

# **WAKEFIELDS AND TRANSVERSE BUNCH DYNAMICS STUDIES OF A PLASMA-DIELECTRIC ACCELERATING STRUCTURE**

**Kostyantyn Galaydych (presenter)**

**Ivan Onishchenko**

**Gennadiy Sotnikov**

**Kharkiv Institute of Physics and Technology  
Kharkiv, Ukraine**



**2021**

## **Introduction**

**–One of the key issues of the accelerators development is the transverse stability of bunches (BBU).**

**\*\*\***

**–In the case of dielectric wakefield accelerators, this issue is especially important, because the accelerating field is created here by the drive bunches, rather than by an external RF source, as in conventional accelerators.**

**\*\*\***

**–As a consequence of the instability, aside from the bunch parameters degradation, it is also possible that particles may deposit on the dielectric surface.**

**\*\*\***

**–The important case of transverse instability is the asymmetric bunch injection.**

# Previous studies (in the dielectric-loaded structures)

PHYSICAL REVIEW D

VOLUME 42, NUMBER 5

1 SEPTEMBER 1990

## Longitudinal- and transverse-wake-field effects in dielectric structures

M. Rosing and W. Gai

*High Energy Physics Division, Argonne National Laboratory, Argonne, Illinois 60439*

(Received 8 March 1990)

PHYSICAL REVIEW D

VOLUME 42, NUMBER 5

1 SEPTEMBER 1990

## Wake fields in a dielectric-lined waveguide

King-Yuen Ng

*Fermi National Accelerator Laboratory, Batavia, Illinois 60510*

(Received 12 February 1990; revised manuscript received 21 May 1990)

## Transverse wake fields due to nonaxisymmetric drive beams in the dielectric wake-field accelerator

Eusebio Garate

*Department of Physics, University of California, Irvine, California 92717*

(Received 18 April 1990; accepted 20 December 1990)

PHYSICAL REVIEW E

VOLUME 55, NUMBER 3

MARCH 1997

## Numerical simulations of intense charged-particle beam propagation in a dielectric wake-field accelerator

W. Gai,<sup>1</sup> A. D. Kanareykin,<sup>2</sup> A. L. Kustov,<sup>2</sup> and J. Simpson<sup>1</sup>

<sup>1</sup>*Argonne National Laboratory, 9700 South Cass Avenue, Argonne, Illinois 60439*

<sup>2</sup>*St. Petersburg Electrical Engineering University, 5 Professor Popov Street, St. Petersburg 197376, Russia*

(Received 24 July 1995; revised manuscript received 5 August 1996)

PHYSICAL REVIEW E

VOLUME 62, NUMBER 1

JULY 2000

## Theory of wakefields in a dielectric-lined waveguide

S. Y. Park\* and J. L. Hirshfield<sup>†</sup>

*Department of Physics, Yale University, P.O. Box 208120, New Haven, Connecticut 06520-8120*

*and Omega-P, Incorporated, Suite 100, 345 Whitney Avenue, New Haven, Connecticut 06511*

(Received 18 February 2000)

## Previous studies (in a plasma)

- The focusing properties of plasma, which allow a drive bunch to be focused, have long been known

*Particle Accelerators*, 1985, Vol. 17, pp. 171–189

0031-2460/85/1704-0171/\$20.00/0

© 1985 Gordon and Breach, Science Publishers, Inc. and OPA Ltd.

Printed in the United States of America

PHYSICAL REVIEW A

VOLUME 44, NUMBER 10

15 NOVEMBER 1991

### Acceleration and focusing of electrons in two-dimensional nonlinear plasma wake fields

J. B. Rosenzweig, B. Breizman,<sup>\*</sup> T. Katsouleas,<sup>†</sup> and J. J. Su

*Department of Physics, University of California at Los Angeles, Los Angeles, California 90024*

(Received 10 June 1991)

### A PLASMA WAKE FIELD ACCELERATOR<sup>†</sup>

R. D. RUTH, A. W. CHAO, P. L. MORTON and P. B. WILSON

*Stanford Linear Accelerator Center*

*Stanford University, Stanford, California, 94305*

\*\*\*

- As an alternative to the quadrupole focusing in dielectric wakefield accelerator, the plasma filling the drift channel in a dielectric structure can be used

\*\*\*

- A combination of plasma and a dielectric structure also makes it possible to focus an accelerated bunch. Focusing in such a plasma-dielectric structure in the linear plasma mode is ensured by a Langmuir wave, and acceleration is provided by a modified eigenwave of the dielectric structure

## Previous studies (in the plasma–dielectric structures)

– It was shown that at a certain plasma density the superposition of the plasma wave and the dielectric waves allows the acceleration of the witness bunch by the field of the dielectric wave together with simultaneous focusing by the plasma wave

Nuclear Instruments and Methods in Physics Research A 740 (2014) 124–129



Contents lists available at ScienceDirect

Nuclear Instruments and Methods in  
Physics Research A

journal homepage: [www.elsevier.com/locate/nima](http://www.elsevier.com/locate/nima)



PUBLISHED BY IOP PUBLISHING FOR SISSA MEDIALAB

RECEIVED: December 11, 2019

REVISED: April 30, 2020

ACCEPTED: May 27, 2020

PUBLISHED: September 1, 2020

XIII INTERNATIONAL SYMPOSIUM ON RADIATION FROM RELATIVISTIC ELECTRONS  
IN PERIODIC STRUCTURES — RREPS-19  
SEPTEMBER 16–20, 2019  
BELGOROD, RUSSIAN FEDERATION

Analytical and numerical studies of underdense and overdense regimes in plasma-dielectric wakefield accelerators

G.V. Sotnikov<sup>a,\*</sup>, R.R. Kniaziev<sup>b</sup>, O.V. Manuilenko<sup>a</sup>, P.I. Markov<sup>a</sup>, T.C. Marshall<sup>c</sup>,  
I.N. Onishchenko<sup>a</sup>

<sup>a</sup> NSC Kharkov Institute of Physics and Technology, Kharkov, Ukraine

<sup>b</sup> V.N. Karazin Kharkov National University, Kharkov, Ukraine

<sup>c</sup> Columbia University, New York, USA



**Focusing of Drive and Test Bunches in a Dielectric  
Waveguide Filled with Inhomogeneous Plasma**

G.V. Sotnikov,<sup>1</sup> P.I. Markov and I.N. Onishchenko

National Science Center “Kharkiv Institute of Physics & Technology”,  
1, Akademichna St., Kharkiv, 61108, Ukraine

Nuclear Inst. and Methods in Physics Research, A 909 (2018) 247–251



Contents lists available at ScienceDirect

Nuclear Inst. and Methods in Physics Research, A

journal homepage: [www.elsevier.com/locate/nima](http://www.elsevier.com/locate/nima)



Wake fields effects in dielectric capillary

A. Biagioni<sup>a,\*</sup>, M.P. Anania<sup>a</sup>, M. Bellaveglia<sup>a</sup>, E. Brentegani<sup>a</sup>, G. Castorina<sup>a</sup>, E. Chiadroni<sup>a</sup>,  
A. Cianchi<sup>b</sup>, D. Di Giovenale<sup>a</sup>, G. Di Pirro<sup>a</sup>, H. Fares<sup>e</sup>, L. Ficcadenti<sup>c</sup>, F. Filippi<sup>a</sup>, M. Ferrario<sup>a</sup>,  
A. Mostacci<sup>c</sup>, R. Pompili<sup>a</sup>, J. Scifo<sup>a</sup>, B. Spataro<sup>a</sup>, C. Vaccarezza<sup>a</sup>, F. Villa<sup>a</sup>, A. Zigler<sup>d</sup>

<sup>a</sup> Laboratori Nazionali di Frascati, INFN, Via E. Fermi 40, 00044 Frascati, Italy

<sup>b</sup> Dipartimento di Fisica, Università di Roma Tor Vergata, V. della Ricerca Scientifica 1, 00133 Roma, Italy

<sup>c</sup> Dipartimento di Scienze di Base e Applicate per l'Ingegneria (SBAI), Sapienza Università di Roma, Via A. Scarpa 14-16, 00161 Roma, Italy

<sup>d</sup> Hebrew University of Jerusalem, Jerusalem 91904, Israel

<sup>e</sup> Assiut University, Department of Physics, Faculty of Science, Assiut 71516, Egypt



–SPARC\_LAB studies

## Statement of the problem

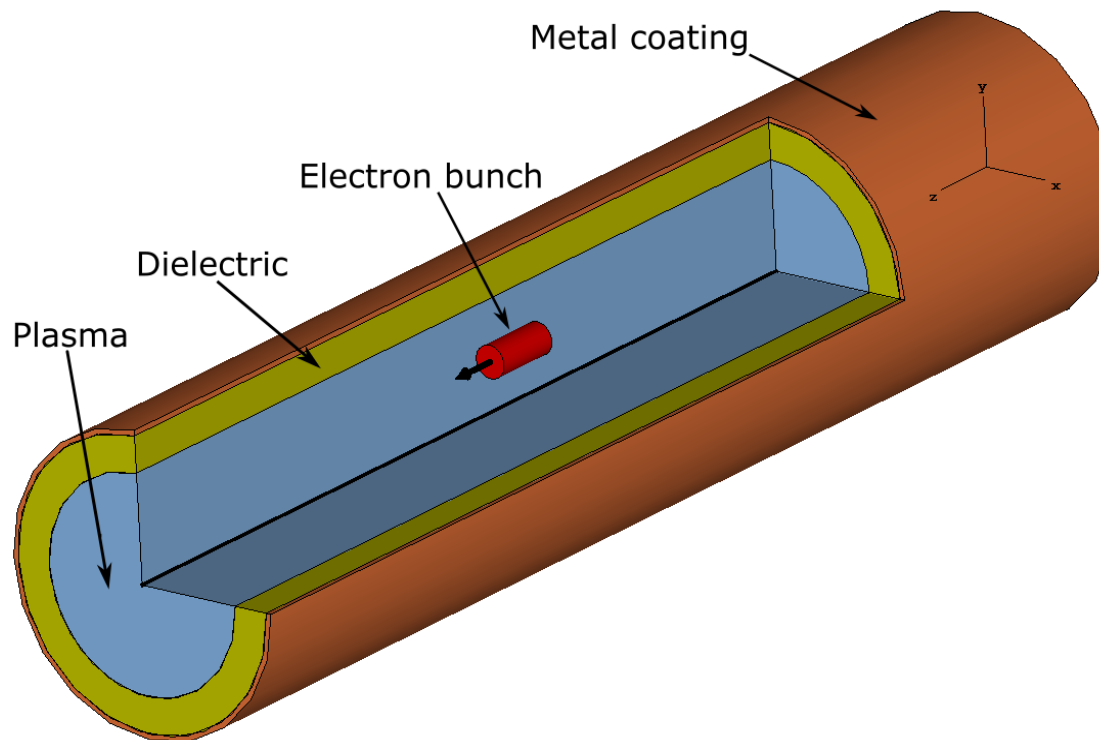
- The structure under investigation is a round dielectric-loaded metal waveguide with channel for the charged particles, filled with homogeneous cold plasma

\*\*\*

- In the plasma a relativistic electron bunch is injected with an offset into the waveguide in parallel to the axis

\*\*\*

- The main goal is to analyze the dynamics of the drive electron bunch in the case of its off-axis injection into the plasma-dielectric structure



## Analitical studies of the wakefield excitation

**-Electromagnetic field components can be expressed in terms of its Fourier transforms**

$$\begin{aligned} \mathbf{E}(r, \varphi, t - z/v) &= \sum_{m=-\infty}^{+\infty} e^{im\varphi} \int_{-\infty}^{+\infty} d\omega \mathbf{E}_m^\omega(r, \omega) e^{-i\omega(t-z/v)}, \quad \mathbf{D}(r, \varphi, t - z/v) = \sum_{m=-\infty}^{+\infty} e^{im\varphi} \int_{-\infty}^{+\infty} d\omega \varepsilon(\omega) \mathbf{E}_m^\omega(r, \omega) e^{-i\omega(t-z/v)}, \\ \mathbf{H}(r, \varphi, t - z/v) &= \sum_{m=-\infty}^{+\infty} e^{im\varphi} \int_{-\infty}^{+\infty} d\omega \mathbf{H}_m^\omega(r, \omega) e^{-i\omega(t-z/v)}, \quad \mathbf{B}(r, \varphi, t - z/v) = \sum_{m=-\infty}^{+\infty} e^{im\varphi} \int_{-\infty}^{+\infty} d\omega \mu(\omega) \mathbf{H}_m^\omega(r, \omega) e^{-i\omega(t-z/v)}, \end{aligned}$$

**-A source of the wakefield is a point charge of charge  $q$  moving with a constant velocity  $v$  along the waveguide axis with an offset  $r_0$**

$$j_z = q \frac{\delta(r - r_0)}{r} \delta(\varphi - \varphi_0) \delta(t - t_0 - z/v)$$

**-The equations for the longitudinal field components are**

$$\begin{aligned} \frac{1}{r} \frac{\partial}{\partial r} \left( r \frac{\partial E_{zm}^\omega}{\partial r} \right) - \frac{m^2}{r^2} E_{zm}^\omega - \frac{\omega^2}{v^2} (1 - \beta^2 \varepsilon(\omega)) E_{zm}^\omega &= \frac{4\pi\omega i}{v^2} \frac{1 - \beta^2 \varepsilon(\omega)}{\varepsilon(\omega)} j_{zm}^\omega, \\ \frac{1}{r} \frac{\partial}{\partial r} \left( r \frac{\partial H_{zm}^\omega}{\partial r} \right) - \frac{m^2}{r^2} H_{zm}^\omega - \frac{\omega^2}{v^2} (1 - \beta^2 \varepsilon(\omega)) H_{zm}^\omega &= 0 \end{aligned}$$

**-All the other field components can be derived from the  $E_z$  and  $H_z$**

## Bunch-excited wakefield components (pencil-like bunch; in the plasma region)

$$\begin{aligned} \frac{F_{zm}}{q} = & -\frac{2Q_b k_p}{L_b} \left( \theta(r_0 - r) \frac{I_m(k_p r)}{I_m(k_p a)} \Delta_m(k_p a, k_p r_0) + \right. \\ & \left. \theta(r - r_0) \frac{I_m(k_p r_0)}{I_m(k_p a)} \Delta_m(k_p a, k_p r) \right) \Psi_{\parallel}^P e^{-im\varphi_0} - \\ & \sum_{s=1}^{+\infty} \frac{4Q_b D_2(\omega_s) v}{a \omega_s^2 D'(\omega_s) L_b} \frac{I_m(\kappa_{ps} r) I_m(\kappa_{ps} r_0)}{I_m^2(\kappa_{ps} a)} \Psi_{\parallel}^S e^{-im\varphi_0} \end{aligned}$$

$$\begin{aligned} \frac{F_{rm}}{q} = & \frac{2Q_b k_p}{L_b} \left( \theta(r_0 - r) \frac{I'_m(k_p r)}{I_m(k_p a)} \Delta_m(k_p a, k_p r_0) + \right. \\ & \left. \theta(r - r_0) \frac{I_m(k_p r_0)}{I_m(k_p a)} \Delta'_m(k_p a, k_p r) \right) \Psi_{\perp}^P e^{-im\varphi_0} + \\ & \sum_{s=1}^{+\infty} \frac{4Q_b D_2(\omega_s) \kappa_{ps} v^2}{a \omega_s^3 D'(\omega_s) L_b} \frac{I_m(\kappa_{ps} r) I_m(\kappa_{ps} r_0)}{I_m^2(\kappa_{ps} a)} \Psi_{\perp}^S e^{-im\varphi_0} \end{aligned}$$

**where:**  $Q_b$  is the bunch charge,  $L_b$  is the bunch length,  $\omega_p$  is the plasma frequency,  $k_p$  is the plasma wave number,  $a$  is the inside radius of the dielectric,  $I_m$  and  $K_m$  are the modified Bessel and Macdonald functions of the  $m^{\text{th}}$  order,  $\Delta_m(x, y) = I_m(x)K_m(y) - K_m(x)I_m(y)$ ,  $\omega_s$  are the eigenfrequencies of the waveguide, which are define by the dispersion equation  $D(\omega_s) = 0$ ,  $\kappa_{ps}^2 = (\omega^2 / v^2)(1 - \beta^2 \varepsilon_p(\omega_s))$ ,  $\varepsilon_p(\omega) = 1 - \omega_p^2 / \omega^2$  is the plasma permittivity,  $\theta(t)$  is the Heaviside function.



## Parameters for the calculations

### **–Parameters of the waveguide (THz frequency range):**

**the inner dielectric radius – 0.5 mm**

**the outer dielectric radius – 0.6 mm**

**the length of the waveguide – 8 cm**

**the dielectric material – quartz ( $\varepsilon = 3.75$  )**

**the plasma density –  $4.41 \cdot 10^{14} \text{ cm}^{-3}$**

### **–Parameters of the bunch (accessible at SLAC):**

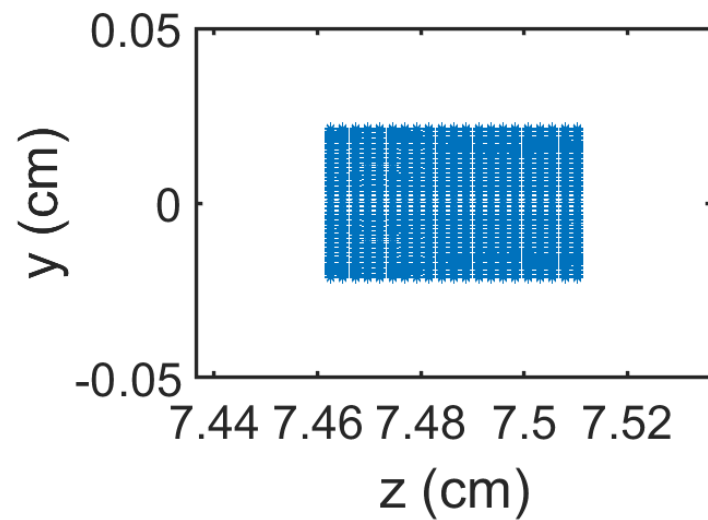
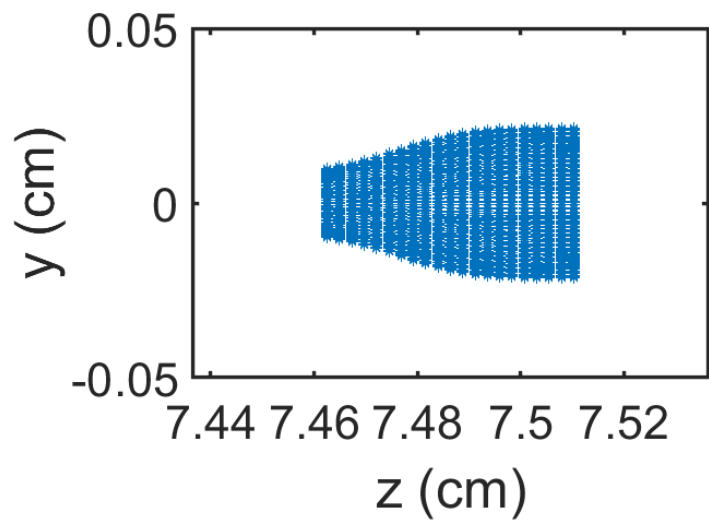
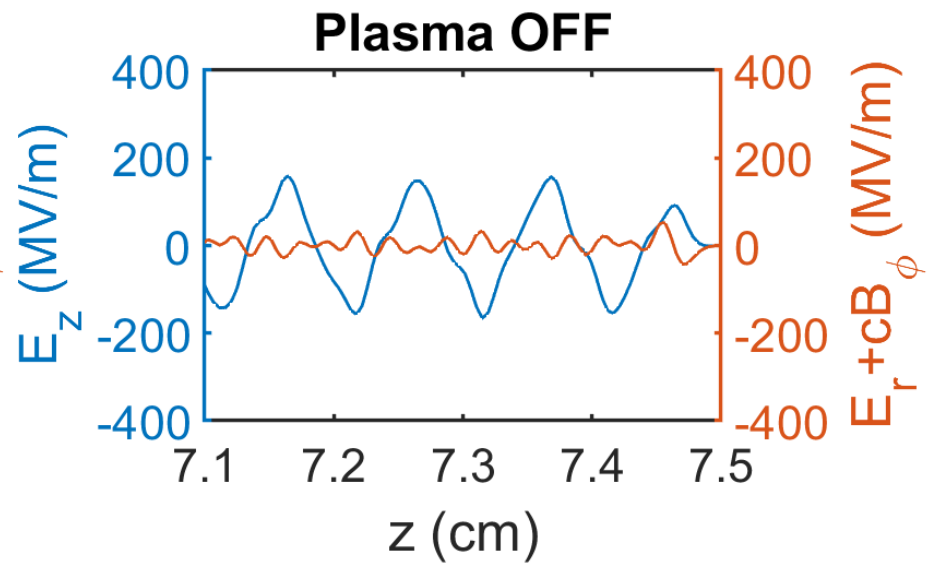
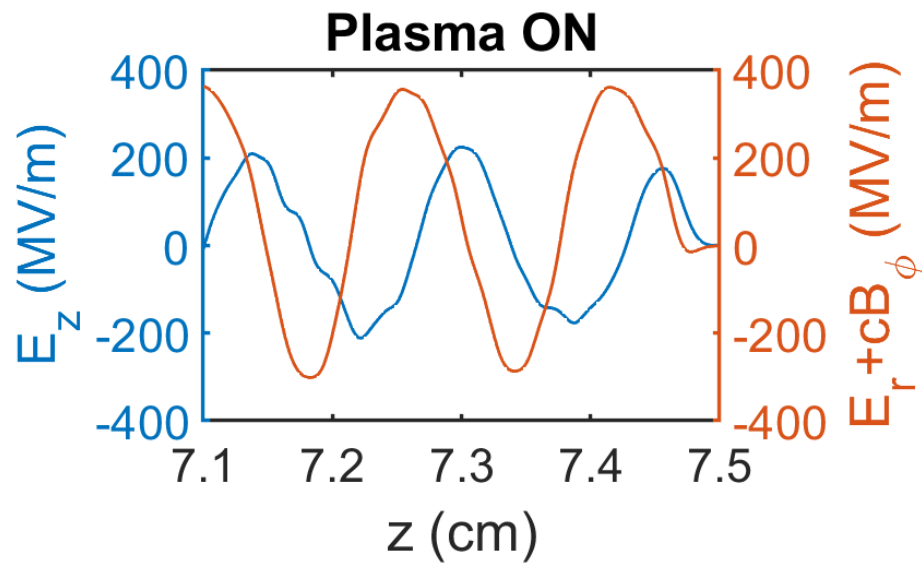
**the energy of bunch electrons – 3 GeV**

**the bunch charge – 3 nC**

**the bunch length – 0.5 mm**

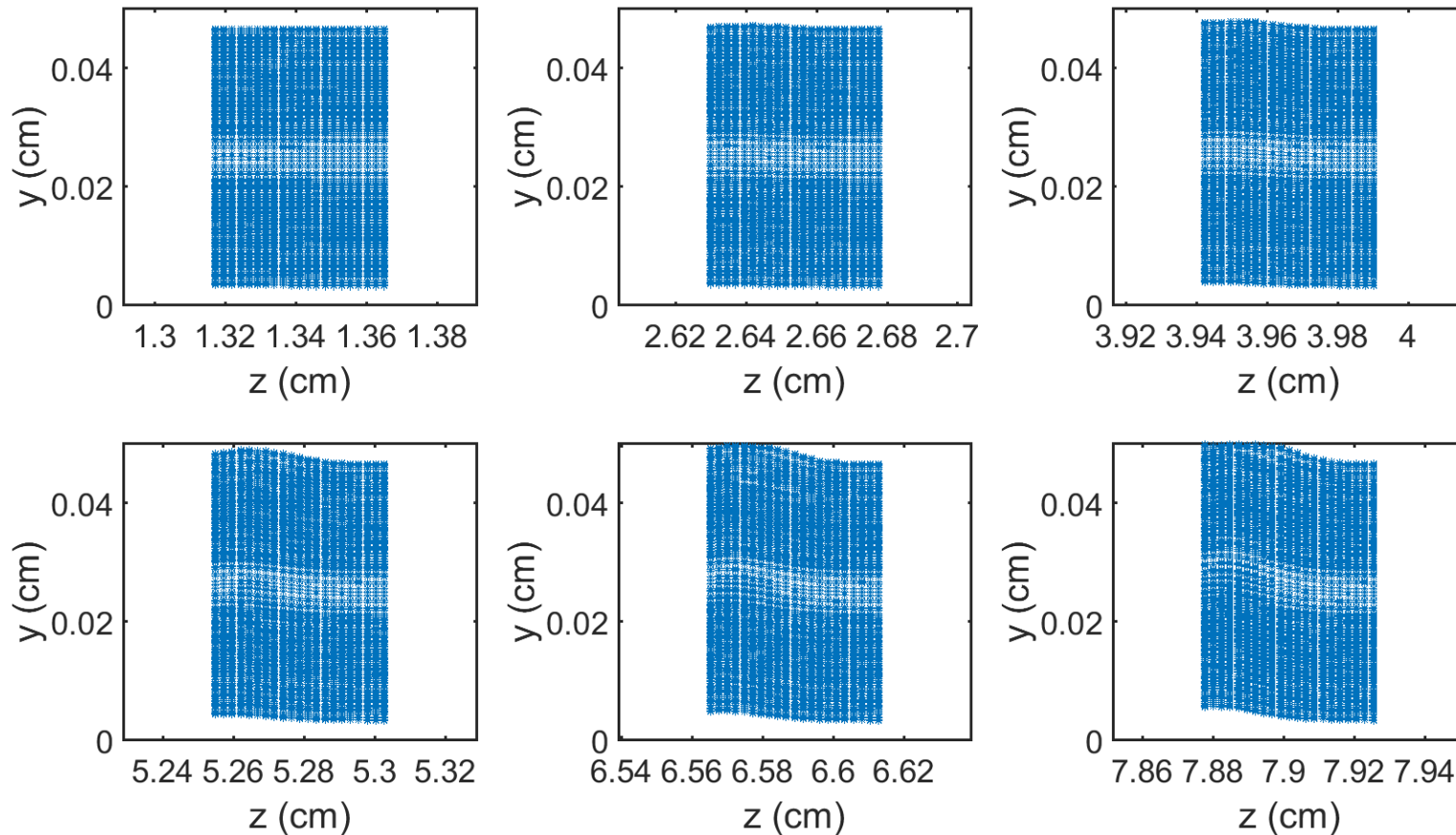
**the bunch radius – 0.23 mm**

**Plasma-dielectric structure VS Dielectric-loaded structure**  
**(on-axis bunch)**



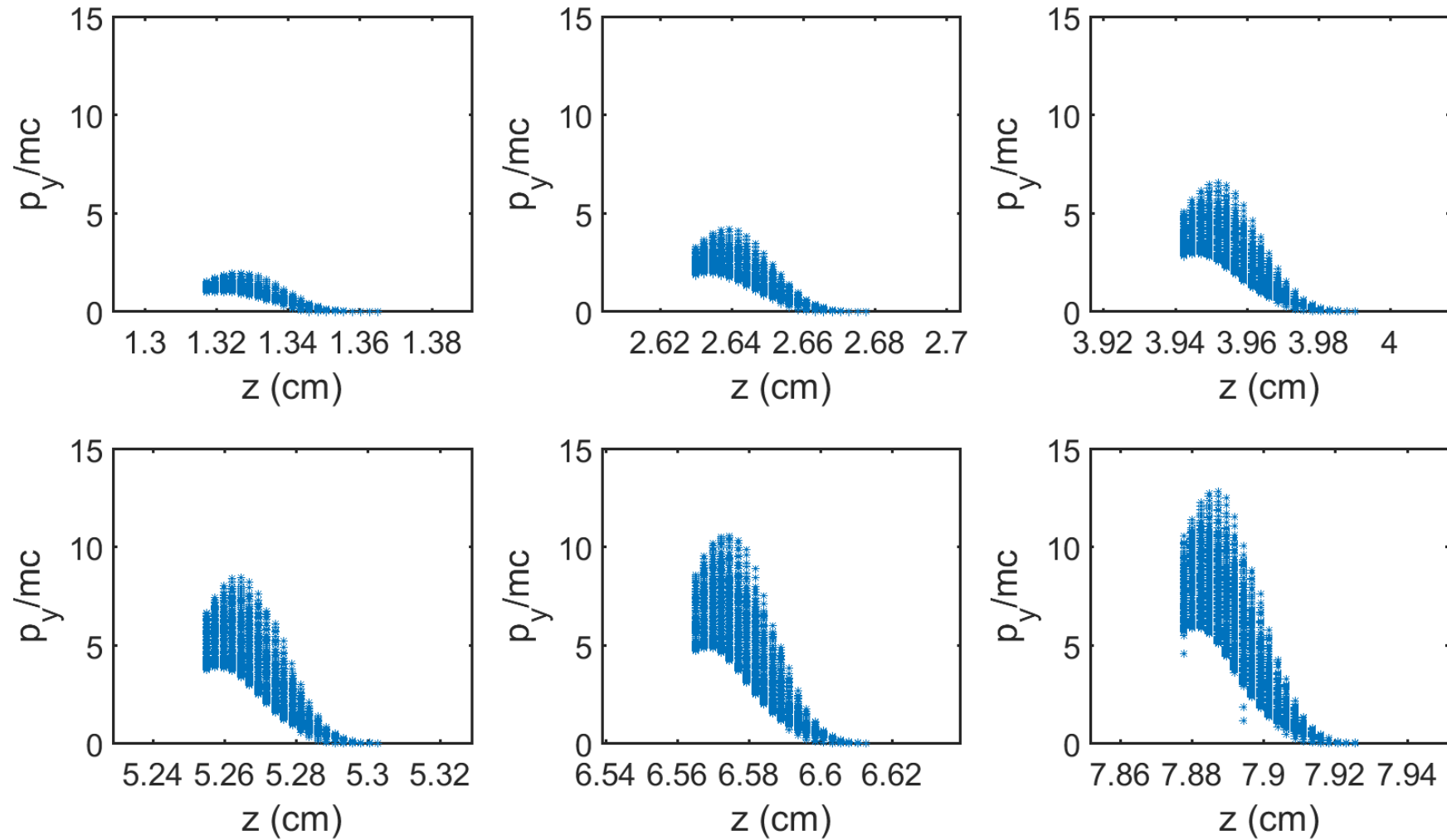
## Transverse bunch dynamics (dielectric-loaded structure) (off-axis bunch)

-In order for the effect of the bunch offset to be more pronounced, we injected it near the dielectric



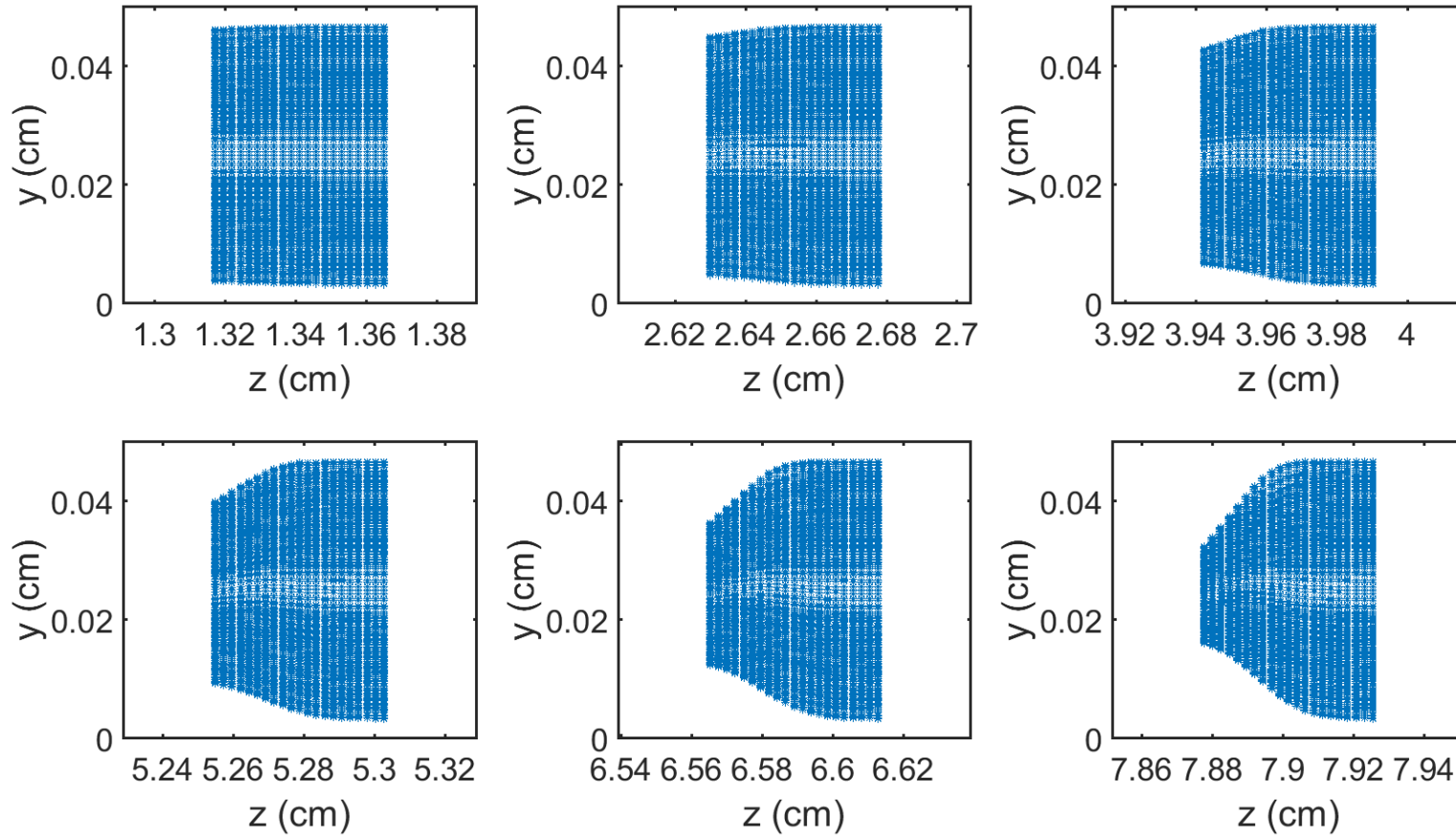
Dynamics of the off-axis bunch on the  $y - z$  plane. Vertical axis limits correspond to half of **vacuum channel** width, horizontal axis limits correspond to the frame around the bunch. The initial vertical offset of the bunch is 0.25 mm, the length of the structure is 8 cm.

**Transverse bunch dynamics (dielectric-loaded structure)**  
**(off-axis bunch)**



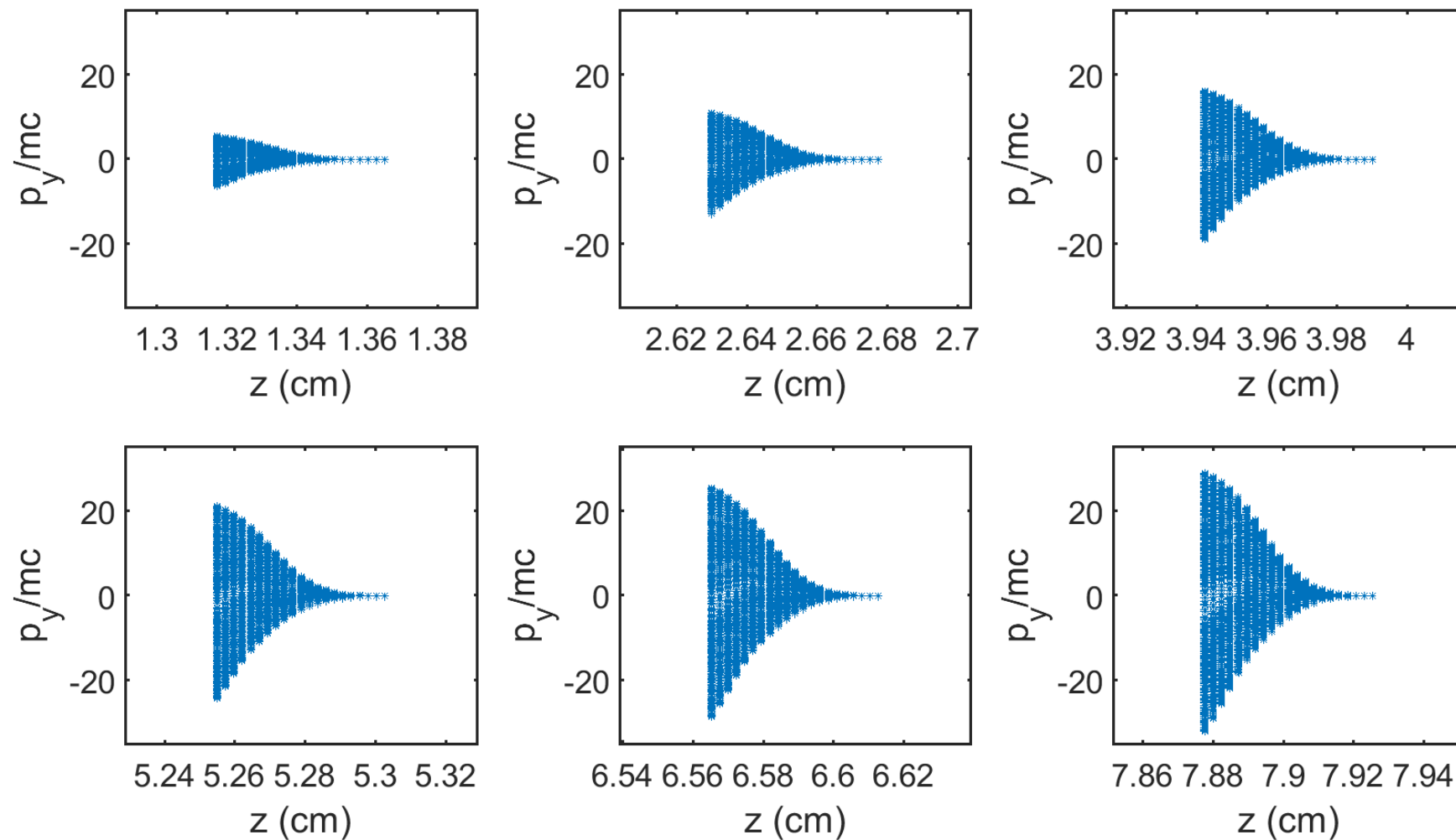
**Bunch particles dynamics in the  $p_y/mc$  -  $z$  plane in the case of off-axis injection**

**Transverse bunch dynamics (plasma-dielectric structure)**  
**(off-axis bunch)**



**Dynamics of the off-axis bunch on the  $y$  –  $z$  plane. Vertical axis limits correspond to half of **plasma channel** width, horizontal axis limits correspond to the frame around the bunch. The initial vertical offset of the bunch is 0.25 mm, the length of the structure is 8 cm.**

**Transverse bunch dynamics (plasma-dielectric structure)**  
**(off-axis bunch)**



**Bunch particles dynamics in the  $p_y/mc$  –  $z$  plane in the case of off-axis injection**

## Conclusions

\*\*\*

**-An analytical theory of wakefield excitation by off-axis particle bunch in a plasma-dielectric waveguide has been formulated. Constructed theory allows carrying out numerical analysis in the rigid bunch approximation**

\*\*\*

**- It was presented the detailed simulation studies of the BBU instability in the plasma-dielectric accelerating structure, excited by a relativistic electron bunch**

\*\*\*

**- A comparison of the off-axis drive bunch transverse dynamics for the cases of the absence and presence of plasma in the channel for charged particles is carried out**

\*\*\*

**- It has been demonstrated that for the plasma-dielectric accelerating structure (unlike the dielectric-loaded structure without plasma) the presence of the initial bunch offset does not lead to the BBU instability. Thus, it is not the critical point, which requires high injection accuracy for the future development and operation of the plasma-dielectric wakefield accelerator**

\*\*\*

**Thank you for your attention !**

**Questions are welcome !**