# SIMULATING BEAM TRANSPORT WITH PERMANENT MAGNET CHICANE FOR THz FEL

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#### Abstract

Free electron lasers are an attractive option for high average and peak power radiation in the THz gap, a region of the electromagnetic spectrum where radiation sources are scarce, as the required beam and undulator parameters are readily achievable with current technology. However, slippage effects require the FEL to be driven with relatively long and low current electron bunches, limiting amplification gain and output power. Previous work demonstrated that a waveguide could be used to match the radiation and e-beam velocities in a meter-long strongly-tapered helical undulator, resulting in 10% energy extraction from an ultrashort 200 pC, 5.5 MeV electron beam. We present simulations for a follow-up experiment targeting higher frequencies with improvements to the e-beam transport including a permanent magnet chicane for strong beam compression. FEL simulations show >20% extraction efficiency from a 125 pC, 7.4 MeV electron beam at 0.32 THz.

#### **INTRODUCTION**

Compact and efficient high average and peak power radiation sources are in high demand for scientific and industrial applications including time-domain spectroscopy, high field resonant and non-resonant excitation of solid state systems, and THz-based imaging for medical and security [1, 2]. Free Electron Lasers (FELs) use the ponderomotive interaction between an electromagnetic wave and a relativistic electron beam copropagating in a magnetic undulator and are an attractive source in the 0.1-10 THz range as the necessary undulator and beam parameters are easily achievable [3, 4]. Addition advantages include high peak power and repetition rates limited only by the electron beam provided. FEL facilities have already played an important role in the development of THz science [5–10], with more facilities coming online [11–13] and being planned for the future [14–16].

Our previous experiment [17] showed that by using a waveguide to contain diffraction and match group velocities, a 10% extraction efficiency could be achieved from an ultrashort 200 pC, 5.5 MeV beam. After reviewing the zero-slippage conditions in a waveguide FEL, we investigate a proposed follow-up experiment to double the frequency of THz produced. We discuss improvements to the beamline, a design for a tunable permanent magnet chicane, and the consequences of increasing the resonant frequency. Start to end simulations are presented for the electron beam transport and FEL interaction.

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Figure 1: Dispersion diagram for a waveguide FEL. Electrons (red) in free space can only be resonant at a single frequency, whereas a waveguide allows interaction over a large bandwidth.

#### ZERO-SLIPPAGE RESONANCE

The zero-slippage FEL interaction requires satisfying the traditional FEL phase resonance condition,  $(k_z + k_u) = \frac{\omega}{\beta_z c}$  and the group-velocity or zero-slippage condition,  $\frac{c^2 k_z}{\omega} = \beta_z c$ . In these expressions, the longitudinal wavevector  $k_z$  and radiation frequency  $\omega$  are connected by the waveguide dispersion relation  $\omega^2/c^2 = k_z^2 + k_\perp^2$  where  $k_\perp = 1.8412/R$  for the TE11 circular waveguide mode [18], *R* is the waveguide radius,  $k_u = 2\pi/\lambda_u$  where  $\lambda_u$  is the undulator period, and  $c\beta_z$  is the longitudinal beam velocity in the undulator. Figure 1 illustrates the large bandwidth interaction when the phase velocity (point) and group velocity (slope) are adequately matched.

It can be shown from these conditions that the resonant frequency at zero-slippage is given by  $2\pi f_{zs} = ck_u\beta_{z0}\gamma_{z0}^2$  where  $\gamma_{z0} = \gamma_0/\sqrt{1+K^2}$ . For relativistic beams,  $\gamma_0 = \frac{k_\perp}{k_u}\sqrt{1+K^2}$  and we see that for given waveguide and undulator parameters, the resonant beam energy is uniquely determined.

To maintain resonance with the decelerating electrons, the magnetic field strength must be strongly tapered along the undulator to enhance the stimulated superradiant radiation emission (TESSA) of the electrons [19].

A final consequence of the zero-slippage conditions is that the ratio of the helical beam trajectory radius to the waveguide radius is  $\frac{r_{max}}{R} = \frac{1}{1.8412} \frac{K}{\sqrt{1+K^2}} \le 0.543$  with an upper bound independent of frequency.

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#### **BEAM TRANSPORT**

It is important to demonstrate the scalability of the waveguide FEL interaction to higher frequencies in the THz gap for broader scientific application. In Table 1 we list the simulated parameters for an experiment doubling the target frequency to 320 GHz. Electron beam parameters are quoted at the undulator entrance.

Table 1: Simulation Parameters

Electron Beam		Chicane	
$\gamma$	14.5 0.7%	Gap B	8 mm 270 mT
$\sigma_{\chi}, \sigma_{y}$	139 $\mu$ m, 122 $\mu$ m	$\theta_{bend}$	30deg
$\sigma_z \\ \epsilon_{n,x}, \epsilon_{n,y}$	90 µm 5 mm∙mrad	<i>R</i> <sub>56</sub>	0.05 m
Undulator		Waveguide	
$\frac{K_{rms,0}}{\lambda_u}$	2.18 3.2 cm 30	Material Radius	Cu 1.6 mm



Figure 2: RADIA model of chicane.

We note that targeting higher frequencies relaxes a couple experimental constraints. First, the diffraction of the produced radiation is diminished, allowing easier transport to and within the THz diagnostics. We have also redesigned and shortened the vacuum system immediately after the undulator to remove apertures that could clip the THz beam. Secondly, the radius of the electron trajectory is reduced, increasing the tuning precision for hall probe and pulsed wire measurements which are practically limited to the magnetic axis by the enclosed helical geometry.

The challenges of an experiment producing higher frequency THz include focusing to a smaller matched spotsize determined by undulator focusing and compressing to achieve bunching factors that can seed the FEL interaction.

A quadrupole triplet was previously used to focus the e-beam into the undulator, but the large distance (1.2 m)

required by beamline real estate constraints limited the minimum spotsize. The mismatched e-beam experienced betatron oscillations in the undulator, reducing charge transmission and degrading the interaction. We have since added a solenoid 30 cm before the undulator to supply the necessary focusing strength to match the 7.4 MeV e-beam into the undulator while the quadrupole triplet is used to symmetrize the beam at the solenoid.

At longer wavelengths, compression of the ebeam could be achieved by tuning the amplitude and phase of a booster linac to both accelerate the beam to the resonant energy and provide an energy chirp to compress the e-beam in the drift to the undulator. Limitations on the maximum accelerating gradient and drift length remove this option for achieving a significant bunching factor at shorter wavelengths. Lengthening the beam by stretching the laser pulse illuminating the cathode reduces space charge effects and strengthens the chirp from the linac, but is still insufficient and would result in large energy spread.

We have instead designed a tuneable permanent magnet chicane using the modeling software RADIA [20] that can achieve compression with a reduced energy chirp, minimizing the e-beams energy spread in the FEL interaction. Figure 2 shows the RADIA model for a single chicane magnet where field lines from the 5 cm x 5 cm blue permanent magnets are guided across the trapezoidal-shaped 8 mm gap via iron yokes. The small bending radius (10 cm) results in a large deflection (30 deg) of the ebeam and significant transverse focusing effects. We chose to split the focusing equally between the x and y directions using a 15 deg shaping of the poles between magnets 1,2 and 3,4. Each chicane magnet has an iron shim that can be adjusted to divert field lines, reducing the peak field by 20% in order to align the electron beam or adjust the R56.



Figure 3: Electron beam transport.

The linac induced energy chirp and chicane field strengths can be tuned to compress beams with relativistic factors in the range  $\gamma = 14 - 16$ , enabling us to study the energy resonance of the zero-slippage regime.

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Figure 3 shows the beamline transport done with the General Particle Tracer code [21] for a 2 ps FWHM laser pulse. After exiting the chicane, the strongly divergent e-beam is focused with the solenoid into the undulator. Although space charge effects will be increased when the beam is both focused and compressed at the exit of the chicane, simulations show a bunching factor of >0.8 is still achieved with only a 40% growth in the transverse emittance.



Figure 4: FEL interaction along undulator.



Figure 5: THz spectrum.

### FEL INTERACTION

The FEL interaction is simulated with a GPT extension module [22] that self-consistently calculates the interaction of electrons and electromagnetic fields inside the undulator taking into account both dispersion and 3D space charge effects.

Results are shown for a 125 pC bunch with the same undulator tapering as in the previous experiment for comparison. At higher frequencies, the smaller waveguide area implies that a smaller amount of charge is necessary to excite large electric field amplitudes and achieve significant conversion efficiencies. A design tradeoff exists between a desire to maximize charge in the FEL and a need to reduce space charge effects in the beam transport.

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To physically achieve a smaller waveguide radius, we place a tight fitting copper pipe inside the vacuum waveguide. This is an improvement from before when the stainless steel vacuum pipe doubled as the waveguide, introducing noticable power loss in the waveguide. At the same time, the copper waveguide will be supported by the vacuum pipe. simplifying the alignment.

Figure 4 shows the FEL interaction along the undulator with an impressive 20% average deceleration of the electron beam producing a 20 ps, 175  $\mu$ J THz pulse. These results emphasize the importance of strong bunching and full charge transmission in the FEL interaction. Figure 5 shows the large bandwidth of the zero-slippage resonance, with frequency components extending beyond 0.4 THz.

### CONCLUSION

Simulations show promising results for operating the zeroslippage waveguide FEL at higher frequencies with 20% energy extraction from a 125 pC, 7.4 MeV beam. This highlights the importance of our beamline improvements including a solenoid for transverse focusing and a permanent magnet chicane to achieve significant bunching factors at shorter wavelengths. Demonstrating full transmission through the undulator at the resonant energy would imply more aggressive tapering could be achieved with a large bunch charge. Future work could include recirculating a fraction of the produced radiation to seed successive passes in the undulator [23].

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