

# Hexapod control system development towards arbitrary trajectories scans at Sirius/LNLS

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# Outline

- Introduction
- Motion Control Development
- Validation Tests
- Conclusion



# Introduction

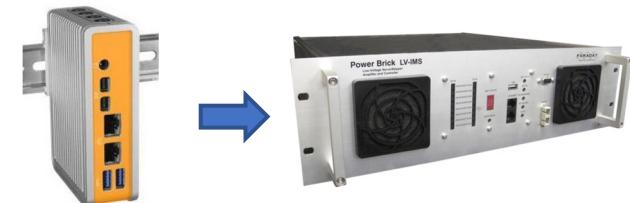
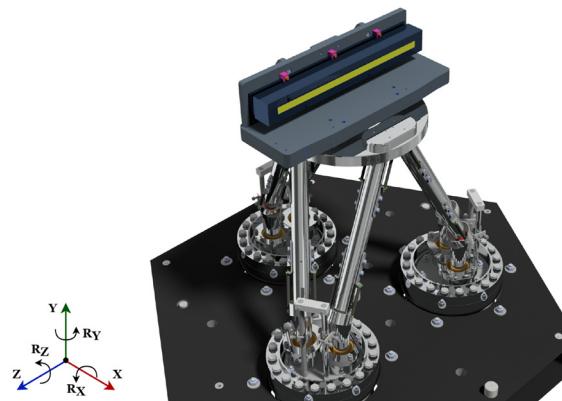
Bestec P478 Mirror Unit as a Motion System

Bestec P494 Control System

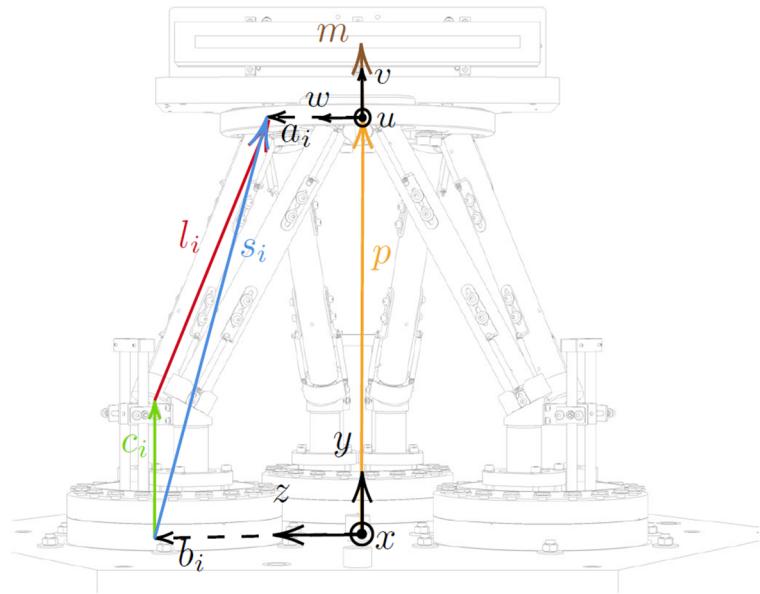
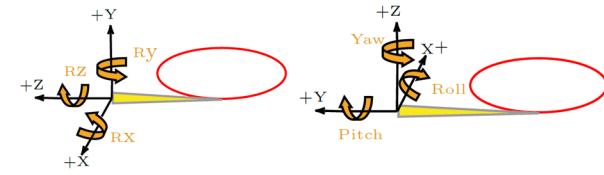
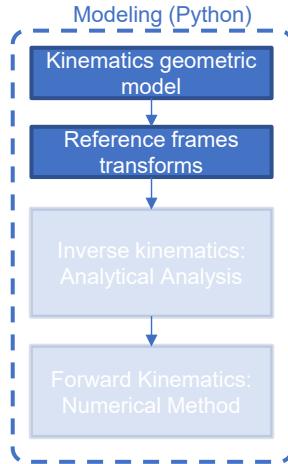
Objective: Control solution developed in-house

Hexapod Kinematics modelling  
Control System implementation

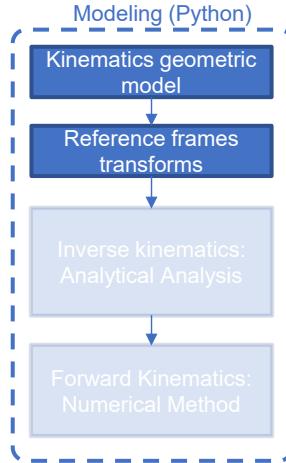
Comparison of control systems  
Arbitrary trajectory functionality validation



# Motion Control Development



# Motion Control Development

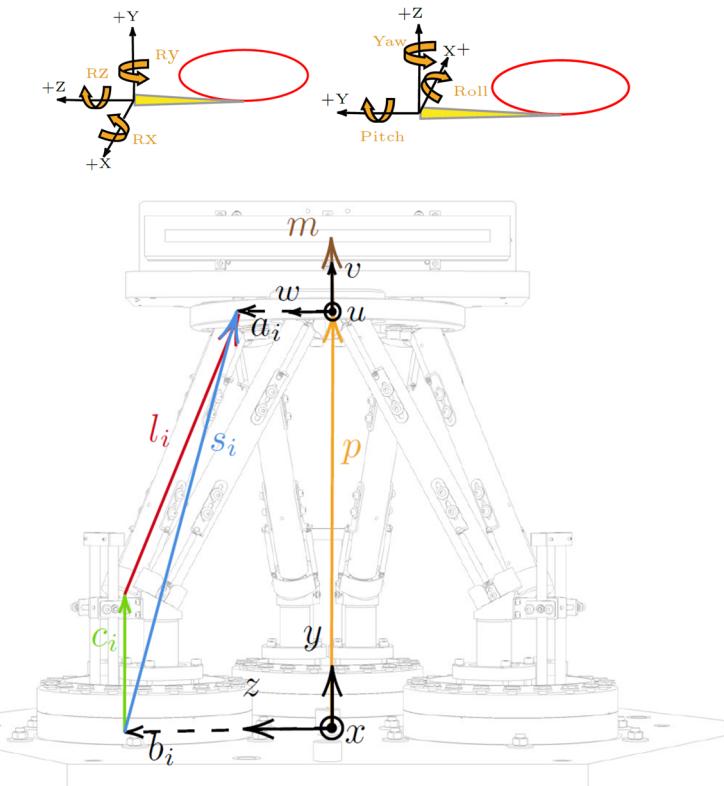


- ❖ 2 auxiliary frames and a set of vectors
- ❖ Rotation matrixes:

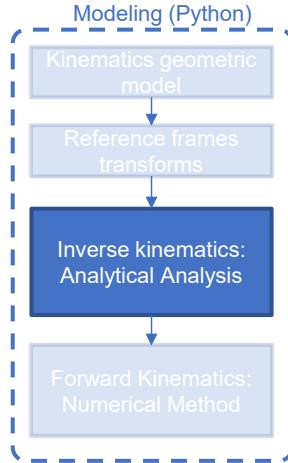
$$R_x(\alpha) = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \alpha & -\sin \alpha \\ 0 & \sin \alpha & \cos \alpha \end{bmatrix}$$

$$R_y(\beta) = \begin{bmatrix} \cos \beta & 0 & \sin \beta \\ 0 & 1 & 0 \\ -\sin \beta & 0 & \cos \beta \end{bmatrix}$$

$$R_z(\gamma) = \begin{bmatrix} \cos \gamma & -\sin \gamma & 0 \\ \sin \gamma & \cos \gamma & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

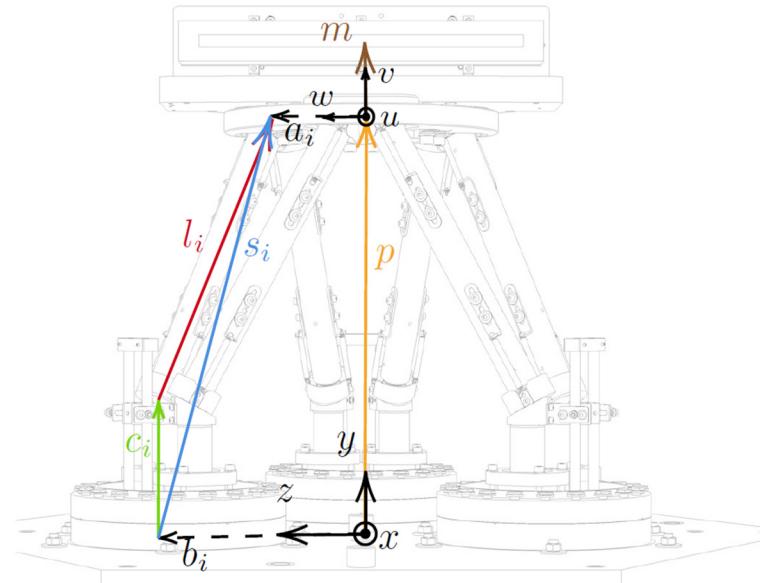


# Motion Control Development



(1)

$$\vec{s}_i = \vec{p} + R \cdot \vec{a}_i - \vec{b}_i$$



# Motion Control Development

Modeling (Python)

Kinematics geometric model

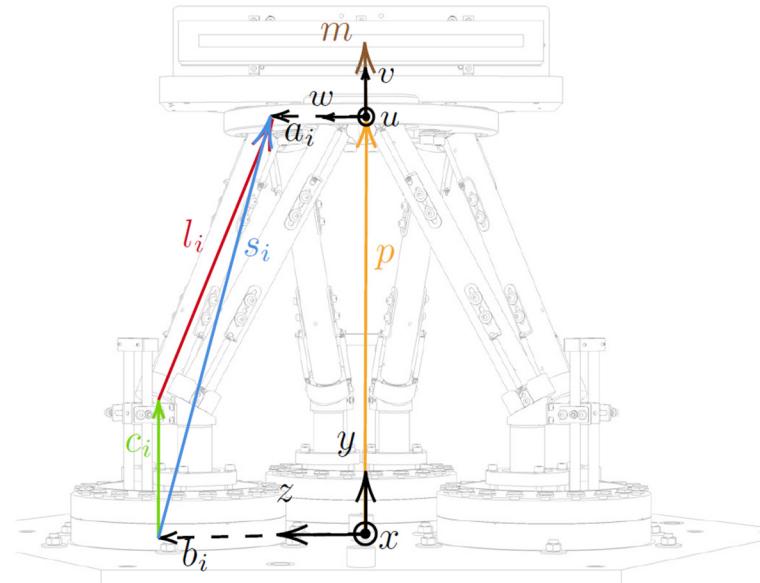
Reference frames transforms

Inverse kinematics:  
Analytical Analysis

Forward Kinematics:  
Numerical Method

$$(1) \quad \vec{s}_i = \vec{p} + R \cdot \vec{a}_i - \vec{b}_i$$

$$(2) \quad y_{ci} = y_{si} - \sqrt{\|\vec{l}_i\|^2 - z_{si}^2 - x_{si}^2}$$



# Motion Control Development

Modeling (Python)

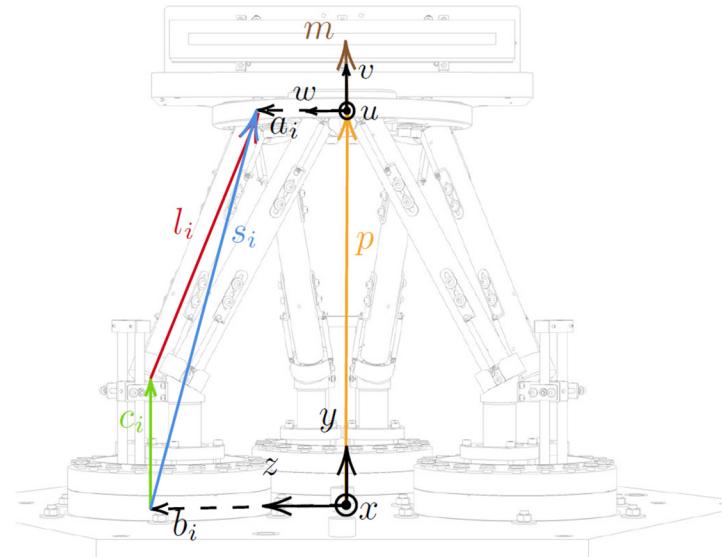
Kinematics geometric model

Reference frames transforms

Inverse kinematics:  
Analytical Analysis

Forward Kinematics:  
Numerical Method

$$(3) \quad c_i = \left\| \vec{p} + R \cdot \vec{a}_i - \vec{b}_i - \vec{s}_i + \vec{l}_i \right\|$$



# Motion Control Development

## Modeling (Python)

Kinematics geometric model

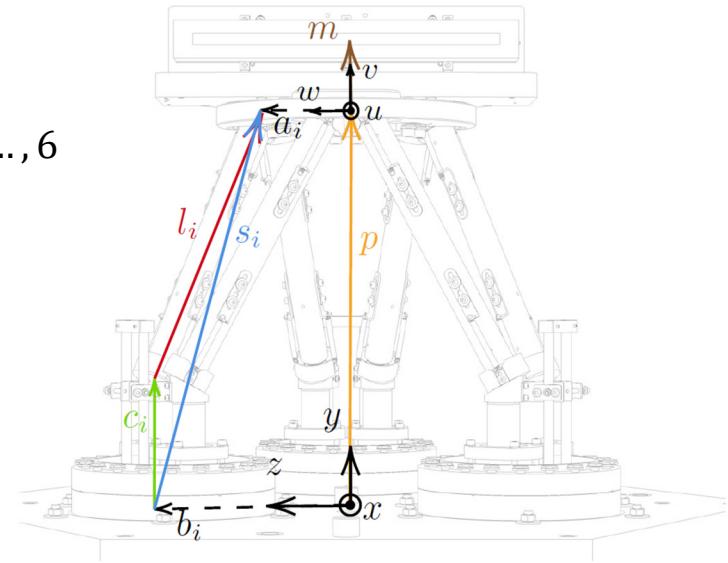
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$$(4) \quad f_i(x) = (y_i)^2 - (y_i^{(k)})^2 = 0, \text{ with } i = 1, \dots, 6$$



# Motion Control Development

Modeling (Python)

Kinematics geometric model

Reference frames transforms

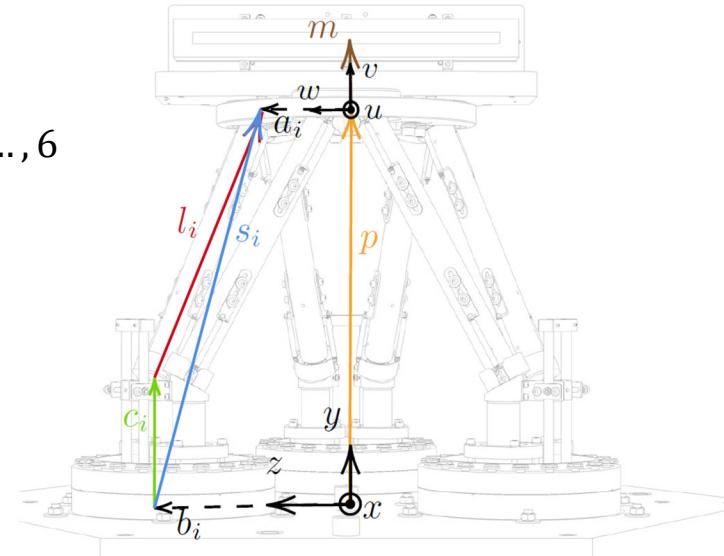
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Analytical Analysis

Forward Kinematics:  
Numerical Method

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$$(4) \quad f_i(x) = (y_i)^2 - (y_i^{(k)})^2 = 0, \text{ with } i = 1, \dots, 6$$

$$(5) \quad J = \begin{bmatrix} \frac{\partial f_1(x)}{\partial x_1} & \dots & \frac{\partial f_1(x)}{\partial x_6} \\ \vdots & \ddots & \vdots \\ \frac{\partial f_6(x)}{\partial x_1} & \dots & \frac{\partial f_6(x)}{\partial x_6} \end{bmatrix}$$



# Motion Control Development

Modeling (Python)

Kinematics geometric model

Reference frames transforms

Inverse kinematics:  
Analytical Analysis

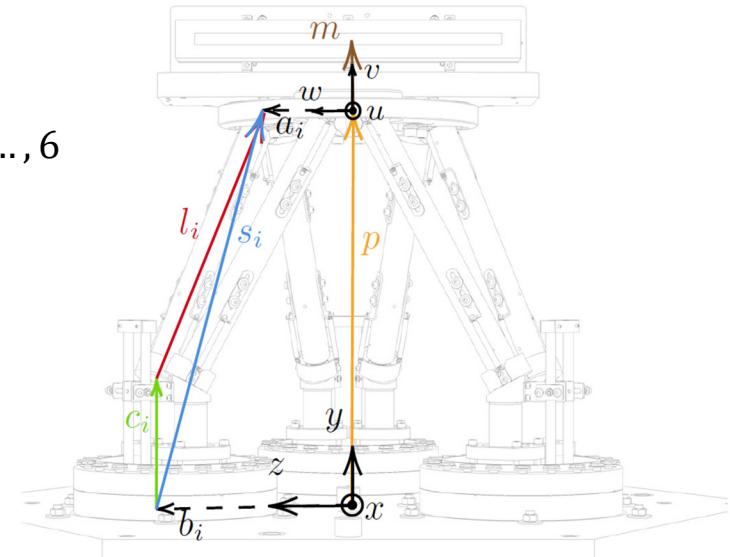
Forward Kinematics:  
Numerical Method

$$(3) \quad c_i = \left\| \vec{p} + R \cdot \vec{a}_i - \vec{b}_i - \vec{s}_i + \vec{l}_i \right\|$$

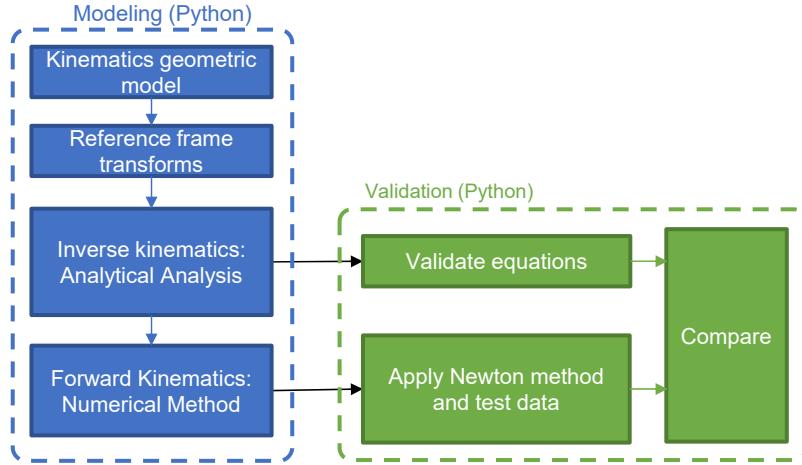
$$(4) \quad f_i(x) = (y_i)^2 - (y_i^{(k)})^2 = 0, \text{ with } i = 1, \dots, 6$$

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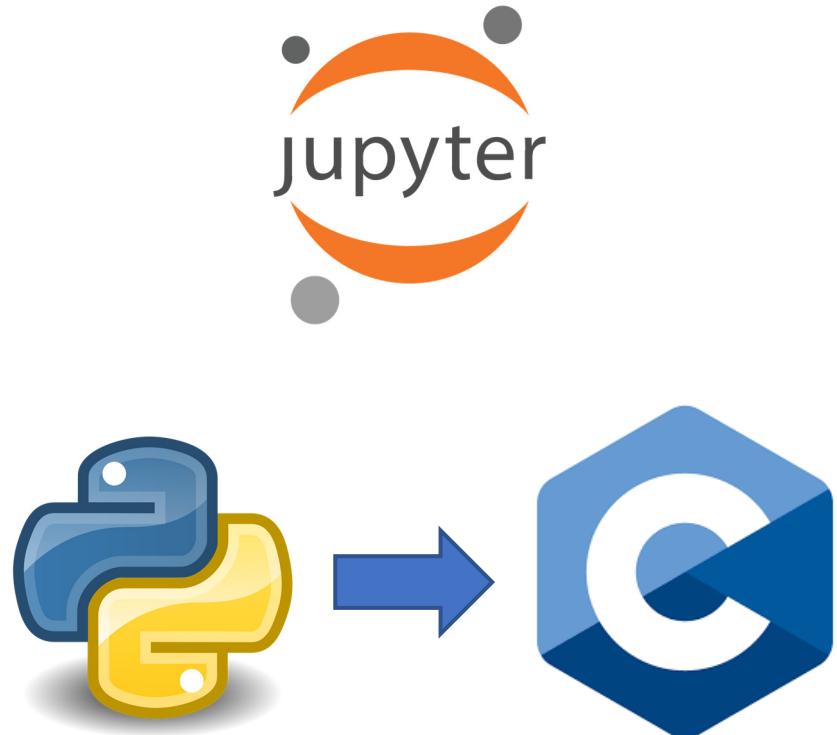
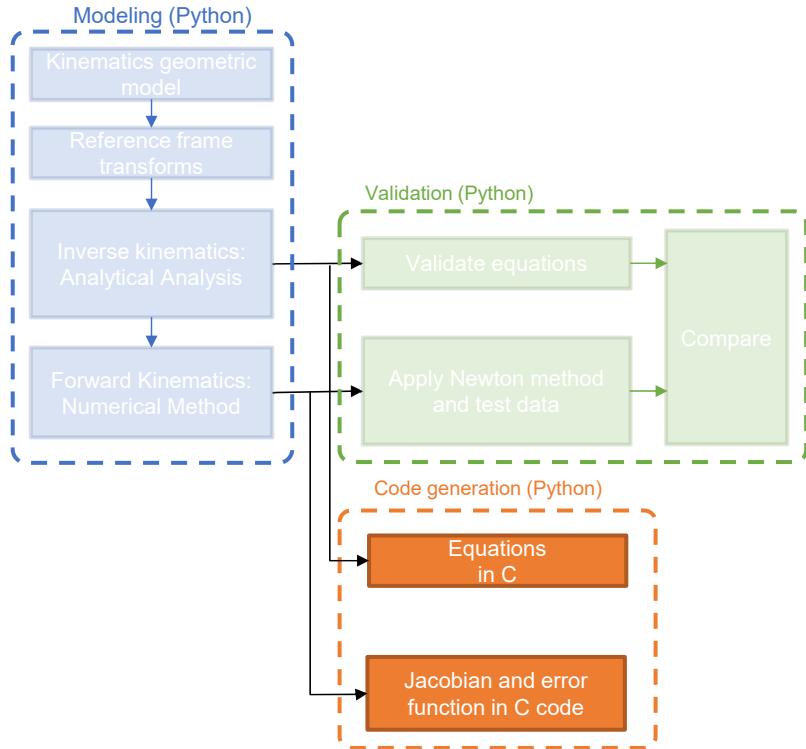
$$(6) \quad f_i(x) < \epsilon \text{ or } k \geq 10$$



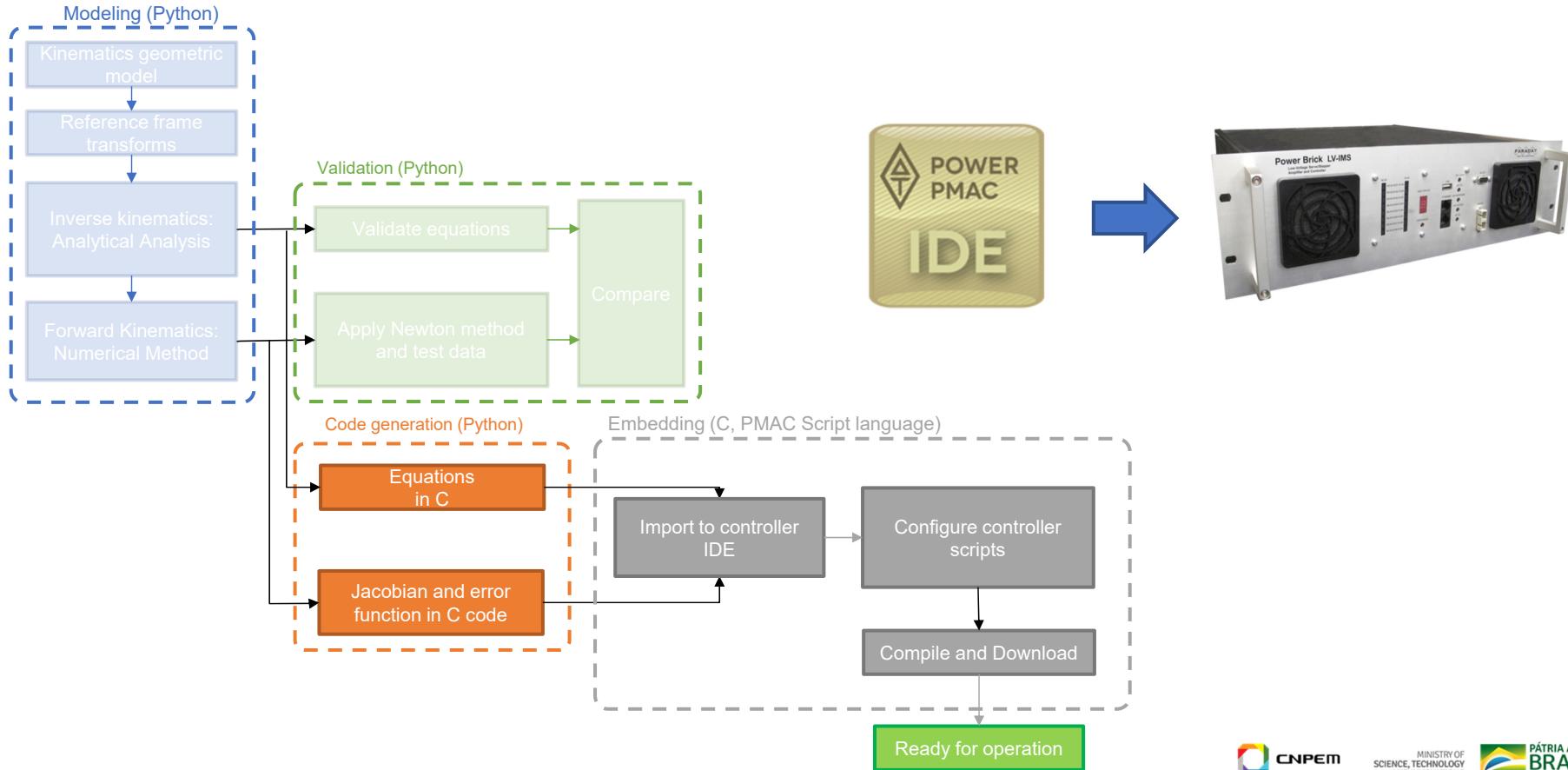
# Motion Control Development



# Motion Control Development



# Motion Control Development



# Validation: Performance Tests

Setup Control Systems with same paramenters

Move one DoF, log position data from all DoFs

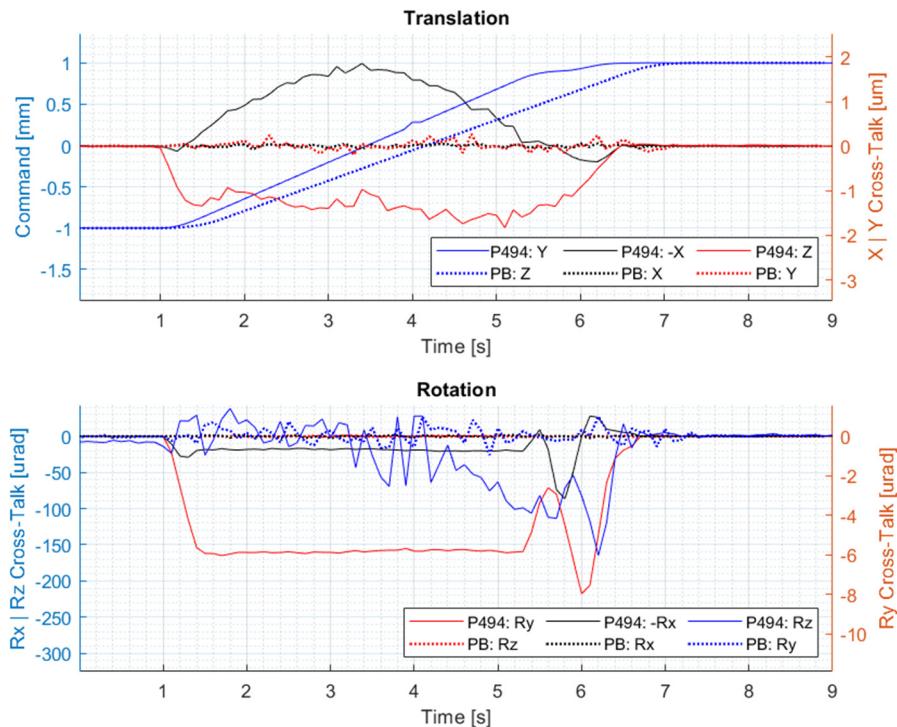
Process Logged data

Compare equivalent movements

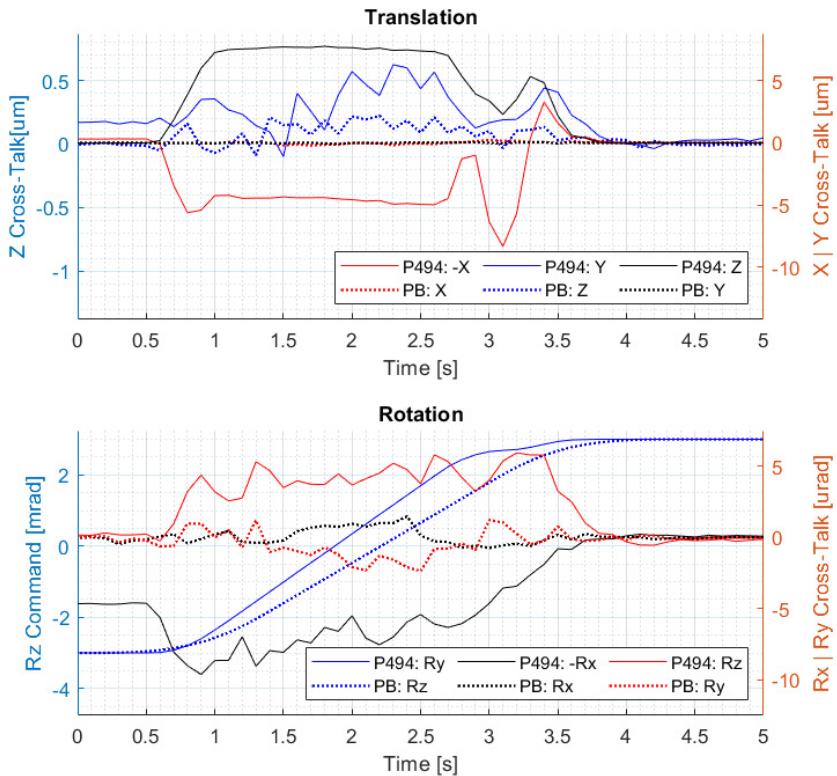


# Validation: Performance Tests

- **Z movement (-1mm to 1mm)**
- P494 reaches before, but with deviations
- Power Brick presents less control errors
- P494 with more cross-talks
- Rx and Ry differences represent an order of magnitude



# Validation: Performance Tests

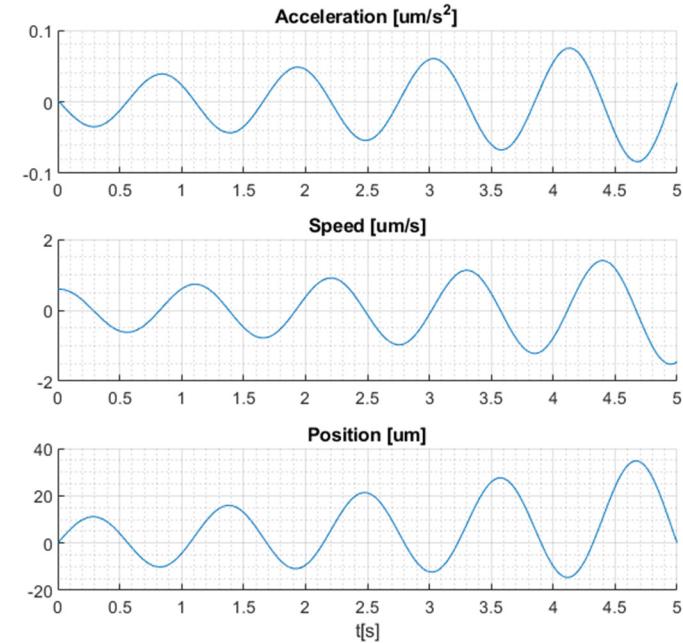
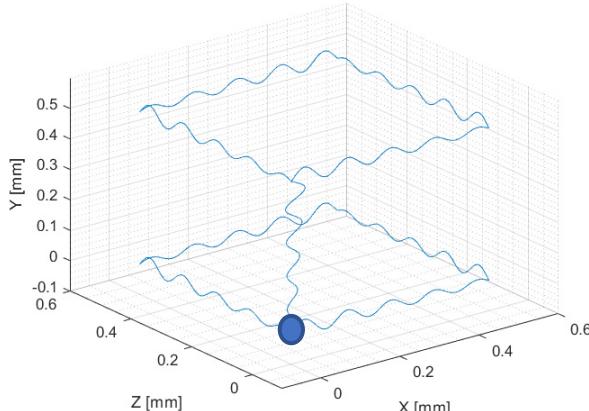


- Rz movement (-3 mrad to 3mrad)**

- P494 reaches destination before, but with deviations
- Power Brick presents less control errors
- Bestec shows more cross-talks
- X and Z cross-talks represent an order of magnitude

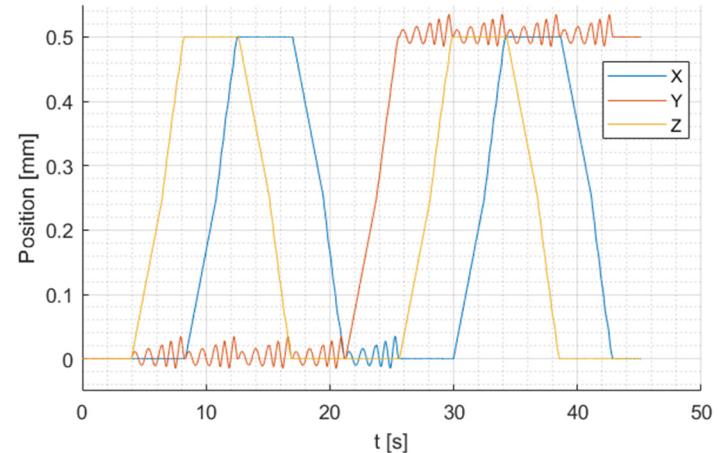
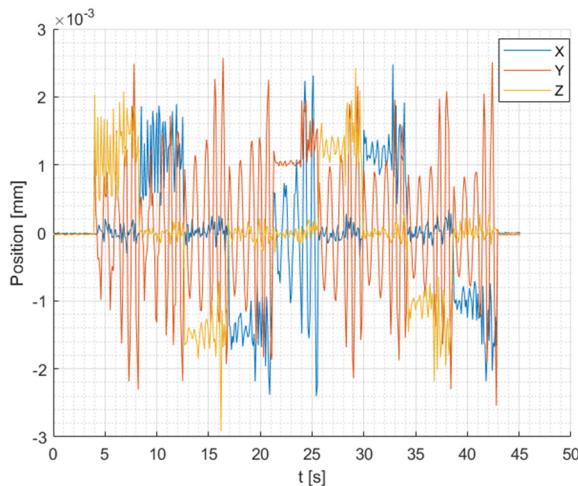
# Arbitrary Trajectory Tests

- Command defined positions, speed or time lapses
- Movement parameters were written using EPICS
- The trajectory generated with Python script
- Movement variates speed and acceleration



# Arbitrary Trajectory Tests

System followed commanded trajectory



Errors ranges: -3 to 3  $\mu\text{m}$ .

# Conclusion

- Motion control system for the P468 Mirror Unit with Delta Tau Power Brick LV
- Bestec P494 control system:
  - Reaches specifications at steady state
  - Cross-talks during movements.
- Designed system's accuracy at transient state overcomes P494
- Validated arbitrary trajectory functionality
- The knowledge acquired can be applied to other systems
  - Kinematics in C language for granite bases
  - Arbitrary trajectory for monochromators.

# Acknowledgement

- Brazilian Ministry of Science, Technology, Innovation (MCTI)
- Brazilian Synchrotron Light Laboratory (LNLS) team
- Omron DeltaTau team for technical support
- Diamond Light Source (DLS)



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