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Institute of High Energy Physics, Chinese Academy of Sciences



# Development of the bent focusing mirror in HEPS from design to test

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**1** Introduction

2 *Design phase*

3 *Off-line test phase*

4 *Conclusion*

## • 4<sup>th</sup> Synchrotron Radiation Source



SIRIUS



APS-U



ESRF-EBS

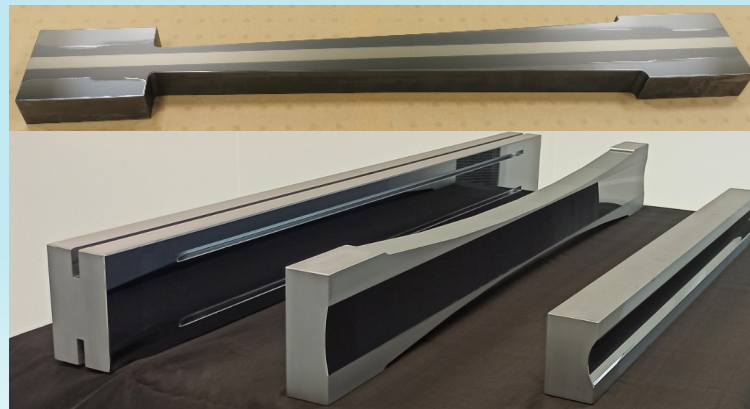
*Brilliance and coherence are the main parameters.*

## • Bent Mirror



HEPS

6GeV, 1364m, 34 $\mu$ m rad



*Various bent mirrors in HEPS*

*Characteristics:  
Adjust spot size;  
Form secondary source;  
Decrease errors.*

**One bent mirror**

*Design  $\rightarrow$  Test*

**Progress and Performance**

1 *Introduction*

2 **Design phase**

3 *Off-line test phase*

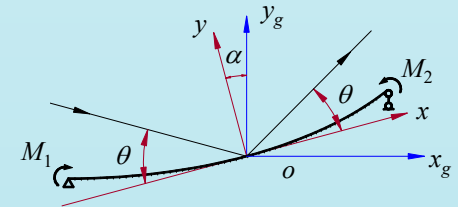
4 *Conclusion*

## • Method

### ■ Basic equation

$$y = \frac{(p+q)\sin\theta}{(p+q)^2 - (p-q)^2 \sin^2\theta} \times \left\{ 2pq - [(p-q)\cos\theta]x - 2\sqrt{pq}\sqrt{pq - (p-q)\cos\theta x - x^2} \right\} \quad \text{Elliptical Eq.}$$

$$K(x) = \frac{\sin\theta(p+q)}{2pq} \left( 1 - \frac{x^2}{pq} - \frac{x(p-q)\cos\theta}{pq} \right)^{3/2} \quad \text{Curvature Eq.}$$



### ■ Gravity compensation

$$M_g(x) = \frac{1}{2L_g} \left( x + \frac{L_g}{2} \right) C \int_{-L_g/2}^{L_g/2} (L_g - 2x)b(x) dx - C \int_{-L_g/2}^s (s-x)b(x) dx \quad \text{Moment by gravity}$$

$$b(x) = \frac{(M(x) + M_g(x))b_0}{EI_0 K(x)} \quad \text{Mirror width with gravity effect}$$

### ■ Iterative method

$$F(\xi) = EI_0 K(x_g)\xi - (M(x_g) + \Phi(\xi))b_0 \quad \xi_{n+2} = \xi_{n+1} - F(\xi_{n+1}) \frac{\xi_{n+1} - \xi_n}{F(\xi_{n+1}) - F(\xi_n)}, \quad n = 0, 1, 2, \dots$$

The theoretical distribution of the mirror width is a **curve**.

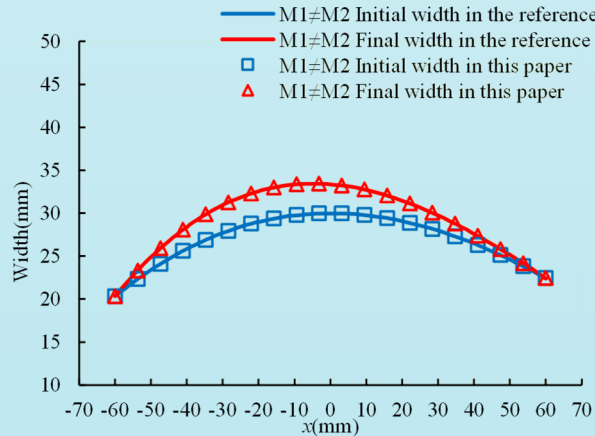
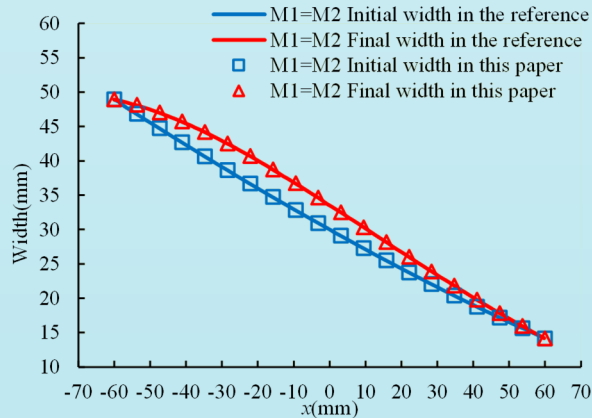


The practical distribution is fitted by a **polyline** for sake of the price



## • Method\*

### ■ Validity



The initial width and the final width are well in coincidence with the reference for M1=M2 or M1≠M2.

### ■ Efficiency

Iteration number	Residual slope error (nrad)		Iteration number	Residual slope error (nrad)	
	$M_1=k \cdot M_2, k=1$			$M_1=k \cdot M_2, k=0.2618$	
	<i>This paper</i>	<i>Reference paper</i>		<i>This paper</i>	<i>Reference paper</i>
Initial width	$5.31 \times 10^4$	$5.31 \times 10^4$	Initial width	$4.42 \times 10^4$	$4.43 \times 10^4$
1st iteration	$5.39 \times 10^2$	$4.29 \times 10^3$	1st iteration	$4.12 \times 10^2$	$3.67 \times 10^3$
2nd iteration	46.68	$3.79 \times 10^2$	2nd iteration	20.91	$3.25 \times 10^2$
3rd iteration	0.75	33.60	3rd iteration	0.89	28.90
4th iteration	-	3.00	4th iteration	-	2.60
5th iteration	-	0.26	5th iteration	-	0.23

The efficiency of the iteration of the solution is around 2 higher than the normal method.

\* Minwei Chen, Lidan Gao, Weifan Sheng, Peng Liu, Fugui Yang, Shaofeng Wang, Ming Li, "Efficient method on the determination of optimized width of bendable mirrors with gravity compensation", Results in Optics, 2021, 5, 100141.

- Parameters

Parameter name	Unit	Value
Active area	mm <sup>2</sup>	605×20
Reflection direction	-	Face-down
Bent shape	-	Cylinder
Tangential slope error	μrad (RMS)	0.3
Object	m	∞
Image	m	4.5
Incident angel	mrad	1.7

- Design difficulties

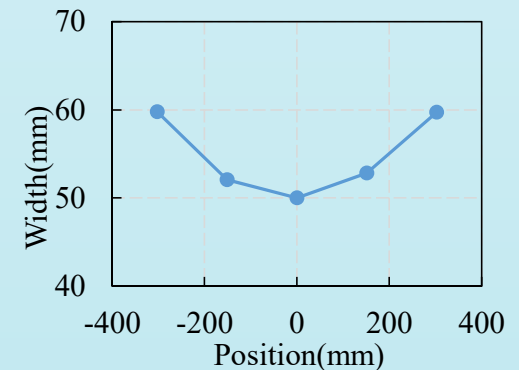
- *Face-down reflection is a new challenge for us due to lacking of the experience;*
- *The precision requirement is relatively high.*

# Design phase

## Results

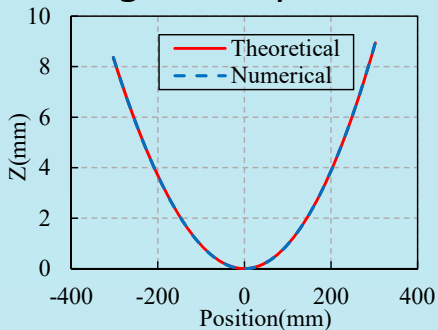
### Mirror width

X(mm)	-302.5	-151.25	0	151.25	302.5
b(mm)	59.78	52.07	50.00	52.81	59.73

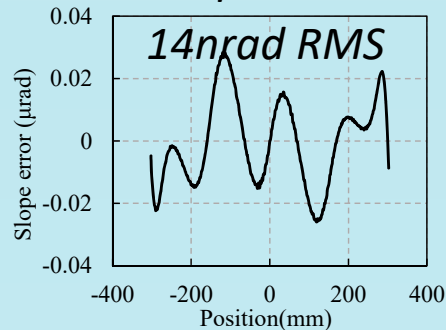


### Design error

#### Height comparison



#### Slope error



### Manufacture error

This error is equal to required error minus design total error.

The suggested manufacture error is less than 0.2 μrad rms.

Bent mirror	Theoretical		Material						
	Item	Theory	Parameter %	Density uniformity ‰	E uniformity ‰				
Requirement	Polyline		4.5	25.7	3.5				
Slope error (nrad)	14		50	50	50				
		Mechanism		Processing					
Item	Friction	Disp. resolution	Rolling	Yawing	Orientation	Shape μm	Height μm	Height uniformity μm	Parallelism μm
Requirement	<1	81	25'	45'	3°	50	100	30	100
Slope error (nrad)	15	20	5	42	14	7	25	11	
Total error (nrad)					108				



1 *Introduction*

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# Off-line test phase

- Test preparation

- Component



*Bent mirror*



*Bender and horizontal LTP*



*Sleeve with MoS<sub>2</sub> coating*

- Difficulties

*The reflection direction in the test **condition** is different from that in the practical direction;*

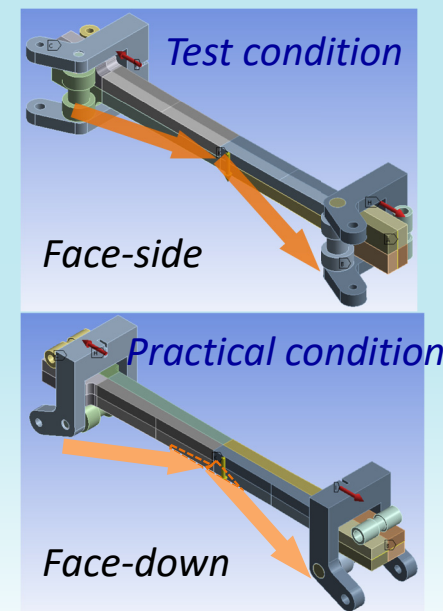
*The results obtained by LTP must be superposed by the mirror **gravity**;*

*How to **adjust the actuator** to reach the desired shape.*

- Solutions

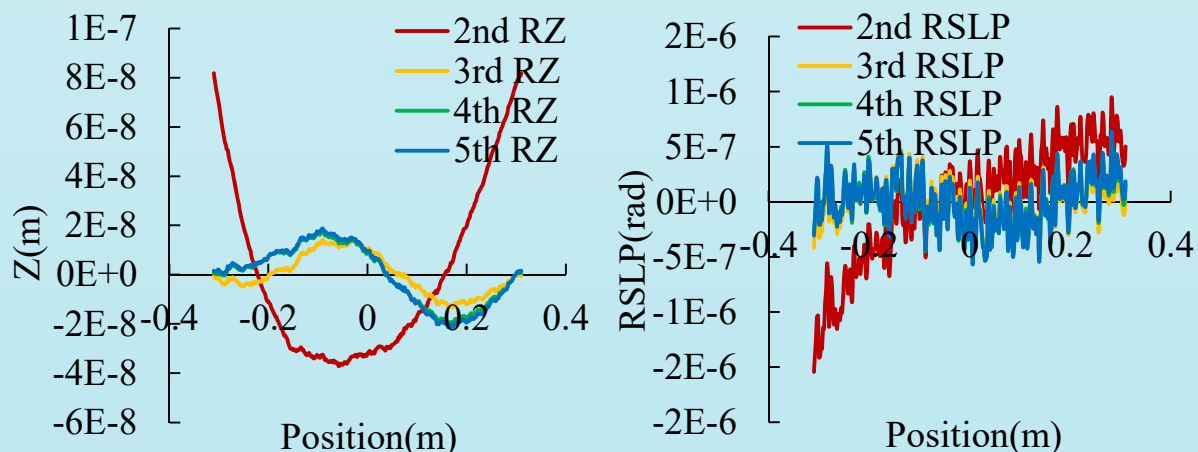
*Consider the influence of the **gravity**;*

***Iterate** between the inspection results and the numerical results.*



## • Test results

### ■ Height error and slope error



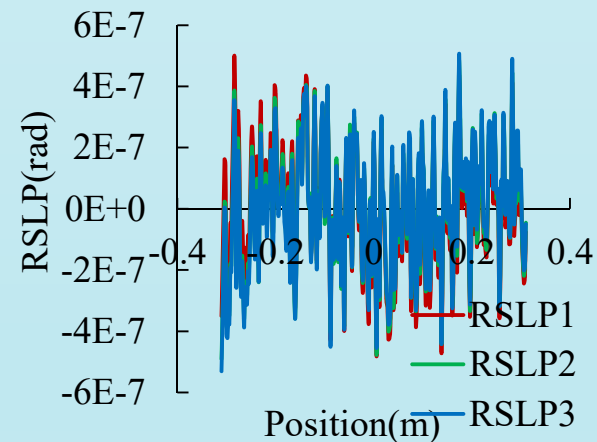
Iteration number	Height error rms [nm]	Slope error rms [ $\mu$ rad]
1	3310	27.0
2	47.7	0.63
3	13.2	0.28
4	14.4	0.25
5	12.1	0.22

*The height error and slope error both decrease as the the iteration number increasing; 4 or 5 iterations are enough to meet the requirement. The final slope error is converged to about  $0.2 \mu$ rad rms, which exceeds the anticipation; The result includes the error of the manufacture, bent mirror, mechanism and others, so the final error is good and acceptable.*

- Test results

- Repeatability

Number	Height error rms [nm]	Slope error rms [ $\mu$ rad]
1	12.1	0.22
2	10.6	0.22
3	10.4	0.23

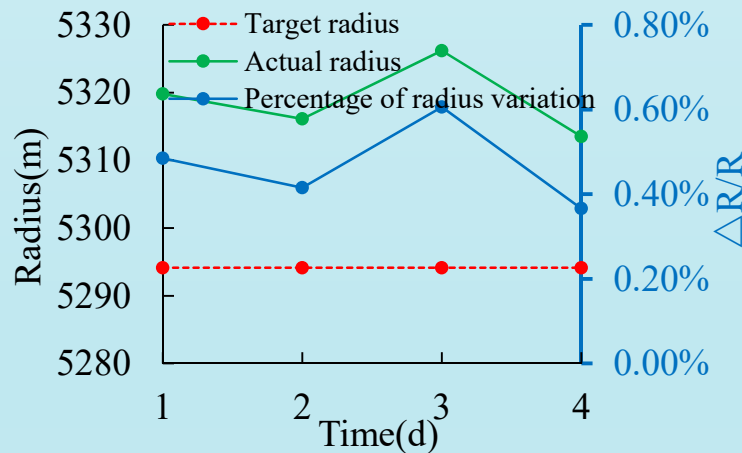


*Test method: Release the force of the actuator, then reload the pervious value.*

*Results: The height error varies a little while the slope error nearly maintains the first value. Thus, the repeatability of the whole system is very good.*

## • Test results

### ■ Stability



*Red dotted line: Target radius*

*Green solid line: Actual radius*

*Blue solid line: Percentage of radius variation*

*Evaluation criterion: The ratio of the variation of the curvature radius to the target radius,  $\Delta R/R$ ;*

*The test period lasts about 4 days. The interval of the actual curvature radius locates in about 5320m and the parameter  $\Delta R/R$  corresponds to around 0.5%.*

*The stability is also acceptable for us.*

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*The topic is related to the performance of the bent mirror system from design to off-line test. The detail is embodied in the followings.*

## • Design phase

- *The method we use is not only proved to be correct but also to be efficient;*
- *In the process of design, we consider lots of factors influencing the bent precision, such as theory, material, processing, mechanism and manufacture. All the errors summed meet the requirement.*

## • Off-line test phase

- *We solve the problem of the difference between the test condition and the practical condition after superposing the effect of the gravity;*
- *After 4 or 5 iterations are enough to meet the requirement, and the slope error is converged to about  $0.2 \mu\text{rad rms}$  that exceeds our expectation;*
- *Repeatability and stability of the system are also been measured. From the view of the height error and the slope error, these parameters are verified to be excellent and acceptable.*



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# Thanks for your attention!

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