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# Design of Muon Collider Lattices

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NAPAC'16 Chicago

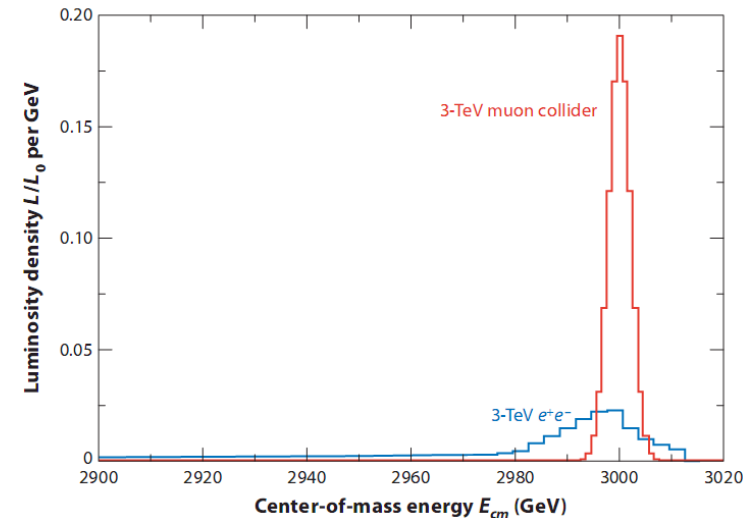
9-14 October 2016

# Motivation

Interest in lepton colliders may get a boost from LHC findings.

Compared to  $e^+e^-$  collider the Muon Collider has a number of important advantages, among them:

- Small collision energy spread,  $<1.e-4$  (if needed) - thanks to practical absence of
  - beamstrahlung - radiation in coherent EM field of opposing bunch
  - quantum fluctuations of bremstrahlung in the field of interacting particle
- $(m_\mu / m_e)^2 \sim 4 \cdot 10^4$  times larger cross-section of s-channel production of scalar particles
- Smaller footprint (in size and energy)
- Theorists give a lot of arguments which are far beyond my comprehension!



Energy spread in high-luminosity lepton colliders (V. Shiltsev)

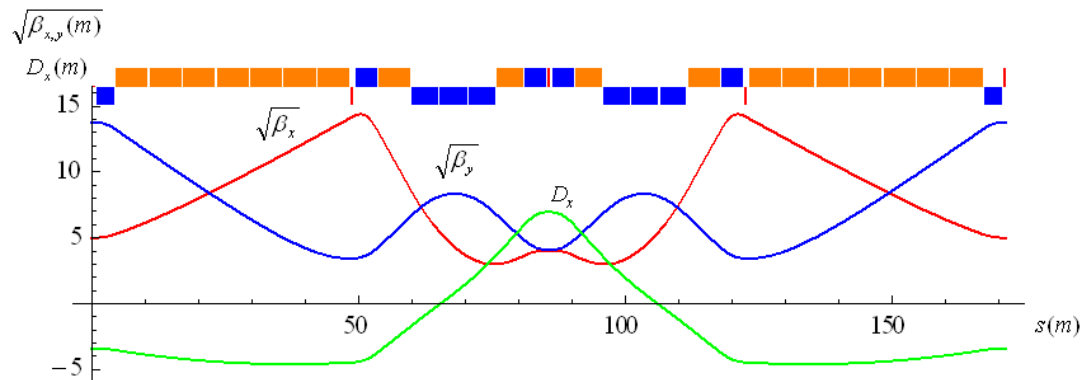
# Challenges

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- Small  $\beta^*$  required for luminosity (3-5mm for high energy MC)
  - ⇒ high chromaticity of the Final Focus (FF)
    - beam dynamics issues
  - ⇒ high  $\beta$ -function in the FF quads
    - high sensitivity to field errors
    - large quad apertures
      - engineering issues
      - detector backgrounds
      - beam dynamics issues (multipoles, fringe fields)
  - ⇒ short bunch length ( $\sigma_z \leq \beta^*$  for high energy MC)
    - very small momentum compaction factor
- Large beam-beam tunes shift  $\sim 0.1$
- Neutrino-induced radiation (for  $E_{\text{c.o.m.}} \geq 3 \text{ TeV}$ )
  - ⇒ no straights longer than  $\sim 0.5 \text{ m}$

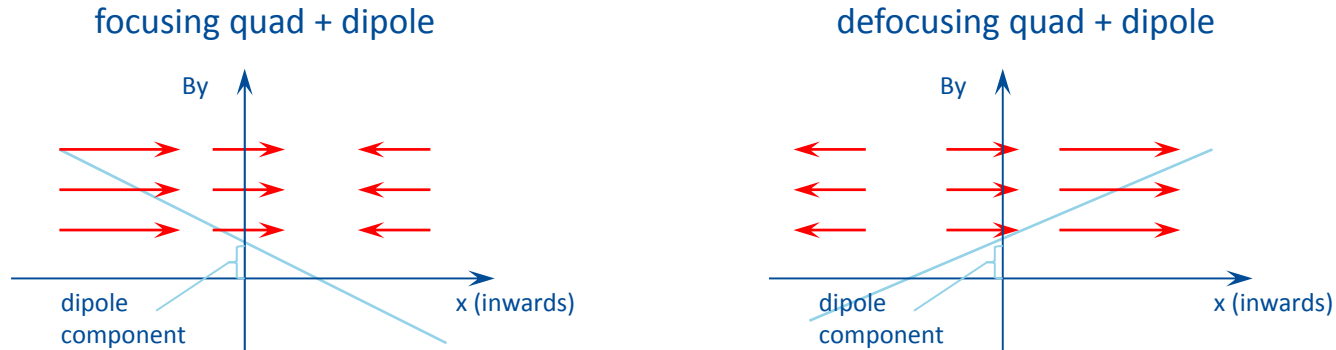
# Basic Solutions

- Quadruplet Final Focus
- “Three sextupoles” chromaticity correction
- Flexible Momentum Compaction (FMC) arccell for HE MC
  - with combined-function magnets to spread  $v$ 's



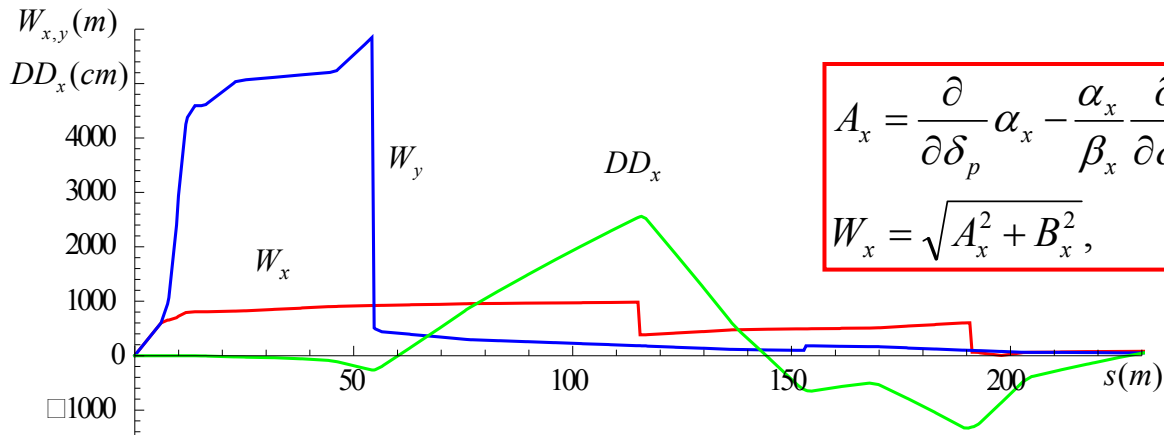
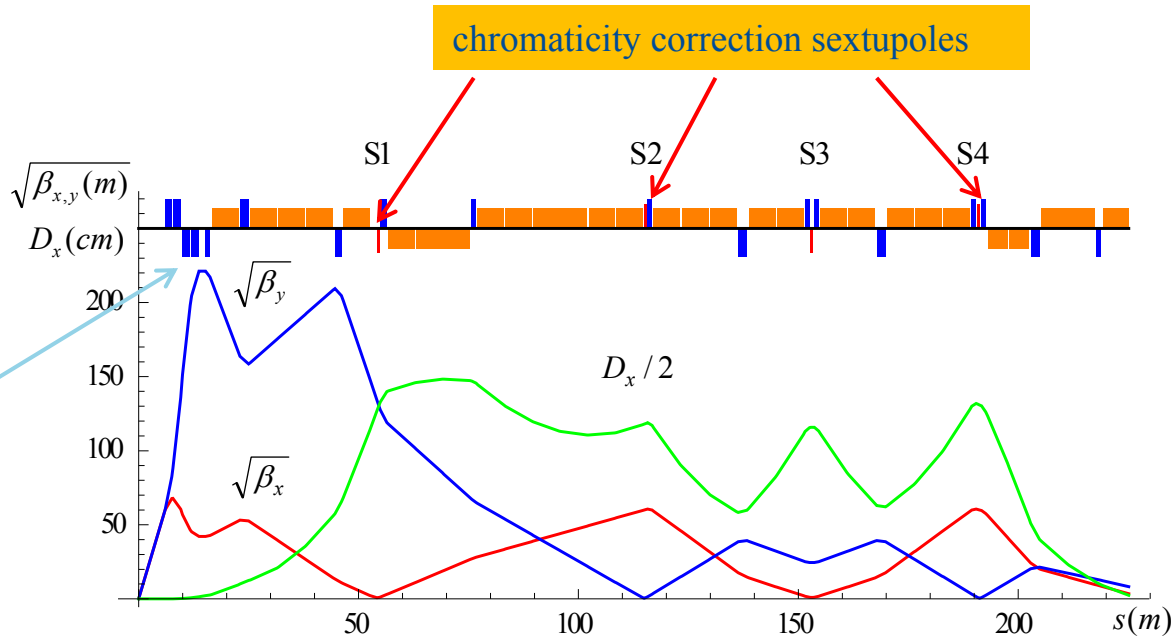
3TeV MC arccell allowing for independent control of tunes, chromaticities, momentum compaction factor and its derivative with momentum

# Why Quadruplet Final Focus?



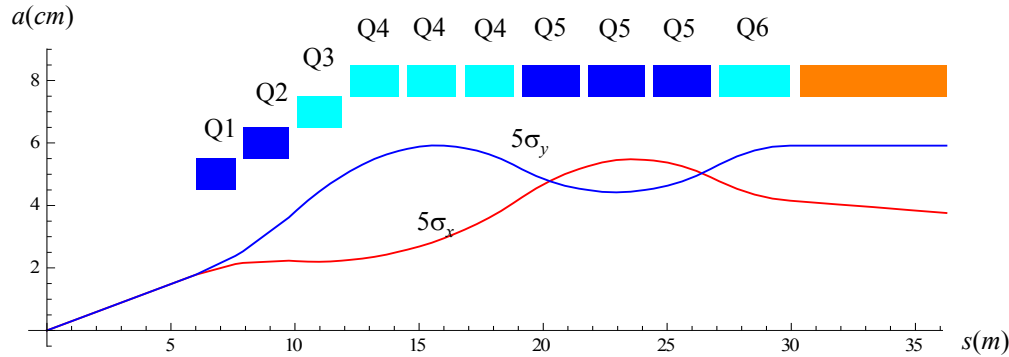
- Dipole component in a defocusing quad is more efficient for cleaning purposes
  - it is beneficial to have the 2<sup>nd</sup> from IP quad defocusing
- The last quad of the FF “telescope” also must be defocusing to limit the dispersion “invariant”
 
$$J_x = \frac{D_x^2 + (\beta_x D'_x + \alpha_x D_x)^2}{\beta_x} \approx \beta_x \phi^2$$
 generated by the subsequent dipole (generating dispersion for chromatic correction)
- both requirements are met with either doublet or quadruplet FF

# “Three sextupole” chromaticity correction (1.5 TeV MC)



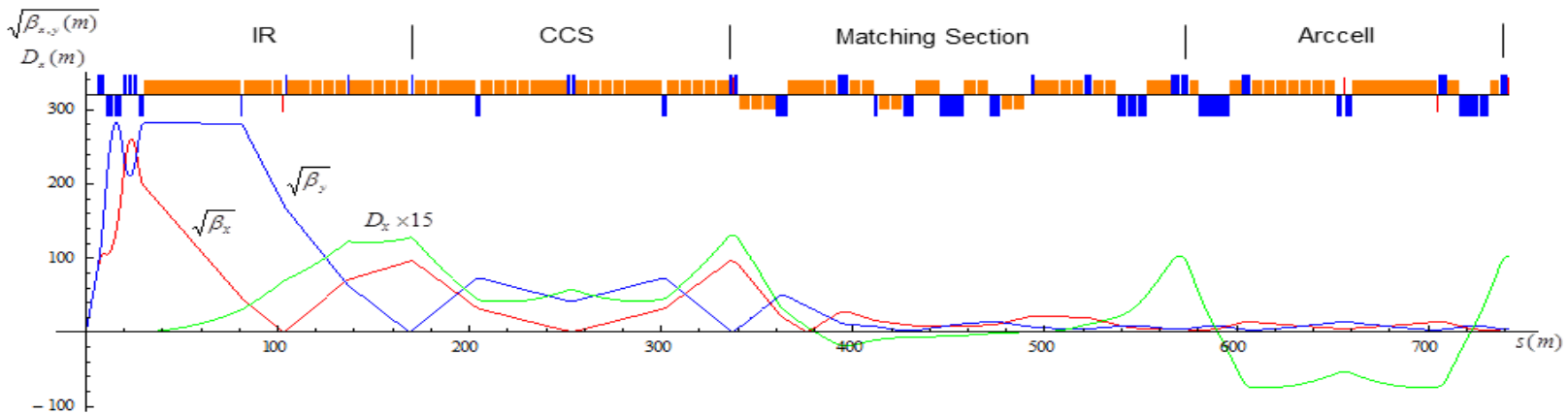
# 3 TeV MC Lattice with Quadruplet FF

$\beta^*=5\text{mm}$



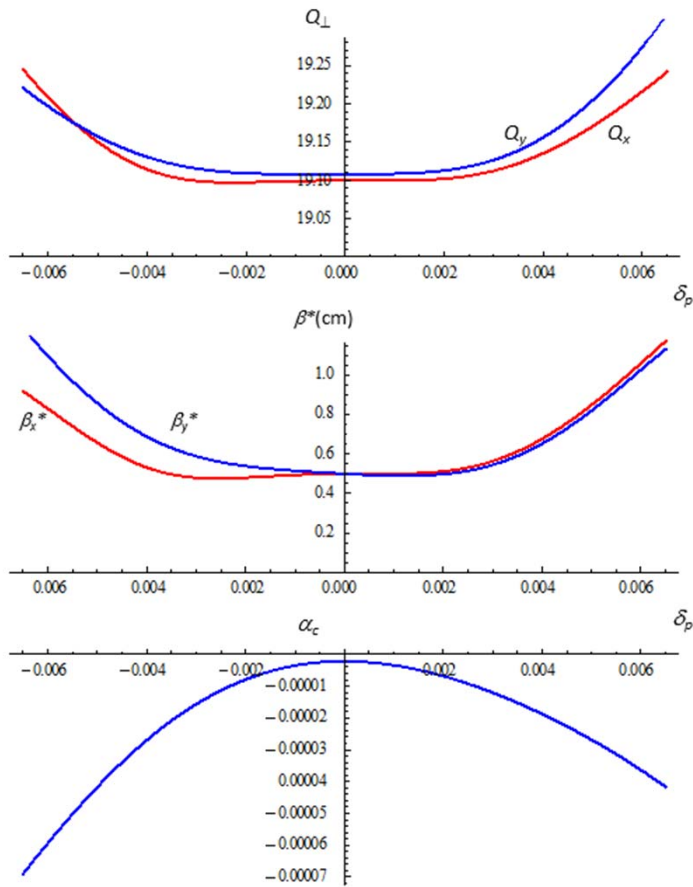
Q3, Q4 and Q6 have 2T dipole component.  
 $B_{\text{pole tip}} = 12\text{T}$  for shown apertures – Nb3Sn is O.K.

5 sigma beam sizes and magnet inner radii.

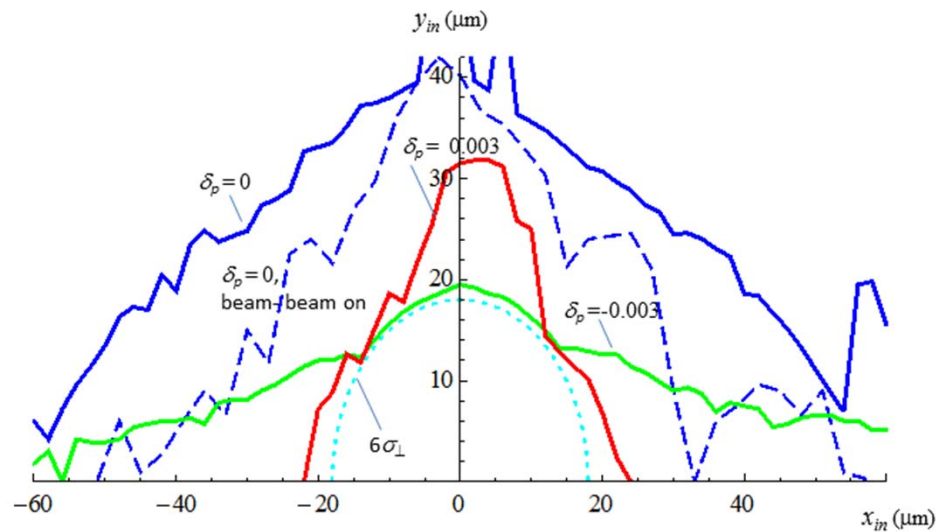


Optics functions from IP to the end of the first arc cell (6 such cells / arc) for  $\beta^*=5\text{mm}$

# 3 TeV MC Lattice Performance



Bare lattice parameters vs.  $\delta_p$ . Accidentally  $\alpha_c(0) = -2.15 \cdot 10^{-6}$  (was shooting for a higher absolute value)



2048 turns dynamic aperture in the plane of initial particle coordinates at IP  $x_{in}, y_{in}$  for indicated values of constant  $\delta_p$  calculated with beam-beam interaction off (solid lines) and on (dashed line) using MADX PTC\_TRACK routine and MAD8 TRACK LIE4 option respectively.

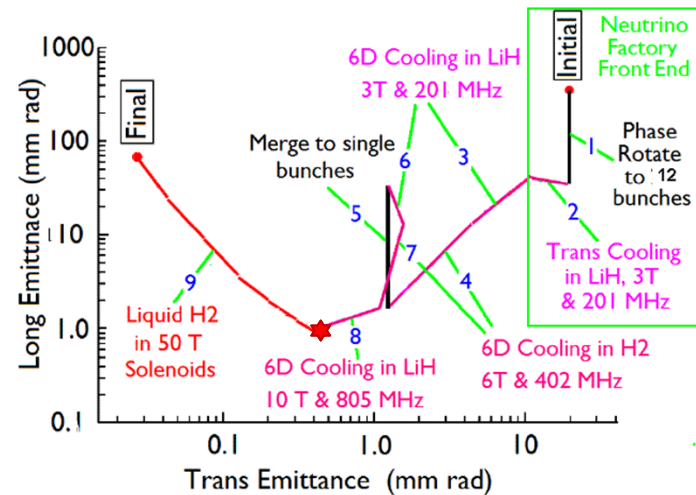
With beam-beam on  $\beta^* \approx 3\text{mm}$  so that  $\sigma_{\perp}^* \approx 2.3\mu\text{m}$ . Still, the OFF-momentum DA is barely sufficient, further work is desirable.



# Higgs Factory Specifics

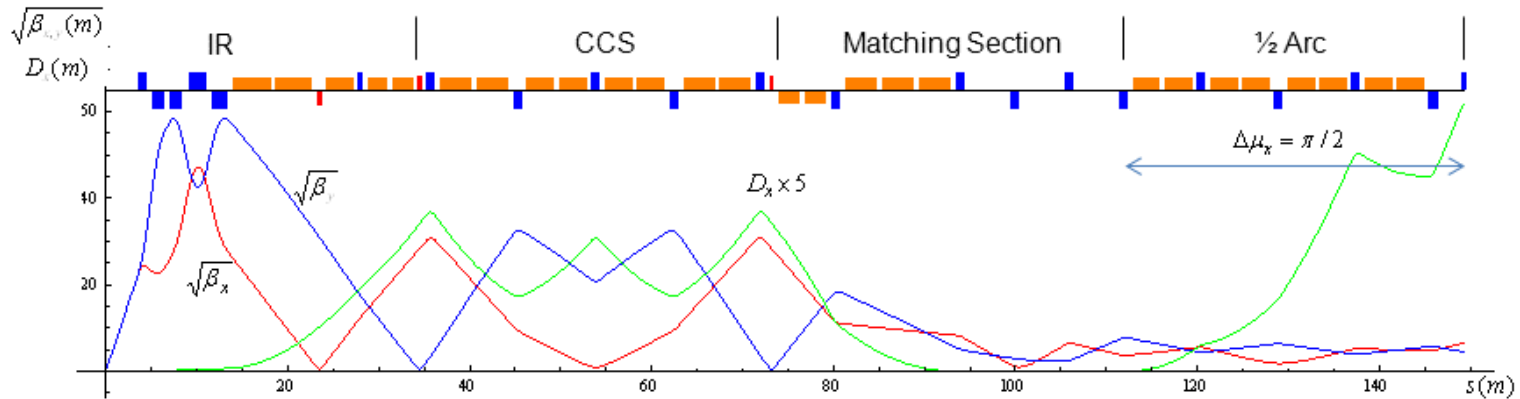
The major advantage of a  $\mu^+\mu^-$  Higgs Factory – the possibility of direct measurement of the Higgs boson width ( $\Gamma \sim 3\text{MeV}$  FWHM expected)  $\Rightarrow$  a very small beam energy spread is required,  $R \sim 0.003\%$

Dave Neuffer proposed to stop after 6D cooling:  
 $\varepsilon_{\perp N} = 0.3(\pi)\text{mm}\cdot\text{rad}$ ,  $\varepsilon_{\parallel N} = 1(\pi)\text{mm}\cdot\text{rad}$  ( $\sigma_s = 5.6\text{cm}$  with  $\sigma_p/p = 3 \cdot 10^{-5}$ )

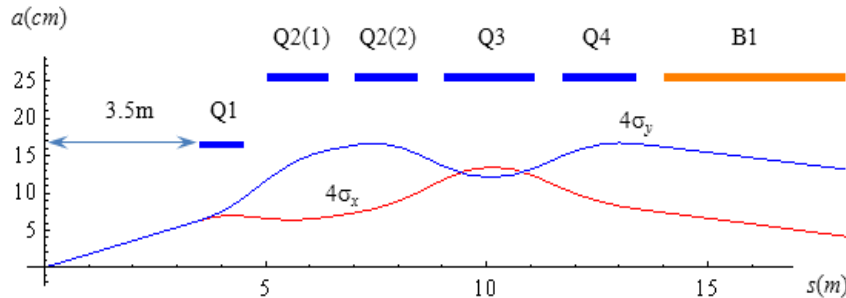


- Large  $\varepsilon_{\perp N} \rightarrow$  small  $\beta^*$  to achieve the required luminosity  $\rightarrow$  very large IR magnet apertures (up to ID $\sim$ 50cm).
- Preservation of small  $\sigma_E/E \sim 3 \cdot 10^{-5}$  in the presence of strong self-fields (I<sub>peak</sub>  $\sim$  1kA !)  $\rightarrow$  LARGE momentum compaction  $\alpha_c \sim 0.1$
- Chromaticity correction is still necessary due to path lengthening effect and operational considerations.

# Higgs Factory Preliminary Design

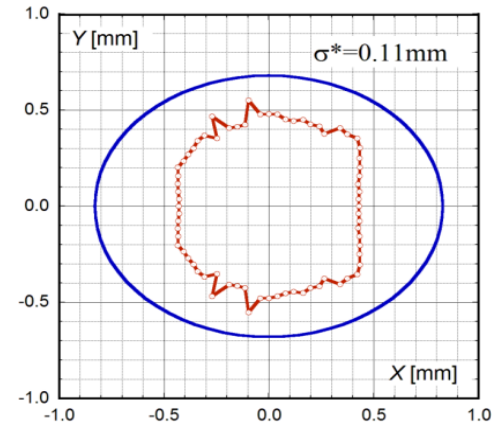


Higgs Factory lattice and optics functions for  $\beta^*=2.5\text{cm}$  in a half-ring starting from IP



IR quad cold mass inner radii and  $4\sigma$  beam envelopes for  $\beta^*=2.5\text{cm}$ . Q2 and Q4 have 2T dipole component

**The purpose of this design was to explore the limitations imposed by very large magnet aperture. We can increase  $\beta^*$  to 4cm losing <20% in luminosity**



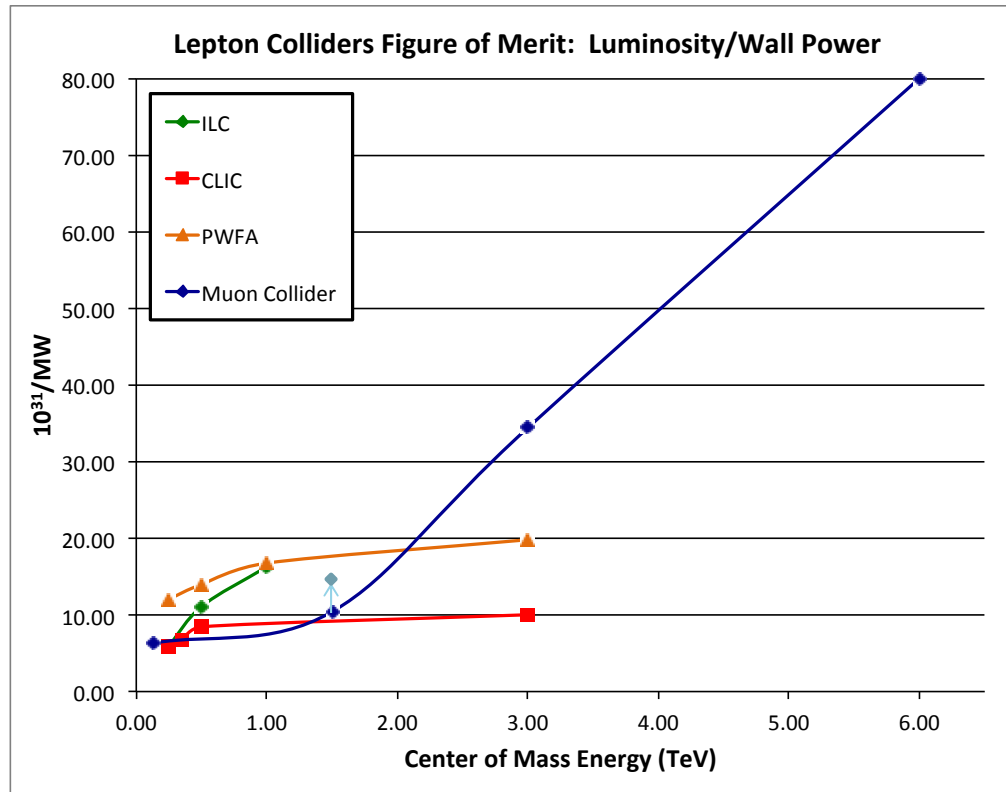
The dynamic aperture (fringe fields + multipoles + correction on) and projection of FF quad aperture (solid ellipse).

# Muon Collider Design Parameters

Collision energy, TeV	0.126	1.5	3.0	6.0*
Repetition rate, Hz	15	15	12	6
Average luminosity / IP, $10^{34}/\text{cm}^2/\text{s}$	0.008	1.25	4.6	11
Number of IPs	1	2	2	2
Circumference, km	0.3	2.5	4.34	6
$\beta^*$ , cm	1.7	1	0.5	0.3
Momentum compaction factor	0.08	$-1.3 \cdot 10^{-5}$	$-0.5 \cdot 10^{-5}$	$-0.3 \cdot 10^{-5}$
Normalized emittance, $\pi \cdot \text{mm} \cdot \text{mrad}$	200	25	25	25
Momentum spread, %	0.004	0.1	0.1	0.083
Bunch length, cm	6.3	1	0.5	0.3
Number of muons / bunch, $10^{12}$	4	2	2	2
Number of bunches / beam	1	1	1	1
Beam-beam parameter / IP	0.02	0.09	0.09	0.09
RF frequency, GHz	0.2	1.3	1.3	1.3
RF voltage, MV	0.1	12	50	150
Proton driver power (MW)	4	4	4	2

\*) The numbers for 6 TeV case are based on the IR design and projection from 3 TeV MC for the rest of the ring

# Luminosity / Wall Power Comparison



1.5 TeV design used doublet FF, with quadruplet FF  $\beta^*$  can be made smaller and luminosity  $\sim 50\%$  higher

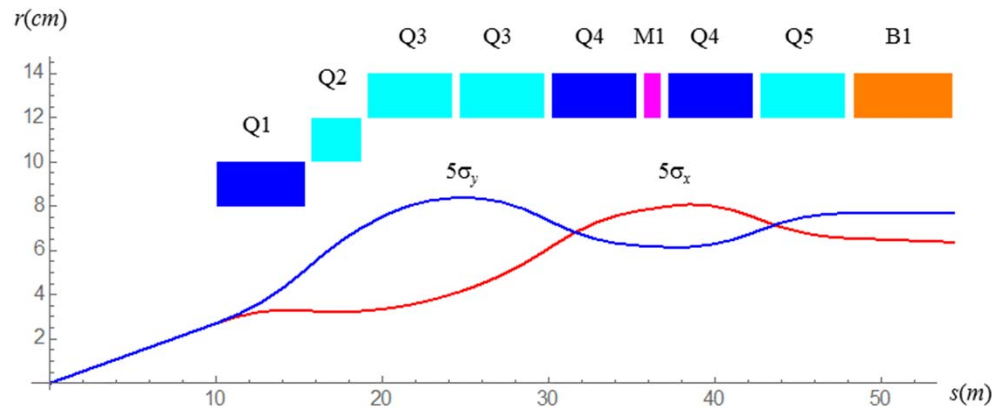
# Summary

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- The line of MC designs was developed spanning the collision energy range 0.126 – 6.0 TeV based on the original solutions
  - Quadruplet Final Focus
  - “Three sextupole” chromaticity correction
  - Flexible Momentum Compaction (FMC) arcell of a special type
  - $\beta^*$ -tuning section with chicane
- New approaches are worth to be studied, e.g. flat beam option – it makes chromaticity correction much easier
- We eagerly wait for the news from LHC – it will undoubtedly renew interest in Muon Collider!

# Preliminary Design of the 6 TeV MC FF Multiplet

$\beta^*=3\text{mm}$



Parameter	Q1	Q2	Q3	Q4	Q5
ID (mm)	160	200	240	240	240
G (T/m)	200	-125	-100	103	-78
B <sub>dipole</sub> (T)	0	3.5	4.0	3.0	6.0
L (m)	5.3	3.0	5.1	5.1	5.1