

# Closed Beam Orbit Calculations in AGS and Fast Beam Extraction

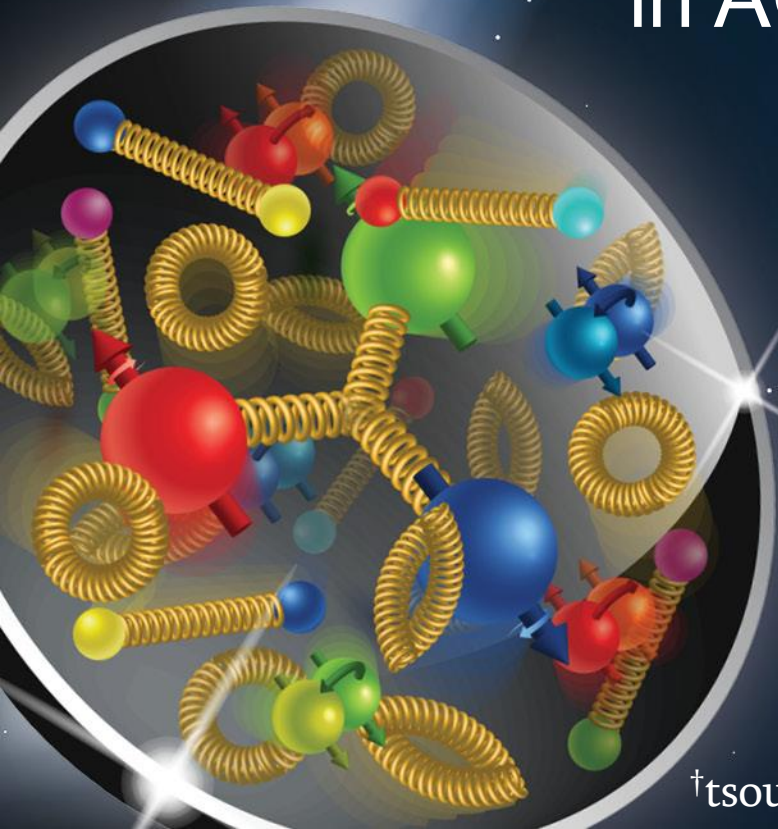
N. Tsoupas<sup>†</sup>, J. S. Berg, S. Brooks, F. Méot,  
V. Ptitsyn, D. Trbojevic

Brookhaven National Laboratory

S. Machida

STFC Rutherford Appleton Laboratory England

Electron Ion Collider – eRHIC

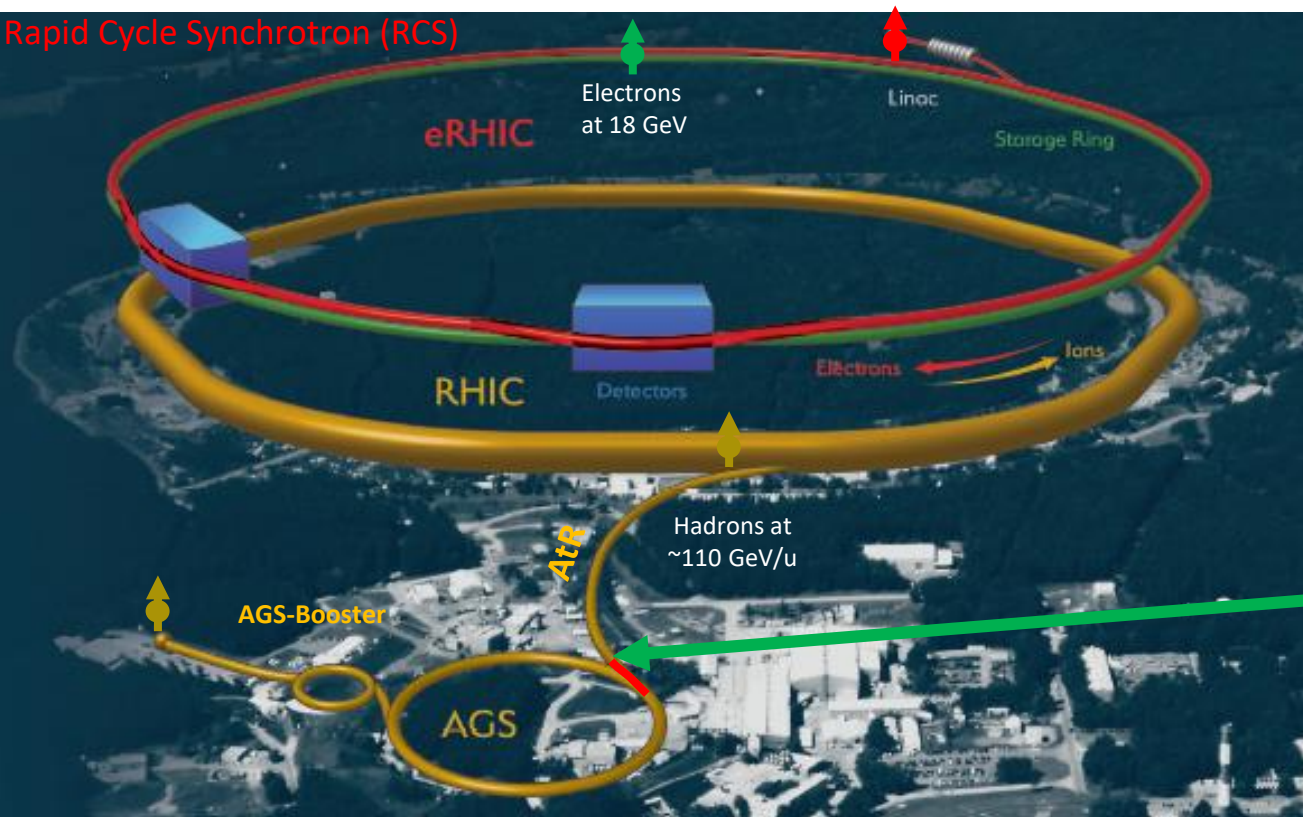
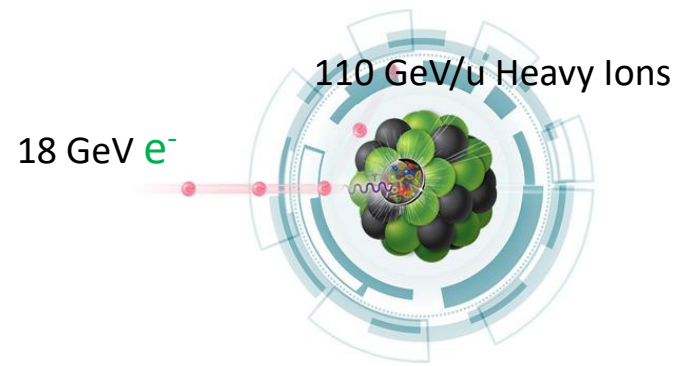


<sup>†</sup>tsoupas@bnl.gov



# The future eRHIC Collider

Work performed in 1994 published in a BNL internal report  
But never reported in a conference.



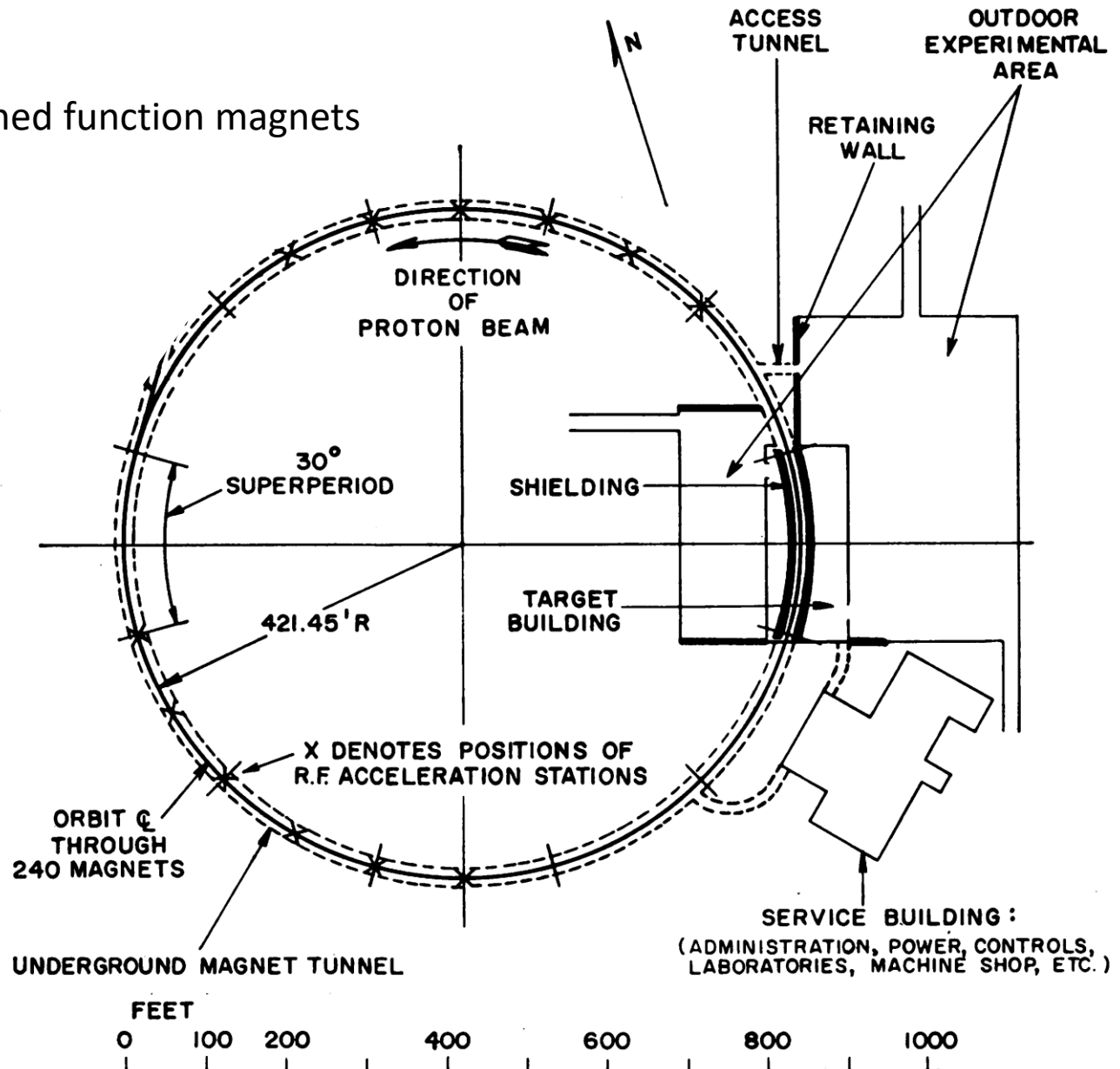
Beam Optics of AGS  
based on  
measured magnetic fields

Beam parameters at the  
Fast Beam Extraction of AGS  
or the start of  
AGS to RHIC (AtR) line





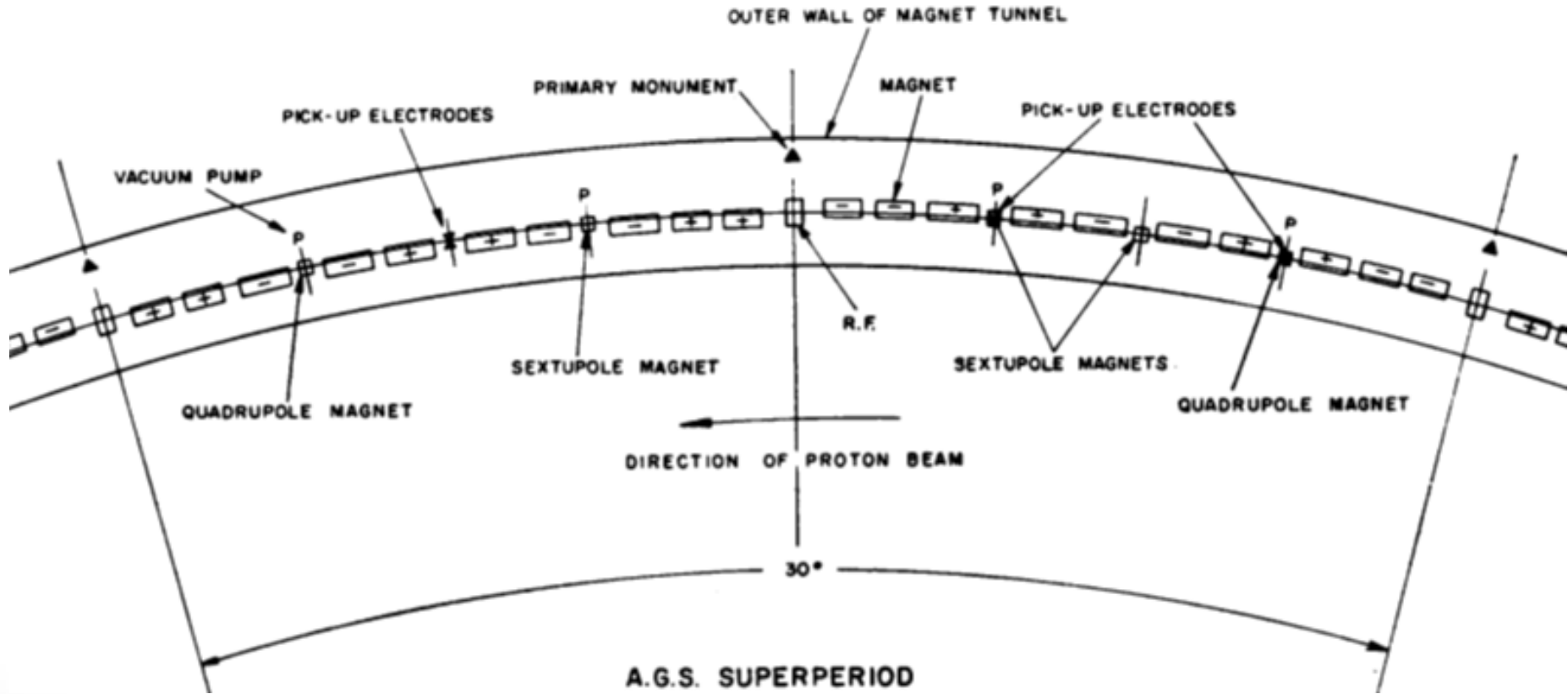
## 240 Combined function magnets



# AGS Superperiod

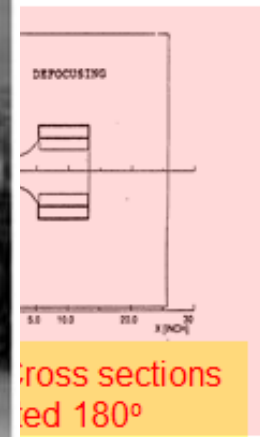
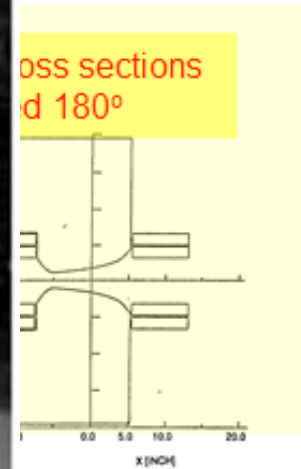
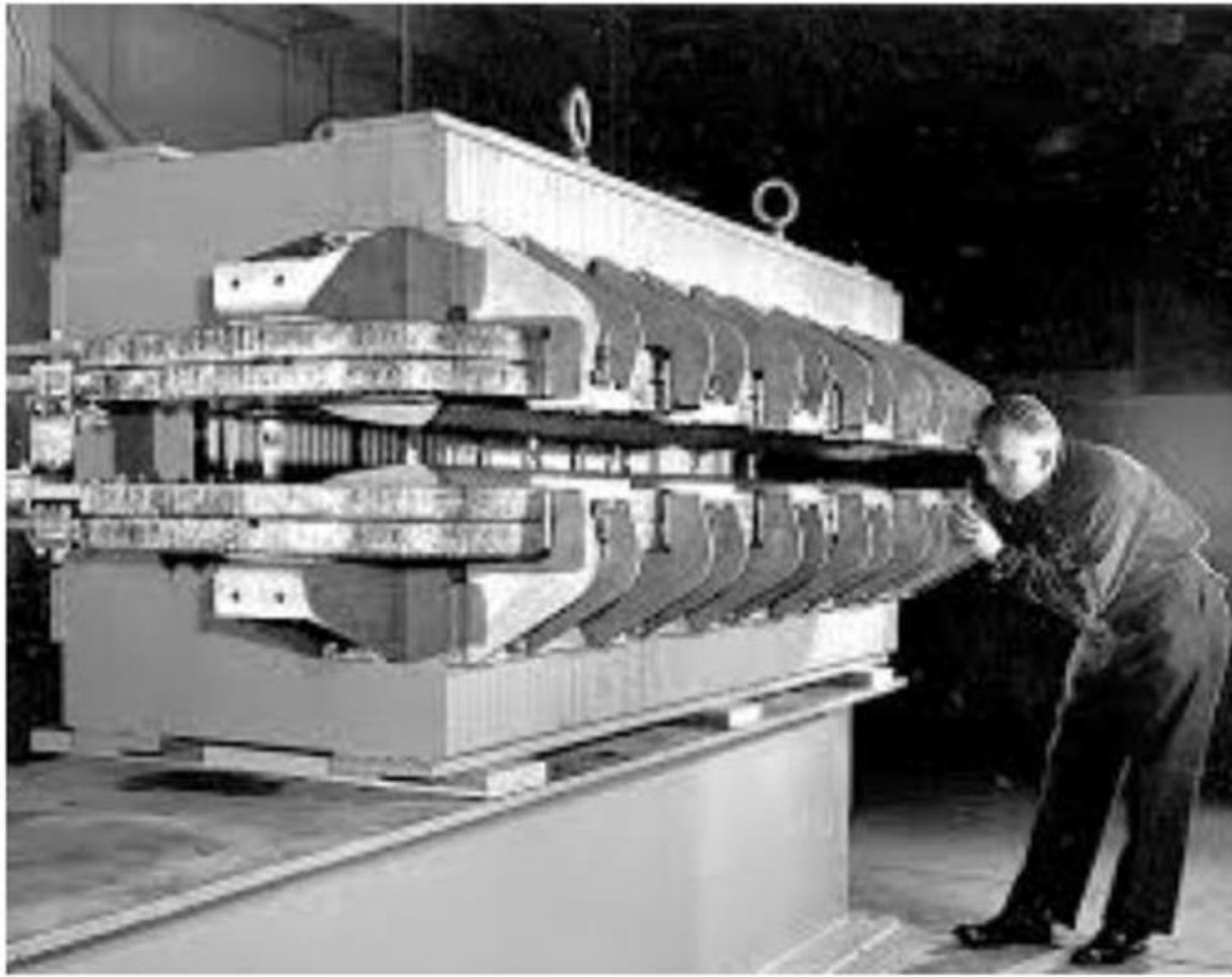
Tune quadrupoles SS03 and SS17

Chromaticity Sextupoles SS05 and SS13

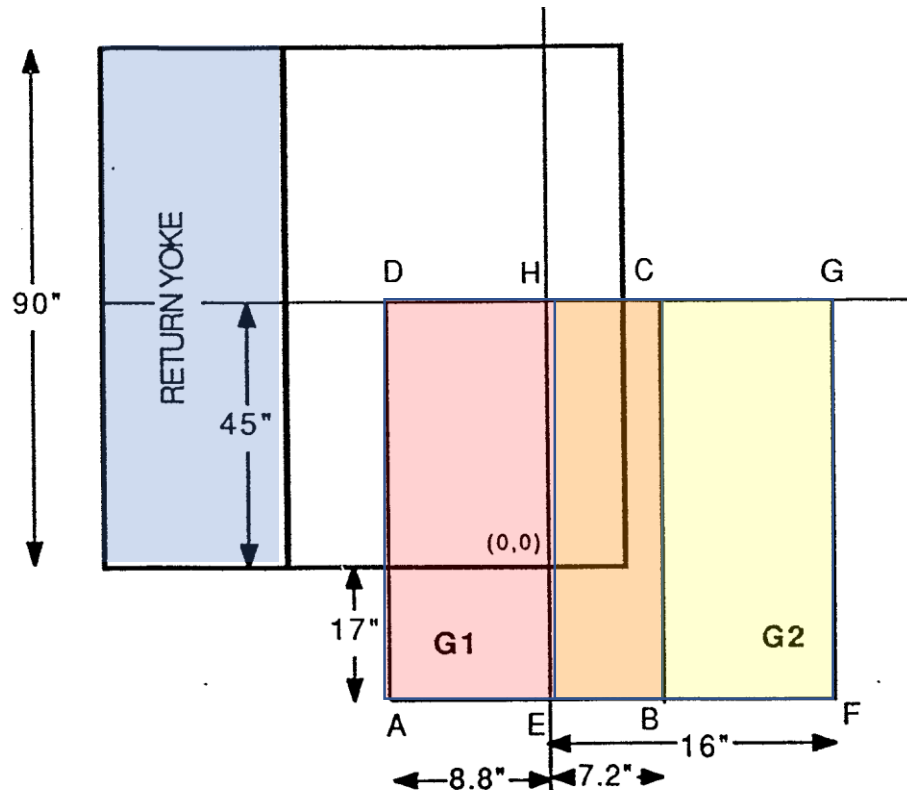


# The three types of the AGS Magnets

Type
A
B
C



# The 2D field maps on plane grids

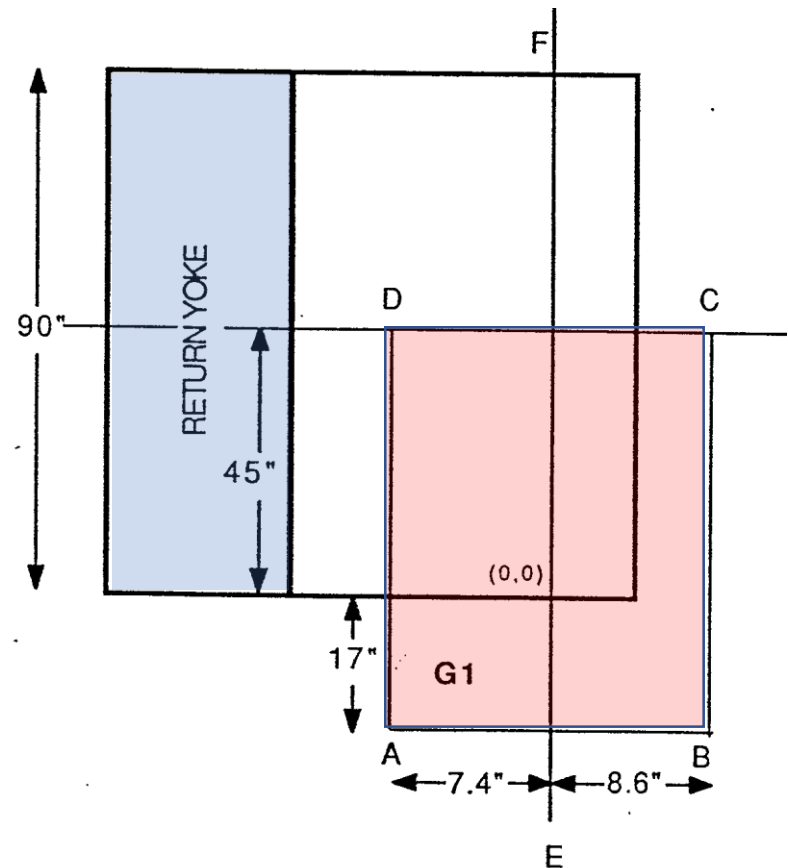


Magnet type A (L=90)

G1 plane  $8.8'' \leq x \leq -7.2''$

G2 plane  $0.0'' \leq x \leq -16''$

Step in x-transverse 0.10"  
Step in z-longitudinal 0.25"



Magnet type C (L=90)

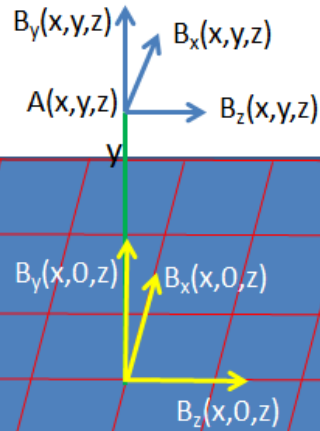
G1 plane  $7.4'' \leq x \leq -8.6''$

Step in x-transverse 0.10"  
Step in z-longitudinal 0.25"

## Algorithm to calculate 3D Fields from field maps on a plane

$$B_i(x, y, z) = \sum_{j=0}^4 \frac{1}{j!} \frac{\partial^j B_i(x, y, z)}{\partial y^j} \Big|_{y=0} y^j = \sum_{j=0}^4 a_{ij}(x, z) y^j \quad (1)$$

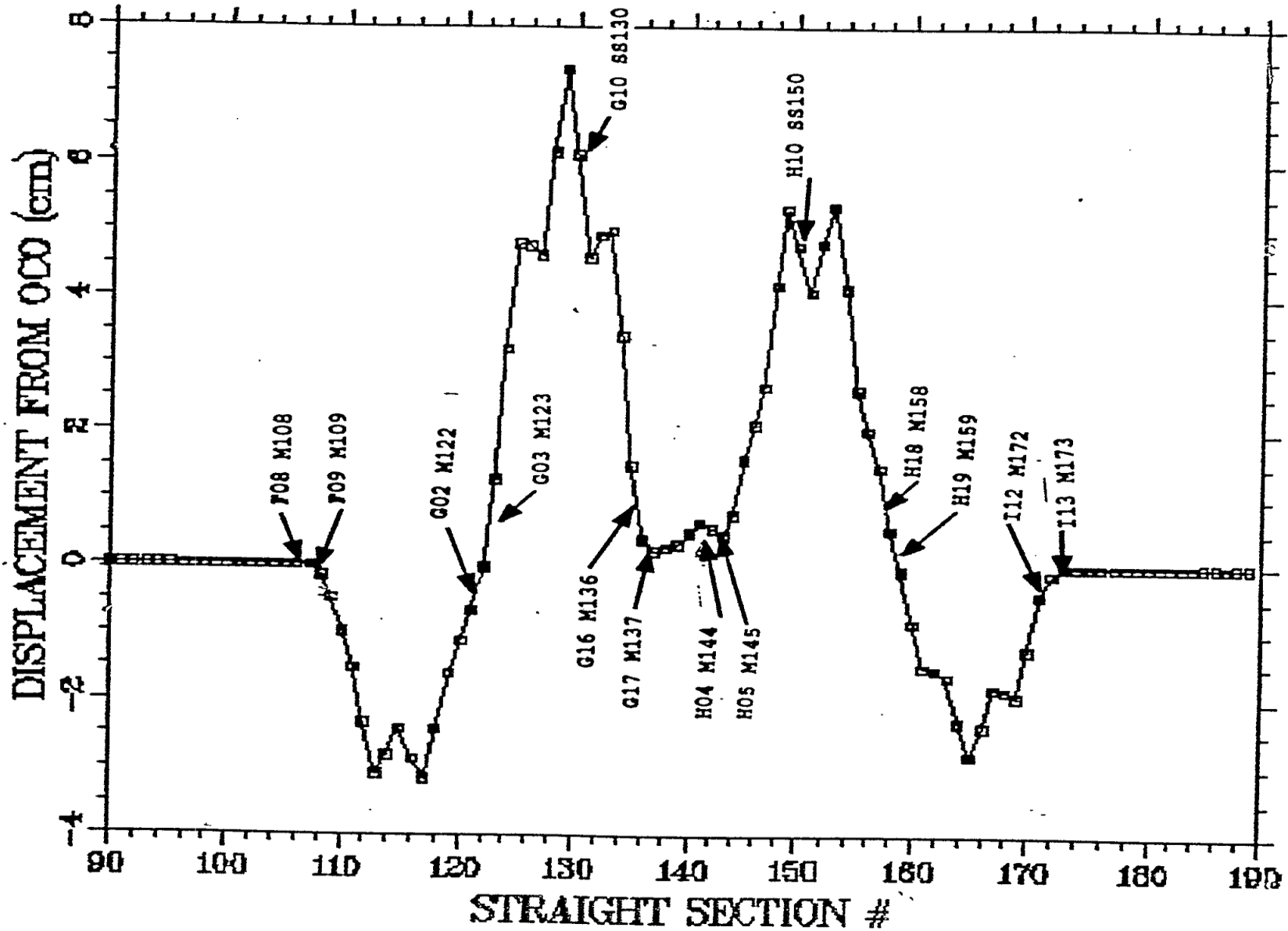
$$\vec{\nabla} \cdot \vec{B}(x, y, z) = 0 \quad \text{and} \quad \vec{\nabla} \times \vec{B}(x, y, z) = 0$$

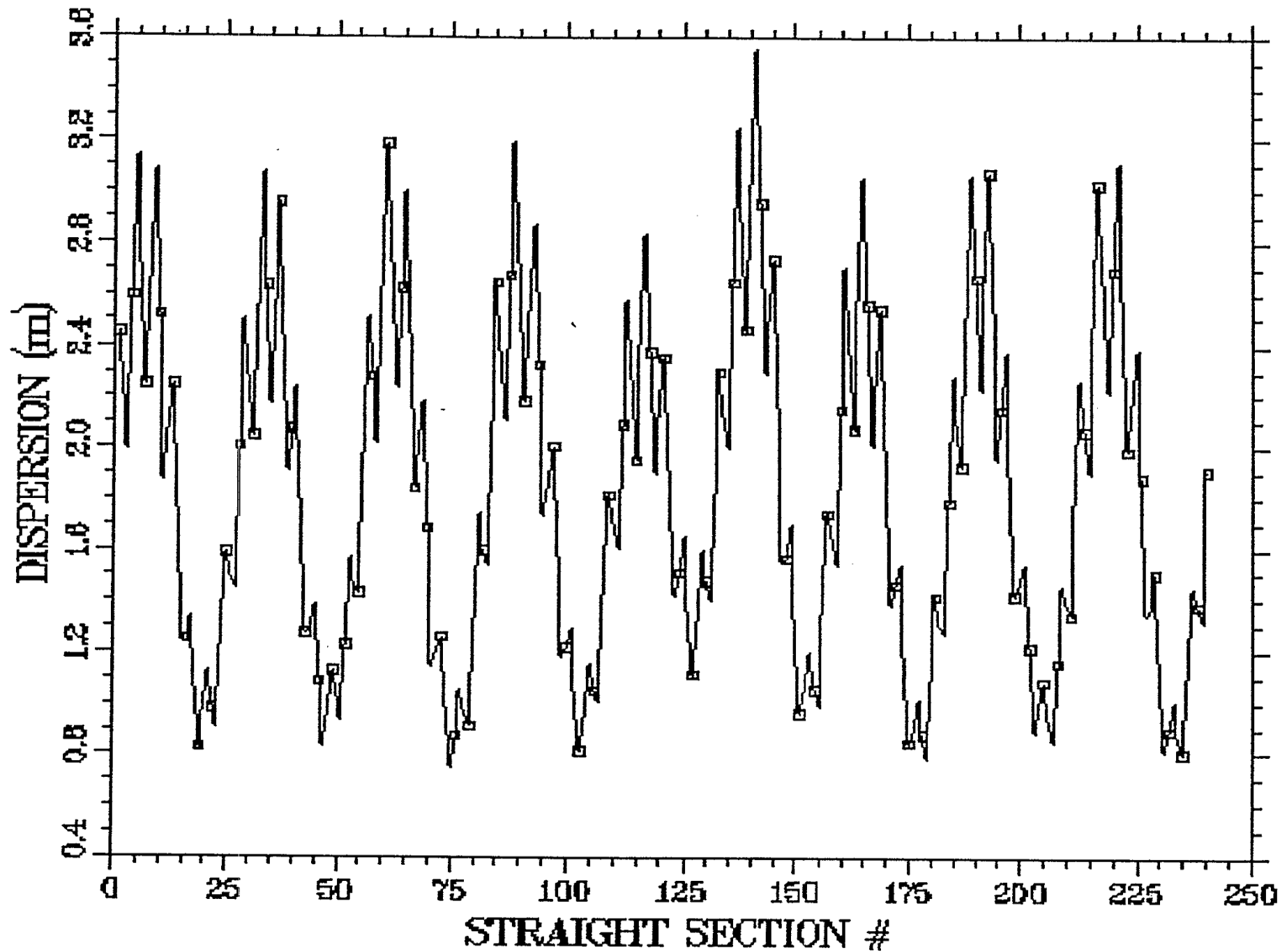


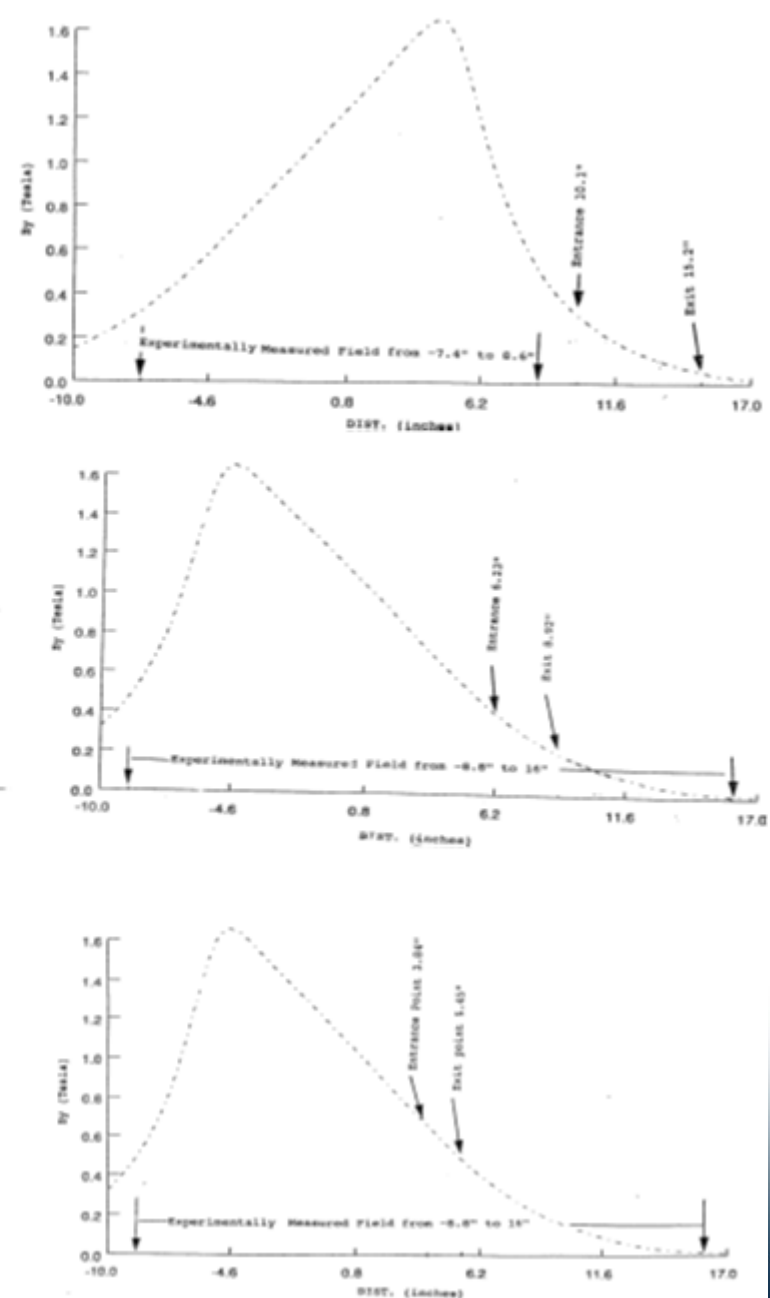
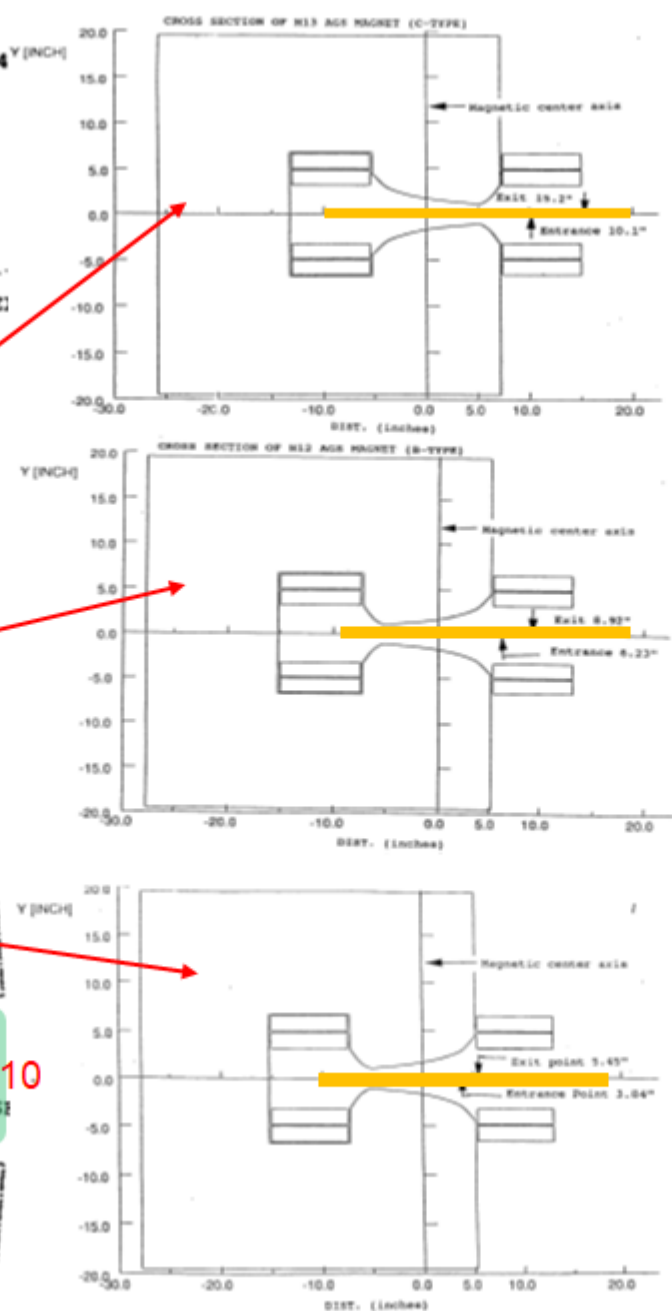
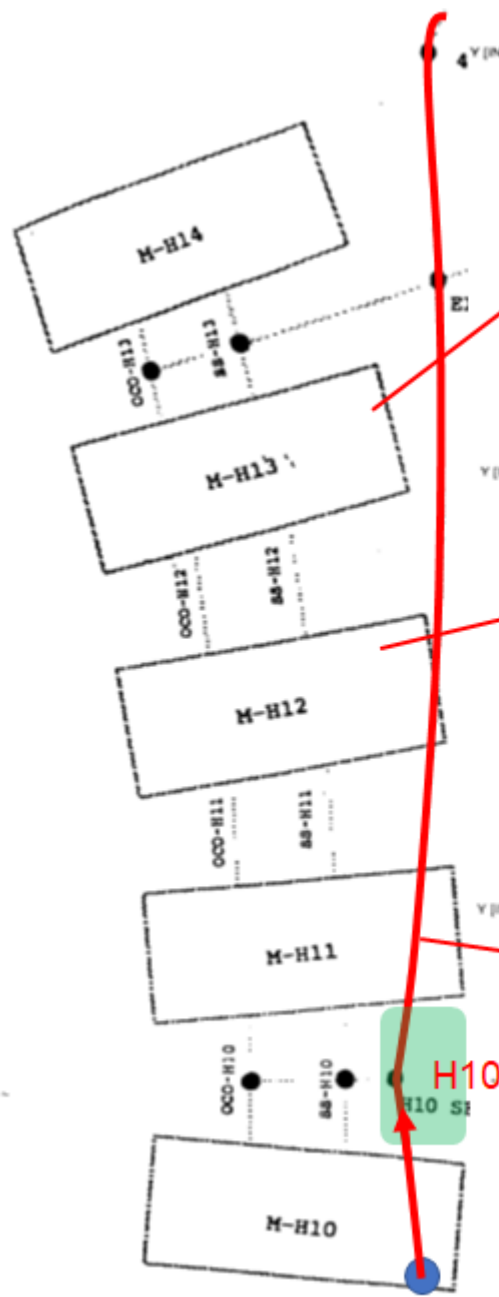
The coefficients  $\alpha_{ij}$  are expressed in terms of the measure field components on the plane and their derivatives with respect to x,z.



# The Extraction Beam bumps G10 and H10

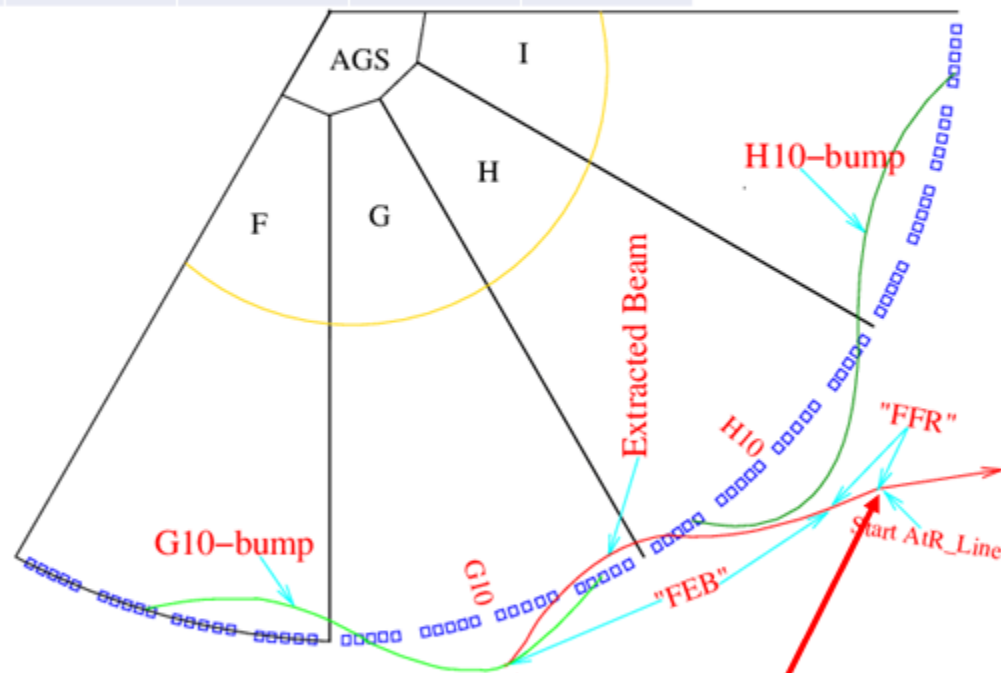






R Matrix G10-kicker to Start-AtR					
-1.8261	-17.443	0.0	0.0	0.0	-2.5889
0.17912	1.1634	0.0	0.0	0.0	0.2517
0.0	0.0	1.125	-15.016	0.0	0.0
0.0	0.0	0.186	-1.5855	0.0	0.0
-0.0041	1.3785	0.0	0.0	1	0.0
0.0	0.0	0.0	0.0	0.0	1.0

	H13
$\beta_x$	34.7 [m]
$\alpha_x$	-3.4
$\eta_x$	-1.06 [m]
$\eta'_x$	-0.68
$\beta_x$	8.1 [m]
$\alpha_x$	1.06



$$\begin{pmatrix} R_{11}^2 & -2R_{11}R_{12} & R_{12}^2 \\ -R_{11}R_{21} & R_{12}R_{21} + R_{11}R_{22} & -R_{12}R_{22} \\ R_{21}^2 & -2R_{21}R_{22} & R_{22}^2 \end{pmatrix} \begin{pmatrix} \beta \\ \alpha \\ \gamma \end{pmatrix}_{start} = \begin{pmatrix} \beta \\ \alpha \\ \gamma \end{pmatrix}_{end}$$





Thank you for your attention