



Robust Design and Control of the Nonlinear Dynamics for BESSY-III

Work-in-Progress

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for the BESSY-III CDR-Project Team

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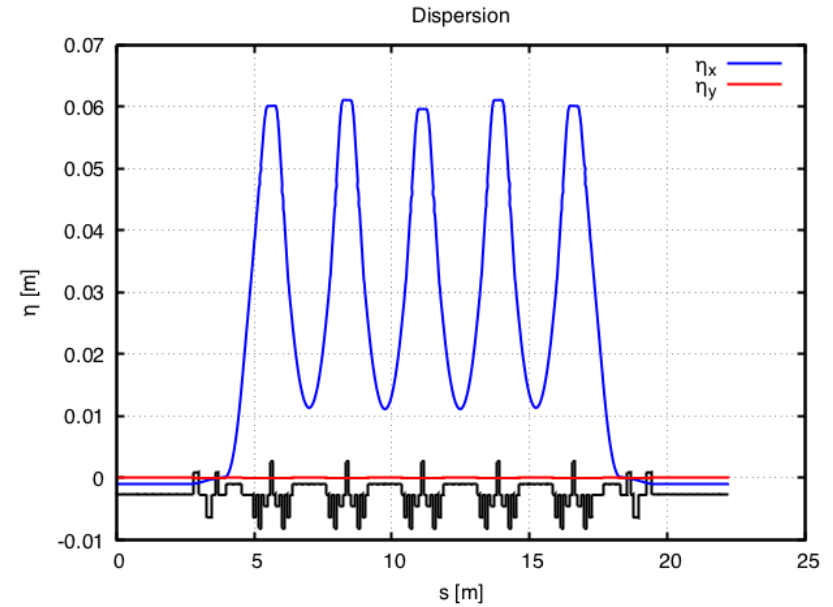
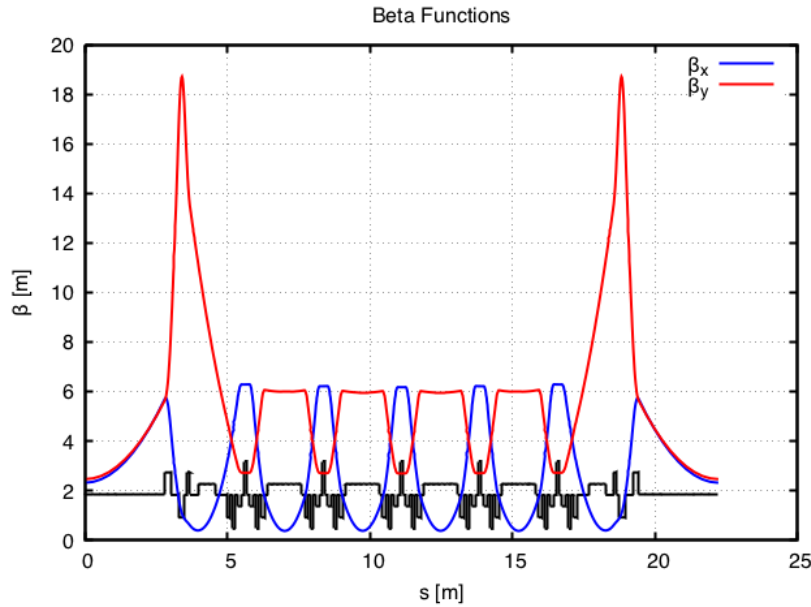
Overview:

1. Requirements: *Straw Man*.
2. Control of Linear Optics – *Bare Lattice*:
 - a) *Higher-Order-Achromat* (HOA)
(SLS, NSLS-II, MAX IV, SLS 2, DIAMOND-II, BESSY-III)
 - b) Driving Terms.
 - c) Tune Footprint.
3. Control of Nonlinear Dynamics – *Real Lattice*:
(incl. the impact of Engineering Tolerances: magnet mechanical misalignments & magnetic multipole errors [random & systematic])
 - a) Control of Orbit.
 - b) Control of Linear Optics (LOCO).
 - c) Frequency Maps.
 - d) On & Off-Momentum Dynamic Aperture (DA).

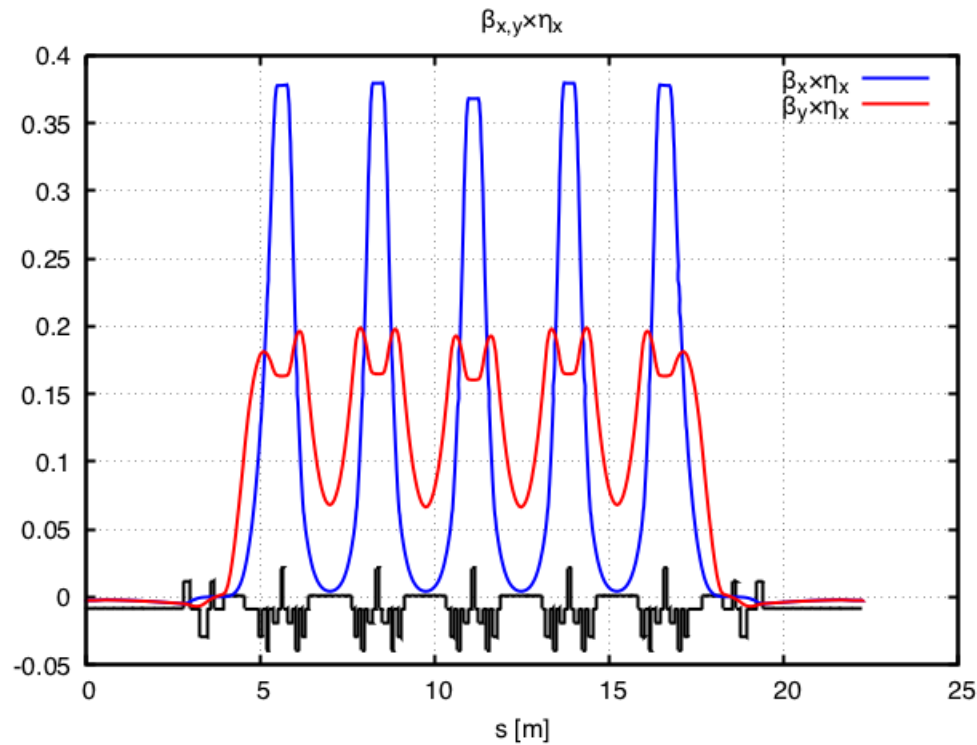
This conference:

- P. Goslawski *BESSY III & MLS II - Status Of The Development Of The New Photon Science Facility In Berlin.*
- B. Kuske *Towards Deterministic Design of MBA-Lattices.*

Beam Lines	
Circumference [m]	~300
Beam Energy [GeV]	2.5
ε_x [pm·rad]	~100
σ_s [mm]	2.5
σ_δ	~1e-3
$\beta_{x,y}$ [m]	[~2.0, ~2.0]
Beam Dynamics	
On-Momentum $A_{x,y}$ DA [mm]	[~2.0, ~1.5]
Off-Momentum δ DA [%]	2.0+
α_c	~1e-4
Beam Lifetime [hrs]	~1.0



Circ. = 356 m.
 ϵ_x = 151 pm·rad.
 α_c = 1.1e-4.
 v_{cell} = [0.40, 0.10].
 v_{sp} = [2.72, 0.76].
 ξ_{sp} = [-4.9, -3.1].



$$\xi_x^{(1)} = -\frac{1}{4\pi} \sum_{i=1}^N \left[(b_2 L)_i - 2(b_3 L)_i \eta_{xi}^{(1)} \right] \beta_{xi},$$

$$\xi_y^{(1)} = \frac{1}{4\pi} \sum_{i=1}^N \left[(b_2 L)_i - 2(b_3 L)_i \eta_{xi}^{(1)} \right] \beta_{yi}$$

- Two Sextupole Families [SF, SD].
- Good separation between ditto.

Sextupole Schemes:

- *-I Transformer*: introduce sextupole pairs separated by $n \cdot \pi$ phase advance in both planes.
- *Higher-Order-Achromat*: introduce a unit cell, repeat it four or more times to generate a super period, and adjust the total phase advance to $n \cdot 2\pi$ in both planes.

(K. Brown *A Second-Order Magnetic Optical Achromat* PAC 1979)

The first approach is standard practice for collider design; and has been generalised by introducing a dispersion bump. However, because the non-linear effects only cancel on-momentum, it tends to yield inferior momentum aperture vs. a HOA; due to systematically driven off-momentum terms: h_{11001} & h_{00111} .

$$M = \begin{bmatrix} \cos(\mu + \xi\delta) & \beta \sin(\mu + \xi\delta) \\ -\frac{\sin(\mu + \xi\delta)}{\beta_x} & \cos(\mu + \xi\delta) \end{bmatrix}$$

$$\rightarrow \begin{bmatrix} -1 & -\beta\xi\delta \\ \frac{\xi\delta}{\beta} & -1 \end{bmatrix} + (\delta^2)$$

$$\mathcal{M}_{\text{cell}} = \mathcal{A}^{-1} \mathcal{R} e^{i h} \mathcal{A}$$

$$\begin{aligned} \mathcal{M} &= \mathcal{M}_{\text{cell}} \mathcal{M}_{\text{cell}} \cdots \mathcal{M}_{\text{cell}} \\ &= \mathcal{A}^{-1} e^{i \mathcal{R} h} e^{i \mathcal{R}^2 h} \cdots e^{i \mathcal{R}^n h} \mathcal{R}^n \mathcal{A} \\ &= \mathcal{A}^{-1} e^{i \mathcal{R} h + i \mathcal{R}^2 h + \cdots + i \mathcal{R}^n h} \mathcal{R}^n \mathcal{A} \end{aligned}$$

$$(\mathcal{R} + \mathcal{R}^2 + \cdots + \mathcal{R}^n) h = \mathcal{R} \sum_{k=0}^{n-1} \mathcal{R}^k h = \mathcal{R} \frac{I - \mathcal{R}^n}{I - \mathcal{R}} = 0$$

- J. Bengtsson *The Sextupole Scheme for the Swiss Light Source (SLS): An Analytic Approach* SLS Tech Note 9/97 (1997).

$$V_{\text{cell}} = [0.40, 0.10].$$

$$V_{\text{sp}} = [2.72, 0.76].$$

$$h_{20001} = h_{02001}^* = \frac{1}{8} \sum_{i=1}^N [(b_2 L)_i - 2(b_3 L)_i \eta_{xi}^{(1)}] \beta_{xi} e^{i2\mu_{zi}} + O(\delta^2),$$

$$h_{00201} = h_{00021}^* = -\frac{1}{8} \sum_{i=1}^N [(b_2 L)_i - 2(b_3 L)_i \eta_{xi}^{(1)}] \beta_{yi} e^{i2\mu_{yi}} + O(\delta^2),$$

$$h_{10002} = h_{01002}^* = \frac{1}{2} \sum_{i=1}^N [(b_2 L)_i - (b_3 L)_i \eta_{xi}^{(1)}] \eta_{xi}^{(1)} \sqrt{\beta_{xi}} e^{i\mu_{zi}} + O(\delta^3)$$

$$h_{21000} = h_{12000}^* = -\frac{1}{8} \sum_{i=1}^N (b_{3i} L) \beta_{xi}^{3/2} e^{i\mu_{xi}},$$

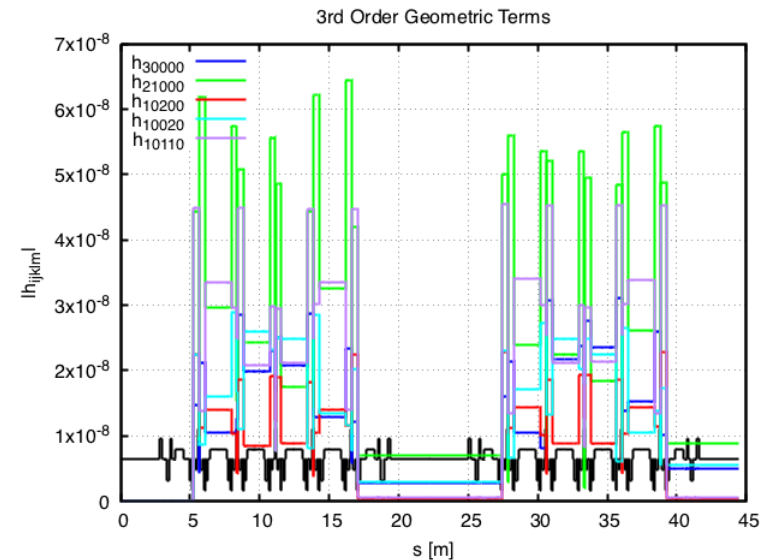
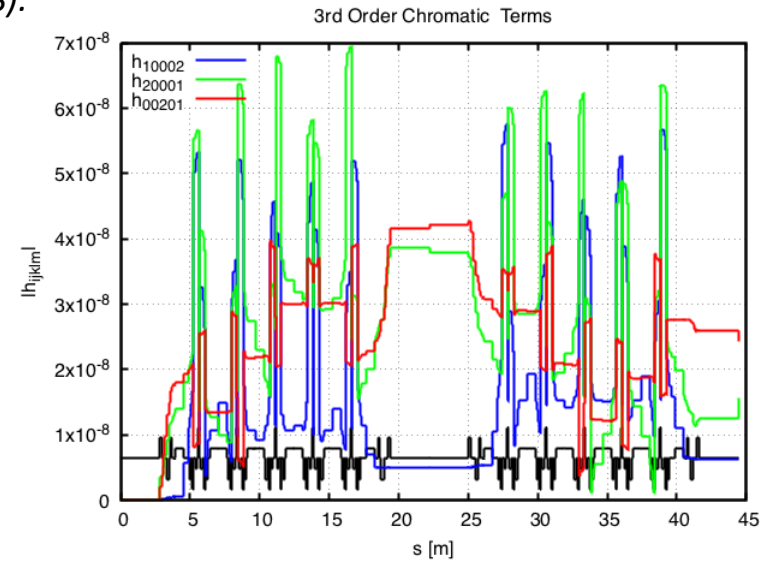
$$h_{30000} = h_{03000}^* = -\frac{1}{24} \sum_{i=1}^N (b_{3i} L) \beta_{xi}^{3/2} e^{i3\mu_{xi}},$$

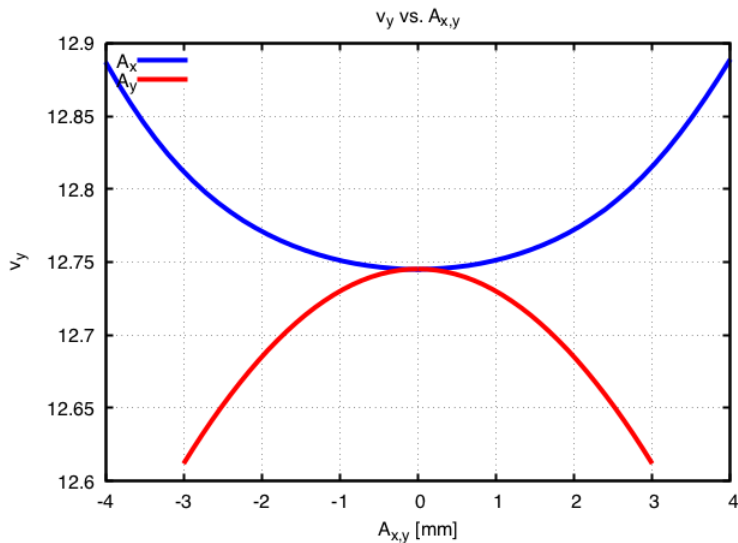
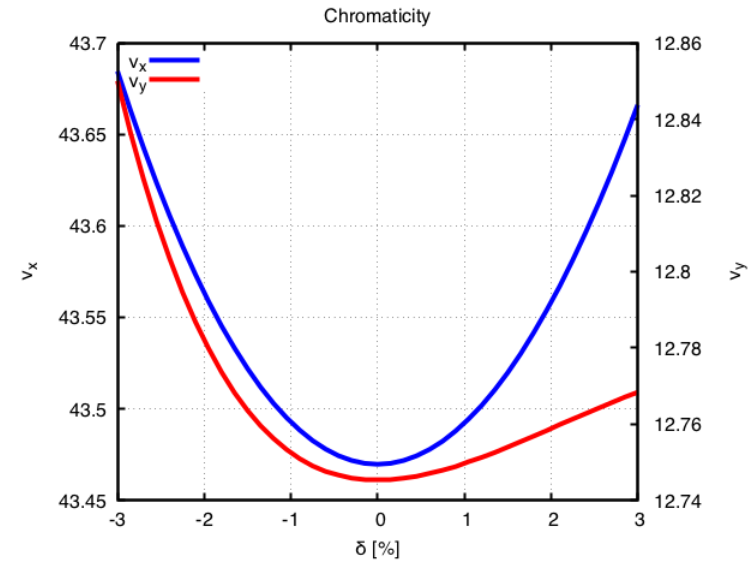
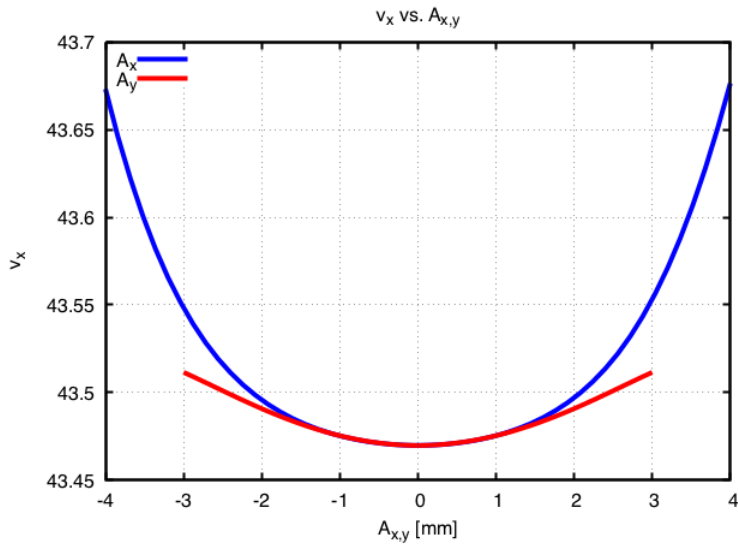
$$h_{10110} = h_{01110}^* = \frac{1}{4} \sum_{i=1}^N (b_{3i} L) \beta_{xi}^{1/2} \beta_{yi} e^{i\mu_{xi}},$$

$$h_{10020} = h_{01200}^* = \frac{1}{8} \sum_{i=1}^N (b_{3i} L) \beta_{xi}^{1/2} \beta_{yi} e^{i(\mu_{xi} - 2\mu_{yi})},$$

$$h_{10200} = h_{01020}^* = \frac{1}{8} \sum_{i=1}^N (b_{3i} L) \beta_{xi}^{1/2} \beta_{yi} e^{i(\mu_{xi} + 2\mu_{yi})}$$

- Chromatic terms (3) cancelled over two super periods.
- Geometric terms (5) cancelled over one super period.

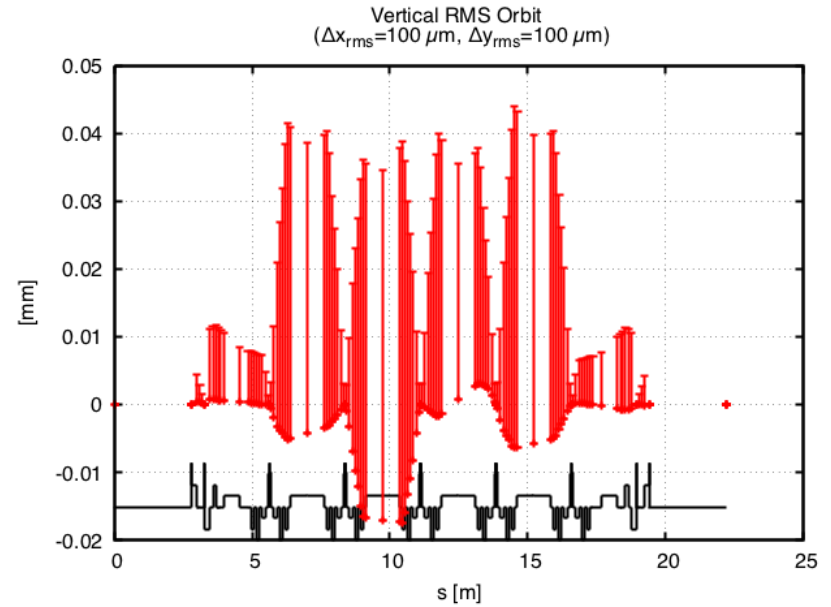
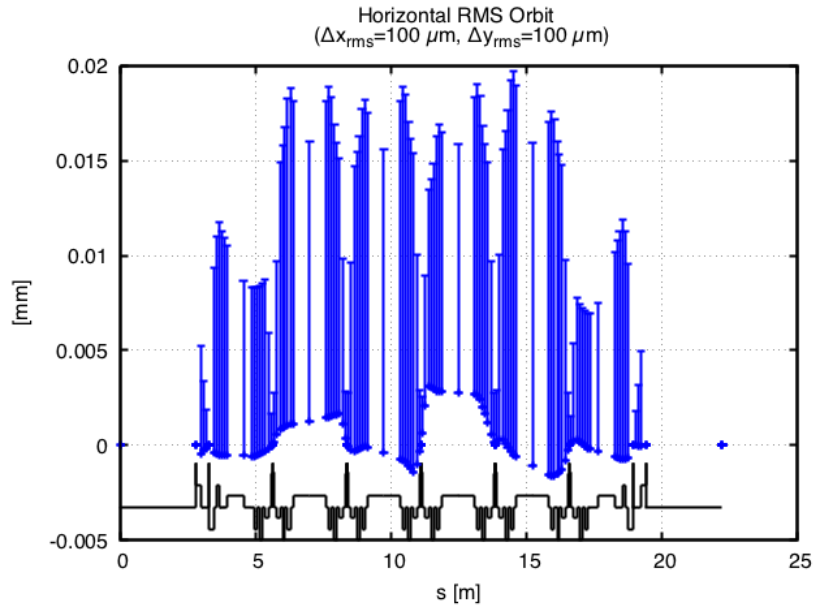




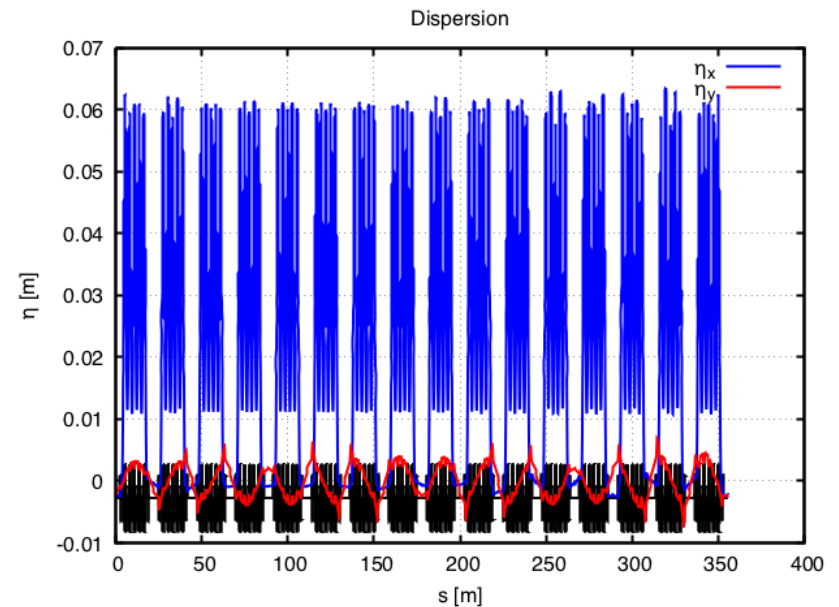
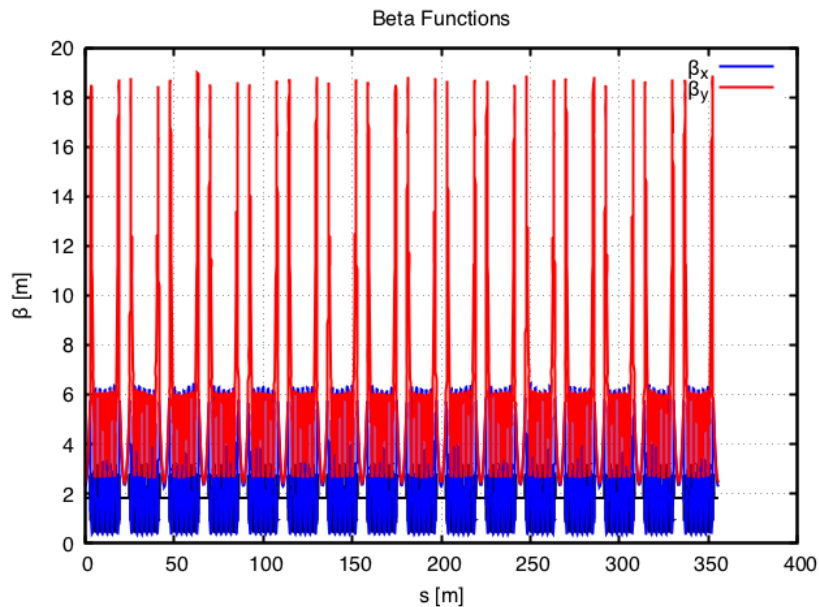
Tune Confinement:

- Two Sextupole Families [SF, SD].
- $\Delta v = 0.1$ benchmark.
- $A \sim [3.0, 2.5]$ mm.
- $\delta \sim 2.0$ %.

J. Bengtsson NSLS-II: *Control of Dynamic Aperture* [BNL-81770-2008-IR \(2008\)](#).

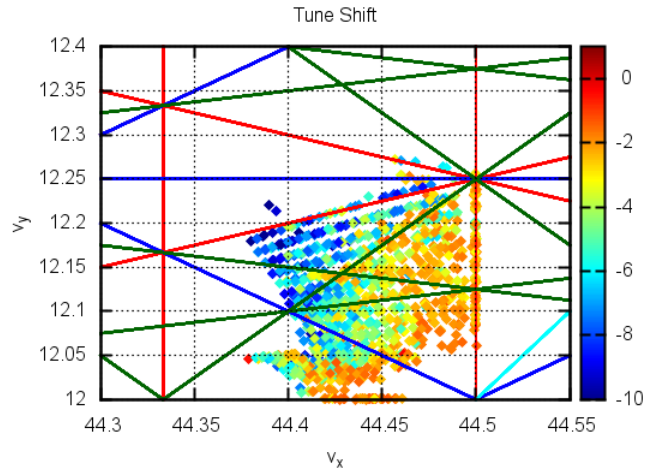


- 9×9 BPMs & Hor/Ver Orbit Trims.
- Average & rms orbit for 100 seeds.

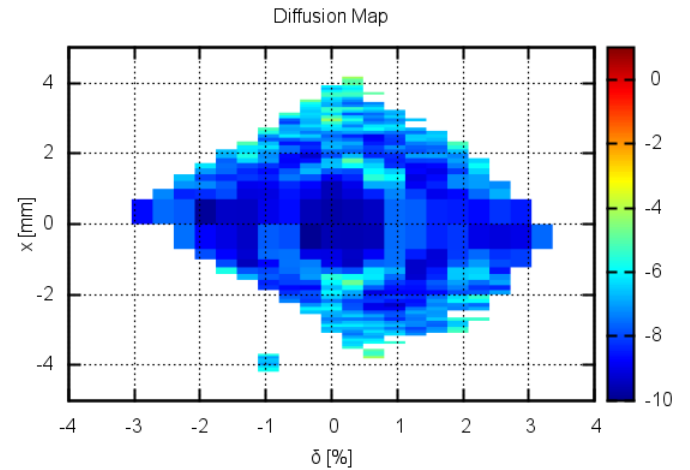
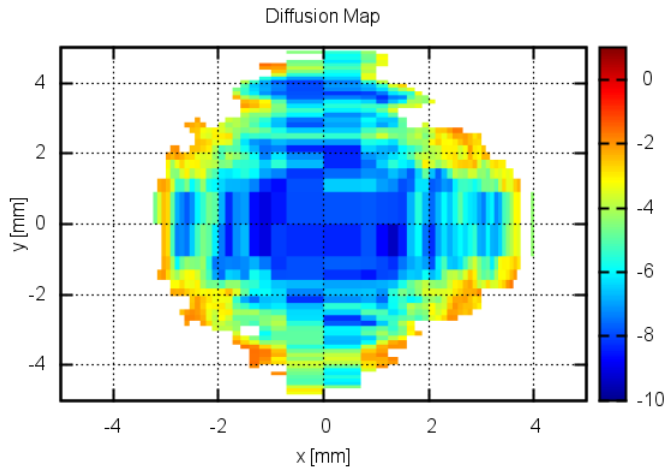
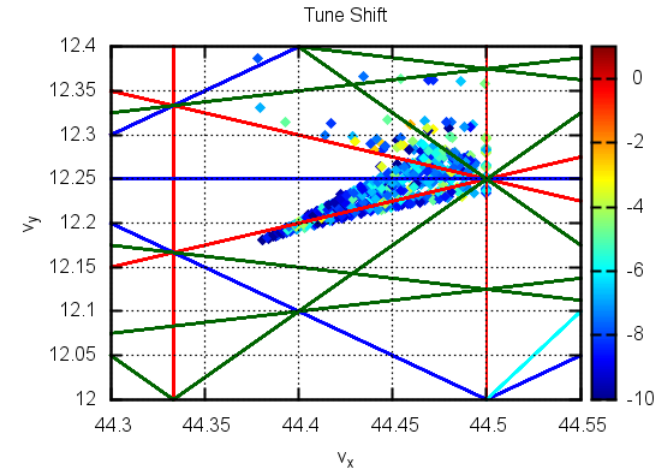


- Magnet mechanical mis-alignments & magnetic multipole errors (random & systematic).
- Closed orbit correction.
- Correction of linear optics by LOCO (*linear optics from closed orbits*).

$\bar{v}(x, y)$

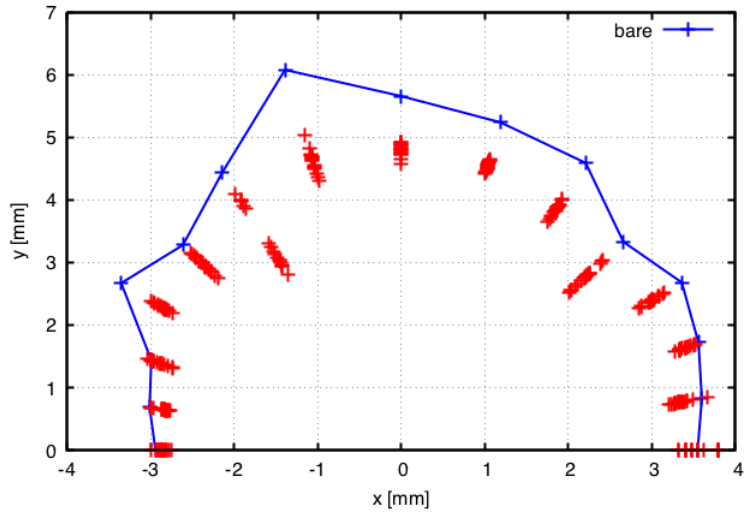


$\bar{v}(x, \delta)$

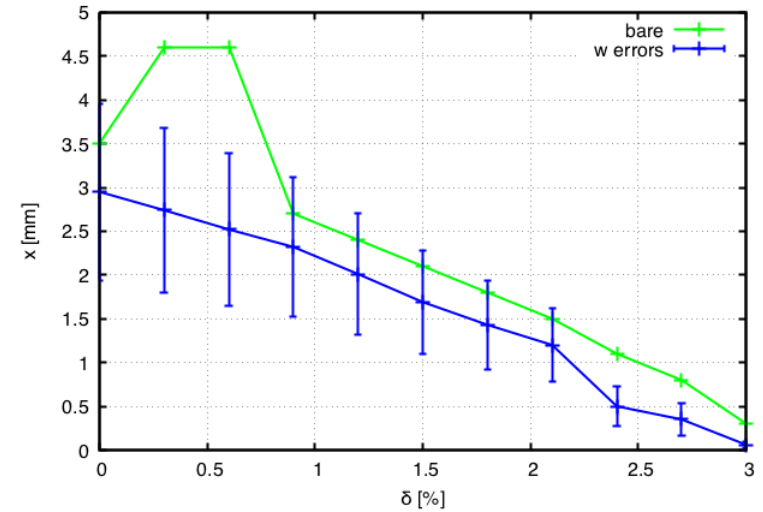


Working point not (yet) optimised.

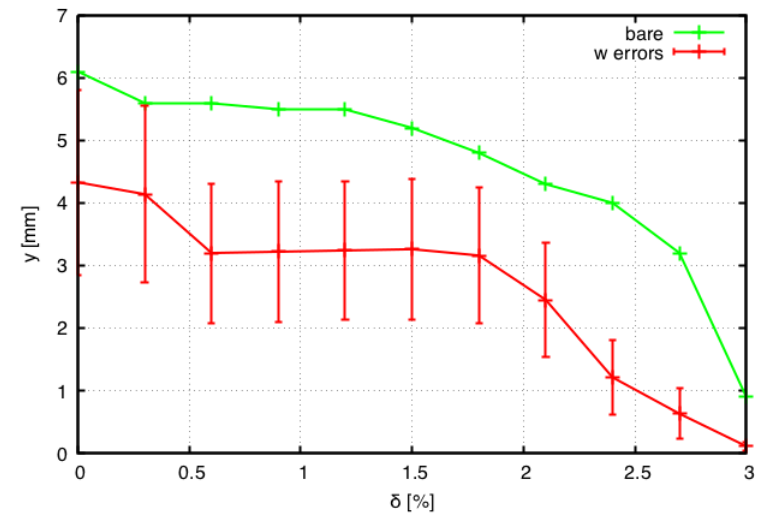
Dynamic Aperture



Horizontal Momentum Aperture



Vertical Momentum Aperture



- $\beta = [2.3, 2.5]$ m.
- For 20 seeds.
- $A \sim [3.0, 4.0]$ mm.
- $\delta \sim 2.5$ %.

Q.E.D. (*quod erat demonstrandum*).

- Convergence on a robust design reference lattice – based on a *Higher-Order-Achromat* with only two sextupole families [SF, SD] (so far) and the *Tune Confinement Approach* – has been achieved for BESSY-III.
- Presumably, control of the off-momentum tune footprint can be improved by introducing two chromatic octupole families.
- After which the trade-off between $\varepsilon_x \leftrightarrow [A_x, A_y, \tau_{\text{TOU}}]$ can be made.