

FLAT BUNCHES WITH A HOLLOW DISTRIBUTION FOR SPACE CHARGE MITIGATION

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Abstract

Longitudinally hollow bunches provide one means to mitigate the impact of transverse space charge. The hollow distributions are created via dipolar parametric excitation during acceleration in CERN's Proton Synchrotron Booster. We present simulation work and beam measurements. Particular emphasis is given to the alleviation of space charge effects on the long injection plateau of the downstream Proton Synchrotron machine, which is the main goal of this study.

INTRODUCTION

In order to push brightness limits given by transverse space charge effects, one can modify the longitudinal bunch shape. Reducing the peak line charge density decreases the space charge tune spread and the beam becomes less prone to betatron resonances located near the working point. The standard approach to flatten the bunch profile makes use of double harmonic RF systems in bunch lengthening mode. In this paper we show that hollow longitudinal distributions provide a viable alternative.

Circular accelerators usually feature the strongest space charge impact at injection. Ideally, bunches should arrive with an already flattened longitudinal profile. Hollow bunches can be created in the upstream accelerator and then transferred into a single harmonic RF system.

Our experiment applies this concept to the CERN Proton Synchrotron Booster (PSB) which provides beams to the Proton Synchrotron (PS). For the double-batch filling scheme, first four bunches are injected into the PS and circulate at the injection energy while the second batch is being prepared in the PSB. After 1.2 s the second batch is injected and the PS acceleration ramp starts. During this period, transverse space charge effects can result in transverse emittance growth and/or beam losses and therefore become a performance limitation for high brightness LHC beams [1].

We present a reliable procedure to create hollow distributions during the PSB acceleration ramp involving minimal changes to the current operational cycle. Finally, we compare emittance blow-up during the PS injection plateau between these hollow bunches and standard parabolic bunches. These efforts build on the experience from past hollow bunch experiments [2, 3].

THEORETICAL CONSIDERATIONS

For a transversely Gaussian normal distributed bunch of particles, the detuning effect of the beam self-fields can

be quantified in terms of the transverse space charge tune spread [4],

$$\Delta Q_u(z) = -\frac{r_p \lambda(z)}{2\pi \beta^2 \gamma^3} \oint ds \frac{\beta_u(s)}{\sigma_u(s) (\sigma_x(s) + \sigma_y(s))} \quad (1)$$

with $u = x$ or $u = y$ for the horizontal resp. vertical plane, z denoting the longitudinal position with respect to the beam centre-of-gravity, $\lambda(z)$ the line charge density in C/m, r_p the classic particle radius, β the speed in units of speed of light, γ the Lorentz factor, $\beta_u(s)$ the betatron function depending on the longitudinal location s around the accelerator ring and $\sigma_u(s)$ the corresponding transverse beam sizes. In presence of dispersion $D_x(s)$, the momentum distribution contributes to the horizontal beam size. Assuming also the momentum distribution to be Gaussian normal distributed yields the well-known expression

$$\sigma_x(s) = \sqrt{\frac{\beta_x(s) \epsilon_x}{\beta \gamma} + D_x^2(s) \delta_{\text{rms}}^2} \quad , \quad (2)$$

where ϵ_x is the normalised beam emittance and δ_{rms} the root mean square of the relative momentum distribution. NB: Eq. (2) is no longer valid for beams with a momentum distribution that significantly deviates from a Gaussian.

Longitudinally hollow phase space distributions address two aspects of Eq. (1) to reduce ΔQ_u^{max} compared to Gaussian or parabolic bunches. They project to

1. intrinsically flat bunch profiles (reduced λ_{max}) and
2. broader momentum profiles (increased δ_{rms} and σ_x).

To create such hollow bunches during the PSB cycle, a longitudinal dipolar parametric resonance is excited by phase modulation [5]. To this end we use the phase loop feedback system, which aligns the RF reference phase ϕ_{rf} with the centre-of-gravity of the bunch. We modulate the phase loop offset around the synchronous phase ϕ_S :

$$\phi_{\text{rf}}(t) = \phi_S + \hat{\phi}_{\text{drive}} \sin(\omega_{\text{drive}} t) \quad . \quad (3)$$

To excite the beam, the driving frequency ω_{drive} needs to satisfy the resonance condition

$$m \omega_{\text{drive}} \simeq n \omega_S \quad , \quad (4)$$

where ω_S denotes the angular synchrotron frequency. The integer numbers m and n characterise the $m : n$ parametric resonance. The actual synchrotron frequency of any particle within the RF bucket decreases with its synchrotron amplitude due to increasingly non-linear synchrotron motion towards the separatrix. Below transition, as in the PSB, longitudinal space charge additionally reduces ω_S .

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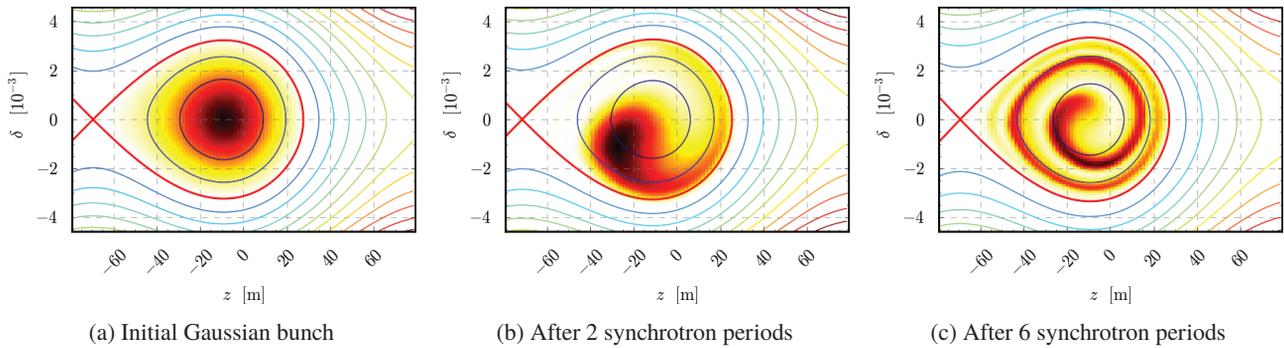


Figure 1: Longitudinal phase space (z, δ) with $\delta = (p - p_0)/p_0$ during the excitation of the 1:1 dipolar parametric resonance in the PSB (from PyHEADTAIL [6] simulations).

PSB HOLLOW BUNCH CREATION

PyHEADTAIL Simulations

By driving the 1 : 1 resonance at a frequency slightly below the linear synchrotron frequency, $\omega_{drive} \approx 0.9\omega_{S,lin}$, the particles in the bunch core are excited to higher synchrotron amplitudes. Figure 1 shows the depletion of the bunch centre within a few synchrotron periods leading to hollow longitudinal phase space distributions. Higher order resonances create two or more filaments spiralling outward from the bunch centre and are thus less effective for depletion.

The synchrotron frequency spread between the inner- and outer-most particles leads to a filamentation-like angular spread. The modulation duration determines the azimuthal span to which the excited particles surround the depleted bucket centre. The optimal duration distributing the particles as evenly as possible depends in descending importance on the excitation amplitude $\hat{\phi}_{drive}$, the ratio between longitudinal emittance and bucket acceptance, and the beam intensity. The latter dependency becomes evident during intensity scans and is explained by decoherence suppression due to longitudinal space charge, which reduces the frequency spread over the particles and may prevent the filamentation process [7].

The final longitudinal emittance ϵ_z varies with the bunch intensity, excitation period and amplitude. To reach a specific ϵ_z , modifying $\hat{\phi}_{drive}$ turns out to be the most effective parameter, while the excitation duration is fixed beforehand by maximising the azimuthal phase space distribution.

Implementation in PSB

Based on the current operational LHC-type beam set-up, we introduced the phase modulation at cycle time C575 (corresponding to an intermediate energy of $E_{kin} = 0.71$ GeV) in a single harmonic accelerating bucket. During 9 ms equivalent to 6 synchrotron periods the beam is driven onto the resonance starting from an initial matched longitudinal emittance of $\epsilon_{z,100\%} = 1.1$ eV s. With these settings, the resulting distributions appeared consistently and reproducibly depleted.

Varying the driving frequency for the parametric resonance revealed a broad resonance window. The beam turned out to be correctly excited for frequencies in the range

$$649 \text{ Hz} \leq \frac{\omega_{drive}}{2\pi} \leq 734 \text{ Hz}$$

This resonance window is sharply defined up to 1 Hz.

Special attention had to be given to optimise the phase loop gain during the excitation process: for a too strong gain, the phase loop continuously realigns the phase of the main C02 cavities with the beam. This counteracts the excitation and leads to severely perturbed distributions.

Eventually, the long filament can be smoothed to a ring-like phase space distribution by high frequency phase modulation at harmonic $h = 9$ with the C16 cavities. Figure 2 shows tomographic reconstructions [8] of longitudinal phase space at important cycle times. The horizontal axis is reverted compared to Fig. 1, since $\phi = -z/R$ with R the machine radius.

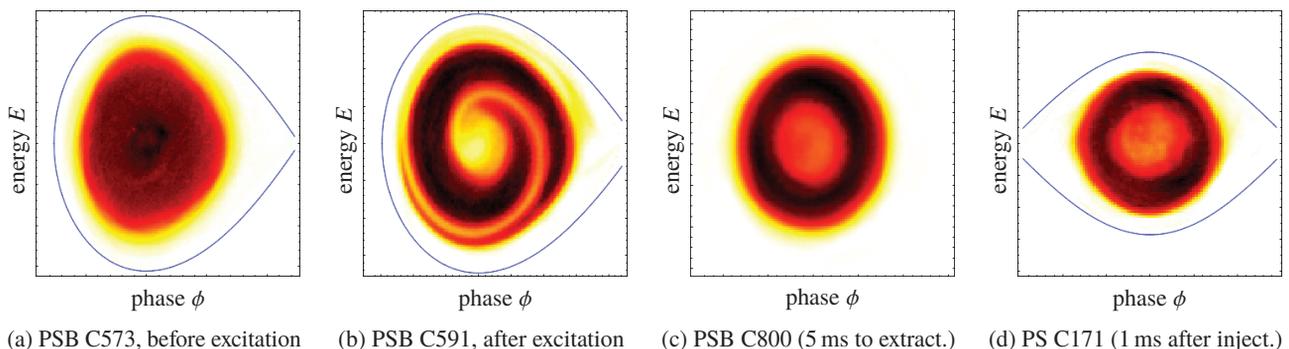


Figure 2: Longitudinal phase space (ϕ, E) reconstructed via tomography at different stages in the PSB (measurements).

SPACE CHARGE MITIGATION IN PS

To assess the impact of direct space charge during the 1.2 s PS injection plateau at $E_{\text{kin}} = 1.4$ GeV and $h = 7$, we compare single bunch beams of the usual LHC parabolic type with the modified hollow type by measuring transverse emittance blow-up and beam loss. For each shot, tomography and wire scans yield the z, δ, x, y distributions 15 ms after injection and again 20 ms before the second batch injection time. Table 1 lists the experiment parameters.

Table 1: Relevant Experiment Beam Parameters for PS

Parameter	Hollow value	Parabolic value
N	$(1.66 \pm 0.05) \times 10^{12}$	$(1.84 \pm 0.03) \times 10^{12}$
$\epsilon_{z,100\%}$	1.43 ± 0.15 eV s	1.47 ± 0.11 eV s
$\epsilon_{z,\text{rms}}$	0.32 ± 0.02 eV s	0.3 ± 0.01 eV s
Q_x, Q_y	$(6.23, 6.22)$	

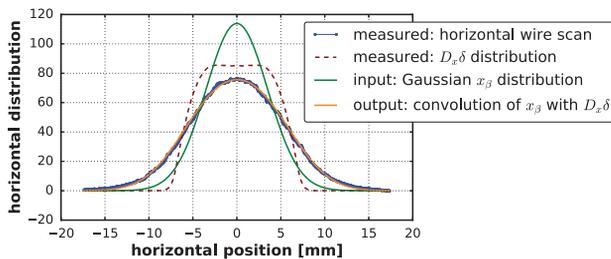
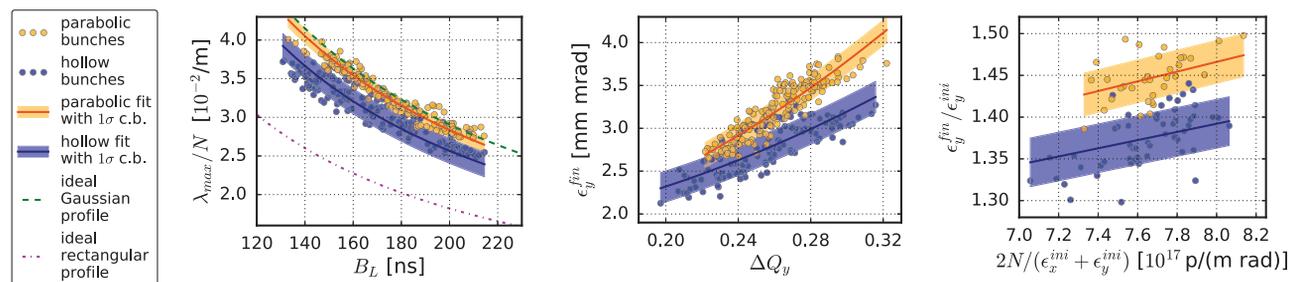


Figure 3: Wire scan comprising betatron and dispersive part.

Determining the horizontal emittance ϵ_x requires special attention: since the momentum δ is by construction not Gaussian distributed for hollow bunches, Eq. (2) is not valid. The horizontal particle position is a sum of two independent random variables, $x = x_\beta + x_{D_x\delta}$. The dispersive profile is given by the measured δ distribution and $D_x = 2.3$ m at the wire scanner location. Convoluting with a Gaussian distributed betatron profile hence yields an estimate of the horizontal profile. The horizontal emittance ϵ_x can then be found by a least squares algorithm comparing the resulting convolution with the actual measured profile, cf. Fig. 3. This



(a) Intensity normalised peak line charge density vs. total bunch length.

(b) Vertical emittances (end of inject. plateau) vs. space charge tune shift.

(c) Vertical emittance blow-up vs. brightness (at $V_{\text{rf}} = 80$ kV).

Figure 4: Comparison of hollow and parabolic bunches. Fits include 1σ confidence bands.

procedure is applied to both beams. Results differ by 24.8% to 34.8% from Eq. (2) in both cases.

Over many shots, we vary the bunch length for both beam types by adiabatically ramping the total RF voltage during the initial 15 ms to values between the initial 25 kV and 80 kV. Due to varying shot-to-shot efficiency of the C16 blow-up, we achieve total bunch lengths over a range of $B_L = 130 \dots 220$ ns. Figure 4a depicts consistently depressed peak line densities by a factor 0.9 for the flattened profiles compared to the parabolic ones. A theoretically ideal rectangular profile of $4\sigma_z$ length would yield a $\sqrt{2\pi}/4 \approx 0.63$ depression factor compared to a perfect Gaussian. Both extrema are plotted in Fig. 4a for comparison.

We want to compare the impact of space charge for both beam types for fixed B_L , N and ϵ_u . To unify this set in one quantity, we choose to evaluate ΔQ_u^{max} assuming a 6D Gaussian distributed beam in Eq. (1). Hence we apply (2) as well as using the Gaussian peak line density $\lambda_{\text{max}} = N/(\sqrt{2\pi}\sigma_z)$ where we set $\sigma_z = B_L/4$. Figure 4b shows how hollow bunches provide statistically significantly lower vertical emittances for the same unified reference tune shift ΔQ_u^{max} . The real tune shift of the hollow bunches is a factor 0.88 lower due to their reduced λ_{max} and the larger σ_x . In contrast, the parabolic bunches are rather well represented by the Gaussian approach (factor 0.97 lower real tune shift).

Finally, keeping the maximum RF voltage 80 kV, we scan the intensity by varying the injected turns in the PSB. Figure 4c exhibits the emittance blow-up $\epsilon_y^{\text{fin}}/\epsilon_y^{\text{ini}}$ versus the brightness, which is again lower for the hollow bunches.

CONCLUSION

We have set up a reliable process to create hollow bunches with minimal changes to the operational PSB cycle. Due to the lower peak line density, the longitudinally hollow bunches are shown to be less affected by space charge compared to the LHC-type parabolic bunches during the PS injection plateau.

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