



NICA heavy ion collider

Beam Dynamics

Required luminosity

Main parameters:

- beam energy – E
- luminosity – L

MPD electronics $\rightarrow \dot{N}_{event} \leq 7 \text{ kHz}$

Event rate $\dot{N}_{event} = L * \sigma$

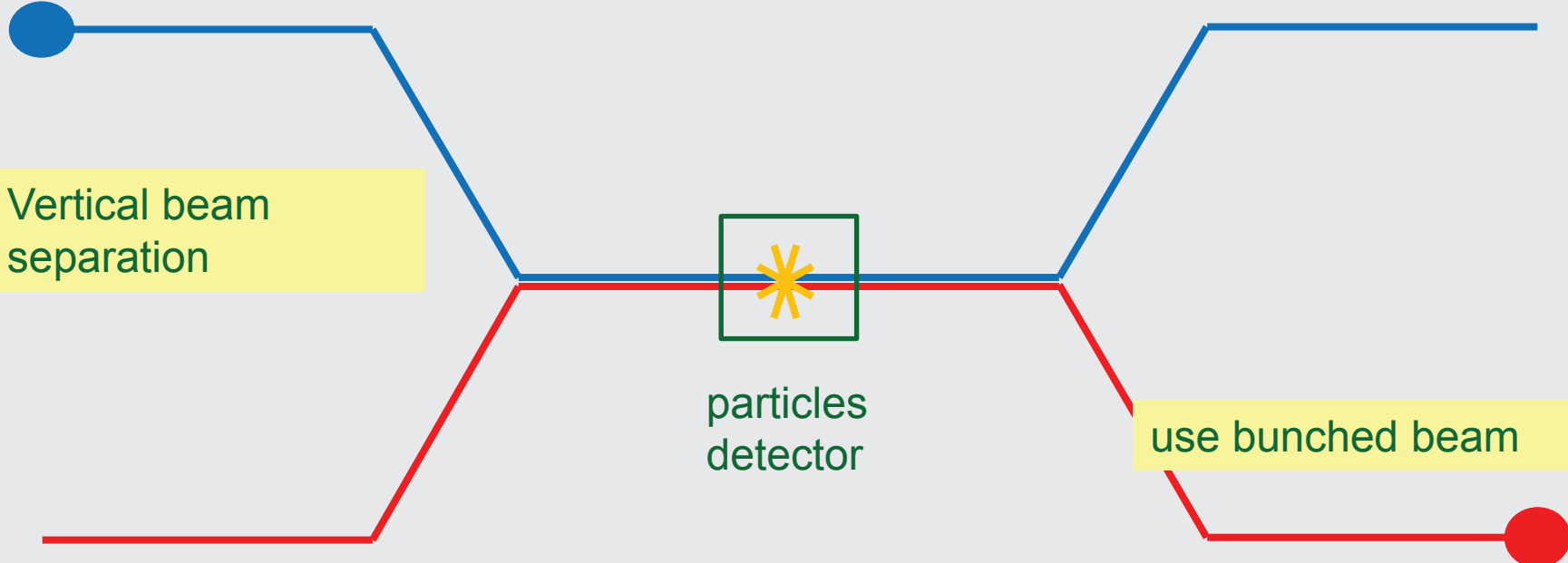
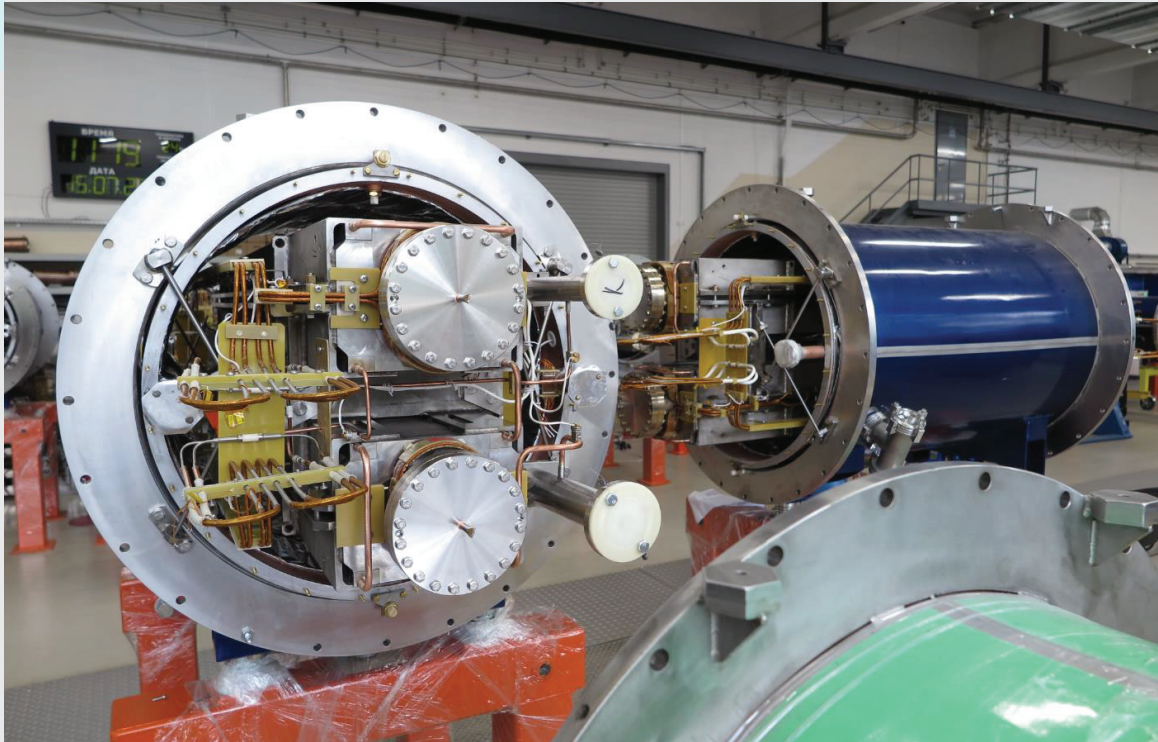
The cross-section $\sigma \approx 7 \cdot 10^{-24} \text{ cm}^{-2}$ $\rightarrow L = \frac{\dot{N}_{event}}{\sigma} \leq 1 * 10^{27} \text{ sm}^{-2}\text{s}^{-1}$

typical for RHIC (Au-Au) and LHC (Pb-Pb)

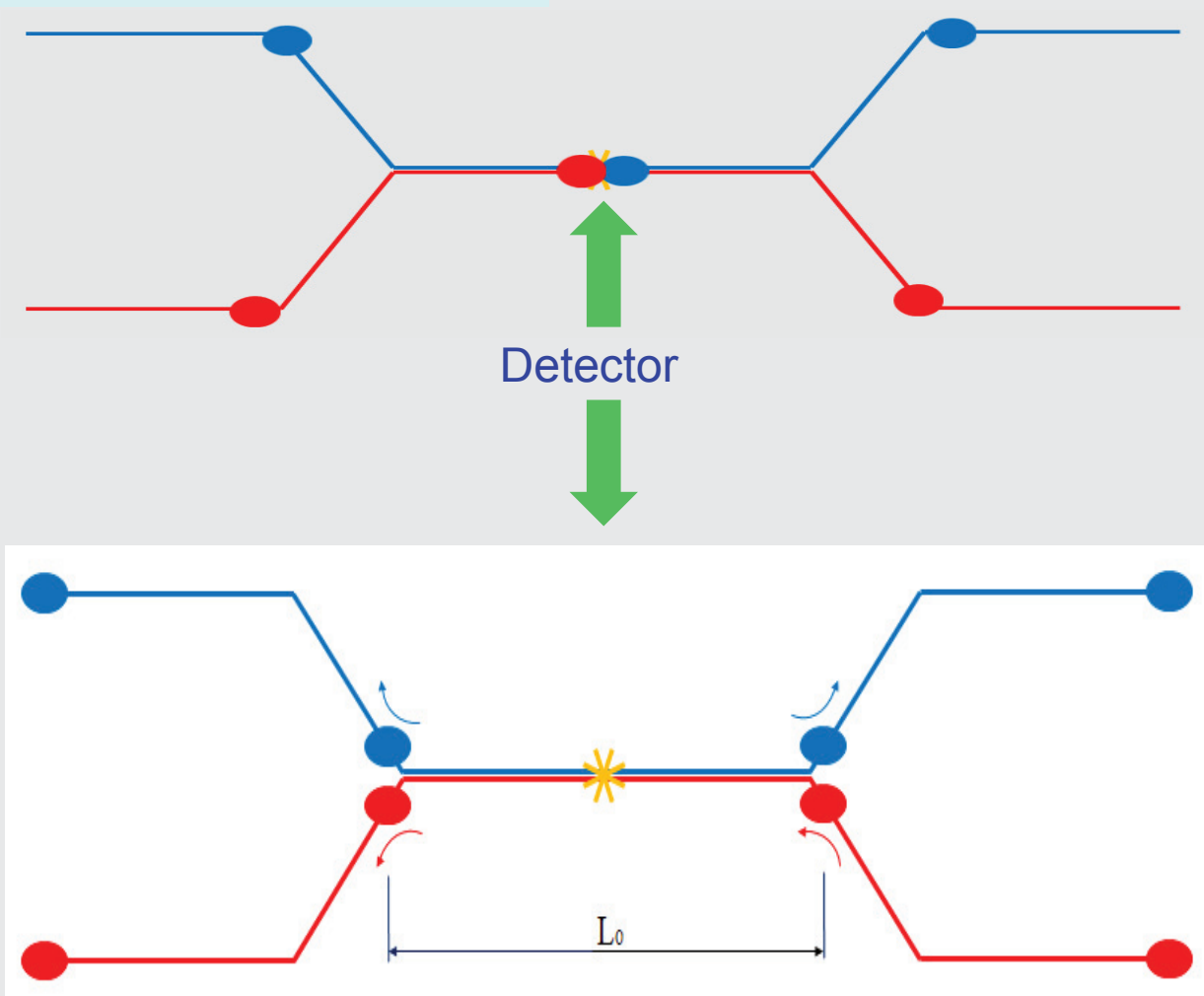
	NICA	RHIC	LHC
$L * 10^{27}$	1	8.7	3.6
$E \text{ [GeV/n]}$	4.5	100	2510

...however, *the ion kinetic energy is below 4.5 GeV/n*

- preparation of the collisions



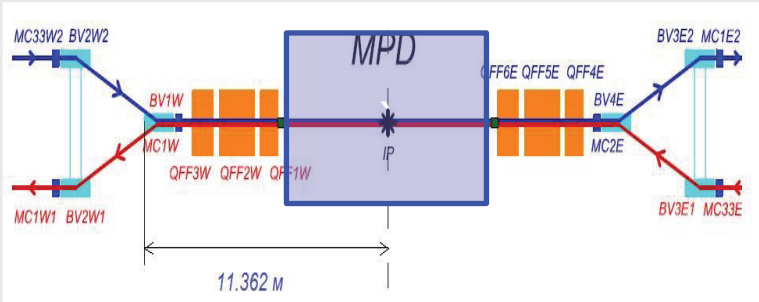
- preparation of the collisions



inter-bunch
distance is to be
large enough
to avoid parasitic
collisions

=>
fixed number of
bunches in the
ring

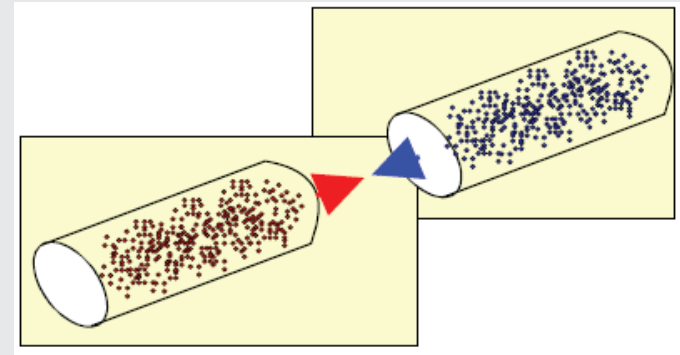
$$n_b = \frac{C_{ring}}{L_0}$$



• Luminosity

For round beams and head-on collisions

$$L = \frac{f_0 n_b N_i^2}{4\pi\beta^* \sqrt{\varepsilon_x \varepsilon_y}} H \left(\frac{\sigma_s}{\beta^*} \right)$$



- **Number of bunches n_b has to be as large as possible**

but the inter-bunch distance is to be large enough to avoid parasitic collisions

- **the bunch intensity N_b has to be maximal**
- **the emittance ε growth has to be minimized in all elements of injection chain**
- **beta function in collision point β^* has to be as small as possible**

but comparable with bunch length σ_s
to avoid luminosity reduction due to “hour-glass” factor

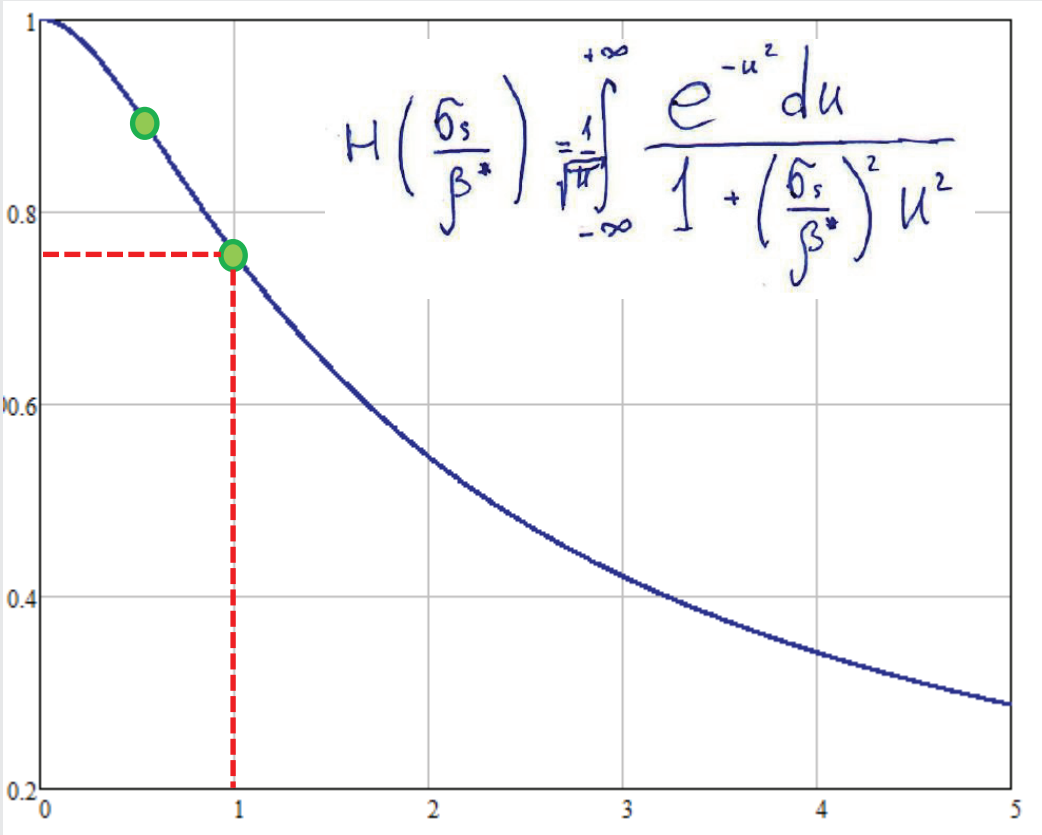

$$L = \frac{f_0 n_b N_i^2}{4\pi\beta^* \sqrt{\varepsilon_x \varepsilon_y}} H \left(\frac{\sigma_s}{\beta^*} \right)$$

Major effects limiting the luminosity

- ☐ IBS
- ☐ Space charge
- ☐ Luminosity lifetime
- ☐ Ring optics
- ☐ Cooling
- ☐ Instabilities

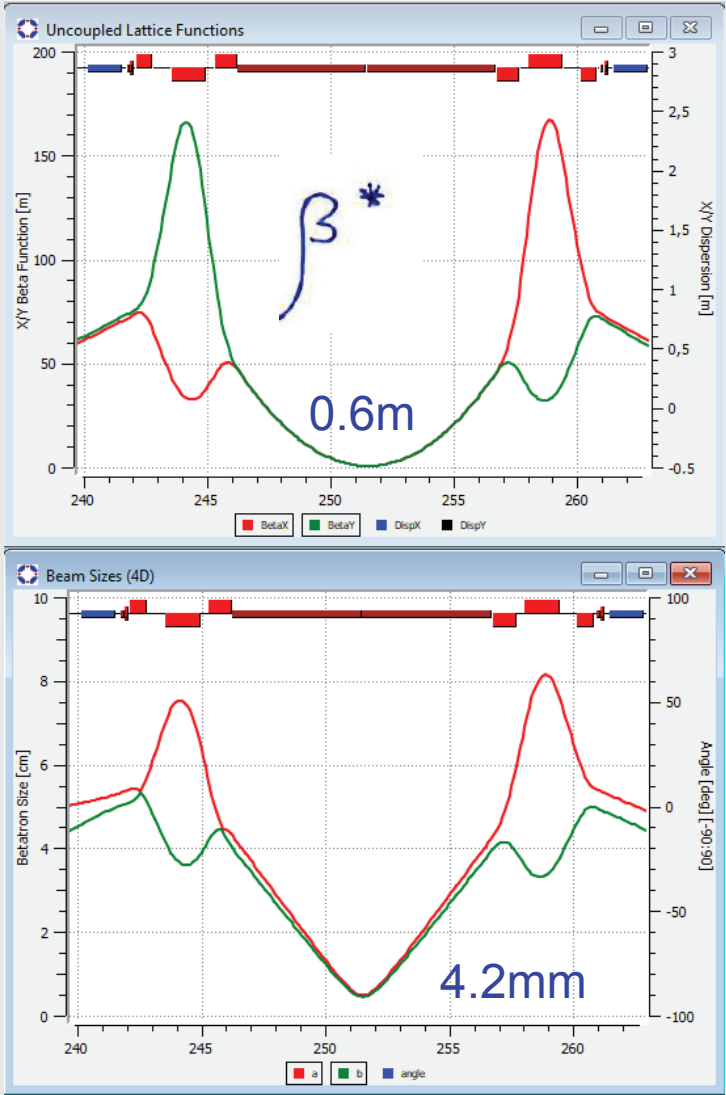
- Luminosity reduction due to hour-glass effect

$$L = \frac{f_0 n_b N_i^2}{4\pi \beta^* \sqrt{\epsilon_x \epsilon_y}} H\left(\frac{\sigma_s}{\beta^*}\right)$$



$$\sigma_s \cong \beta^*$$

Interaction point

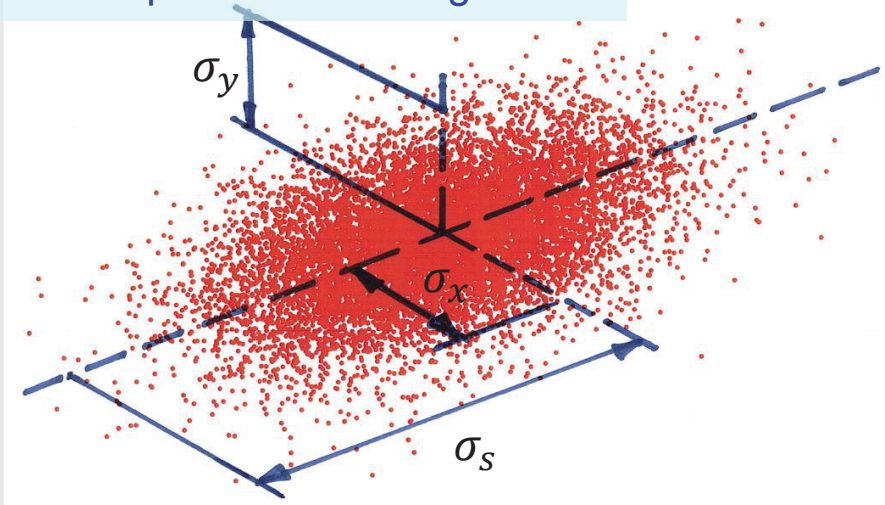


6-sigma rms beam-size

Figure 1 is a scatter plot showing the ratio of the number of particles in the first and second halves of the event, plotted against the vertex Z position in cm. The x-axis ranges from -200 to 200 cm, and the y-axis ranges from -80 to 80. Data points are colored according to the number of particles in the event, with a color bar on the right ranging from 0 (dark blue) to 5 (red). A dashed line represents the expected distribution for a uniform event. A legend in the top right corner provides summary statistics for the data.

Event		2011
Mean x		-1.526
Mean y		-13.204
Mean z		44.46
Mean t		22.24
Mean p		2.0
Mean q		2.0
Mean r		2.0
Mean s		2.0
Mean t		2.0
Mean u		2.0
Mean v		2.0
Mean w		2.0
Mean x		2.0
Mean y		2.0
Mean z		2.0
Mean t		2.0
Mean p		2.0
Mean q		2.0
Mean r		2.0
Mean s		2.0
Mean t		2.0
Mean u		2.0
Mean v		2.0
Mean w		2.0

Required bunch long size 2

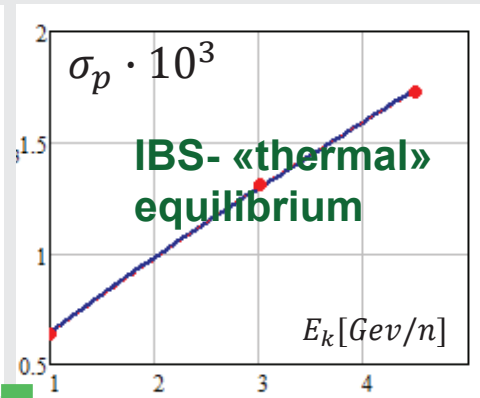
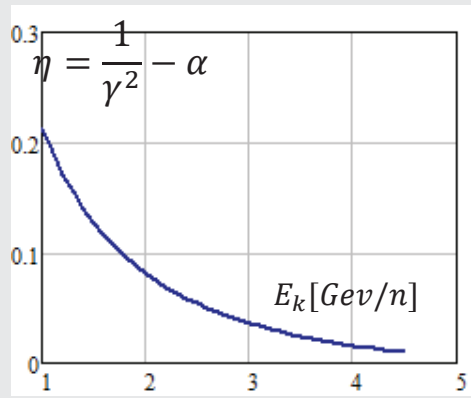
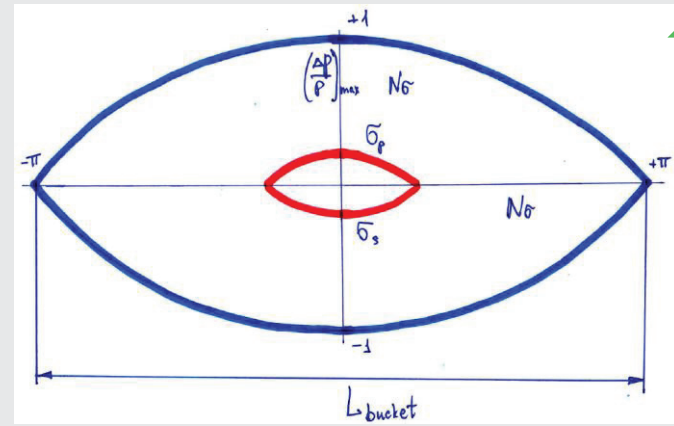


$$N\sigma_{RF} = 4$$

$$6\sigma_s \cong TPC$$

0.6m

$$L_{bucket-desired} = N\sigma_{RF} \cdot \sigma_s \cdot \pi = 7.5m$$

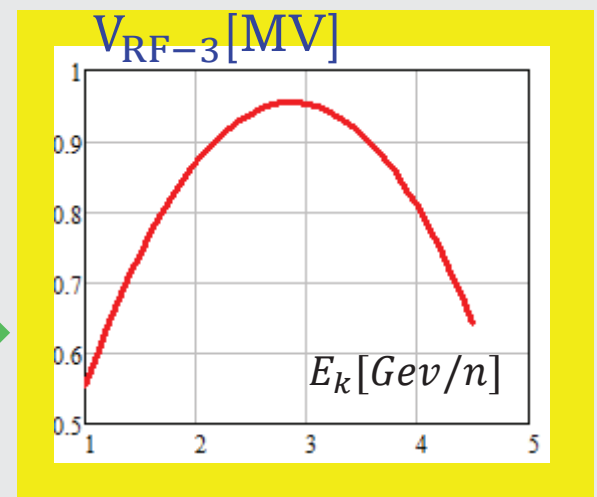


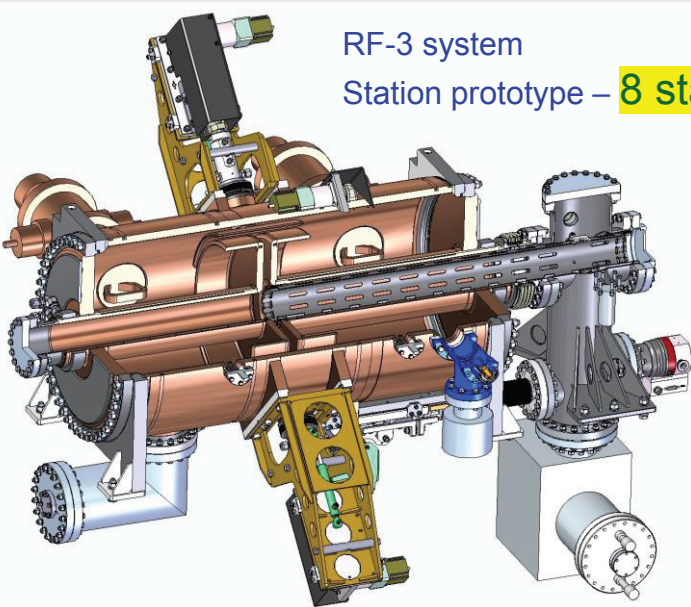
$$n_b = 22 \quad (= \frac{C_{ring}}{L_0})$$

$$h = 3 \cdot n_b = 66$$

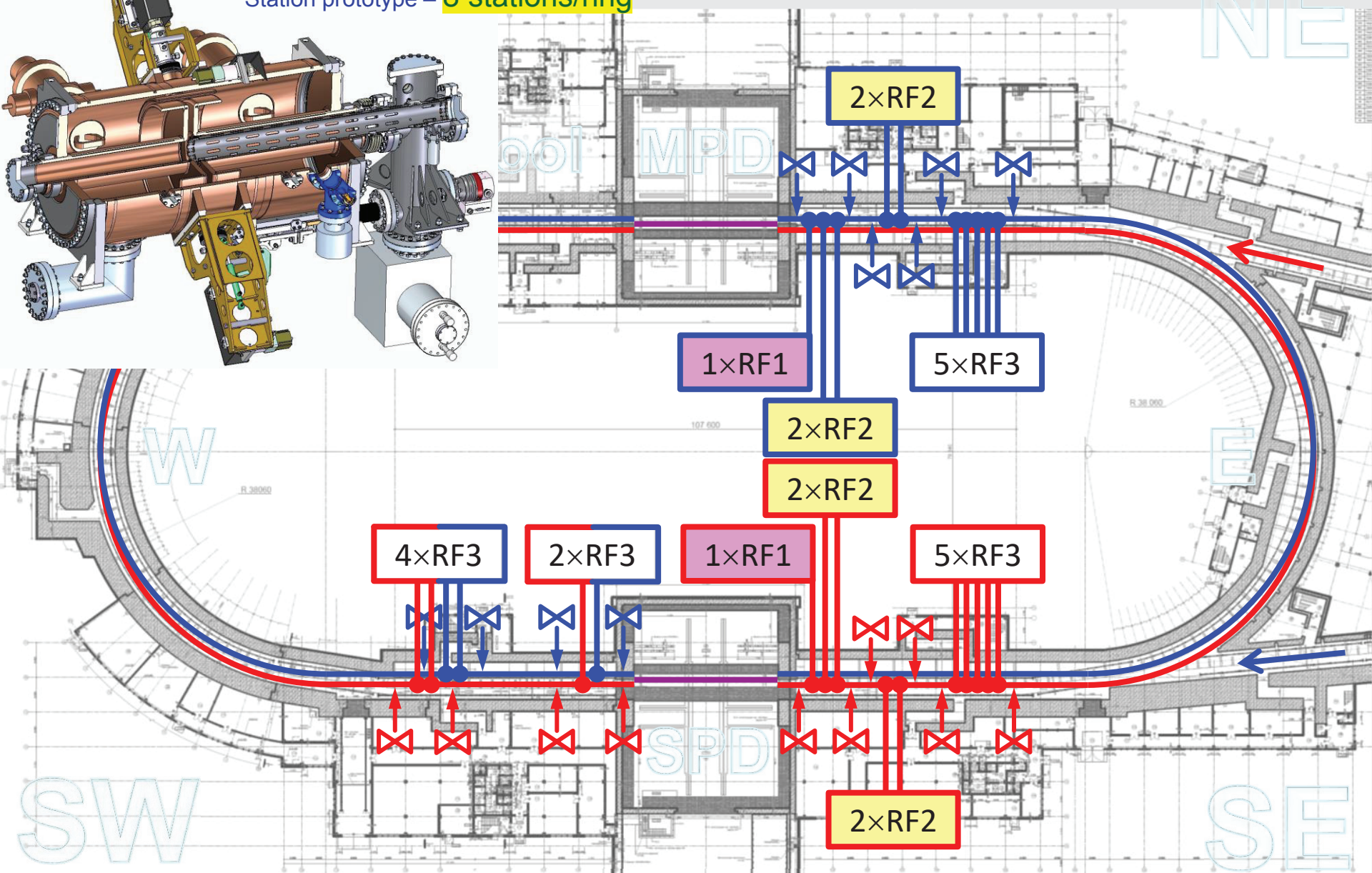
$$L_{bucket-RF} = \frac{C_{ring}}{h} = 7.6m$$

$$V = \left(\frac{C_{ring} \sigma_p}{\sigma_s} \right)^2 \cdot \frac{\beta^2 r}{2\pi h} \cdot \frac{A m_n}{z} |\eta|$$





Location of RF cavities in the accelerator tunnel.



RF systems of the NICA collider

A.Tribendis

Intra-Beam Scattering

IBS - Coulomb scattering of charged particles in a beam results in an exchange of energy between different degrees of freedom

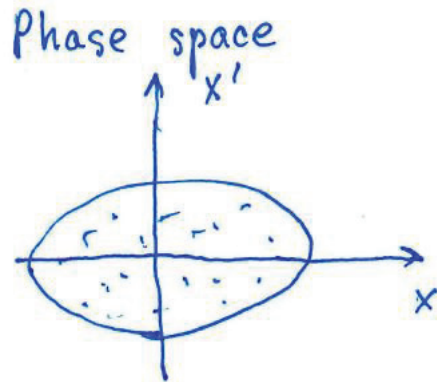
→ Causes the beam size to grow up → limits luminosity lifetime

IBS is important constraint for circular machines

Cyclotrons	skipped
Synchrotrons	skipped
Colliders	effect

Visible effect in 10th to 1000th seconds

$$\begin{cases} \frac{1}{\tau_x} = \frac{1}{\varepsilon_x} \frac{d\varepsilon_x}{dt} \\ \frac{1}{\tau_y} = \frac{1}{\varepsilon_y} \frac{d\varepsilon_y}{dt} \\ \frac{1}{\tau_p} = \frac{1}{\sigma_p^2} \frac{d(\sigma_p^2)}{dt} \end{cases}$$



distr. function.

$$f(x, x') = \frac{1}{2\pi\sigma_x\sigma_{x'}} \exp\left\{-\frac{x^2}{2\sigma_x^2} - \frac{x'^2}{2\sigma_{x'}^2}\right\}$$

Beam temp.

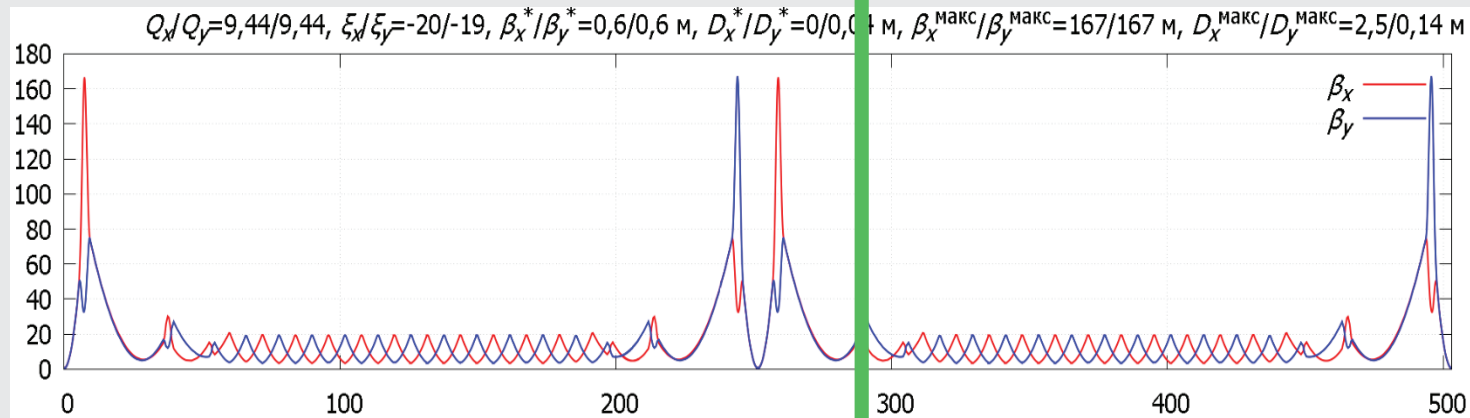
$$T \stackrel{\text{def}}{=} \frac{m\sigma_{x'}^2}{2k_B} = \frac{m\sigma_x^2}{2k_B}$$

$$\sigma_x \equiv \sqrt{\sigma_x^2}$$

IBS leads to

- relaxation (equation) between 3 “temperatures” in the beam faster than 6D-emittance growth rate
- infinite beam 6D-phase space volume growth in circular machines

Intra-Beam Scattering



$E, \text{GeV/u}$	$N, 10^9$	$\varepsilon_x, \pi \text{ mm} \cdot \text{mrad}$	$\varepsilon_y, \pi \text{ mm} \cdot \text{mrad}$	σ_s, m	$\sigma_p, 10^{-3}$	τ_x, s	τ_y, s	τ_s, s
4.5	2.8	1.1	0.82	0.6	1.73	2500	2500	2500
3	2.71		0.95		1.31	770	770	770
1	0.28		1.08		0.64	220	220	220

❑ operation in vicinity of thermal equilibrium still significantly reduces IBS heating

$$\frac{d\varepsilon}{dt} \sim \left(\frac{Z^2}{A}\right)^2 \cdot N_i \cdot L_c \cdot \frac{1}{\beta^2 \gamma^4} \cdot \frac{1}{\sigma_x \sigma_y \sigma_s}$$

Fast grows of the beam phase volume due to **Intra-Beam Scattering**:

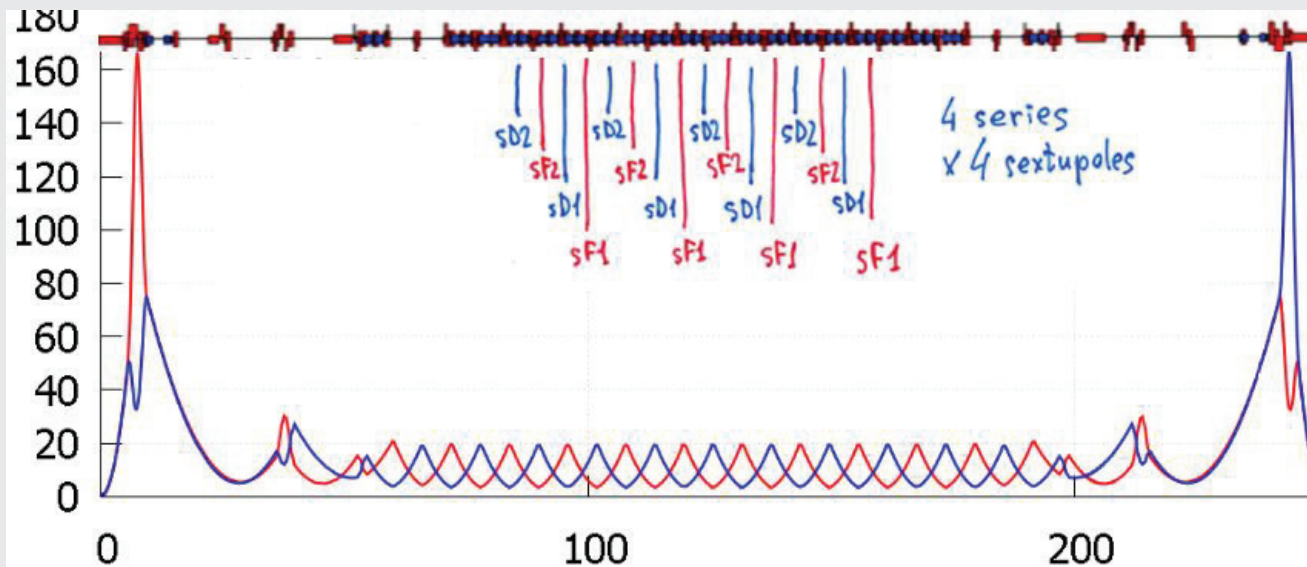
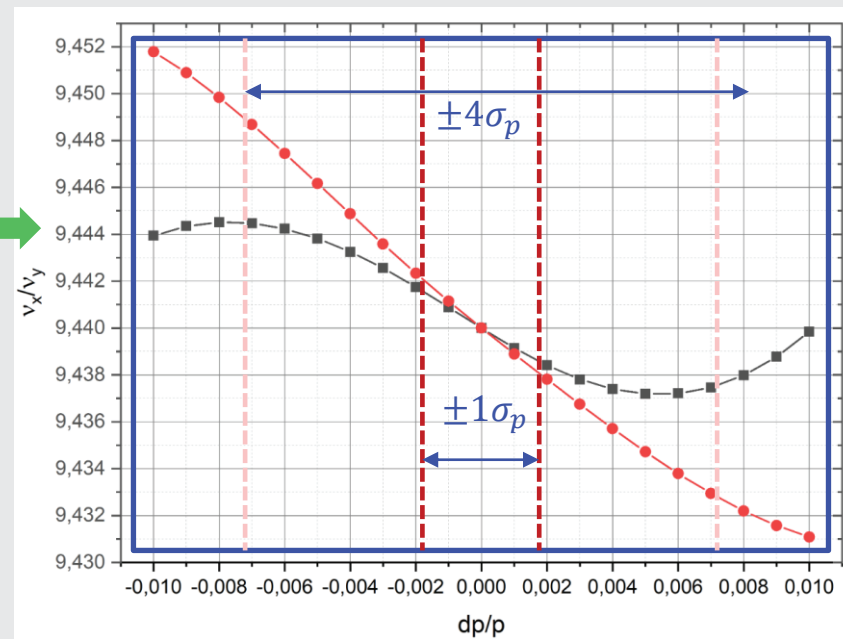
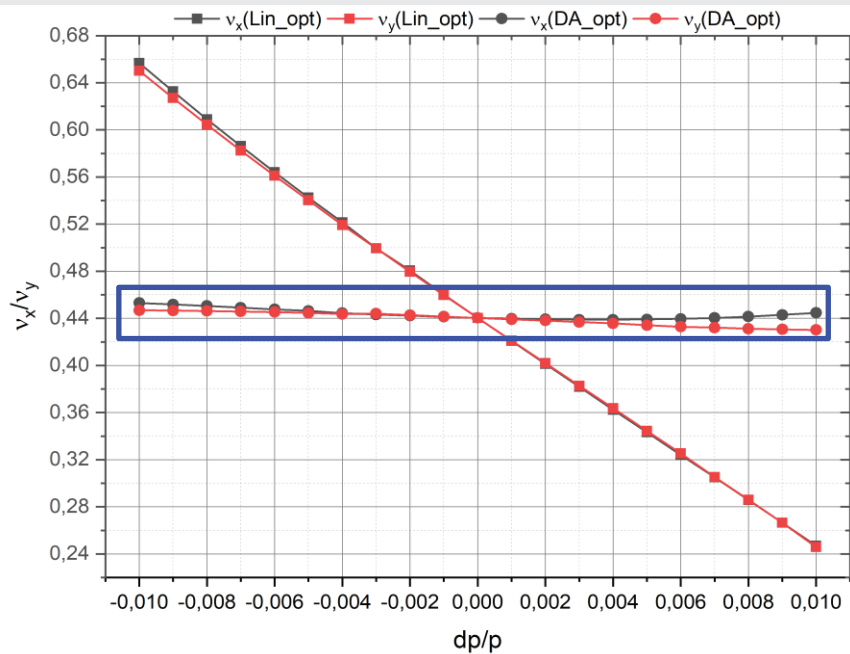
RHIC ~ 4 h

LHC >> 10 h

NICA 3 ÷ 30 minutes → Beam cooling during experiment is mandatory

Requirements to cooling systems

Collider non-linearities 1



$sF1 = -47 \text{ T/m}^2$
 $sD1 = 11 \text{ T/m}^2$

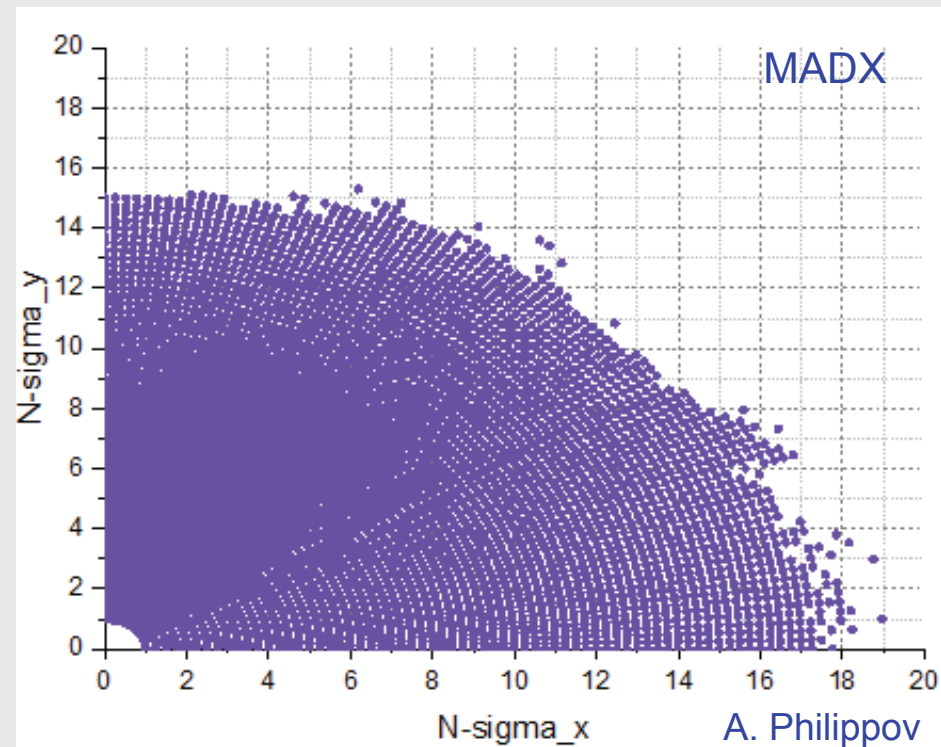
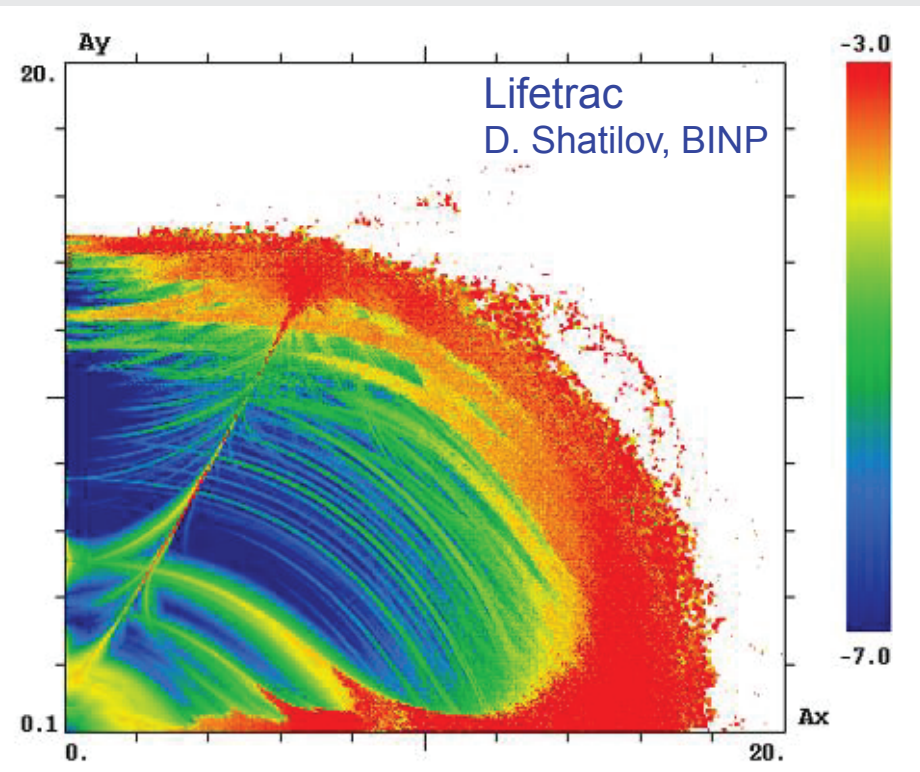
$sF2 = -48 \text{ T/m}^2$
 $sD2 = 10 \text{ T/m}^2$

DA ??

DA

Linear
optics

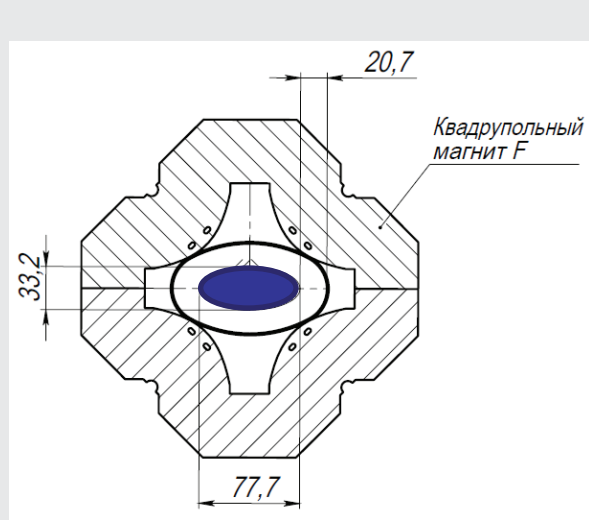
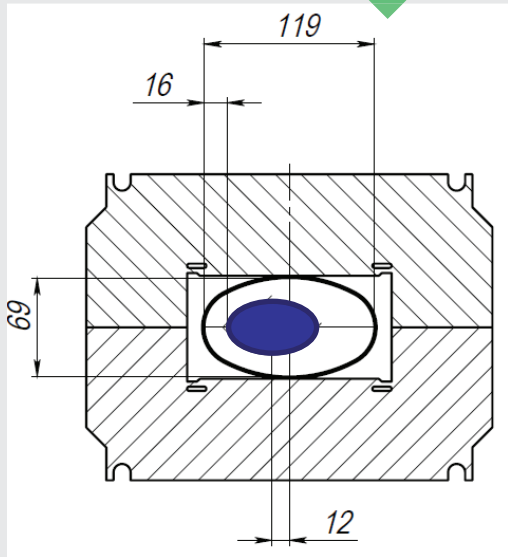
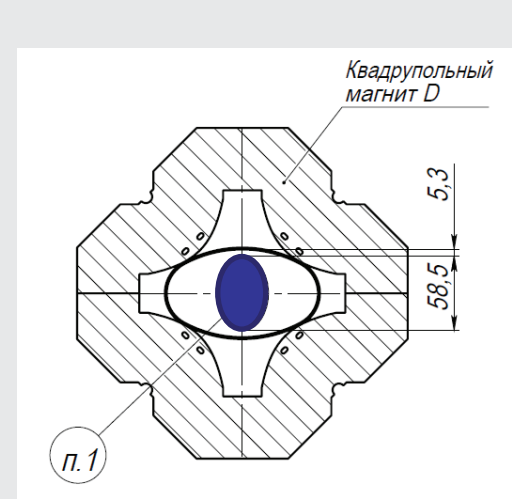
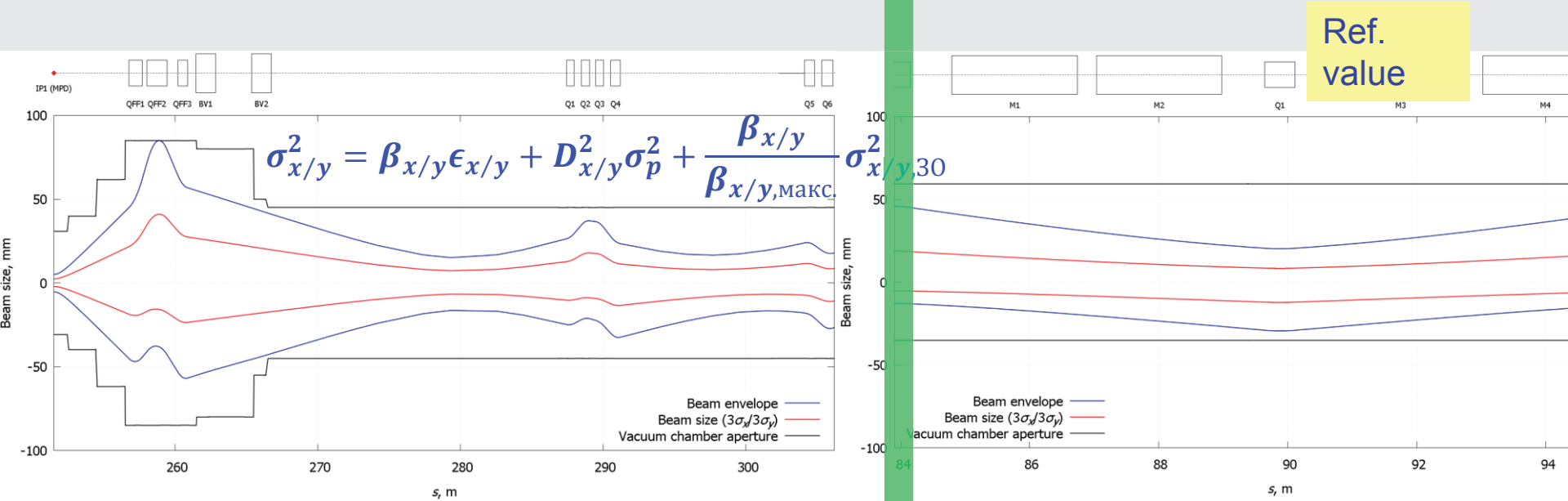
chromaticity correction

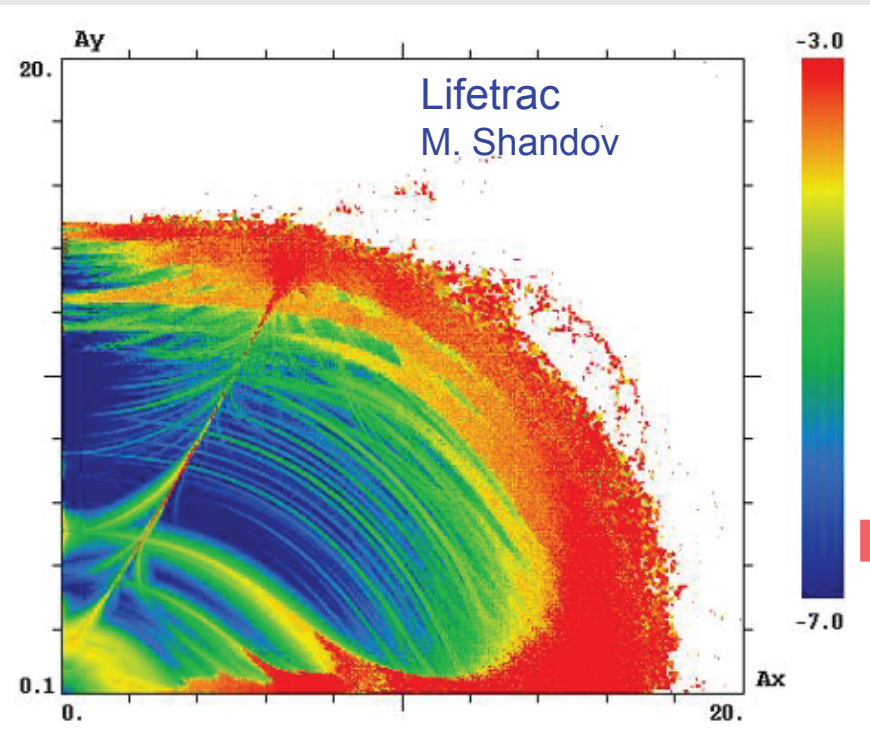


$$DA \approx 16 \div 18 \sigma$$

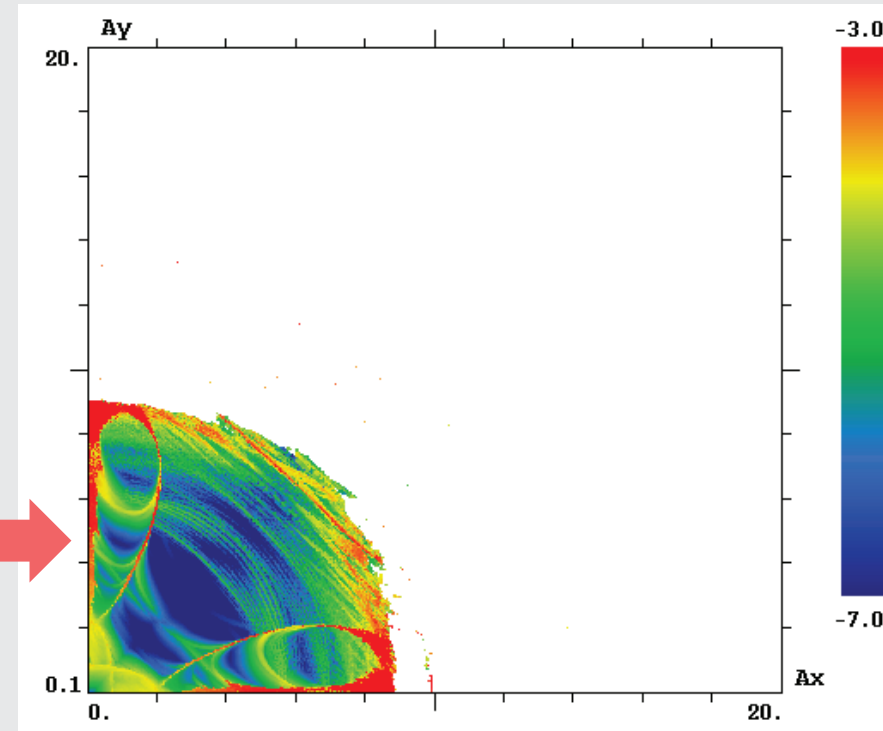
• Transverse beam size

$E, \text{GeV/u}$	$N, 10^9$	$\varepsilon_x, \pi \text{ mm} \cdot \text{mrad}$	$\varepsilon_y, \pi \text{ mm} \cdot \text{mrad}$	σ_s, m	$\sigma_p, 10^{-3}$	τ_x, S	τ_y, S	τ_s, S
4.5	2.8	1.1	0.82	0.6	1.73	Intra-Beam Scattering		
3	2.71		0.95		1.31			
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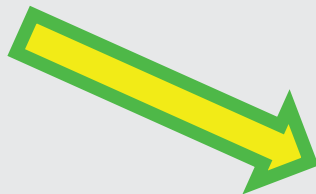


$$DA \approx 16 \div 18 \sigma$$



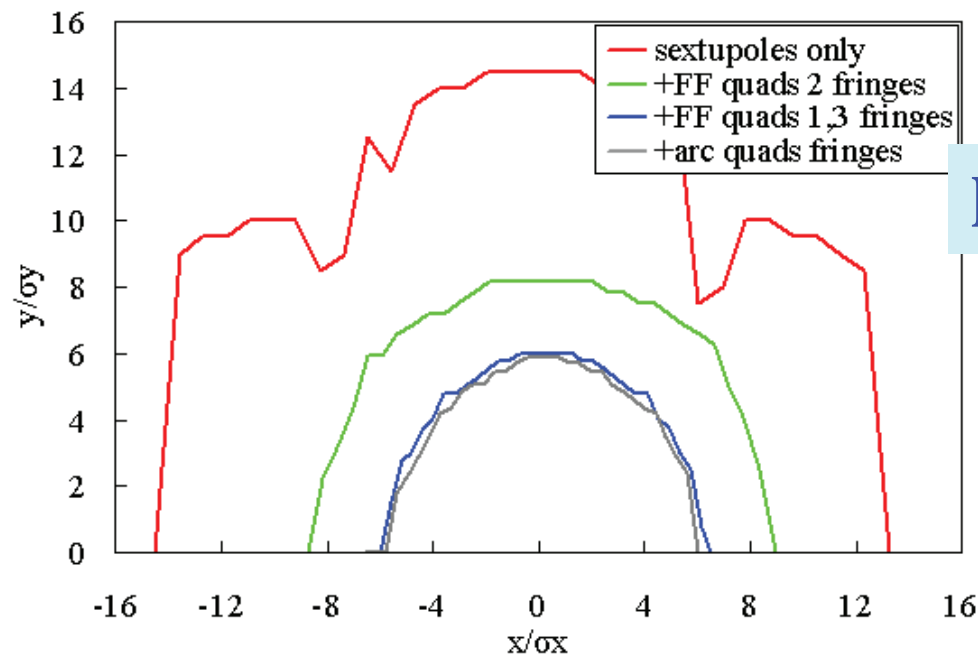
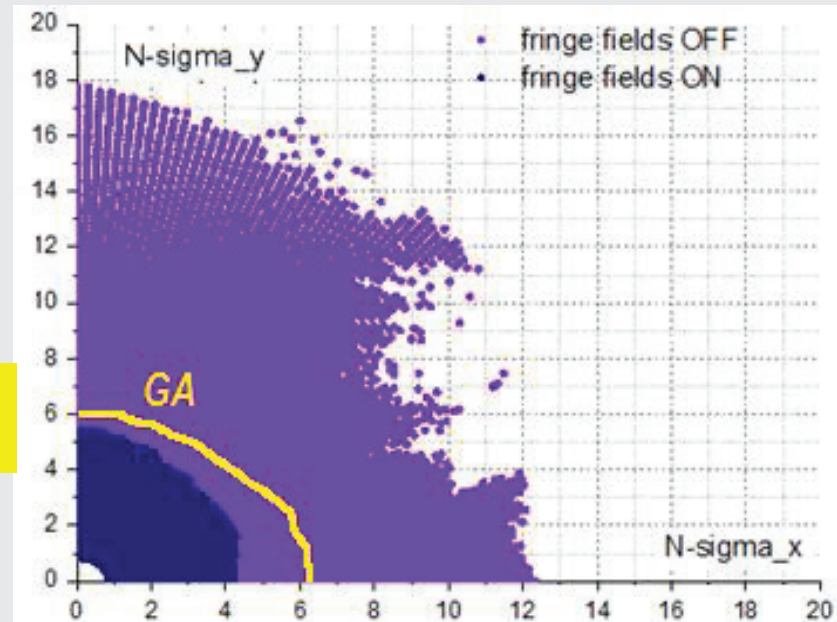
$$DA \approx 8 \div 9 \sigma$$

FF-quads fringe fields shrink DA



Initially designed

$$\beta^* = 0.35 \text{ m}$$



$$DA \approx 4 \div 5 \sigma$$

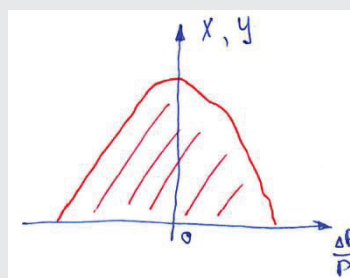
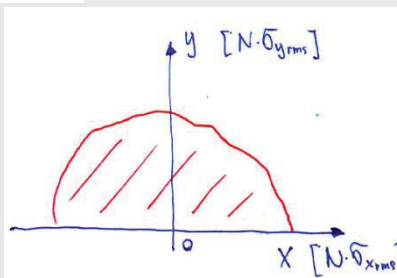


$$\beta^* = 0.35 \text{ m}$$

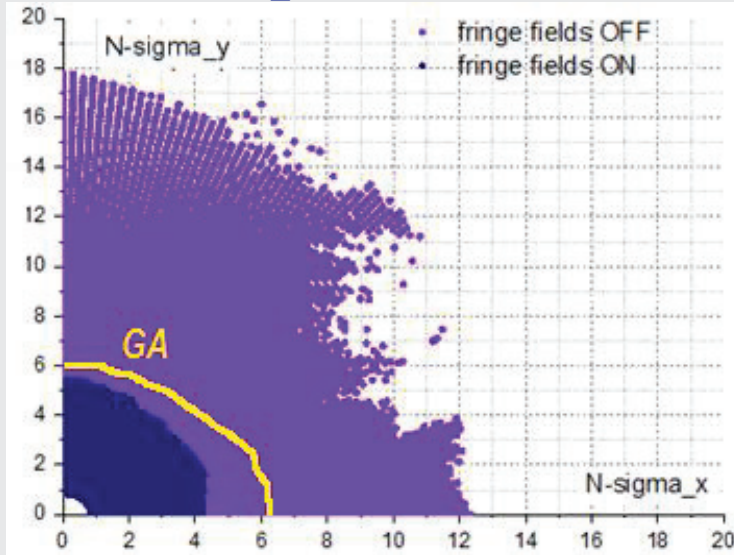


$$\beta^* = 0.60 \text{ m}$$

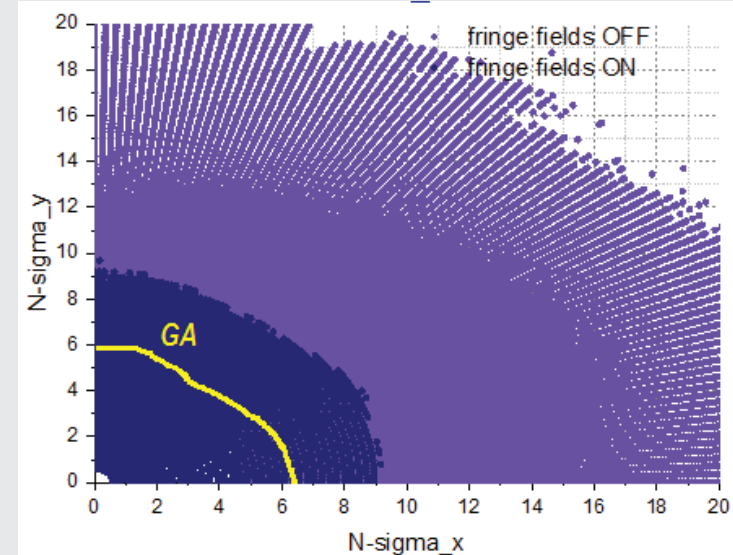
S.A. Glukhov, E.B. Levichev,
RuPAC-2016



Beta_IP=0.35 m



Beta_IP=0.60 m



$$L = \frac{f_0 n_b N_i^2}{4\pi\beta^* \sqrt{\epsilon_x \epsilon_y}} H\left(\frac{\sigma_s}{\beta^*}\right)$$

25 % luminosity decrease

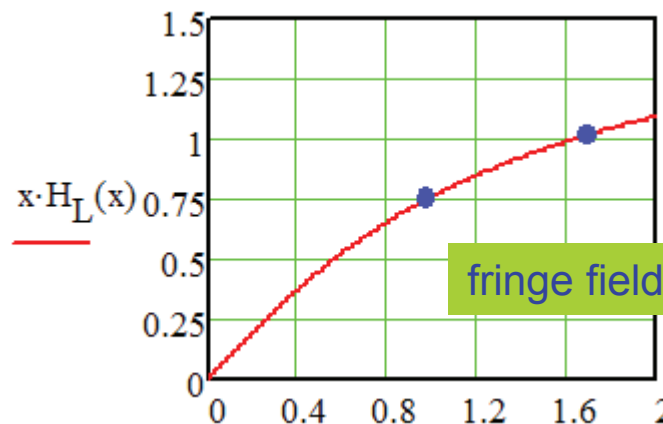
$$\beta^* = 0.35 \text{ m}$$

$$\frac{\sigma_s}{\beta_{IP}} \cdot H_L\left(\frac{\sigma_s}{\beta_{IP}}\right) = 1.02$$

$$L = \frac{\sqrt{2\pi} A \beta^2 \gamma^3}{r_p Z^2} \frac{f_0 N_i}{(C/n_b)} \left(\frac{\sigma_s}{\beta^*} H\left(\frac{\sigma_s}{\beta^*}\right) \right) \delta v_{SC}$$

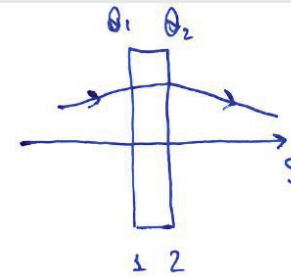
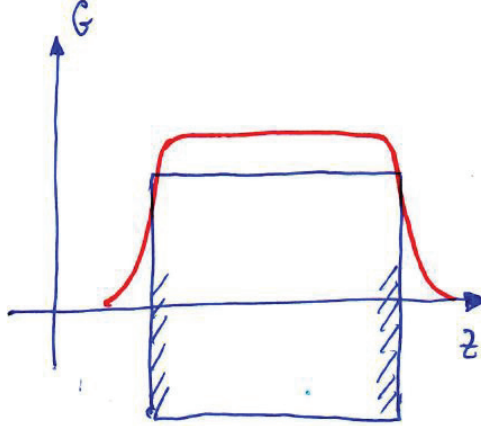
$$\beta^* = 0.60 \text{ m}$$

$$\frac{\sigma_s}{\beta_{IP}} \cdot H_L\left(\frac{\sigma_s}{\beta_{IP}}\right) = 0.758$$



fringe field effect need to be corrected

Quadrupoles' fringe field effect



монка

мунга:

$$\Delta X = \Delta Y$$

$$\Delta P_x = \Delta P_{x_2} + \Delta P_{x_1} =$$

$$= \frac{k_1}{4} \left[(x^2 + y^2) (\underbrace{P_{x_2} - P_{x_1}}_{\theta_{x_2} - \theta_{x_1}}) - 2xy (\underbrace{P_{y_2} - P_{y_1}}_{\theta_{y_2} - \theta_{y_1}}) \right] =$$

$$= \frac{k_1}{4} \left[-(x^2 + y^2) \frac{x}{F} - 2xy \frac{y}{F} \right] =$$

$$= \frac{k_1^2 L}{4} \left[-x(x^2 + y^2) - 2xy^2 \right] = -\frac{x k_1^2 L}{4} (x^2 + 3y^2)$$

even $y \approx 0$

$$\Delta P_x \approx \Delta \left(\frac{dX}{ds} \right) \approx \Delta \theta_x = -\frac{k_1^2 L}{4} x^3$$

$$\frac{\Delta \theta_x}{\theta_x} = \frac{\Delta \theta_x}{\sqrt{\frac{\epsilon}{\beta_x}}} = -\sqrt{\frac{\beta_x}{\epsilon}} \frac{k_1^2 L}{4} (\sqrt{\epsilon \beta_x})^3 = \boxed{-\frac{1}{4} \beta \cdot \epsilon \cdot L \cdot k_1^2}$$

$$\psi(x, y, z) =$$

$$= -G(z) \cdot x \cdot y + \frac{x^3 y + x y^3}{12} \cdot \frac{d^2}{dz^2} G(z)$$

Второй/третий б мунга (F)

$$\Delta X = \pm \frac{k_1}{12} (x^3 + 3xy^2)$$

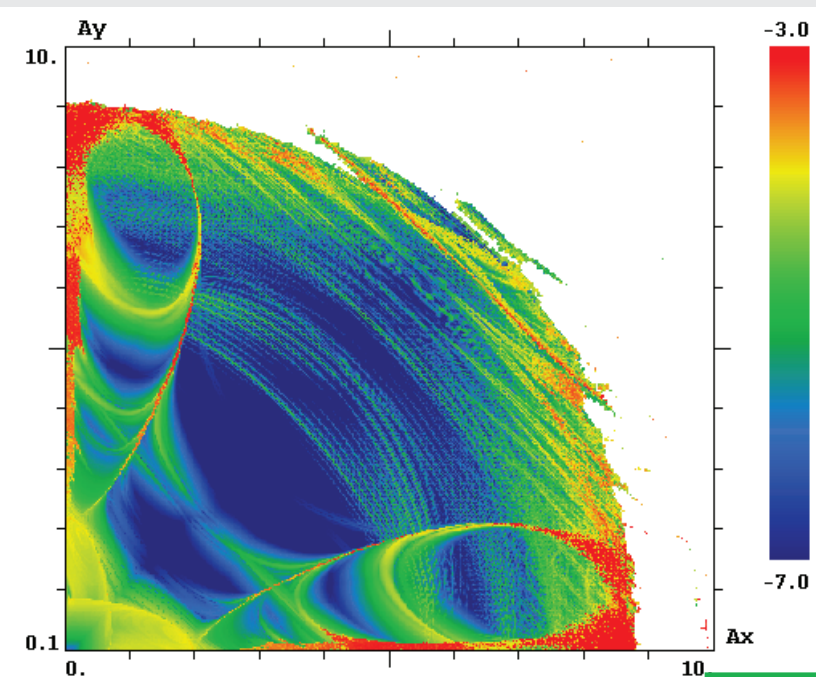
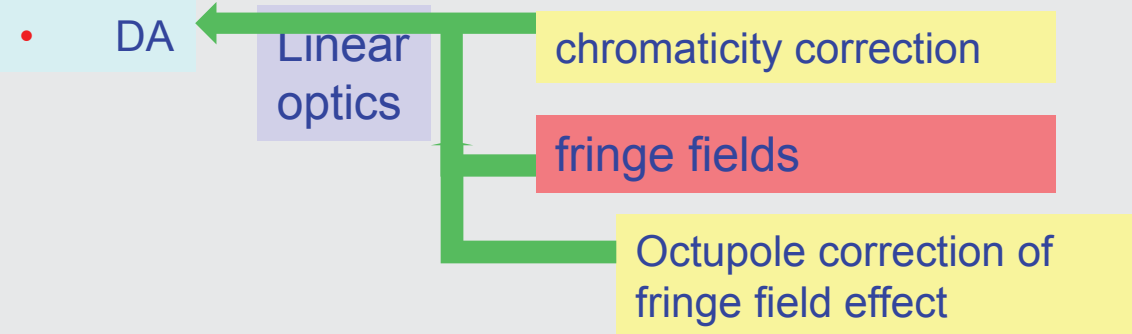
$$\Delta P_x = \pm \frac{k_1}{4} [(x^2 + y^2) P_x - 2xy P_y]$$

$$\Delta Y = \pm \frac{k_1}{12} (y^3 + 3x^2 y)$$

$$\Delta P_y = \pm \frac{k_1}{4} [(x^2 + y^2) P_y - 2xy P_x]$$

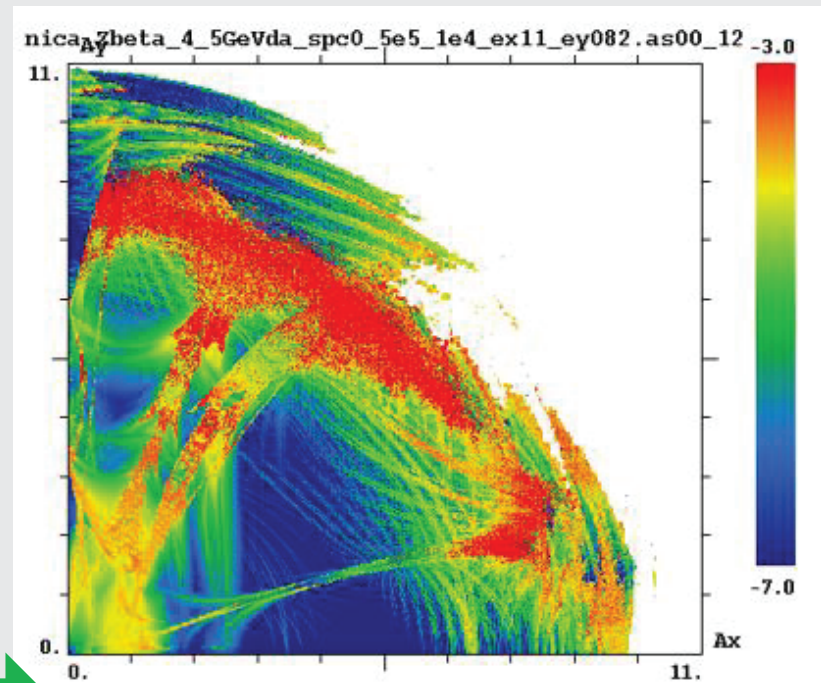
	β , [m]	k_1 , [1/m ²]	L, [m]	$\epsilon \cdot 10^{-6}$ [m ² rad]	ff-effect
LHC	235	0,0084	5,5	2	0,05
RHIC	145	0,052	3,4	1	0,4
NICA	120	0,4	1,65	1	7,9

In NICA effect 2-3 orders stronger due to "lower" energy range



DA $\approx 8 \div 9 \sigma$

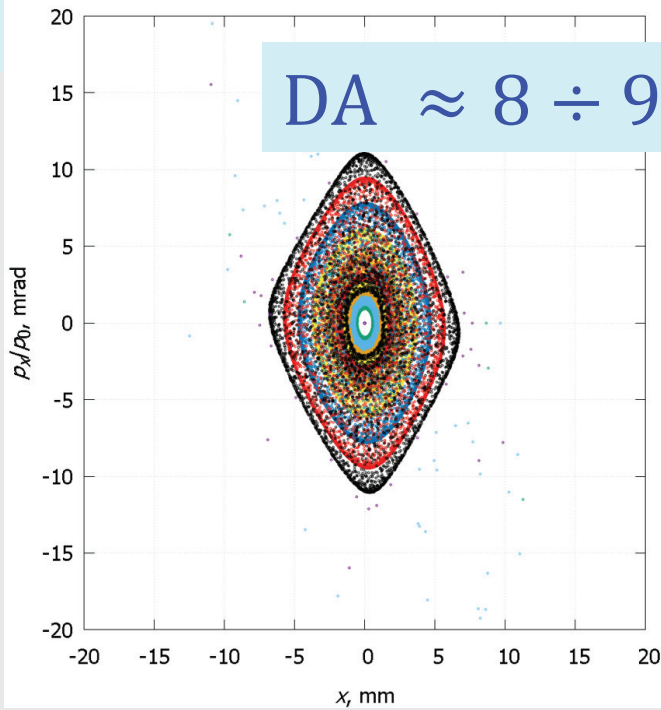
Octupole correction



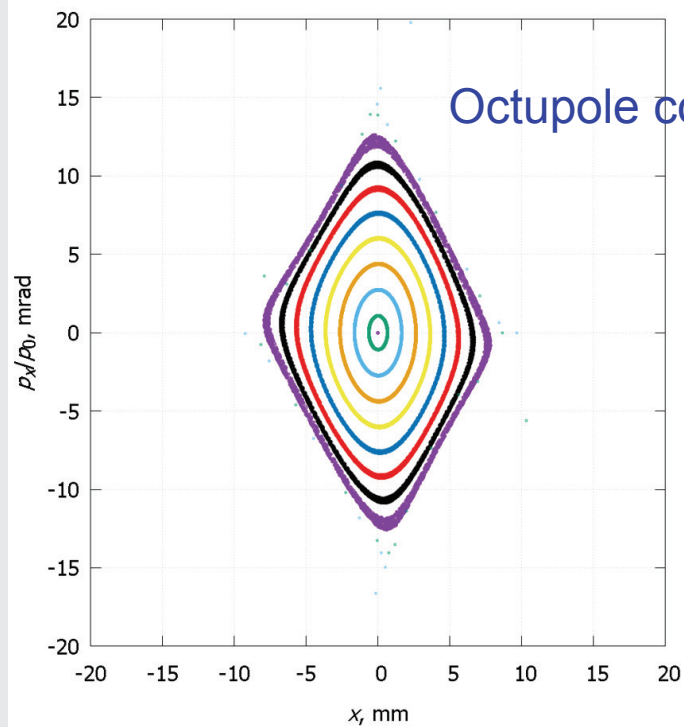
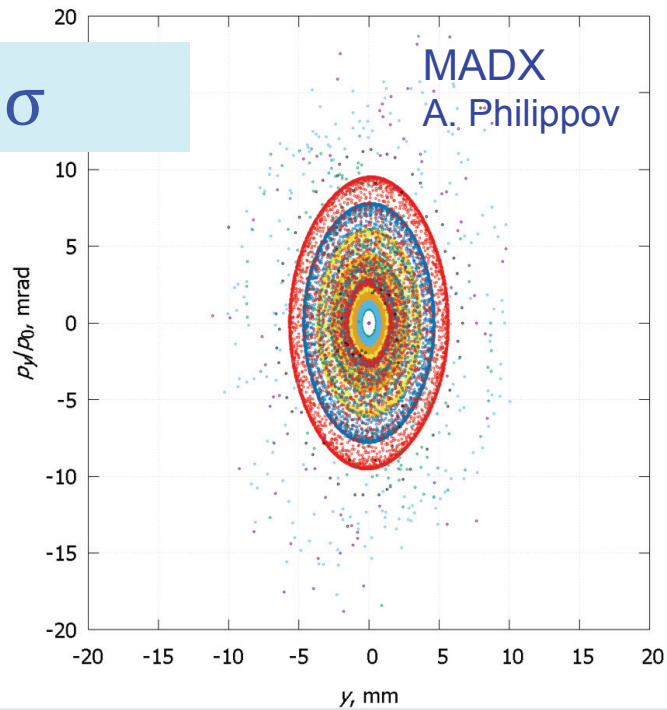
DA $\approx 10 \div 11 \sigma$

DA

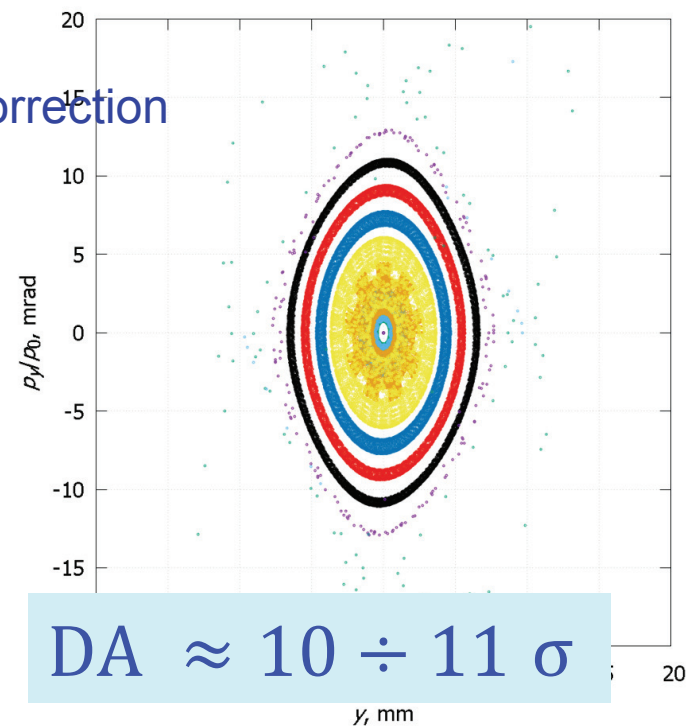
$$DA \approx 8 \div 9 \sigma$$



MADX
A. Philippov

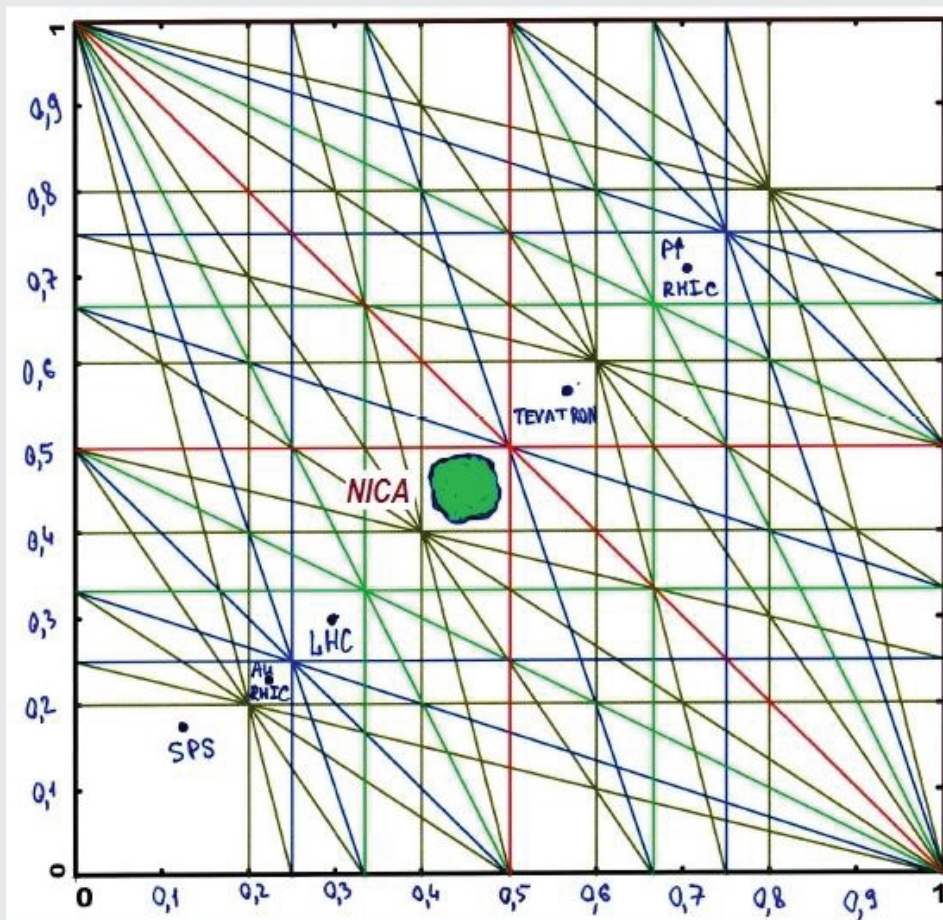


Octupole correction



$$DA \approx 10 \div 11 \sigma$$

Ring tune

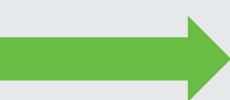


ideal if
= **const** for all
particles in the
beam

$$Q = Q_0 + \delta Q_{sc} + \delta Q_{bb} + \xi_1 \frac{\delta p}{p} + \xi_2 \left(\frac{\delta p}{p} \right)^2$$

$$\Delta Q < 0,05$$

- ☐ self space charge effect
- ☐ beam-beam effect
- ☐ tunes vs dp/p :



$$F_b = \frac{C}{\sqrt{2\pi}\sigma_s}$$

□ Space charge

The bunch brightness N_b/ϵ is limited by two main space charge effects:

$$\Delta Q = \Delta Q_L + 2 \Delta Q_{BB}$$

□ shift of the betatron tune due to action of beam self space charge field (Laslett tune shift)

$$\Delta Q = -\frac{Z^2 r_p}{A} \frac{N_b}{4\pi\epsilon\beta^2\gamma^3} F_b \quad (\text{for round beam and smooth focusing})$$

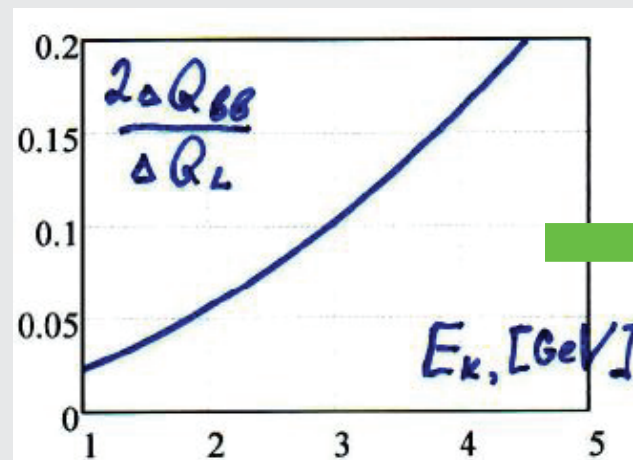
$$F_b = \frac{C}{\sqrt{2\pi}\sigma_s} \quad - \text{bunching factor}$$

□ shift of the betatron tune due to action of the colliding bunch field (beam-beam parameter)

$$\xi = \frac{Z^2 r_p}{A} \frac{N_b}{4\pi\epsilon\beta^2\gamma} \frac{1 + \beta^2}{2}$$

$$\delta Q_{BB} = \delta Q_L \sqrt{\frac{\pi}{2}} \frac{\sigma_s}{C} \gamma^2 (1 + \beta^2)$$

For NICA collider parameters



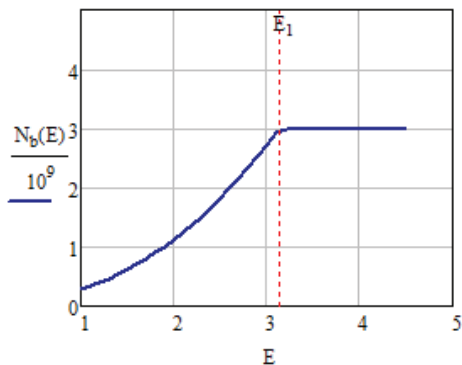


$$\Delta Q \approx \Delta Q_L$$

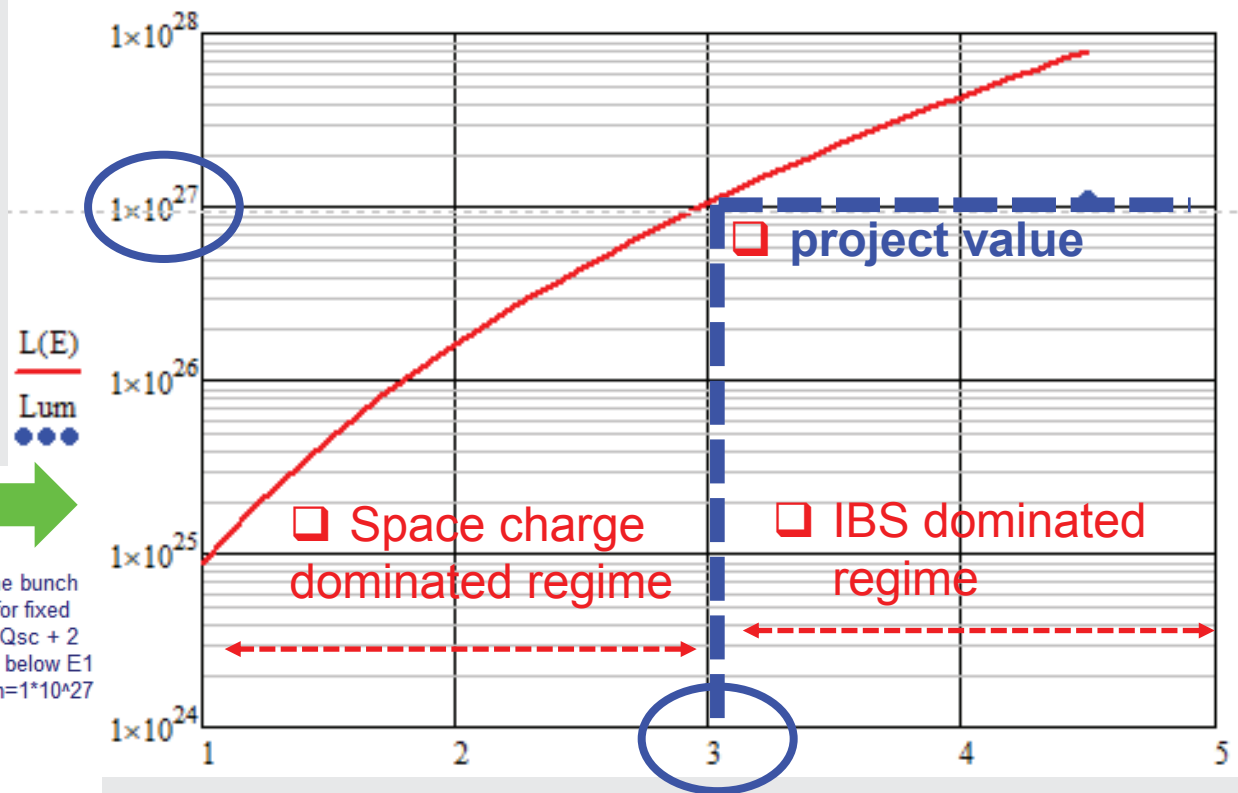
$\Delta Q \leq 0,05$
 $\rightarrow \delta Q_L = \frac{r_p Z^2 N_i}{4\pi A \beta^2 \gamma^3 \varepsilon} \frac{C}{\sqrt{2\pi} \sigma_s}$
 $\rightarrow L = \frac{f_0 n_b N_i^2}{4\pi \beta^* \sqrt{\varepsilon_x \varepsilon_y}} H\left(\frac{\sigma_s}{\beta^*}\right)$

$$L = 8\pi^2 \frac{A^2 c \beta^5 \gamma^6}{Z^4 r_p^2} \frac{n_b \sigma_s \varepsilon}{C^3} \left(\frac{\sigma_s}{\beta^*} H\left(\frac{\sigma_s}{\beta^*}\right) \right) \delta v_{sc}^2 \xrightarrow{C \propto \beta \gamma} \propto \beta^2 \gamma^3$$

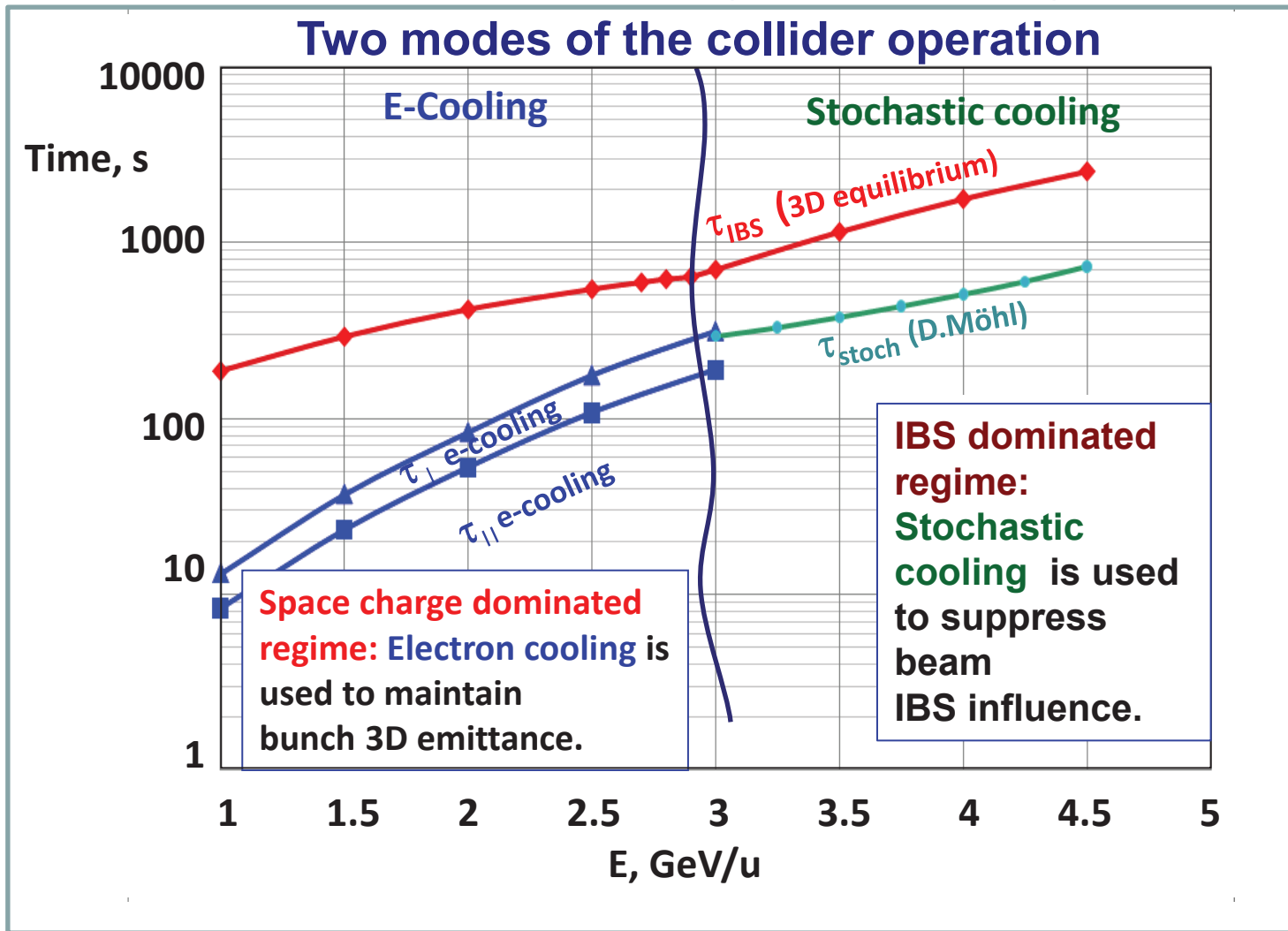
The beam **space charge** creates the **major luminosity limitation**



N-ions in the bunch
 via energy for fixed
 $\Delta Q = \Delta Q_{sc} + 2$
 $\Delta Q_{bb} = 0.05$ below E_1
 and for $Lum = 1 \cdot 10^{27}$
 above E_1



Beam Maintenance in Collider Rings with Cooling Technique



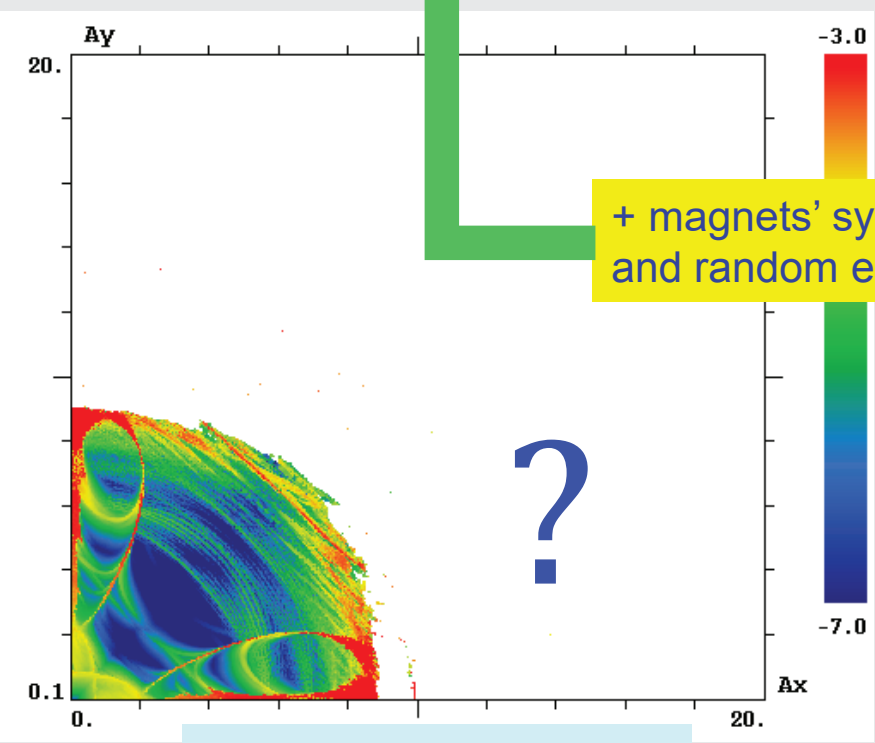
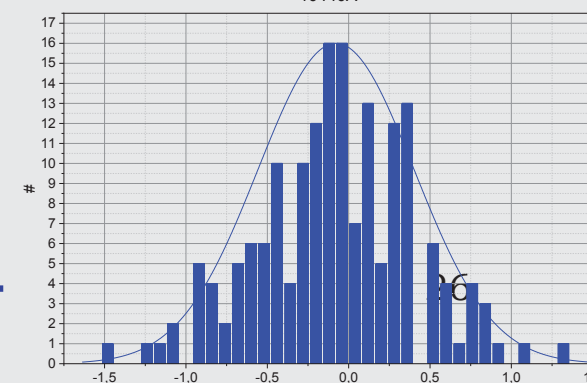
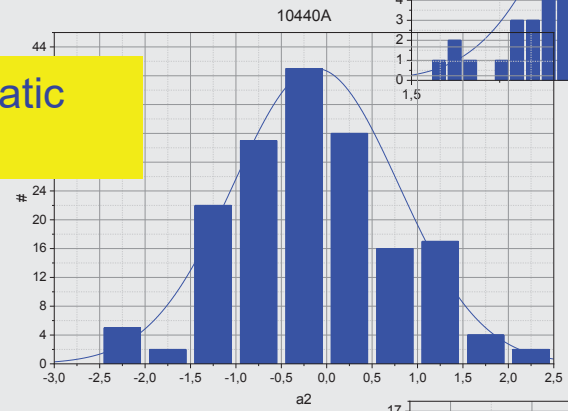
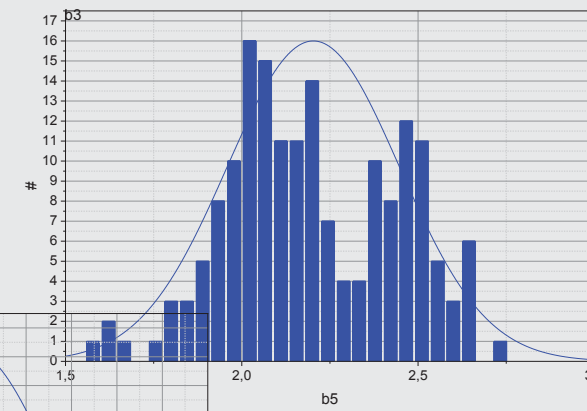
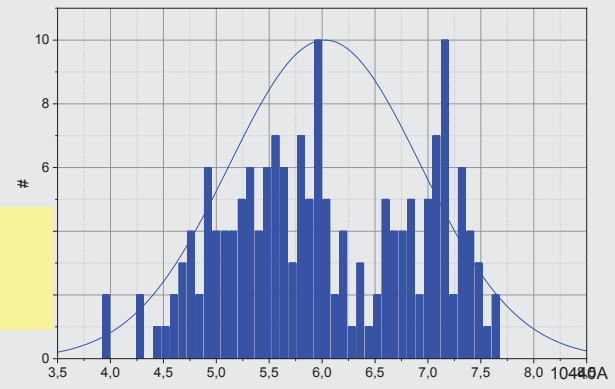
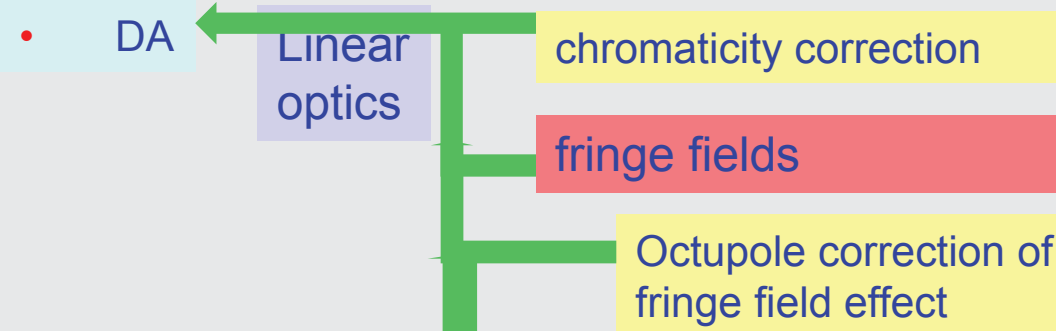
Space charge dominated mode ($\Delta Q \leq 0.05$)

ϵ and dp/p are optimized independently. The bunch relaxation? is suppressed by cooling. Luminosity is limited by space charge effects

IBS dominated mode

ϵ and dp/p are “equi-partitioned”, either fast bunch relaxation. Luminosity can be obtained at small $\Delta Q < 0.05$

I.N. Meshkov



+ magnets' systematic and random errors

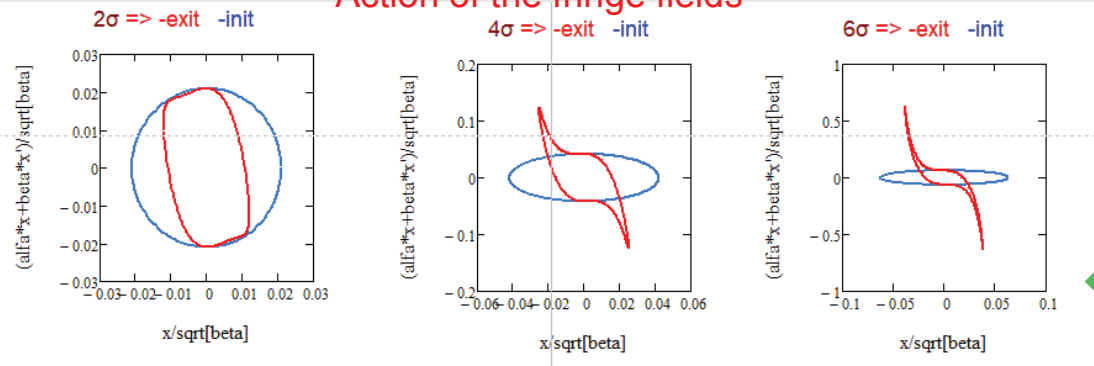
DA $\approx 8 \div 9 \sigma$ need to be checked...

DA

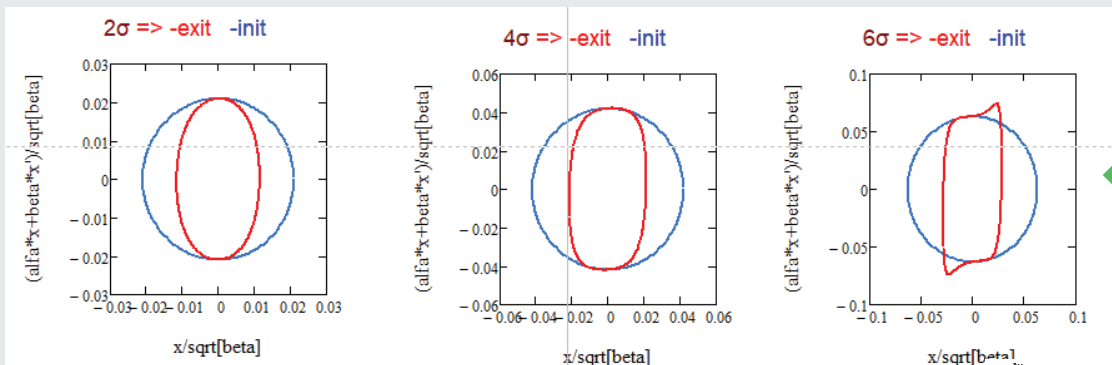
to be solved:

how calculate mitigation scheme
for main DA limitation factor ?

Action of the fringe fields

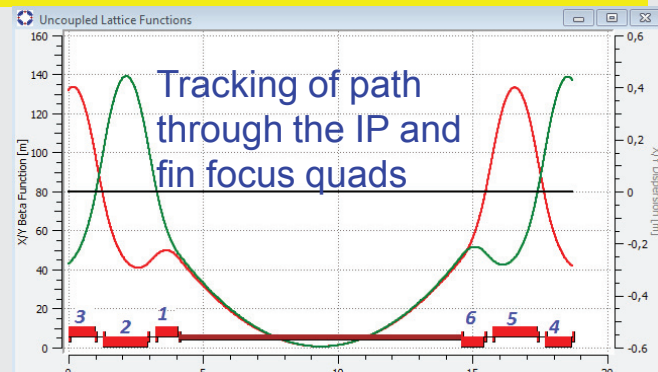


Distortion of the phase space



Fringe fields + octupoles

Magnets' fringe fields

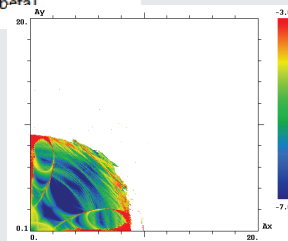


$$\text{Edge}(X, k_0) := \begin{cases} Y_0 \leftarrow X_0 + \frac{k_0}{12} \cdot \left[(X_0)^3 + 3 \cdot (X_2)^2 \cdot X_0 \right] \\ Y_1 \leftarrow X_1 + \frac{k_0}{4} \cdot \left[2 \cdot X_0 \cdot X_2 \cdot X_3 - \left[(X_0)^2 + (X_2)^2 \right] \cdot X_1 \right] \\ Y_2 \leftarrow X_2 - \frac{k_0}{12} \cdot \left[(X_2)^3 + 3 \cdot (X_0)^2 \cdot X_2 \right] \\ Y_3 \leftarrow X_3 - \frac{k_0}{4} \cdot \left[2 \cdot X_0 \cdot X_2 \cdot X_1 - \left[(X_0)^2 + (X_2)^2 \right] \cdot X_3 \right] \\ Y \end{cases}$$

$$\text{TrOct}(V, k3dL) := \begin{cases} k3dL \leftarrow k3dL \\ V_{f0} \leftarrow V_0 \\ V_{f1} \leftarrow V_1 - \frac{(k3dL) \cdot \left[(V_0)^3 - 3 \cdot (V_0) \cdot (V_2)^2 \right]}{6} \\ V_{f2} \leftarrow V_2 \\ V_{f3} \leftarrow V_3 - \frac{(k3dL) \cdot \left[(V_2)^3 - 3 \cdot (V_0)^2 \cdot (V_2) \right]}{6} \\ V_{f4} \leftarrow V_4 \\ V_{f5} \leftarrow V_5 \\ V_f \end{cases}$$

...seems better but did not confirmed by

yet...





Thank you