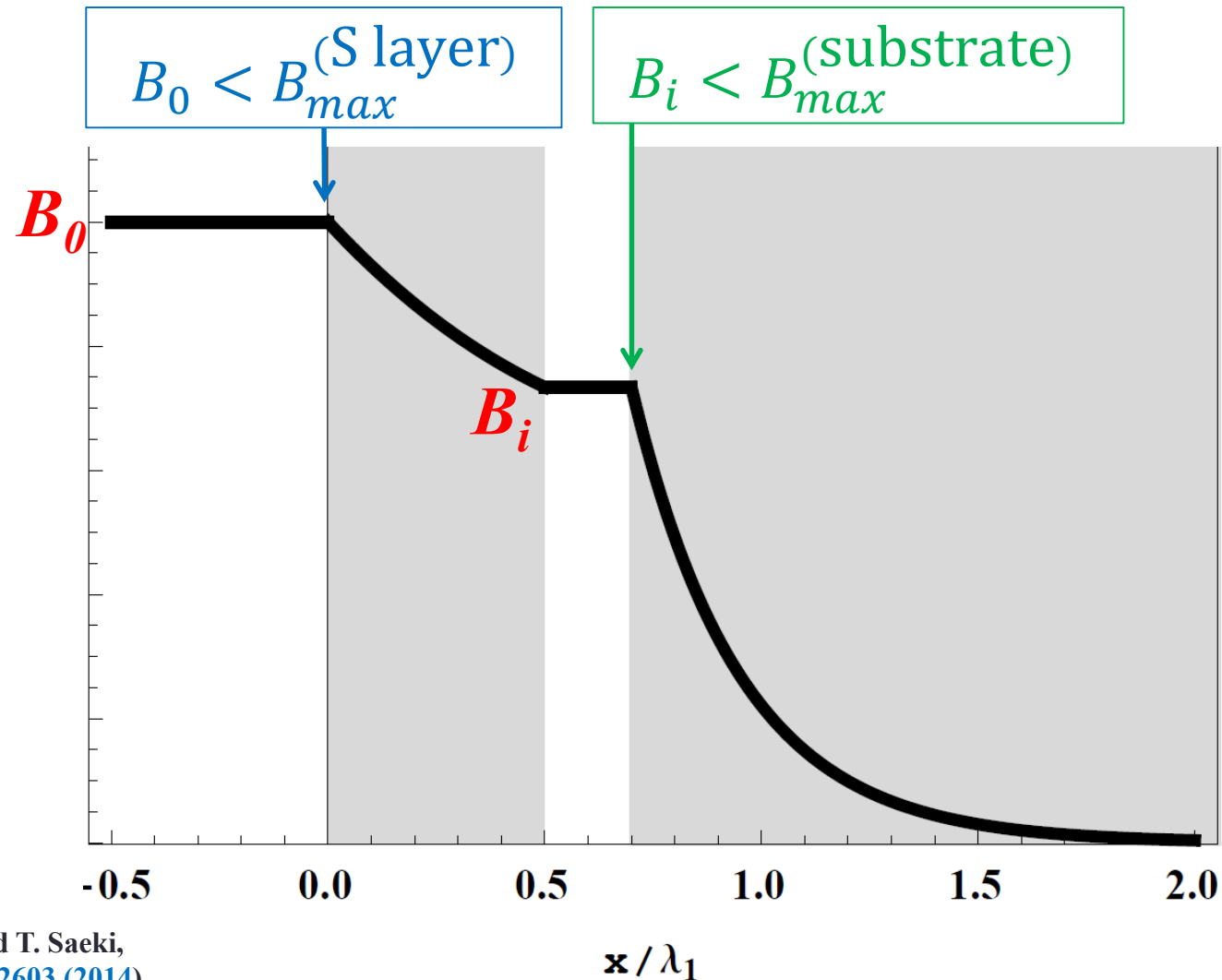
are assumed here.

T. Kubo, Y. Iwashita, and T. Saeki, [Appl. Phys. Lett. 104, 032603 \(2014\)](#)

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3. However, an extremely thin d_s can not protect the SC substrate. Thus **the S layer must have some thickness to decay the magnetic field** and protect the SC substrate.



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Formula for the maximum screening field of the multilayer

$$B_{\max}^{(\text{multilayer})} = \begin{cases} B_{\max}^{(\text{S layer})} & (\text{if } \gamma B_{\max}^{(\text{S layer})} < B_{\max}^{(\text{substrate})}) \\ \gamma^{-1} \times B_{\max}^{(\text{substrate})} & (\text{if } \gamma B_{\max}^{(\text{S layer})} \geq B_{\max}^{(\text{substrate})}) \end{cases}$$

where

$$\left\{ \begin{array}{l} B_{\max}^{(\text{S layer})} = B_s^{(\text{S layer})} \frac{\cosh \frac{d_S}{\lambda_1} + \left(\frac{\lambda_2}{\lambda_1} + \frac{d_I}{\lambda_1} \right) \sinh \frac{d_S}{\lambda_1}}{\sinh \frac{d_S}{\lambda_1} + \left(\frac{\lambda_2}{\lambda_1} + \frac{d_I}{\lambda_1} \right) \cosh \frac{d_S}{\lambda_1}} \quad B_s^{(\text{S layer})} = 0.84 B_c^{(\text{S layer})} \\ \gamma = \frac{1}{\cosh \frac{d_S}{\lambda_1} + \left(\frac{\lambda_2}{\lambda_1} + \frac{d_I}{\lambda_1} \right) \sinh \frac{d_S}{\lambda_1}} \\ B_{\max}^{(\text{substrate})} = 170\text{mT} - 240\text{mT} \quad (\text{if the substrate is Nb}) \end{array} \right.$$

3. However, an extremely thin d_S can not protect the SC substrate. Thus **the S layer must have some thickness to decay the magnetic field** and protect the SC substrate.

Formula for the optimum thickness of the S layer

$$d_S = \lambda_1 \ln \left[\frac{\lambda_1}{\lambda_1 + \lambda_2 + d_I} \frac{B_S^{(S \text{ layer})}}{B_{max}^{(substrate)}} + \sqrt{\left(\frac{\lambda_1}{\lambda_1 + \lambda_2 + d_I} \frac{B_S^{(S \text{ layer})}}{B_{max}^{(substrate)}} \right)^2 + \frac{\lambda_1 - \lambda_2 - d_I}{\lambda_1 + \lambda_2 + d_I}} \right]_{d_I \lesssim 0(10) \text{ nm}}$$

T. Kubo (2015),

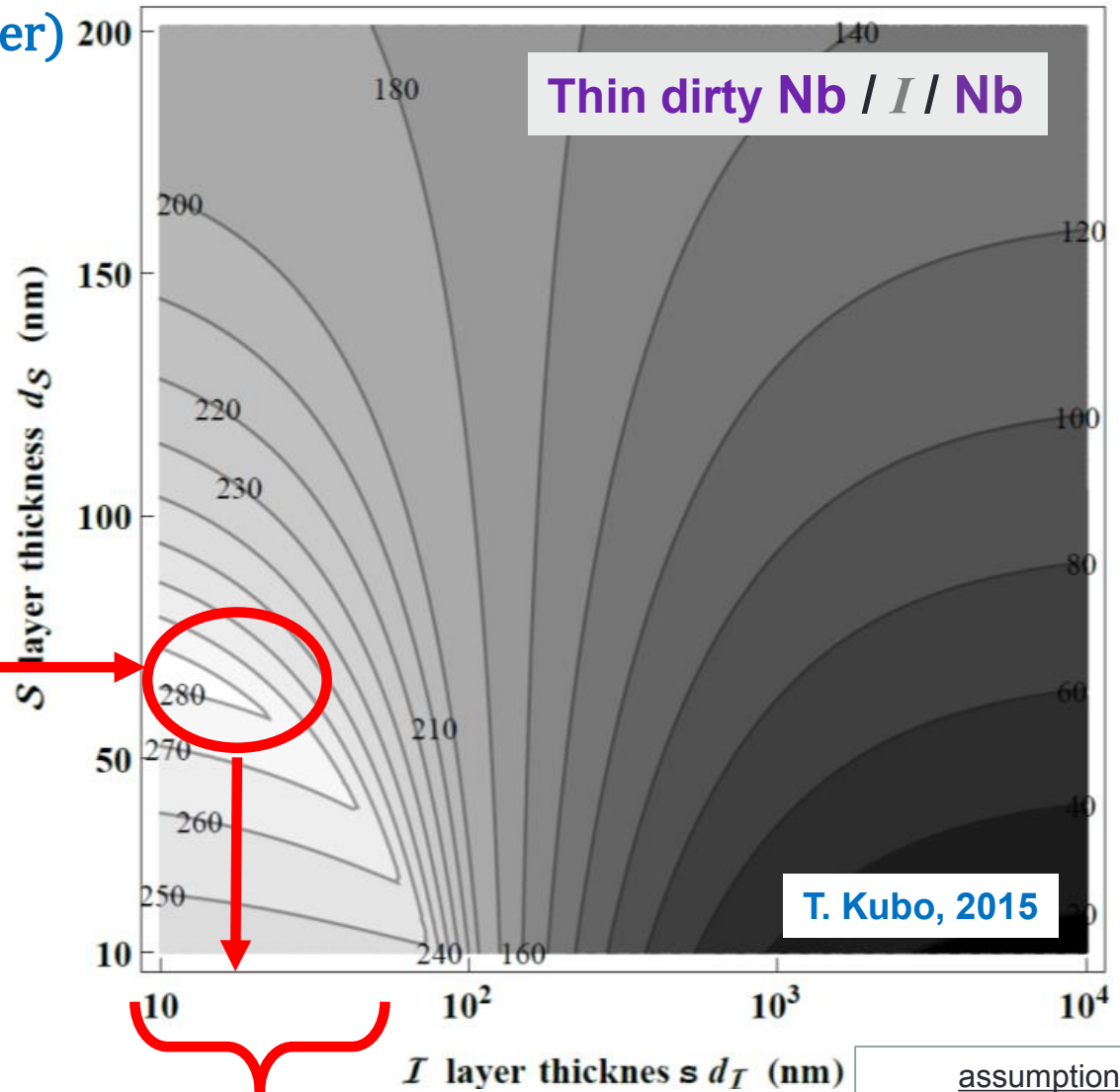
Obtained by using T. Kubo et al., *Appl. Phys. Lett.* **104**, 032603 (2014) and A. Gurevich, *AIP Advances* **5**, 017112 (2015)

- The formulae can be derived by using the discussion of A. Gurevich, *AIP Advances* **5**, 017112 (2015) and are described by using the superheating field of the quasi-classical theory and thus valid even at $T \ll T_c$.
- The formulae are generalized version of the Gurevich's formulae. The formulae includes effects of insulator layer with a finite thickness. **When $d_I \ll \lambda_1$, the formulae are reduced to the Gurevich's formulae** [A. Gurevich, *AIP Advances* **5**, 017112 (2015)].

Contour plot of $B_{\max}^{(\text{multilayer})}$

Optimum $d_s \sim 70\text{nm}$

see also A Gurevich, the 6th international workshop on thin films and new ideas for RF superconductivity, October 2014, Italy and A. Gurevich, AIP Advances 5, 017112 (2015)



T. Kubo, 2015

**d_I should be thin.
Up to several tens of nm acceptable.**

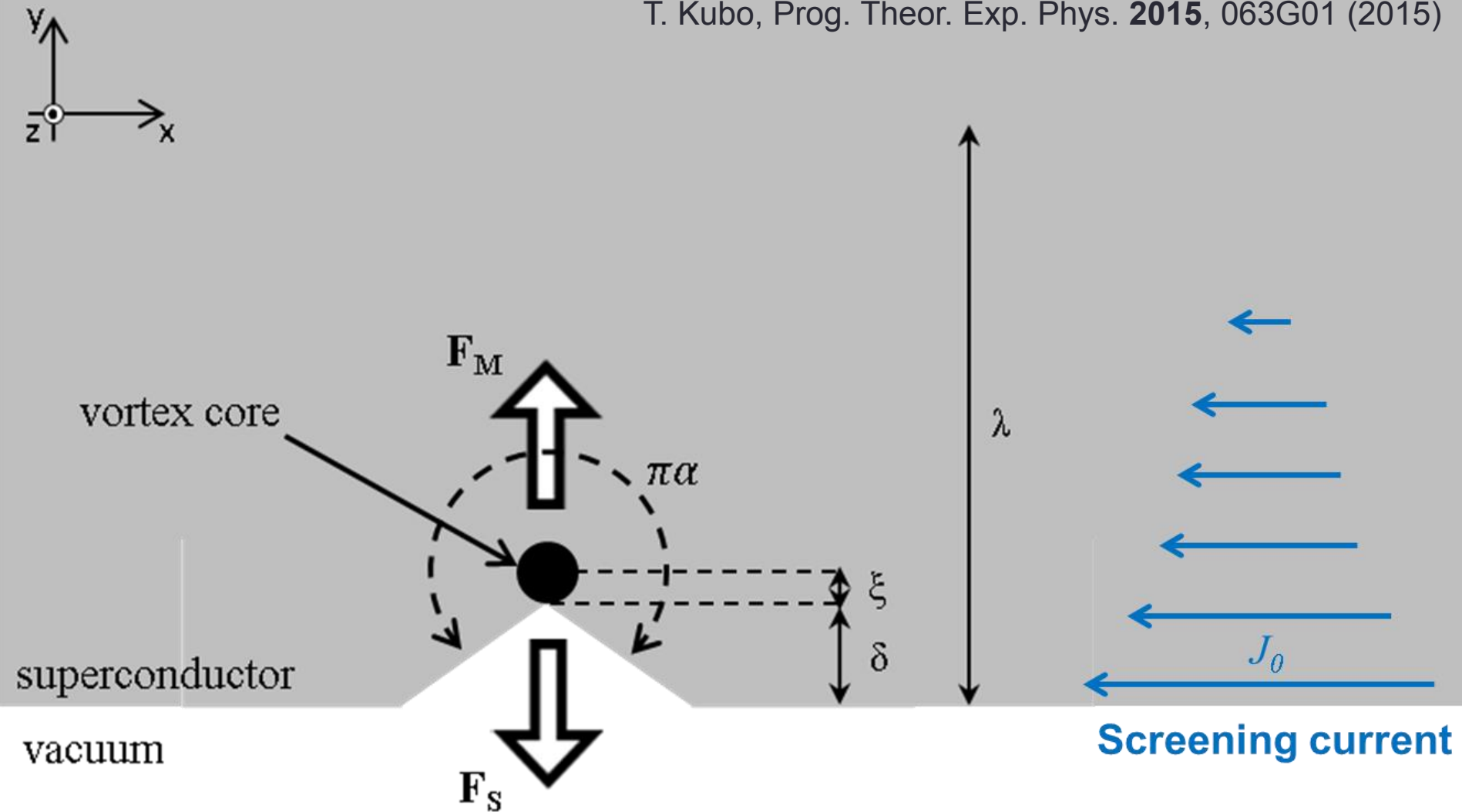
assumption
S layer: **Dirty Nb**
 $B_c^{(\text{Nb})} = 200\text{mT}$
 $\lambda_1 = \lambda^{(\text{dirty Nb})} = 180\text{nm}$
SC substrate: **clean Nb**
 $B_{\max}^{(\text{Nb})} = 240\text{mT}$
 $\lambda_2 = \lambda^{(\text{Nb})} = 40\text{nm}$

§ 2

A further step forward

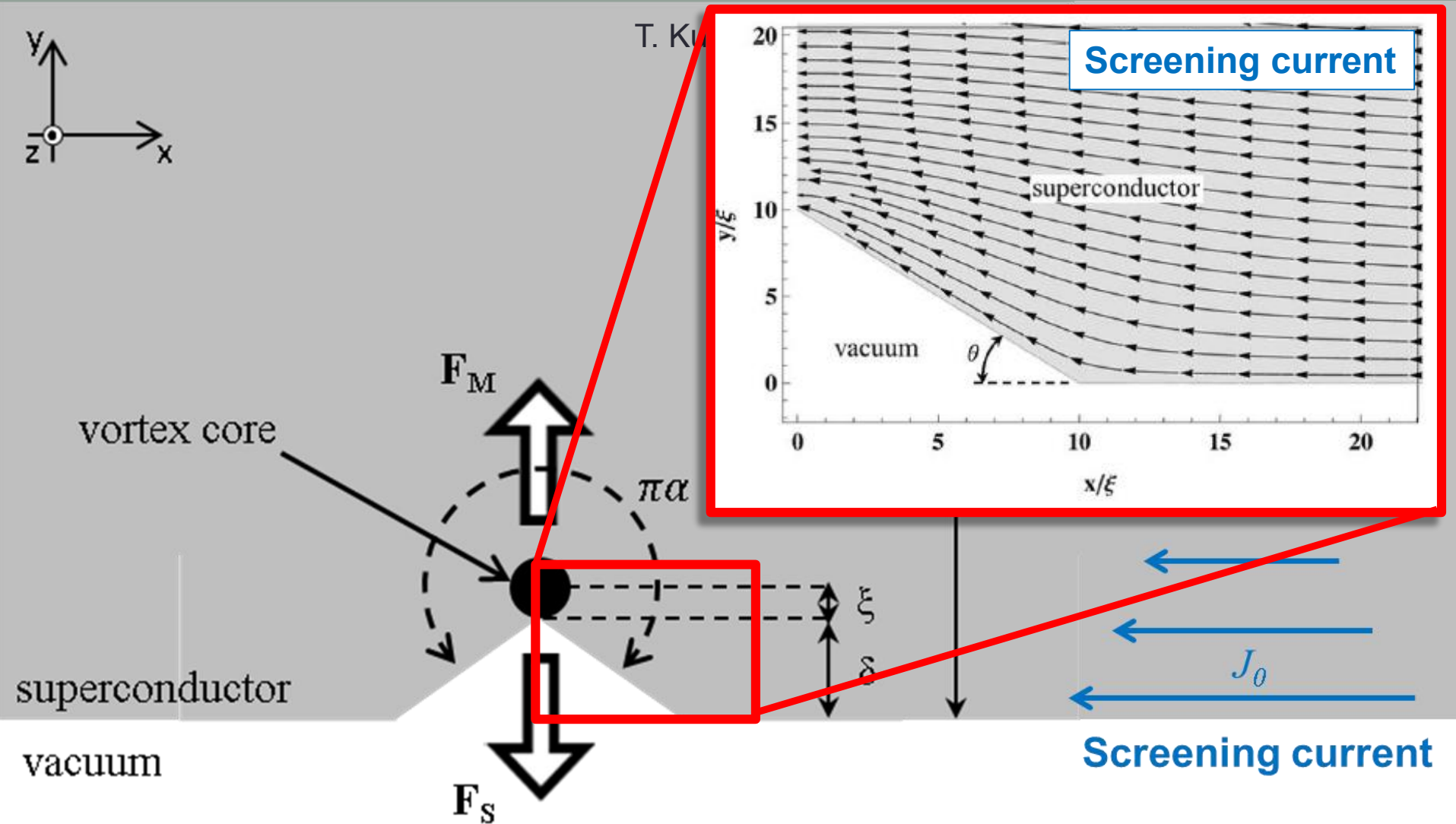
incorporate non-ideal surfaces

T. Kubo, Prog. Theor. Exp. Phys. **2015**, 063G01 (2015)



We assume $\xi < \delta < \lambda$.

Such small defects almost continuously distribute on the surface.



We assume $\xi < \delta < \lambda$.

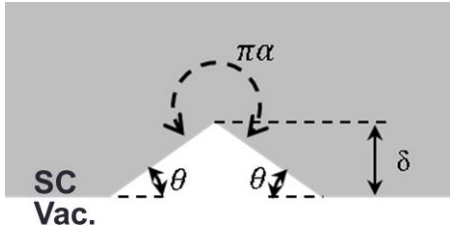
Such small defects almost continuously distribute on the surface.

The superheating field is suppressed due to the enhanced screening current.

Suppression factor

$$\tilde{B}_s = \eta B_s$$

$$\eta = \frac{1}{\alpha} \left(\frac{\Gamma\left(\frac{\alpha}{2}\right) \Gamma\left(\frac{3-\alpha}{2}\right) \alpha \sin \frac{\pi(\alpha-1)}{2} \xi}{\sqrt{\pi} \delta} \right)^{\frac{\alpha-1}{\alpha}}$$

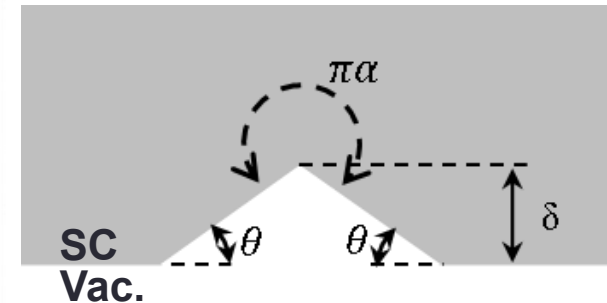
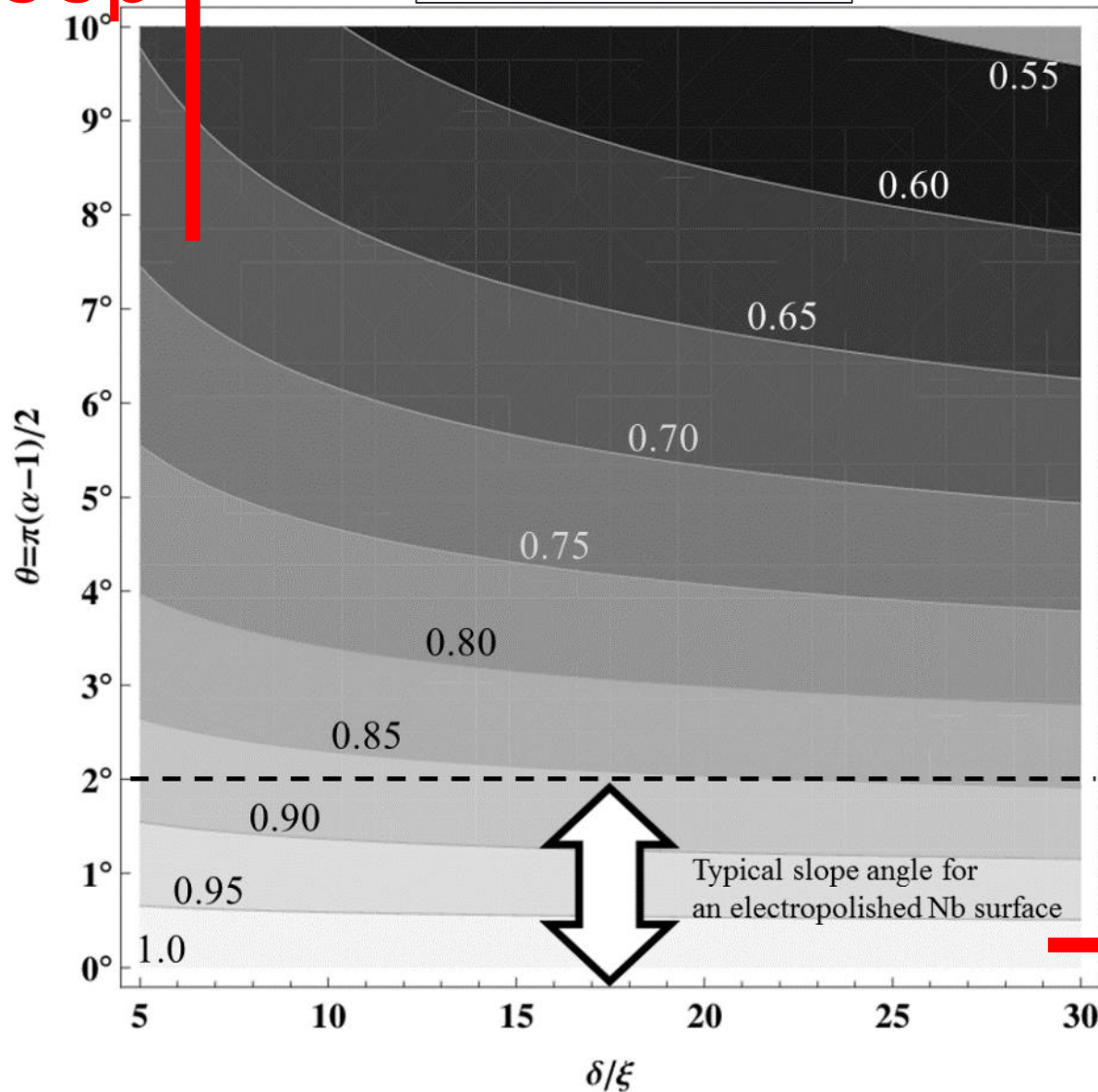


T. Kubo, Prog. Theor. Exp. Phys. **2015**, 063G01 (2015)

We can evaluate a “**suppression factor η** ” for materials, if we have **data of surface topographic studies**

(see for example “C. Xu et al. Phys. Rev. ST Accel. Beams **14**, 123501 (2011)”).

steep↑

Contour plot of η 

deep→

The formula for the maximum screening field of the multilayer

$$B_{\max}^{(\text{multilayer})} = \begin{cases} B_{\max}^{(\text{S layer})} & (\text{if } \gamma B_{\max}^{(\text{S layer})} < B_{\max}^{(\text{substrate})}) \\ \gamma^{-1} \times B_{\max}^{(\text{substrate})} & (\text{if } \gamma B_{\max}^{(\text{S layer})} \geq B_{\max}^{(\text{substrate})}) \end{cases}$$

where

$$\left\{ \begin{array}{l} B_{\max}^{(\text{S layer})} = B_s^{(\text{S layer})} \frac{\cosh \frac{d_s}{\lambda_1} + \left(\frac{\lambda_2}{\lambda_1} + \frac{d_I}{\lambda_1} \right) \sinh \frac{d_s}{\lambda_1}}{\sinh \frac{d_s}{\lambda_1} + \left(\frac{\lambda_2}{\lambda_1} + \frac{d_I}{\lambda_1} \right) \cosh \frac{d_s}{\lambda_1}} \times \eta \\ \gamma = \frac{1}{\cosh \frac{d_s}{\lambda_1} + \left(\frac{\lambda_2}{\lambda_1} + \frac{d_I}{\lambda_1} \right) \sinh \frac{d_s}{\lambda_1}} \\ B_{\max}^{(\text{substrate})} = 170\text{mT} - 240\text{mT} \end{array} \right. \quad \begin{array}{l} B_s^{(\text{S layer})} = 0.84 B_c^{(\text{S layer})} \\ \eta \text{ can be estimated by} \\ \eta = \frac{1}{\alpha} \left(\frac{\Gamma\left(\frac{\alpha}{2}\right) \Gamma\left(\frac{3-\alpha}{2}\right) \alpha \sin \frac{\pi(\alpha-1)}{2} \xi}{\sqrt{\pi} \delta} \right)^{\frac{\alpha-1}{\alpha}} \end{array}$$

T. Kubo (2015),

Obtained by using **T. Kubo et al.**, Appl. Phys. Lett. **104**, 032603 (2014), **A. Gurevich**, AIP Advances **5**, 017112 (2015), and **T. Kubo**, Prog. Theor. Exp. Phys. **2015**, 063G01 (2015)

The formula for the optimum thickness of the S layer

$$d_S = \lambda_1 \ln \left[\frac{\lambda_1}{\lambda_1 + \lambda_2 + d_I} \frac{\eta B_S^{(S \text{ layer})}}{B_{max}^{(substrate)}} + \sqrt{\left(\frac{\lambda_1}{\lambda_1 + \lambda_2 + d_I} \frac{\eta B_S^{(S \text{ layer})}}{B_{max}^{(substrate)}} \right)^2 + \frac{\lambda_1 - \lambda_2 - d_I}{\lambda_1 + \lambda_2 + d_I}} \right]_{d_I \lesssim 0(10)\text{nm}}$$

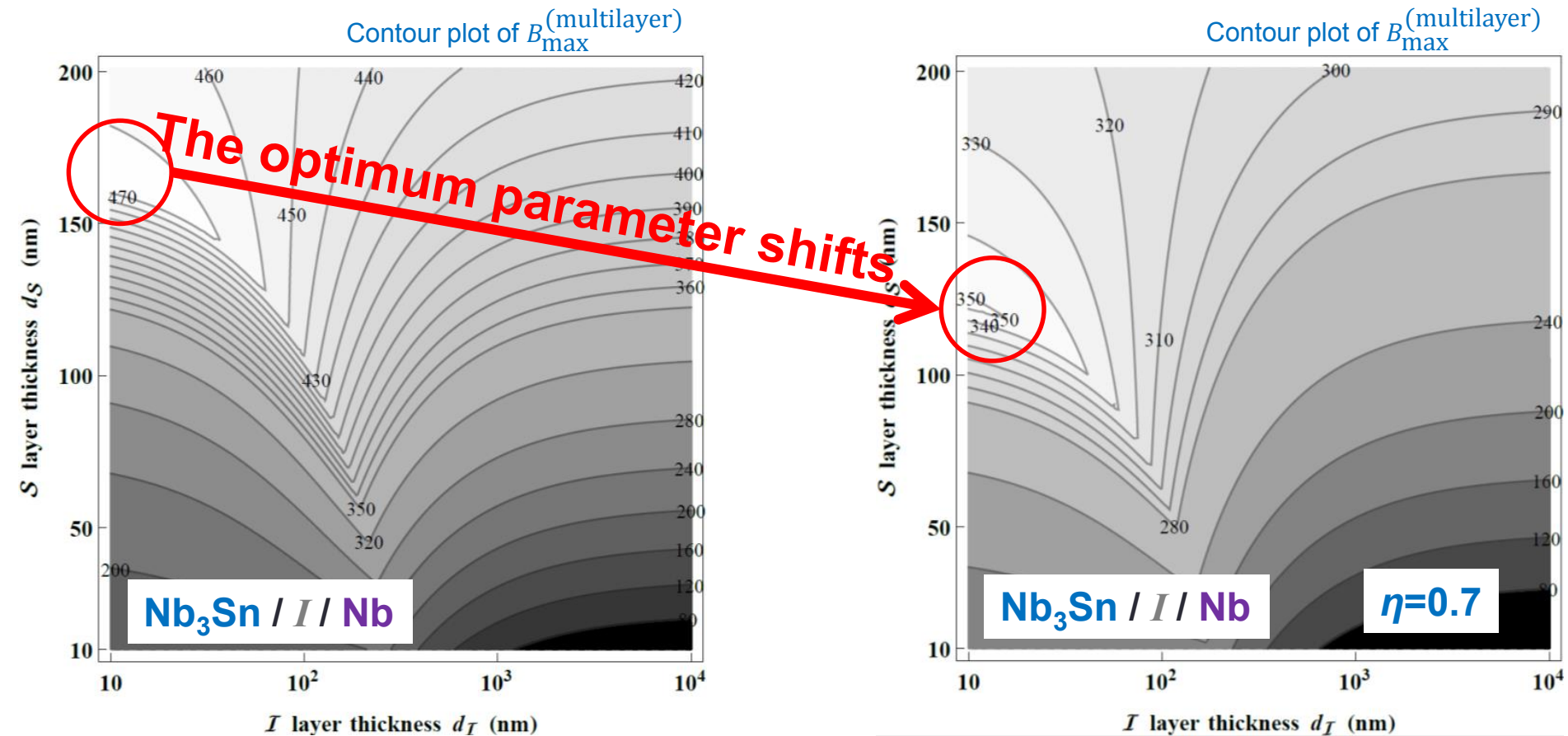
where

$$\left\{ \begin{array}{l} B_S^{(S \text{ layer})} = 0.84 B_c^{(S \text{ layer})} \\ B_{max}^{(substrate)} = 170\text{mT} - 240\text{mT} \quad (\text{if the substrate is Nb}) \\ \eta \text{ can be estimated by } \eta = \frac{1}{\alpha} \left(\frac{\Gamma\left(\frac{\alpha}{2}\right) \Gamma\left(\frac{3-\alpha}{2}\right) \alpha \sin \frac{\pi(\alpha-1)}{2} \xi}{\sqrt{\pi} \delta} \right)^{\frac{\alpha-1}{\alpha}} \end{array} \right.$$

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and **T. Kubo**, Prog. Theor. Exp. Phys. **2015**, 063G01 (2015)

The optimum thickness becomes thin in order to compensate **the suppressed superheating field.**



Optimum $d_s \sim 170\text{nm}$
Maximum field $\sim 470\text{mT}$

assumption
 S layer: **Nb₃Sn** (moderately dirty)
 $B_c^{(\text{Nb3Sn})} = 540\text{mT}$
 $\lambda_1 = \lambda^{(\text{Nb3Sn})} = 120\text{nm}$
 SC substrate: clean **Nb**
 $B_{\max}^{(\text{Nb})} = B_{c1}^{(\text{Nb})} = \underline{170\text{mT}}$
 $\lambda_2 = \lambda^{(\text{Nb})} = 40\text{nm}$

Optimum $d_s \sim 130\text{nm}$
Maximum field $\sim 350\text{mT}$

Summary

The optimum S layer thickness is a function of

- λ_1 , penetration depth of the S layer
- λ_2 ($\lambda_1 > \lambda_2$), penetration depth of the substrate
- d_I (< several tens of nm), thickness of the insulator
- $B_c^{(S \text{ layer})}$, thermodynamic critical field of the S layer
- $B_{max}^{(\text{substrate})}$ (170-240mT for Nb).
- η ($0 < \eta < 1$), superheating field suppression factor

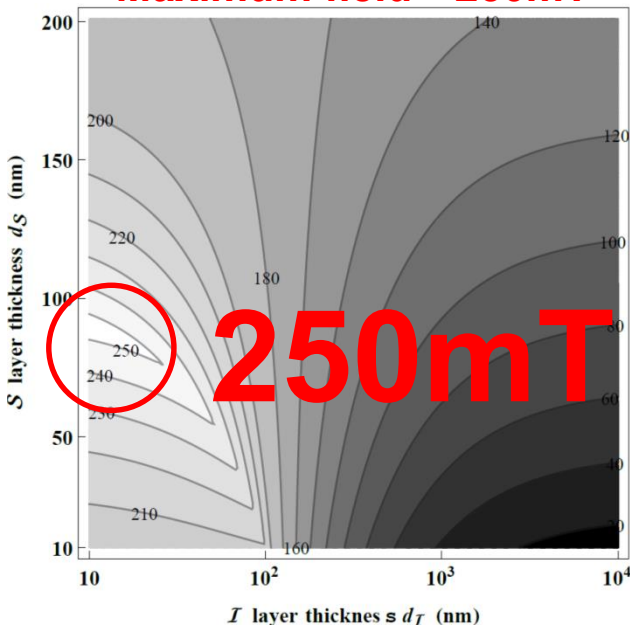
Material parameters and surface topographic studies are necessary in order to obtain the optimum S layer thickness.

The defect model and the formula for η may be useful to extract η from surface topographic studies.

*Let us go beyond Nb
by using the optimum parameters!*

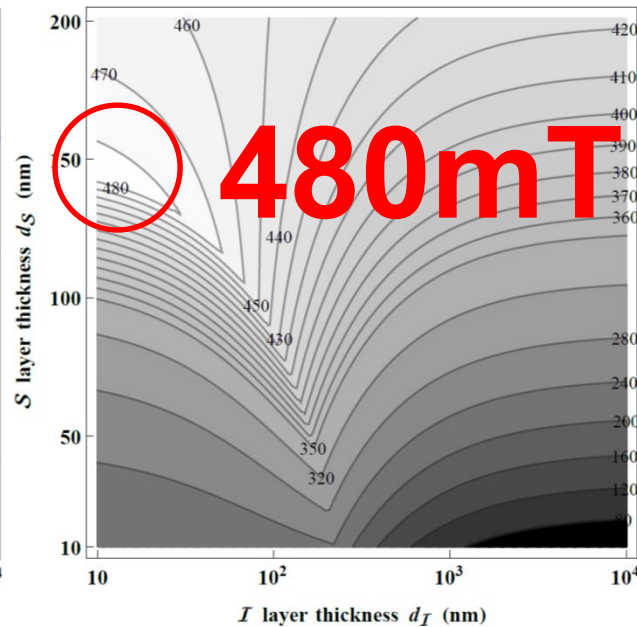
Dirty Nb / I / Nb

Optimum $d_s \sim 90\text{nm}$
Maximum field $\sim 250\text{mT}$



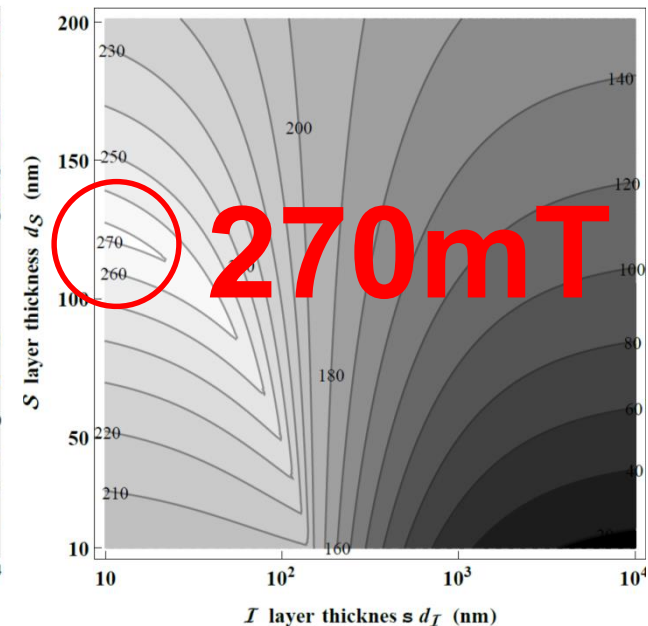
Nb₃Sn / I / Nb

Optimum $d_s \sim 150\text{nm}$
Maximum field $\sim 480\text{mT}$



NbN / I / Nb

Optimum $d_s \sim 130\text{nm}$
Maximum field $\sim 270\text{mT}$



Appendix for multilayer researchers

The optimum parameters for

Dirty Nb / *I* / **Nb**

Nb₃Sn / *I* / **Nb**

NbN / *I* / **Nb**

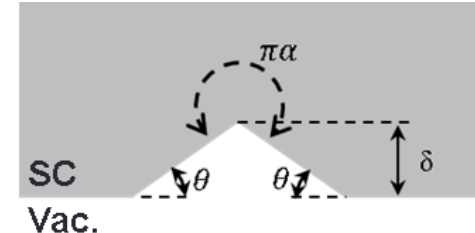
are given below!

The formula for the maximum screening field

$$B_{\max}^{(\text{multilayer})} = \begin{cases} B_{\max}^{(\text{S layer})} & (\text{if } \gamma B_{\max}^{(\text{S layer})} < B_{\max}^{(\text{substrate})}) \\ \gamma^{-1} \times B_{\max}^{(\text{substrate})} & (\text{if } \gamma B_{\max}^{(\text{S layer})} \geq B_{\max}^{(\text{substrate})}) \end{cases}$$

where

$$\left\{ \begin{array}{l} B_{\max}^{(\text{S layer})} = B_s^{(\text{S layer})} \frac{\cosh \frac{d_S}{\lambda_1} + \left(\frac{\lambda_2}{\lambda_1} + \frac{d_I}{\lambda_1} \right) \sinh \frac{d_S}{\lambda_1}}{\sinh \frac{d_S}{\lambda_1} + \left(\frac{\lambda_2}{\lambda_1} + \frac{d_I}{\lambda_1} \right) \cosh \frac{d_S}{\lambda_1}} \times \eta \\ \gamma = \frac{1}{\cosh \frac{d_S}{\lambda_1} + \left(\frac{\lambda_2}{\lambda_1} + \frac{d_I}{\lambda_1} \right) \sinh \frac{d_S}{\lambda_1}} \\ B_{\max}^{(\text{substrate})} = 170\text{mT} - 240\text{mT} \end{array} \right\} \left\{ \begin{array}{l} B_s^{(\text{S layer})} = 0.84 B_c^{(\text{S layer})} \\ \eta = \frac{1}{\alpha} \left(\frac{\Gamma\left(\frac{\alpha}{2}\right) \Gamma\left(\frac{3-\alpha}{2}\right) \alpha \sin \frac{\pi(\alpha-1)}{2} \xi}{\sqrt{\pi}} \right)^{\frac{\alpha-1}{\alpha}} \end{array} \right.$$



The formula for the optimum thickness of the S layer

$$d_S = \lambda_1 \ln \left[\frac{\lambda_1}{\lambda_1 + \lambda_2 + d_I} \frac{\eta B_s^{(S \text{ layer})}}{B_{max}^{(substrate)}} + \sqrt{\left(\frac{\lambda_1}{\lambda_1 + \lambda_2 + d_I} \frac{\eta B_s^{(S \text{ layer})}}{B_{max}^{(substrate)}} \right)^2 + \frac{\lambda_1 - \lambda_2 - d_I}{\lambda_1 + \lambda_2 + d_I}} \right]_{d_I \lesssim 0(10) \text{ nm}}$$

Necessary parameters

S layer:

$$B_s^{(S \text{ layer})} = 0.84 \times B_c^{(S \text{ layer material})}$$

$$\lambda_1 = \lambda^{(S \text{ layer material})}$$

η (suppression factor)

I layer:

$$d_I \sim 10\text{-}100 \text{ nm}$$

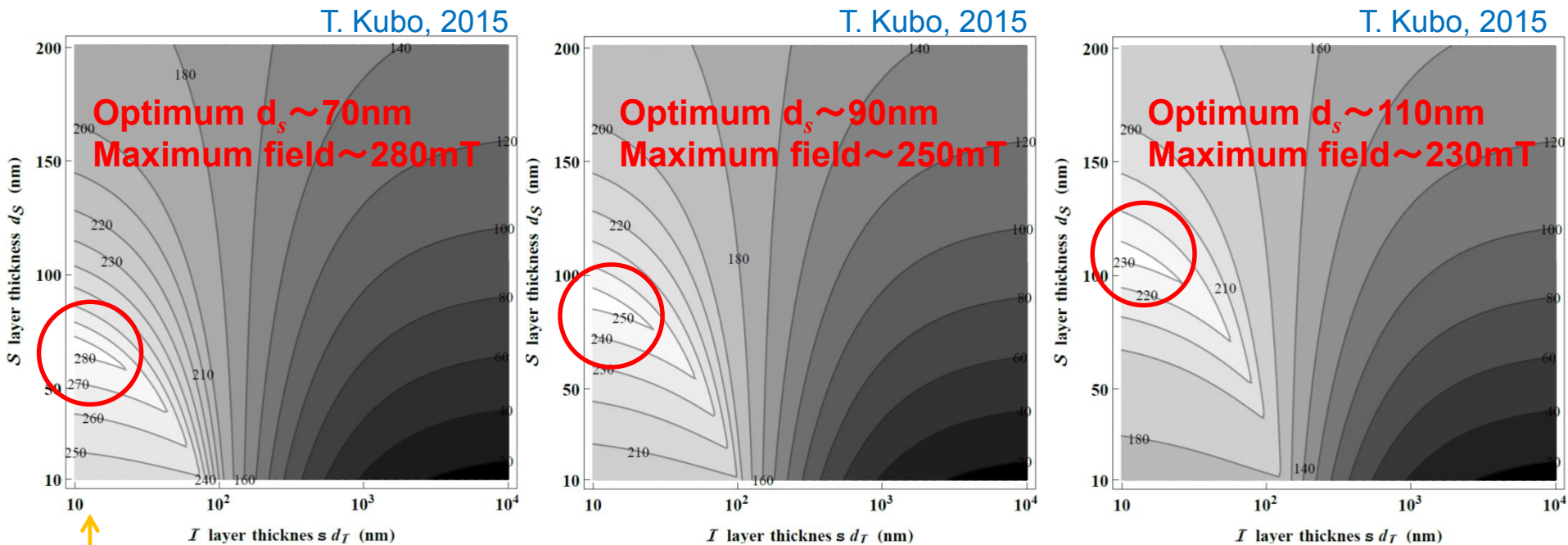
Substrate:

$$B_{max}^{(substrate)} = 170 \text{ mT} - 240 \text{ mT} \text{ (if the substrate is Nb)}$$

$$\lambda_2 = \lambda^{(substrate)} = 40 \text{ nm} \text{ (if the substrate is Nb)}$$

$$\eta=1$$

The optimum d_s and the maximum field for **Dirty Nb / I / Nb** system, where Nb substrate is assumed to withstand up to **240, 200, and 170mT**.



A. Gurevich, AIP Advances 5, 017112 (2015) and 6th thin film workshop at Italy

assumption

S layer: **Dirty Nb**

$$B_c^{(\text{Nb})} = 200\text{mT}$$

$$\lambda_1 = \lambda^{(\text{dirtyNb})} = 180\text{nm}$$

SC substrate: **clean Nb**

$$B_{\text{max}}^{(\text{Nb})} = \underline{240\text{mT}}$$

$$\lambda_2 = \lambda^{(\text{Nb})} = 40\text{nm}$$

assumption

S layer: **Dirty Nb**

$$B_c^{(\text{Nb})} = 200\text{mT}$$

$$\lambda_1 = \lambda^{(\text{dirtyNb})} = 180\text{nm}$$

SC substrate: **clean Nb**

$$B_{\text{max}}^{(\text{Nb})} = \underline{200\text{mT}}$$

$$\lambda_2 = \lambda^{(\text{Nb})} = 40\text{nm}$$

assumption

S layer: **Dirty Nb**

$$B_c^{(\text{Nb})} = 200\text{mT}$$

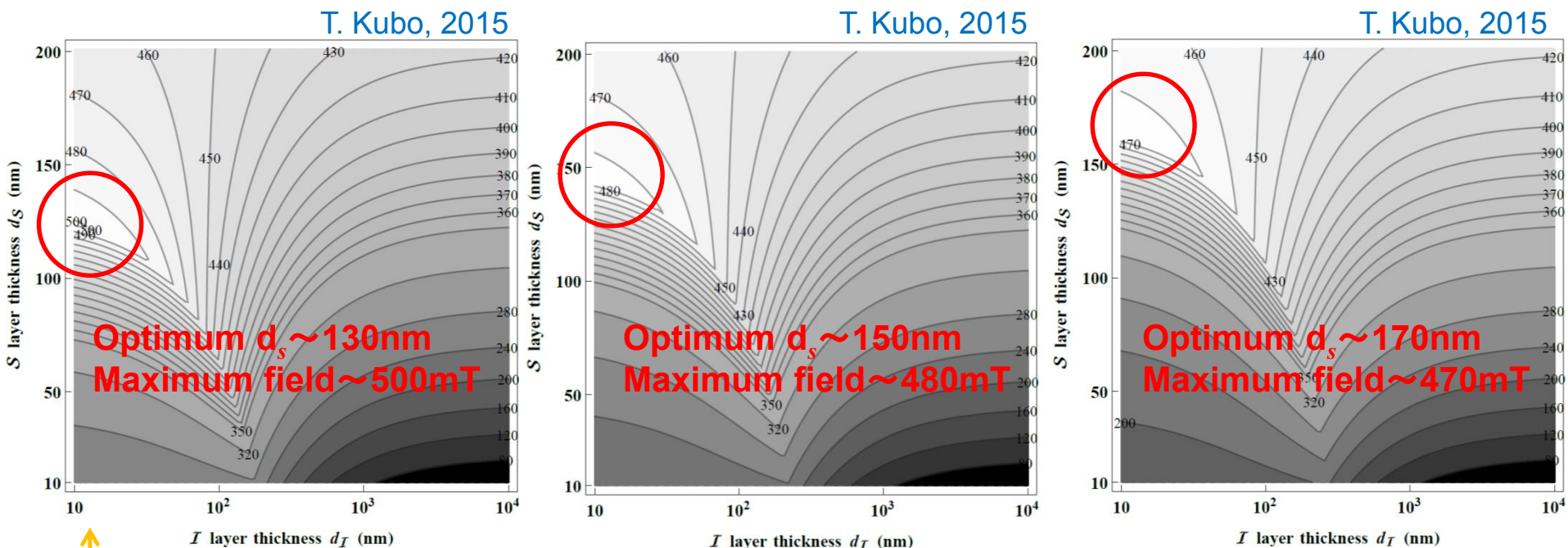
$$\lambda_1 = \lambda^{(\text{dirtyNb})} = 180\text{nm}$$

SC substrate: **clean Nb**

$$B_{\text{max}}^{(\text{Nb})} = B_{c1}^{(\text{Nb})} = \underline{170\text{mT}}$$

$$\lambda_2 = \lambda^{(\text{Nb})} = 40\text{nm}$$

The optimum d_s and the maximum field for **Nb₃Sn** / *I* / **Nb** system, where Nb substrate is assumed to withstand up to **240, 200, and 170mT**.



Consistent with the Gurevich's recent result

A. Gurevich, AIP Advances 5, 017112 (2015) and 6th thin film workshop at Italy

assumption

S layer: **Nb₃Sn** (moderately dirty)

$$B_c^{(\text{Nb}_3\text{Sn})} = 540 \text{mT}$$

$$\lambda_1 = \lambda^{(\text{Nb}_3\text{Sn})} = 120 \text{nm}$$

SC substrate: clean **Nb**

$$B_{\text{max}}^{(\text{Nb})} = \underline{\underline{240 \text{mT}}}$$

$$\lambda_2 = \lambda^{(\text{Nb})} = 40 \text{nm}$$

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$$B_c^{(\text{Nb}_3\text{Sn})} = 540 \text{mT}$$

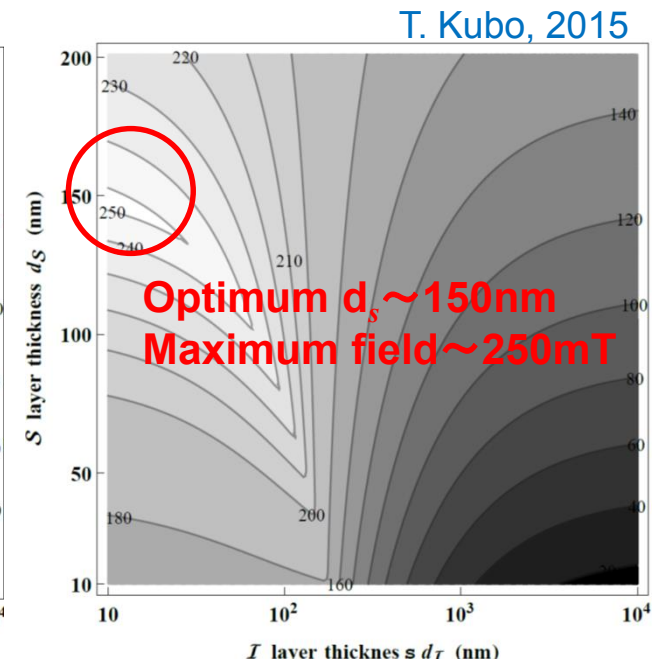
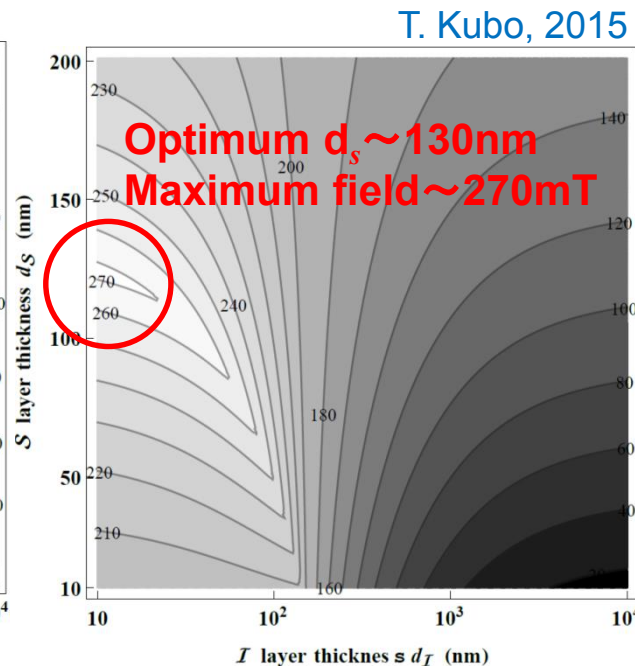
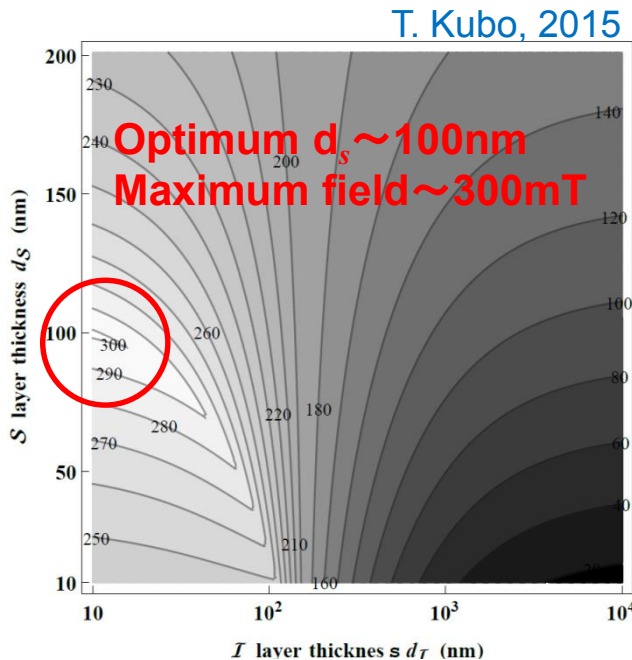
$$\lambda_1 = \lambda^{(\text{Nb}_3\text{Sn})} = 120 \text{nm}$$

SC substrate: clean **Nb**

$$B_{\text{max}}^{(\text{Nb})} = B_{c1}^{(\text{Nb})} = \underline{\underline{170 \text{mT}}}$$

$$\lambda_2 = \lambda^{(\text{Nb})} = 40 \text{nm}$$

The optimum d_s and the maximum field for **NbN** / **I** / **Nb** system, where Nb substrate is assumed to withstand up to **240, 200, and 170mT**.



assumption

S layer: **NbN**

$$B_c^{(\text{NbN})} = 230\text{mT}$$

$$\lambda_1 = \lambda^{(\text{NbN})} = 200\text{nm}$$

SC substrate: clean **Nb**

$$B_{\text{max}}^{(\text{Nb})} = \underline{\underline{240\text{mT}}}$$

$$\lambda_2 = \lambda^{(\text{Nb})} = 40\text{nm}$$

assumption

S layer: **NbN**

$$B_c^{(\text{NbN})} = 230\text{mT}$$

$$\lambda_1 = \lambda^{(\text{NbN})} = 200\text{nm}$$

SC substrate: clean **Nb**

$$B_{\text{max}}^{(\text{Nb})} = \underline{\underline{200\text{mT}}}$$

$$\lambda_2 = \lambda^{(\text{Nb})} = 40\text{nm}$$

assumption

S layer: **NbN**

$$B_c^{(\text{NbN})} = 230\text{mT}$$

$$\lambda_1 = \lambda^{(\text{NbN})} = 200\text{nm}$$

SC substrate: clean **Nb**

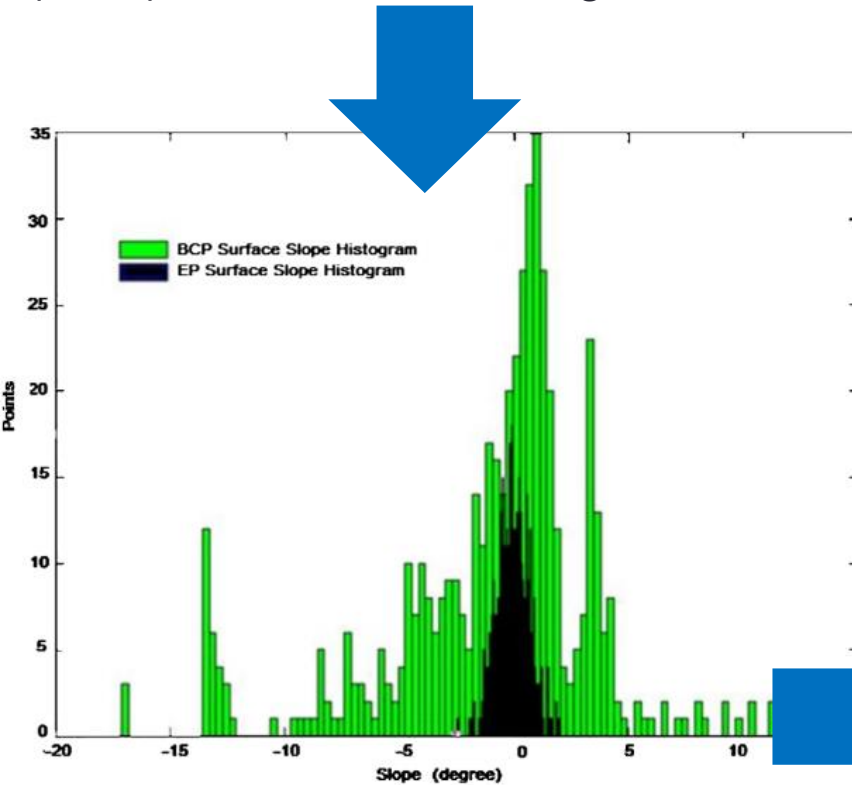
$$B_{\text{max}}^{(\text{Nb})} = B_{c1}^{(\text{Nb})} = \underline{\underline{170\text{mT}}}$$

$$\lambda_2 = \lambda^{(\text{Nb})} = 40\text{nm}$$

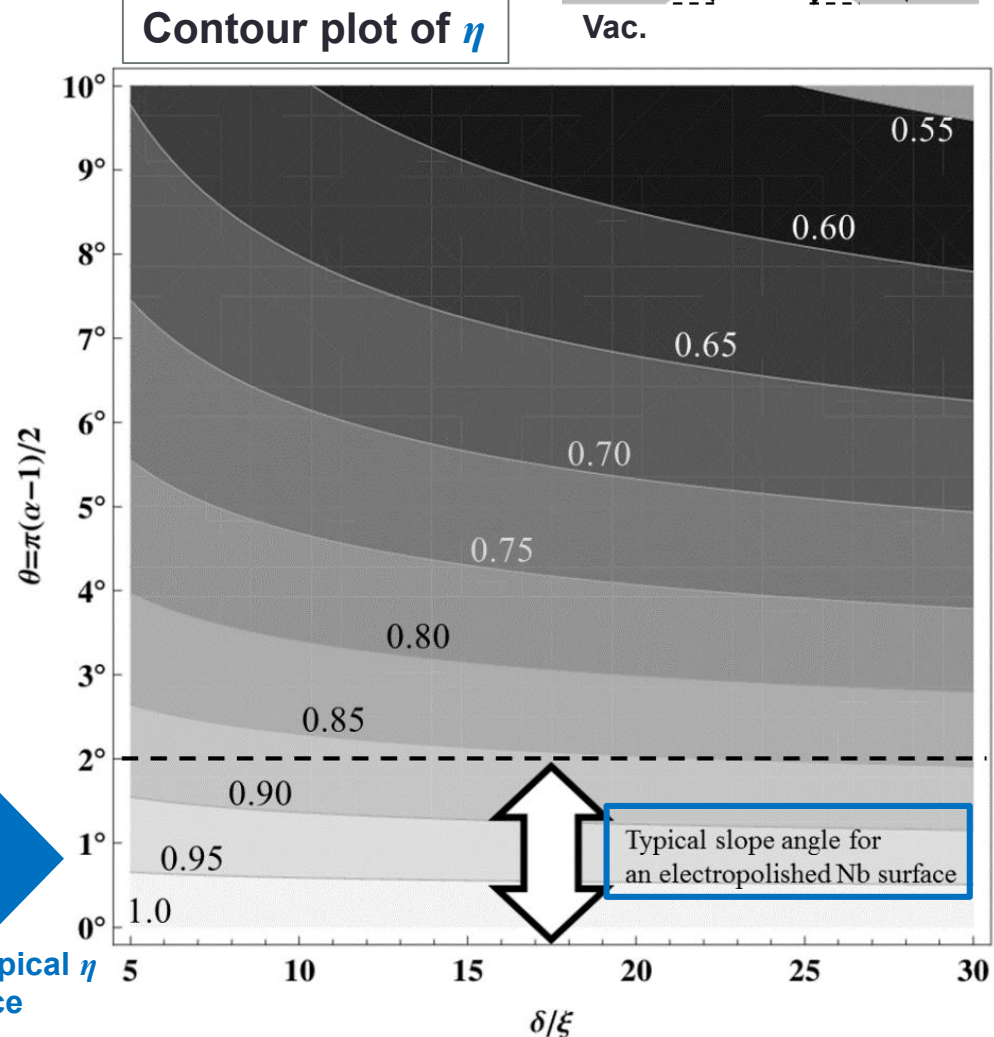
$$\eta < 1$$

Example: electropolished Nb

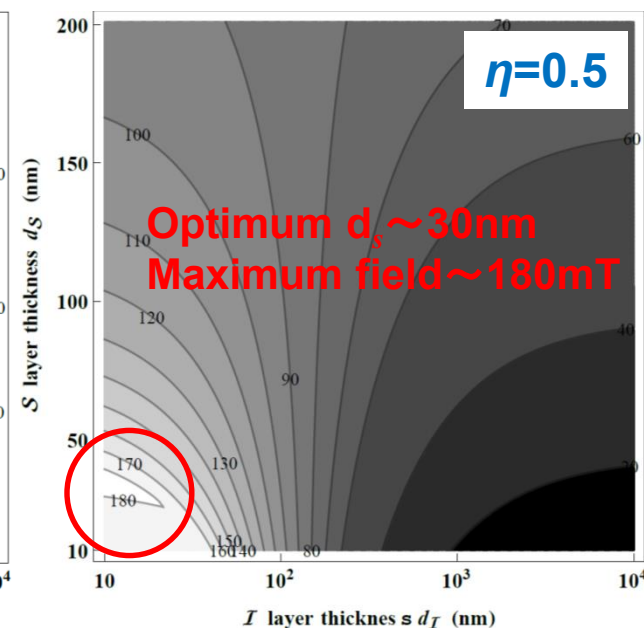
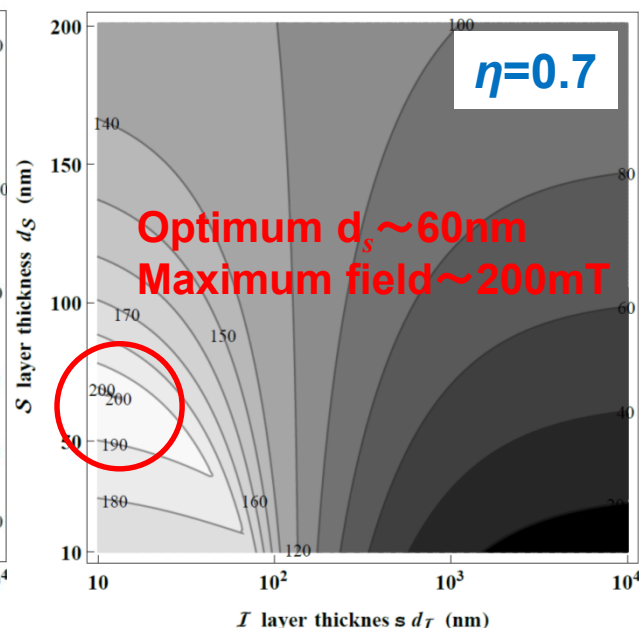
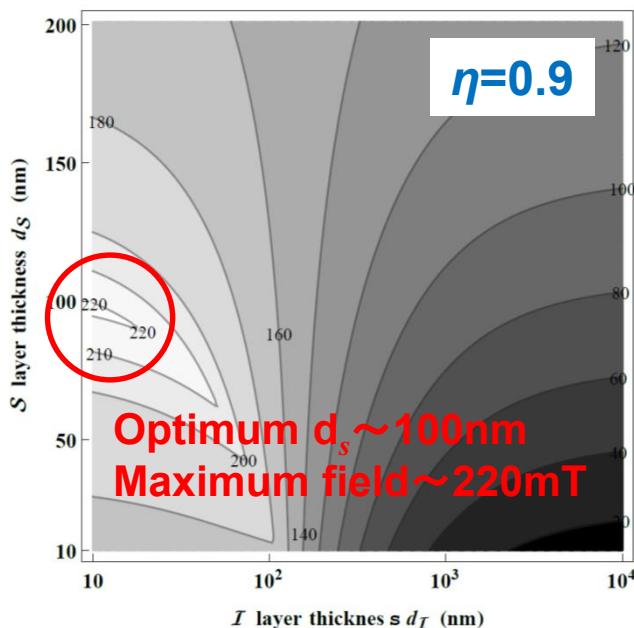
A surface after EP is studied by C.Xu, H.Tian, C.Reece, and M.Kelley, Phys. Rev. ST Accel. Beams **14**, 123501 (2011), which shows the figure below.



We can find typical η of EPed surface



The optimum d_s and the maximum field for **Dirty Nb / I / Nb** system, when the suppression factor due to nano-defects are given by $\eta=0.9$, 0.7, and 0.5. Nb substrate is assumed to withstand up to **170mT**.



assumption

S layer: **Dirty Nb**

$$B_c^{(\text{Nb})} = 200\text{mT}$$

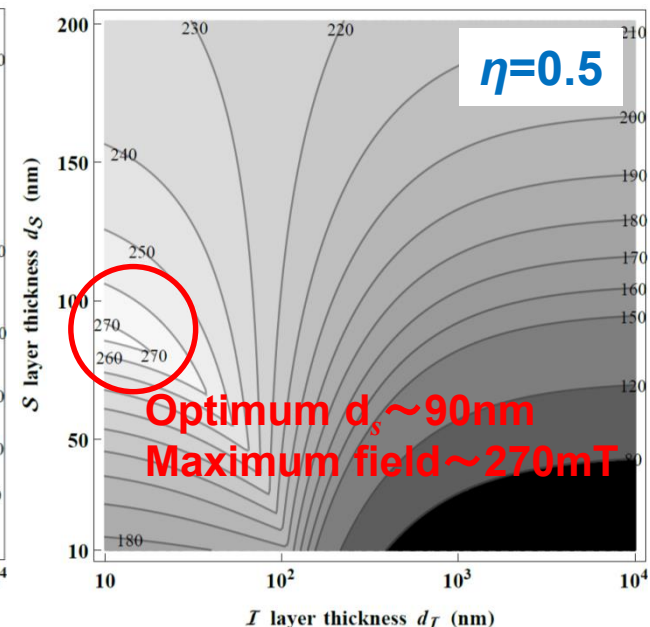
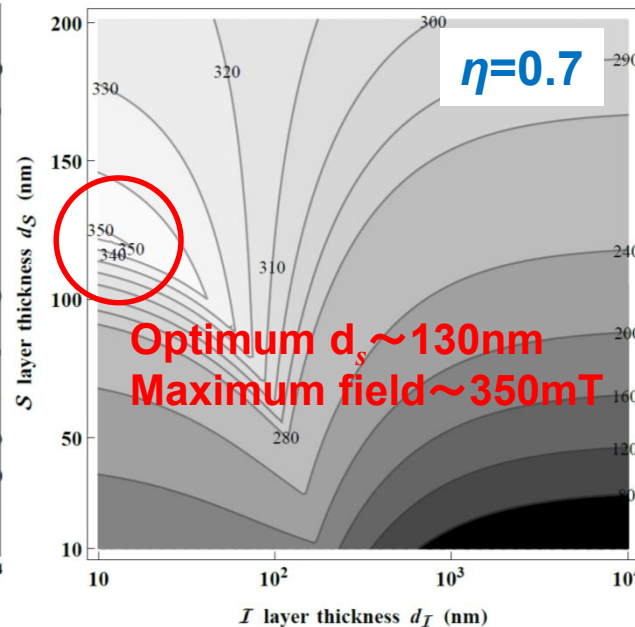
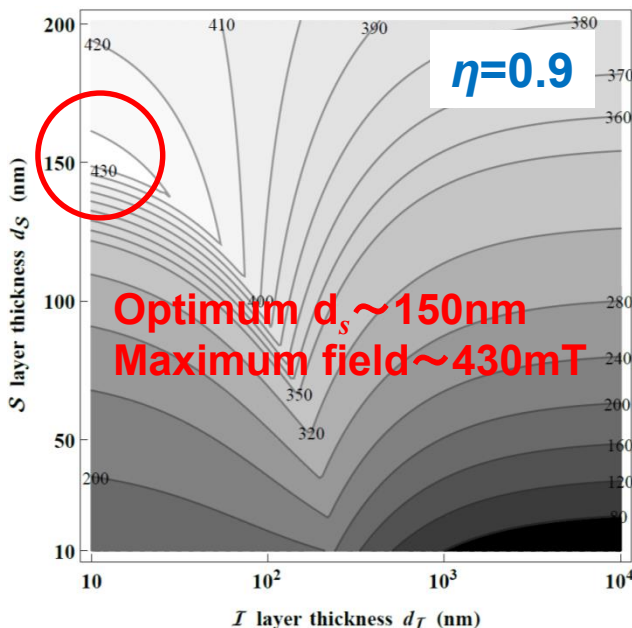
$$\lambda_1 = \lambda^{(\text{dirtyNb})} = 180\text{nm}$$

SC substrate: **clean Nb**

$$B_{\text{max}}^{(\text{Nb})} = B_{c1}^{(\text{Nb})} = \underline{170\text{mT}}$$

$$\lambda_2 = \lambda^{(\text{Nb})} = 40\text{nm}$$

The optimum d_s and the maximum field for Nb_3Sn / I / Nb system, when the suppression factor due to nano-defects are given by $\eta=0.9$, 0.7, and 0.5. Nb substrate is assumed to withstand up to **170mT**.



assumption

S layer: Nb_3Sn (moderately dirty)

$$B_c^{(\text{Nb}_3\text{Sn})} = 540\text{mT}$$

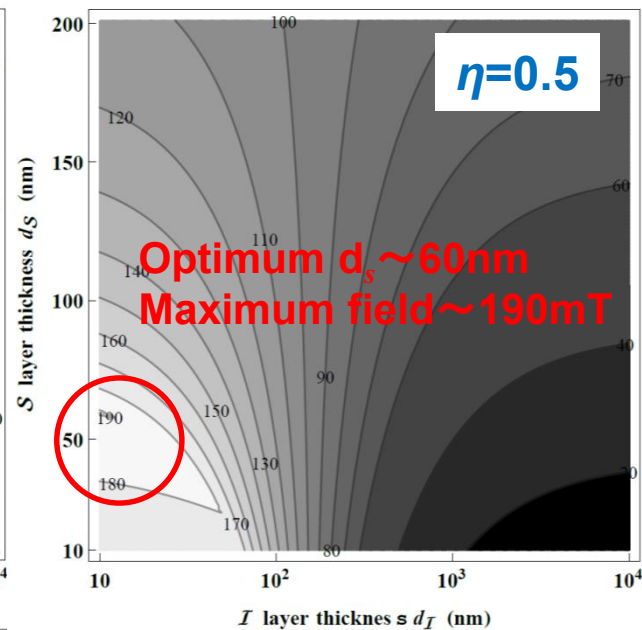
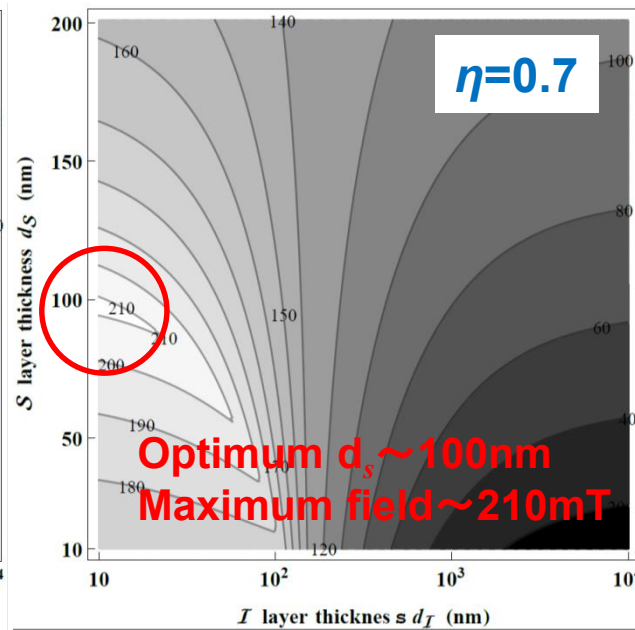
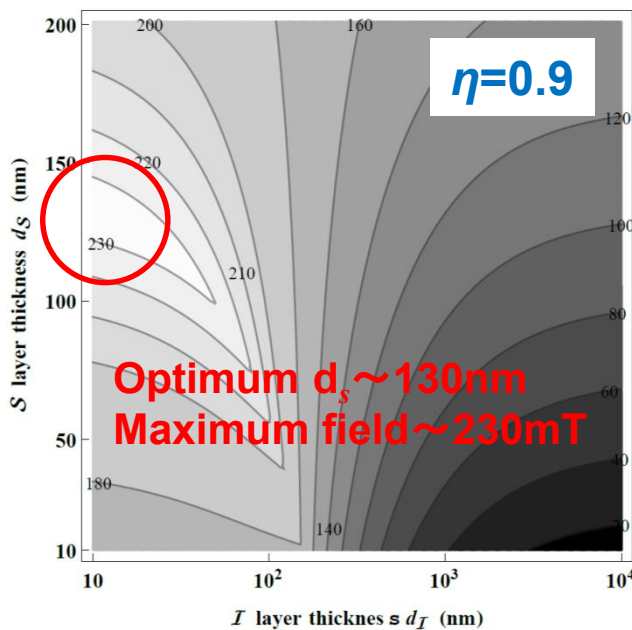
$$\lambda_1 = \lambda^{(\text{Nb}_3\text{Sn})} = 120\text{nm}$$

SC substrate: clean Nb

$$B_{\text{max}}^{(\text{Nb})} = B_{c1}^{(\text{Nb})} = \mathbf{170\text{mT}}$$

$$\lambda_2 = \lambda^{(\text{Nb})} = 40\text{nm}$$

The optimum d_s and the maximum field for NbN / I / Nb system, when the suppression factor due to nano-defects are given by $\eta=0.9$, 0.7, and 0.5. Nb substrate is assumed to withstand up to **170mT**.



assumption

S layer: **NbN**

$$B_c^{(\text{NbN})} = 230 \text{ mT}$$

$$\lambda_1 = \lambda^{(\text{NbN})} = 200 \text{ nm}$$

SC substrate: clean **Nb**

$$B_{\text{max}}^{(\text{Nb})} = B_{c1}^{(\text{Nb})} = \underline{170 \text{ mT}}$$

$$\lambda_2 = \lambda^{(\text{Nb})} = 40 \text{ nm}$$