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# **EFFECT OF DIFFERENT MODELS OF COMBINED-FUNCTION DIPOLES ON THE HEPS PARAMETERS**\* Y.Y. Guo<sup>+</sup>, Y. Jiao, N.Li

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#### **Abstract:**

The high energy photon source (HEPS) is a 6 GeV, kilometer-scale storage ring light source being built in Beijing, China. In the current ring lattice, the combined-function dipoles are used and assumed to have constant dipole field. However, in the actual magnet design, an eccentrically placed quadrupole is adopted, in which the bending field along the trajectory is not constant. In this paper, we will present the effect of the two models of combined-function dipoles on the parameters of the storage ring.





Curvilinear (left) and straight (right) model of combinedfunction dipoles. In the evolution process of the storage ring lattice, the model of curvilinear combined-function dipole with constant dipole field is used. However, in the actual magnet design it is considered to be a quadrupole with a transverse offset.

# PARAMETERS OF STRAIGHT LINE COMBINED-

# **FUNCTION DIPOLE**

### **Method 1: Geometric method**

•  $\operatorname{Cor}_1 = [z_1 = 0, x_1 = x_{off}]$  as the starting point

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- Scan  $x_{off}$  to get the optimal value

#### Method 3: Differential equation method

- $x''[t] = K * x[t] * c^2 * (1 (x'[t])^2/c^2)^{0.5}$
- $z''[t] = K * x[t] * c^2 * x'[t]/c$
- t=0, x'[0]=0, z'[0]=c, x[0]=dx, z[0]=0
- $x_{off} = x[L_B/2/c], L_O = 2*z[L_B/2/c]$

| parameter        | Method1      | Method2      | Method 3     |
|------------------|--------------|--------------|--------------|
| X <sub>off</sub> | -14.713 mm   | -14.714mm    | -14.714mm    |
| L <sub>O</sub>   | 1.0972m–22µm | 1.0972m–24µm | 1.0972m–24µm |

Note: 1.0972m is the nominal arc length of the combined-function dipole

# **EFFECTS ON THE PARAMETERS OF STORAGE RING**

#### Model 1 from method 1

- $B = G^* x_1 \rightarrow \delta \theta \rightarrow \operatorname{Cor}_2 = [z_2, x_2] \rightarrow B = G^* x_2$
- By minimizing  $[L_{curve}, q_{total}]$ - $[L_B, q_B]$ , the optimal  $x_{off}$  and  $L_Q$ can be obtained.

# Method 2: Transfer matrix method



Dividing the magnet into 116 slices, The transfer matrixes of straight line and curvilinear combined-function dipole are close. Then the slice model is substituted into the lattice and some main parameters are calculated.

#### Model 2 from method 2

The straight line combined-function dipole is replaced by 100 dipoles. Each dipole has the same length  $l_s = L_R / 100$ and a little different bending angle.

#### Model 3 base on ELEGANT

In the ELEGANT lattice file, we replace the combinedfunction dipole with 'CCBEND' and calculate the parameters of the lattice.

| parameters                                 | curvilinear model (AT) | straight line  | straight line  | straight line    |
|--|------------------------|----------------|----------------|------------------|
|  |                        | model(model 1) | model(model 2) | model(model 3)   |
| Circumference (m)                          | 1360.4                 | 1360.4013      | 1360.4         | 1360.4           |
| Net bending angle (deg.)                   | 360                    | 360-0.0071     | 360+1.3E-5     | 360 <sup>c</sup> |
| Horizontal natural emittance (pm·rad)      | 34.8271                | 35.8311        | 35.8312        | 36.0510          |
| Working point $(x/y)$                      | 115.1521/              | 115.1521/      | 115.1520/      | 115.1618/        |
|  | 104.2905               | 104.2908       | 104.2903       | 104.2169         |
| Beta functions at the center of            | 8.1757/                | 8.1754/        | 8.1756/        | 8.2038/          |
| high-beta sections (x/y) (m)               | 4.9976                 | 4.9978         | 4.9970         | 4.9540           |
| Momentum compaction (10 <sup>-5</sup> )    | 1.8311                 | 1.8621         | 1.8621         | 1.8476           |
| Energy loss per turn, U <sub>0</sub> (MeV) | 2.6412                 | 2.6461         | 2.6473         | 2.5888           |
| Energy spread (10 <sup>-3</sup> )          | 1.0031                 | 1.0095         | 1.025          | 1.0280           |

#### Summary

As described above, we studied the difference of straight line and curvilinear combined-function dipole. The differences come from that the dipole field along the beam trajectory in the straight line combined-function dipole is not constant while that in the curvilinear combined-function dipole is constant. This leads to the differences of bending radius which result in the differences of the parameters related to the bending radius. Among them, the most concerned is the horizontal natural emittance, which increases by about 1 pm·rad.

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