AN ULTRA LOW NOISE AC BEAM TRANSFORMER FOR DECELERATION AND DIAGNOSTICS OF LOW INTENSITY BEAMS.

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Abstract

The design of a broad band ultra-low noise ferrite loaded AC beam transformer is presented. It is designed for use in the CERN Antiproton Decelerator [1] (AD), where beams of a few 10⁷ charges must be decelerated from 3.5 GeV/c to 100 MeV/c. It is used in the RF beam-phase loop, and for intensity and bunch shape measurements during deceleration. When the beam is debunched for cooling on magnetic flat tops, the pick-up is used for measurements of intensity and momentum distribution by means of longitudinal Schottky scans. When used as Schottky pick-up, the signal to noise ratio should be better by about 40 dB than the existing stripline based longitudinal Schottky pick-up. The integrated design of pick-up and associated low-noise amplifier is presented. The achieved noise performance of a few pA/\sqrt{Hz} from

1 to 3 MHz is obtained by attaching a low-noise, highimpedance silicon JFET (junction field effect transistor) amplifier to a high-Q resonant ferrite loaded cavity, and then eliminating the resonant response by low-noise RF feedback such that broad band response over almost 2 decades of frequency (0.3 - 15 MHz) is obtained. The longitudinal coupling impedance is close to 10 Ω in this frequency range, and the equivalent noise temperature of this resistance is about 0.4 °K mid-band although all components operate at ambient temperature. Finally the application of a similar design for single-pass bunch intensity measurements is discussed.

1 INTRODUCTION

The DC beam currents in the CERN AD (typically 0.2 to 15 μ A with antiprotons) are too low to be measured with a DC beam transformer. Beam intensity is therefore measured by RF beam current measurements when the beam is bunched and longitudinal Schottky scans when the beam is debunched. The range of RF frequencies is 0.17 to 1.6 MHz, so to measure these quantities as well as bunch lengths an ultra-low noise AC beam transformer with a bandwidth from 0.1 to 15 MHz is required.

2 BEAM TRANSFORMER AND HEAD AMPLIFIER

The AC beam transformer consists of a ferrite loaded cavity with a ceramic gap in the beam pipe, a secondary winding of one additional turn (the cavity enclosure forms the first turn), and a low noise head amplifier with feedback connected to the secondary winding and mounted close to the cavity, Figure 1.



Figure 1. Ferrite loaded beam transformer and amplifier

A noise free amplifier cannot reduce noise already introduced by the pick-up itself, so the pick-up is made resonant with high Q to reduce this noise. The whole device is doubly shielded: an outer cavity (7 mm copper walls) surrounds the head amplifier and the inner cavity (also 7 mm copper), which contains the ferrite, the ceramic gap and the secondary winding and is assembled by e-beam welding to avoid RF contacts.

2.1 Transformer and Amplifier Noise Sources

It is easier and more transparent to characterise the noise properties of the amplifier [2] in terms of equivalent current and voltage noise sources and their dependence on frequency, device type and bias rather than noise figure which is often confusing.



Figure 2: Equivalent circuit and noise sources

The equivalent circuit for the resonant step-up transformer and its head amplifier is shown on Figure 2.

Here N is transformer step-up ratio, I_b the desired signal, V_{na} [V/ $\sqrt{\text{Hz}}$] and I_{na} [A/ $\sqrt{\text{Hz}}$] amplifier voltage and current noise, C_p and C_s primary and secondary capacities of the transformer, C_a amplifier input capacity, L_p primary inductance, and G amplifier gain. The Johnson noise I_{nth} of the shunt impedance R_p (~ 9 k Ω) is:

$$I_{nth} = \sqrt{4kT / R_p} \tag{1}$$

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where k [J/°K] is Boltzman's constant and T [°K] the absolute temperature.

The secondary circuit quantities can all be transformed to the primary circuit, Figure 3. Increasing N lowers voltage noise, but increases current noise and capacity.



Figure 3: Noise sources transformed to primary

The amplifier voltage noise V_{nd}/N can be transformed into an equivalent current noise I_{vna} by the relation:

$$I_{vna} = V_{na} / (NZ_{pu}) \tag{2}$$

where Z_{pu} is the primary pick-up impedance. If the 3 noise currents are uncorrelated (not quite true for I_a and V_{na}), they add as sum of the squares, and the total equivalent, input-noise current $I_{n,in}$ becomes:

$$I_{n,in} = \sqrt{I_{nth}^2 + (NI_a)^2 + (V_{na} / NZ_{pu})^2}$$
(3)

There is an optimum value of N at a given frequency as amplifier current noise can be traded for voltage noise. If the amplifier noise is small, the total noise is dominated by the shunt impedance noise.

2.2 Amplifier Design

While bipolar transistors may have low voltage noise, the current noise at low frequencies $f \ll f_T$ is much larger than for FETs (field effect transistors) due to the electronic shot (Schottky) noise I_s :

$$I_s = \sqrt{2qI_{base}} \quad [A/\sqrt{Hz}] \tag{4}$$

where q is the elementary charge and I_{base} the DC base bias current. A FET has an input voltage noise [3] closely related to the Johnson noise of the conducting channel:

$$V_n = \sqrt{8kT/3g_m} \quad [V/\sqrt{Hz}]$$
 (5)

where g_m is the transconductance [A/V], and an input current noise which is proportional to frequency:

$$I_n = \omega C_c V_n \left[A / \sqrt{Hz} \right]$$
(6)

where C_c is the coupling capacitance, which is about 2/3 of the total gate to channel capacity C_{gs} . Due to the very low gate bias current, the Schottky noise can usually be neglected. It is always possible to lower the noise voltage by connecting several transistors in parallel (square root dependence), but this will of course increase the noise current in the same ratio. This is similar to the noise matching obtained with the step-up transformer discussed in the previous subsection. The noise quality (lowest current noise for a given voltage noise) is therefore given by the ratio g_m/C_{gs} , which is also the high

frequency figure of merit f_T . At frequencies below a certain corner frequency, all devices exhibit 1/f noise or flicker noise, where noise spectral densities higher than V_n given above (5) are observed.

The different types of FET transistors which may be considered [4] are: i) GaAs (Gallium Arsenide) MESFET: very high f_T (typically 15-25 GHz), but also high 1/f corner frequency: > 10 MHz typically, ii) Si (silicon) dual gate MOSFET: lower f_T (typically. 5 GHz), but somewhat better 1/f corner frequency: 1 - 5 MHz, iii) Si JFET: still lower f_T (typically 2 GHz), but much lower 1/f corner frequency: typically 10 Hz for Philips BF861C.

For the frequency range of interest (0.1 to 20 MHz), Si JFET's will be the best choice due to the low 1/f corner frequency. Although monolithic amplifiers with JFET inputs are available, none of them have sufficiently low voltage noise and propagation delay ($t_d \le 5$ ns required for feedback stability) and an amplifier has therefore been designed with discrete SMD components.



Figure 4: Low noise wide band amplifier

The conceptual design (bias details omitted) of the low noise, wide bandwidth feedback amplifier with an overall gain of 300 and a propagation delay of 5 ns (bandwidth 75 MHz) is shown on Figure 4. The input stage with a gain of 11 consists of 16 parallel Si JFETs with each group of 4 forming a cascode with a bipolar transistor with high f_T (8 GHz). The JFETs are operating near their maximum current at 10 mA (for high g_m and low V_n) and the bipolar transistors near their optimum current of 40 mA. This results in a low input voltage noise (theory $0.22 \text{ nV}/\sqrt{\text{Hz}}$, achieved $0.28 \text{ nV}/\sqrt{\text{Hz}}$), and a very small propagation delay: < 1 ns.

The output stage is a current mode feedback op-amp with very high slew rate (2.5 kV/ μ s) and voltage swing (20 V_{pp}) capable of driving the low impedance feedback circuitry. The bipolar second stage provides the extra gain to prevent the rather noisy output stage from contributing to the noise. For this amplifier design, the equivalent, input-noise current sources are shown on Figure 5. The cavity shunt impedance noise (~1.5 pA/ \sqrt{Hz}) dominates from 1.5 to 3.5 MHz, and corresponds to a noise temperature of 0.4 °K of a 10 Ω resistor. The longitudinal Schottky noise current densities for the AD are typically 4 to 500 pA/ \sqrt{Hz} around 1.6 MHz and lower at higher frequencies as the width of the Schottky bands are

proportional to the harmonic while the total power in each Schottky band is constant.



Figure 5: Equivalent, input-noise current sources (at gap)

2.3 Feedback Resistor and Circuits

Although the resonant high Q transformer with amplifier has a very good signal to noise ratio, the response is highly resonant ($Q \sim 120$, $f_r \sim 2$ MHz) and the amplifier will saturate for very small currents near the resonance. The response can be made broad band if a current feedback resistor is introduced around the amplifier, Figure 6. This converts the amplifier input impedance into a low resistive impedance $R_{fb}/G \sim 40 \Omega$, or $R_{fb}/(GN^2)$ ~10 Ω referred to primary and the response becomes broad band with 3 dB frequencies of 0.3 and 15 MHz and a loop gain at resonance about 60 dB.



Figure 6: Equivalent circuit with current feedback

However, unless the feedback resistor and the gain are made very large ($R_{fb} > 0.4 \text{ M}\Omega$, G > 10'000), the noise of the feedback resistor will contribute significantly to (or even dominate) the noise. A large feedback resistor is difficult to implement at high frequencies, the amplifier will still saturate at very low currents, and large gain with short delay is difficult.



Figure 7: Low noise feedback 'resistor'

By passing the feedback signal through an integrator and injecting the feedback current through a small capacitor the equivalent feedback transfer function is still that of a resistor, Figure 7. For R_{int} small and $C_{int} >> C_{fb}$, the effective noise temperature T_{noise} of the feedback resistor is low: 15 °K for $R_{fb} = 12 \text{ k}\Omega$, or a current noise corresponding to a 240 k Ω resistor. The dynamic range is much increased (saturation for $I_b = 1.6$ mA) with only a very small increase in noise level.

2.4 Low Frequency Version

The low frequency response cut-off frequency (0.3 MHz) can be lowered by an appropriate integrating correcting network in the feedback amplifier, but the low frequency noise current is unchanged: limited by inductance $L_p = 6 \,\mu\text{H}$ and noise voltage $V_n/N = 0.14 \,\text{nV}/\sqrt{\text{Hz}}$. To decrease the low frequency cut-off and at the same time lower the noise by 10 - 20 dB at 400 kHz and below, a low frequency cavity with higher inductance (4A15 ferrite, μ =1200, L_p = 40 μ H) and with a step-up ratio of N = 4 (which halves the noise voltage to $V_n/N = 0.07 \text{ nV}/\sqrt{\text{Hz}}$) has been built. It is installed in the AD ring adjacent to the high frequency device. Its response bandwidth is from 40 kHz to 3 MHz. The signals from the two devices are then combined to a single broadband signal with a crossover frequency (1 MHz) chosen for minimum noise.

3 LOW NOISE BEAM TRANSFORMER FOR BEAM TRANSFER LINE

To measure the charge of the extracted low intensity antiproton bunch (about 10⁷ charges, length about 300 ns), an additional transformer (low frequency version) will be installed in the extraction line. The extracted charge is measured by integrating the current signal during $t_i = 1 \mu s$. A bandwidth of 3 kHz (18 kHz with response shaping) to 3 MHz is needed for less than 1% error due to the response limitations. The mean square error of the charge signal q due to noise is related to the (double-sided) power spectral density of the current noise $G_i(f) [A^2/Hz]$:

$$\overline{q^{2}} = t_{i}^{2} \int_{0}^{\infty} 2G_{i}(f) \frac{\sin^{2}(\omega t_{i}/2)}{(\omega t_{i}/2)^{2}} df$$
(7)

which results in an expected RMS fluctuation of 1.9×10^4 charges (4 sigma is 7.6×10^4 charges).

4 REFERENCES

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