





Wir schaffen Wissen – heute für morgen

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Structural dynamic modelling and measurement of SwissFEL Bunch Compressor



Magnetic chicanes are used in SwissFEL to longitudinally compress the accelerated particle bunches.

The second compression chicane (BC2) of SwissFEL consists of four dipole magnets bending the beam on the horizontal plane along a C-shaped orbit with adjustable deflection angle



SwissFEL layout schematic



- BCII Structural design and stability requirement
- Finite element analyses
 - Static and modal analysis
 - Harmonic response analysis
- Random Vibration measurement
- Random vibration analysis
- Summary



BC2 Mechanical Structure Design

Total length: 17 m





SwissFEL BC kinematics





Mechanical stability requirement











Girder length (dipole separation):7.7 mTransverse movement of dipole:-10 to 495 mmBending angle:3.8 deg.





Linear bearings

- If friction forces in the joint are high enough to withstand excitation forces, joint is well defined, contact is closed.
- f the excitation force is higher than friction force, the contact becomes open

Free: in the rigid dynamic analysis Fixed or Constraint Stiffness: in modal based dynamic analysis, only if excitation force is too small to overcome friction force

Boundary conditions:

- 1. Free
- 2. Constraint stiffness
- 3. Constraint stiffness
- 4. Fixed

k=2e4 N/mm *k*=2e7 N/mm





Static and Modal Analysis

Static deflection under gravity load:

Deflection:

0.152 mm (fixed) to 0.157 (free)

Relationship between natural frequency *f*/Hz and maximum static deflection *d*/mm for pinned-pinned prismatic beam:

 $f = 17.8 / \sqrt{d}$

First bending frequency estimated to be 45.7 Hz (fixed) to 45.1 Hz (free)



	1. Torsional mode	1. Bending Mode	2. Torsional mode
Free	16.4 Hz	41.3 Hz	47.8
Soft	20.3 Hz	41.7 Hz	45.5
Hard	22.7 Hz	42.0 Hz	48.6
fixed	22.8 Hz	41.8 Hz	49.0

Free boundary has in addition first rotational mode at 1.6 Hz and transversal bending mode at 31.2 Hz Soft boundary hat additional transversal bending mode at 34.6 Hz Harmonic Response Analysis

In a harmonic response analysis system response to steady-state sinusoidal loading at a given frequency $[M]{\ddot{x}}+[C]{\dot{x}}+[K]{x}={F}$

Both excitation $\{F\}$ and response $\{x\}$ are assumed to be harmonic.

 $\Omega:$ imposed circular frequency, $\psi, \phi:$ phase shift

$$\{F\} = \{F_{\max}\} e^{j(\Omega t + \psi)}$$
$$\{x\} = \{x_{\max}\} e^{j(\Omega t + \phi)}$$

Base excitation RMS 1 mm/s² is applied to all support conditions in all directions. Damping ratio 2% is assumed to be 2%.

Ground vibration has in general broadband distribution. In harmonic response analysis excitation frequency is swept linearly to identify critical frequency at critical location.



Harmonic Response Analysis

Frequency response at magnet position, Acceleration in transversal direction, base excitation 1 mm/s² in all directions at all supports. Damping ratio 2%. Transmissibility function:



Transversal displacement frequency response at position of magnet. At a frequency of 22.8 Hz, the maximum response was 0.9 μ m for fixed and stiff linear bearing. With soft spring constraints, the maximum response was 1.7 μ m at 22 Hz.





Vibration measurement

Measurement has performed with eight-channel LMS SCADAS Mobile. Seismic accelerometers PCB393B31 were placed on

- Floor
- Granite tables
- Steel Girder



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The amplification ratio girder to ground is below 1.35 in transversal direction, and below 1.14 in vertical direction. BC2 structure shows excellent mechanical stability behavior



Spectral Displacement Measurement





Random Vibration Analysis

Power spectral density (PSD) of acceleration from 5 Hz to 100 Hz is applied to all supports with fixed boundary conditions. Again a constant damping ratio of 2% is assumed. Response PSD displacements and reaction forces are solved A minimum friction coefficient of 0.00034 is required





Summary

- BCII shows excellent stable behavior. The amplification ratio girder to floor is below 1.35 in transversal direction, and below 1.14 in vertical direction.
- From vibration measurement, the first two transversal modes from finite element analysis can be confirmed. However, the vertical bending mode can not be identified in the measurement. The vibration level in vertical is smaller than in horizontal direction so that not all modes can be measured.
- If dynamic excitation forces are very small compared to sliding friction forces, a good representation can be achieved with fixed degree of freedom.
- The verification of excitation forces can be achieved in a random vibration analysis. This
 procedure is iterative, because PSD analysis relies on modal representation, and finally on
 correct modelling of boundary conditions.
- The final confirmation of the linear representation of linear guide system is given by vibration measurement.



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