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All-optical undulator using array of pulse-front tilted laser beams with alternated phases

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Outline



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1 Background

2 Scheme description

3 General analyses of FEL performance

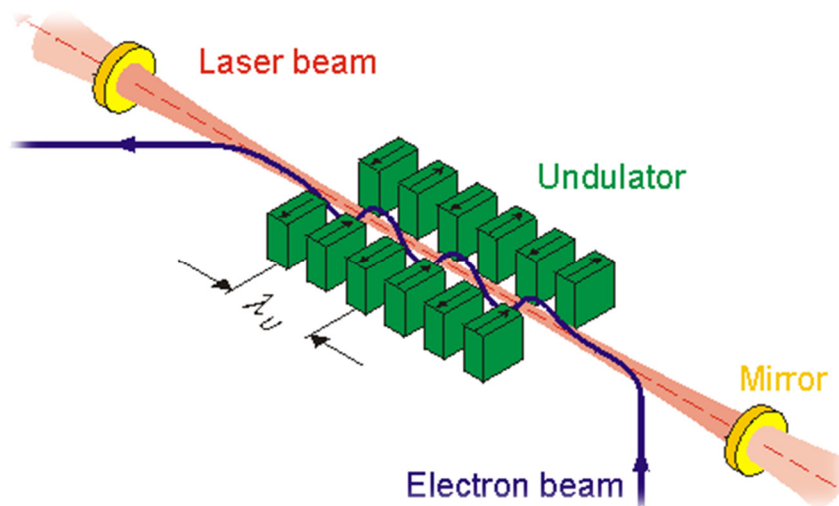
4 Conclusion

I. Background



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Conventional undulator



**Tremendous in cost,
Huge in shape**

Alternatives



**Low cost,
Compact in shape**

I. Background



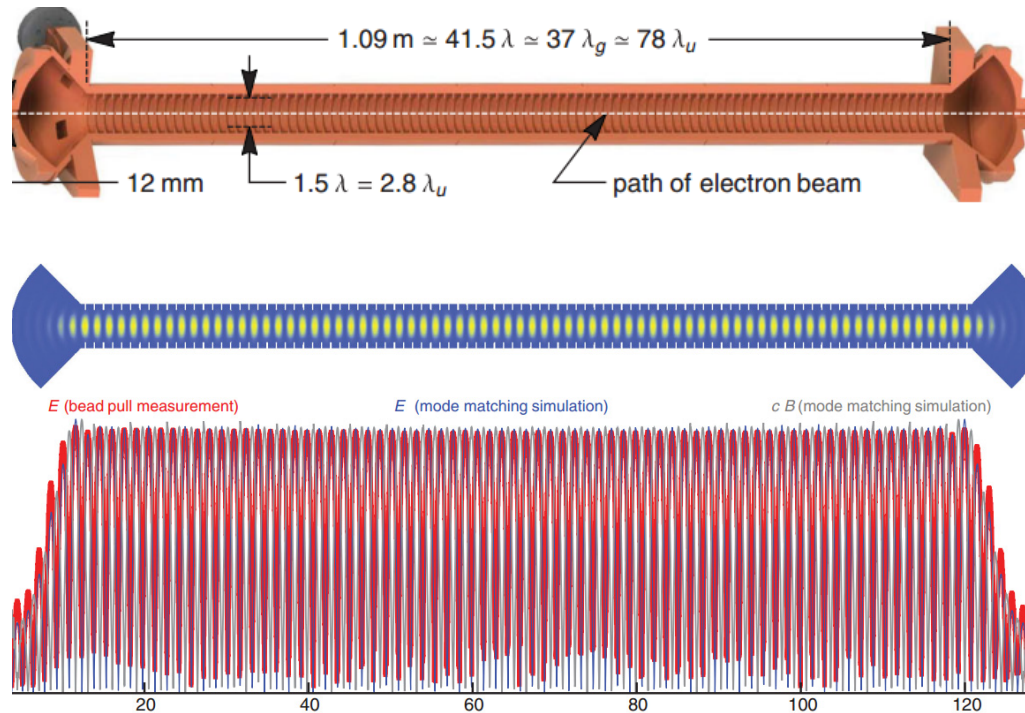
Resonant condition:
$$\lambda_\ell = \frac{\lambda_u}{2\gamma^2} \left(1 + \frac{K^2}{2} + \gamma^2 \theta^2 \right)$$

I. Background

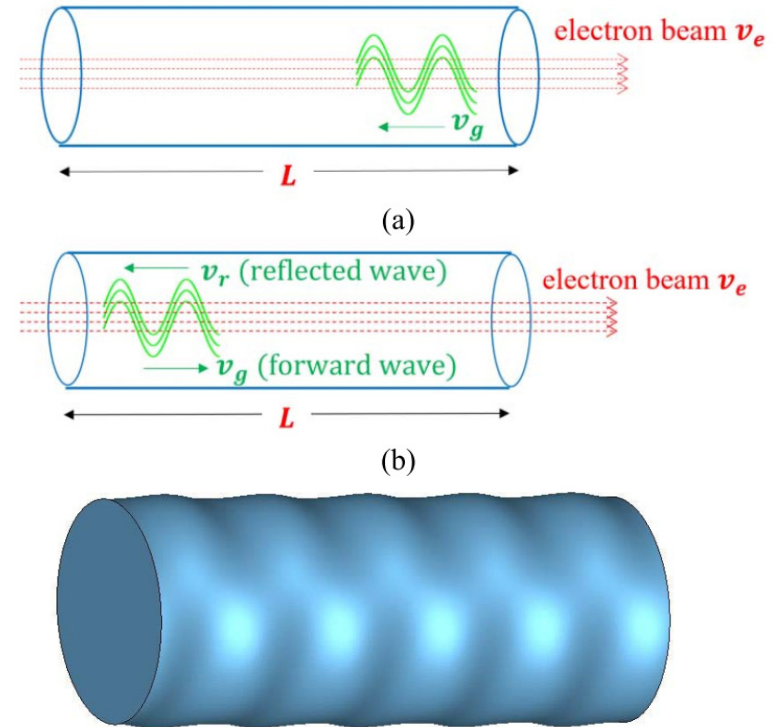


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Microwave undulator



Sami Tantawi, et al., PRL 112, 164802 (2014)



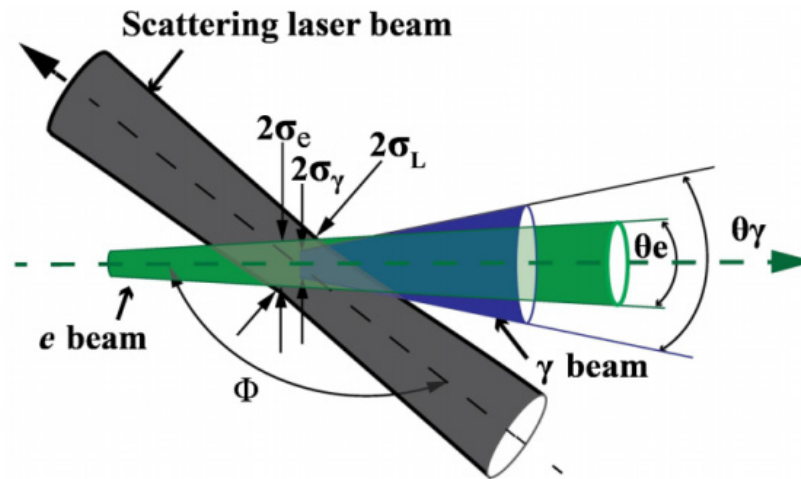
Liang Zhang, et al. IEEE TRANSACTIONS ON ELECTRON DEVICES 2018.

**Relies on high power microwave sources;
Breakdown threshold of the metallic waveguides!**

I. Background



Optical undulator (inverse Compton scattering)



S. Chen, et al., PRL 110, 155003 (2013)

$$K = \frac{2\pi\lambda_u}{mc^2} F_{\perp}$$

$$\lambda_u \approx \lambda_l/2$$

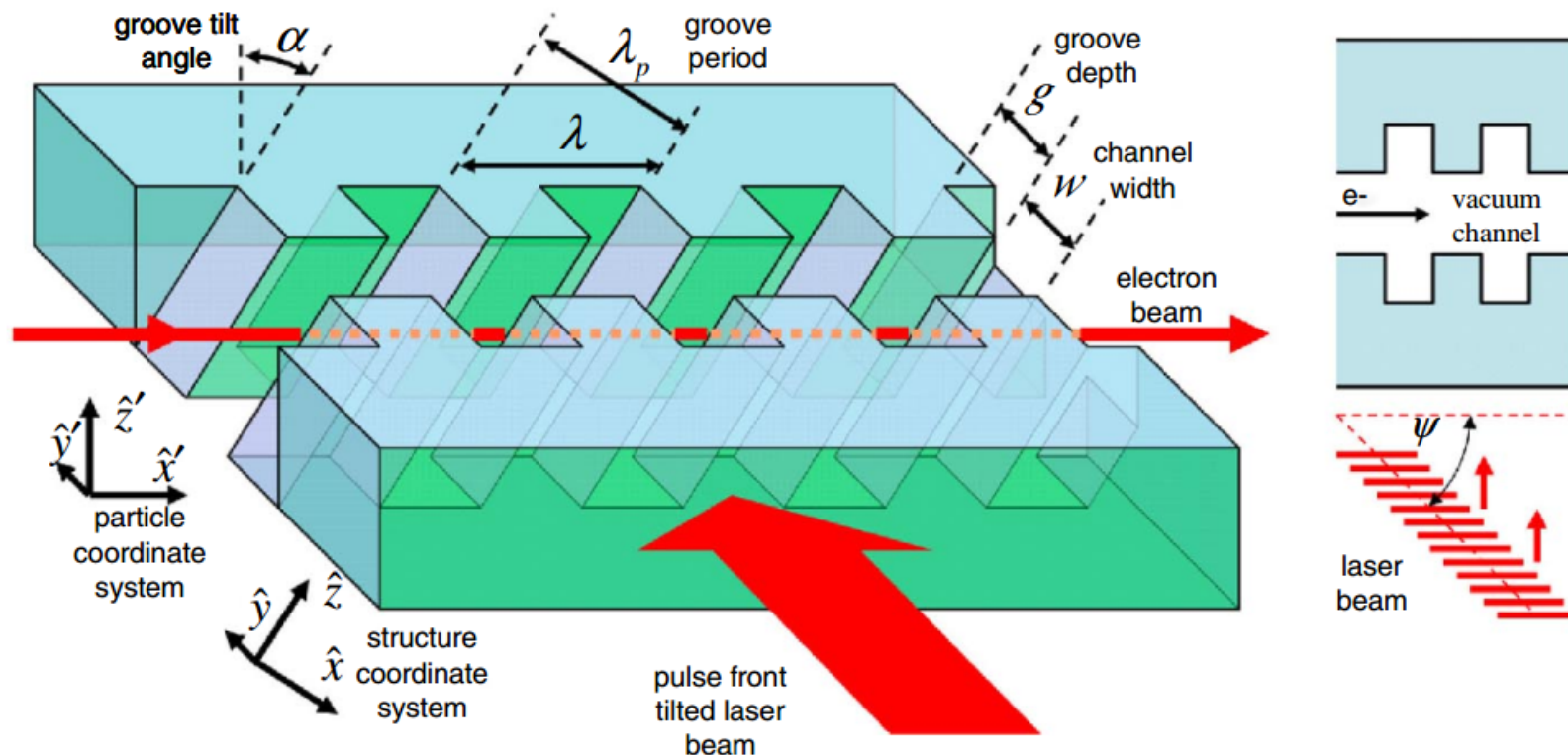
**Tremendous laser field intensity,
Undulating length is not enough long.**

I. Background



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Micro dielectric undulator



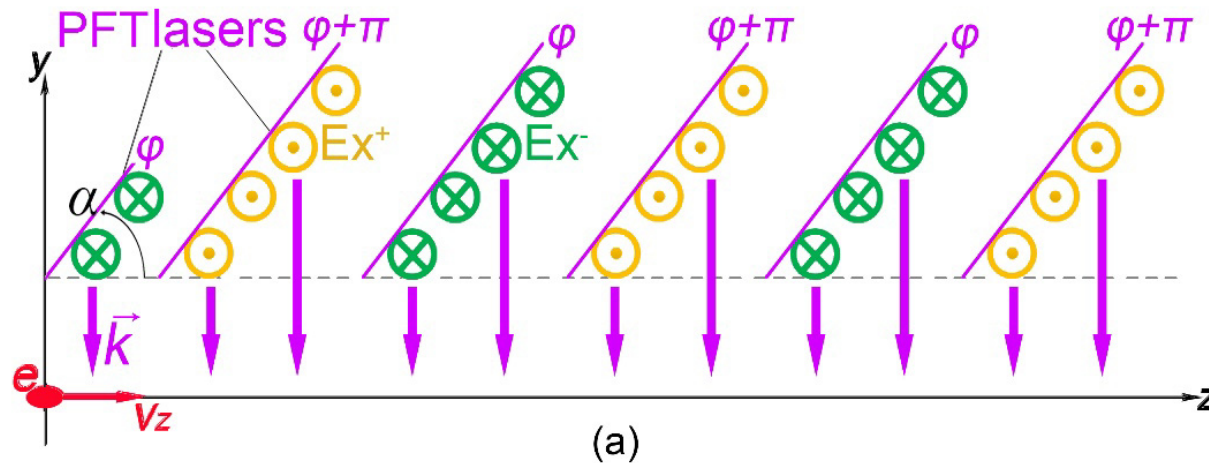
T. Plettner and R. L. Byer, PRst-AB 11, 030704 (2008)

Small beam channel; breakdown; low efficiency; deflection.



II. Description of scheme

1. Model description



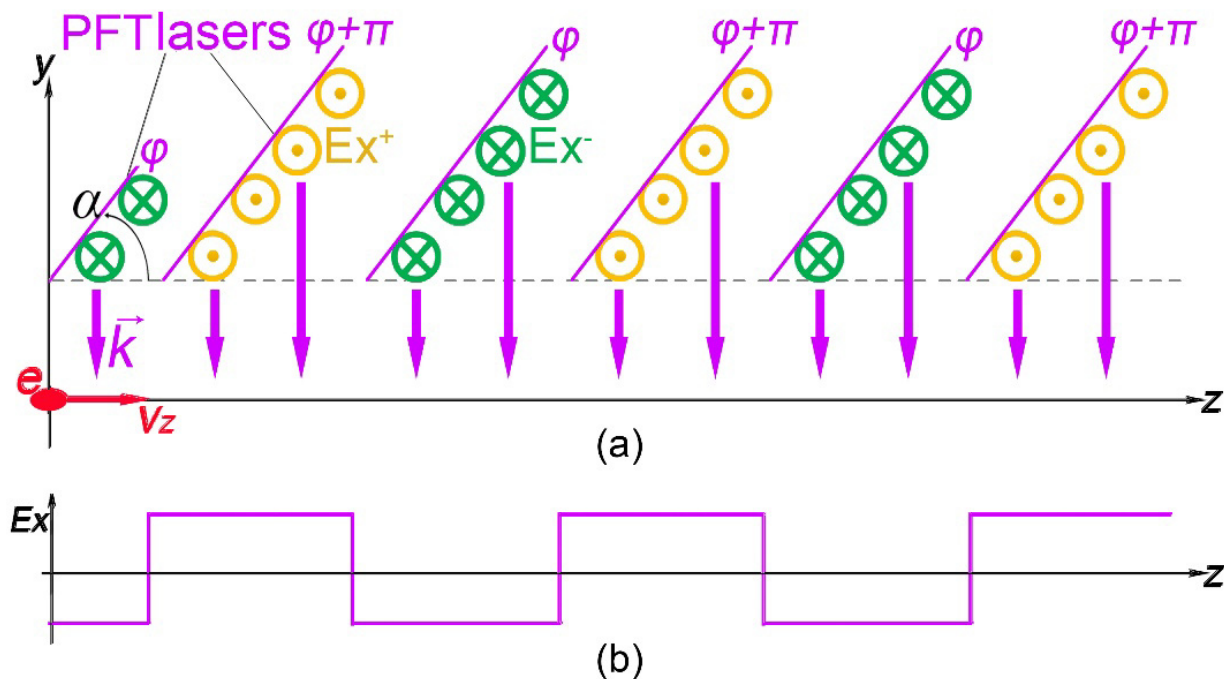
$$\tan \alpha = 1/\beta_z = c/v_z$$

$$L_\varphi = L_{\varphi+\pi} = m\beta_z\lambda_l$$



II. Description of scheme

1. Model description

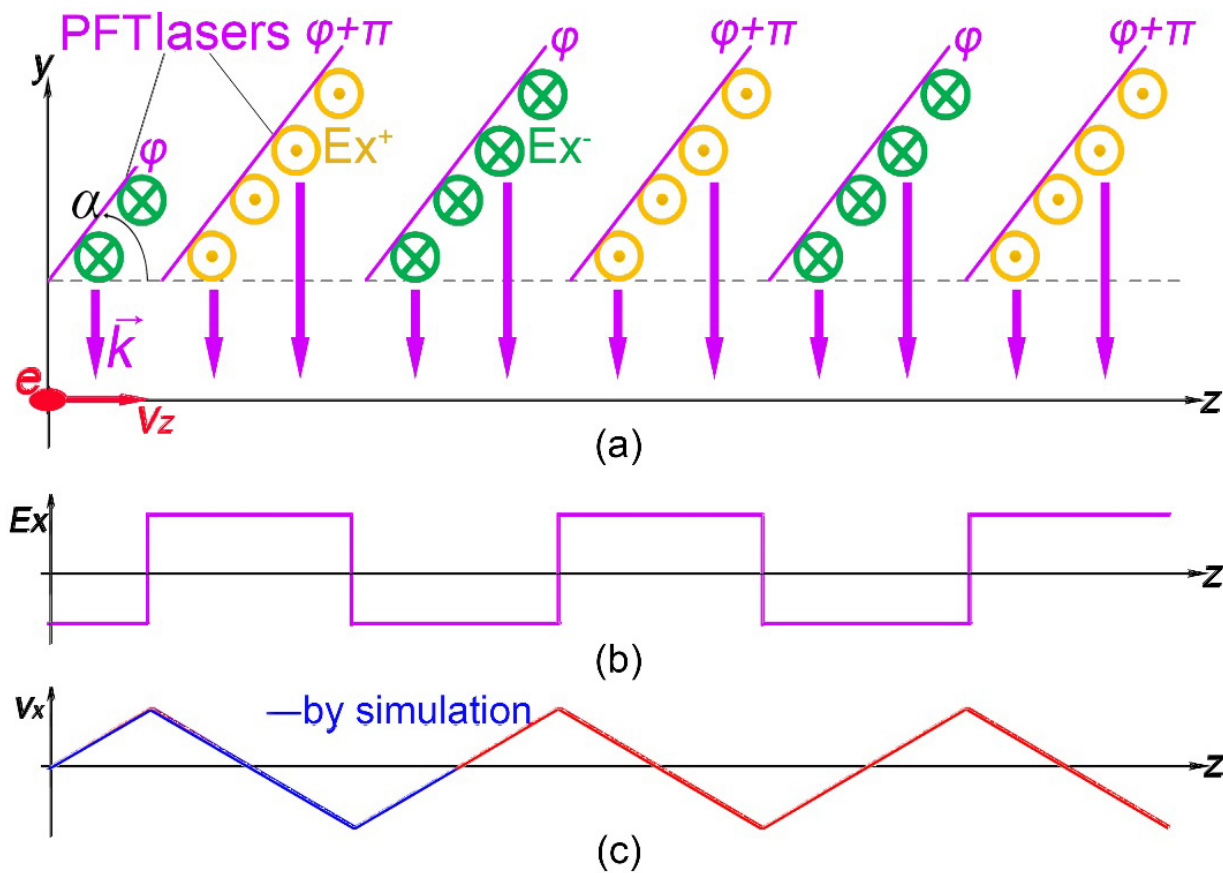


$$\frac{d\gamma m_e v_x}{dt} = -e E_x$$



II. Description of scheme

1. Model description

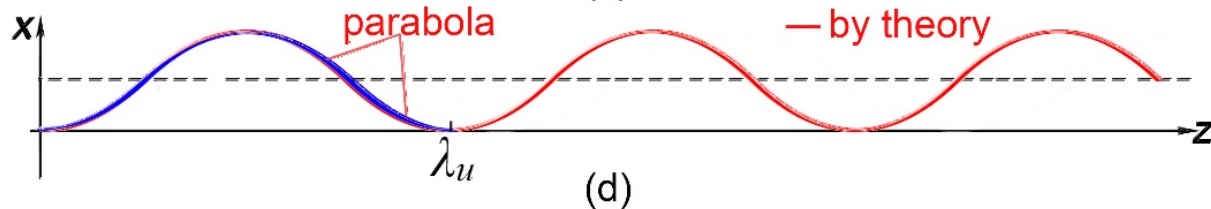
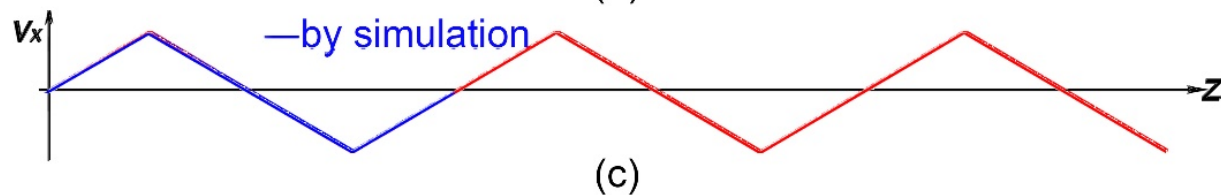
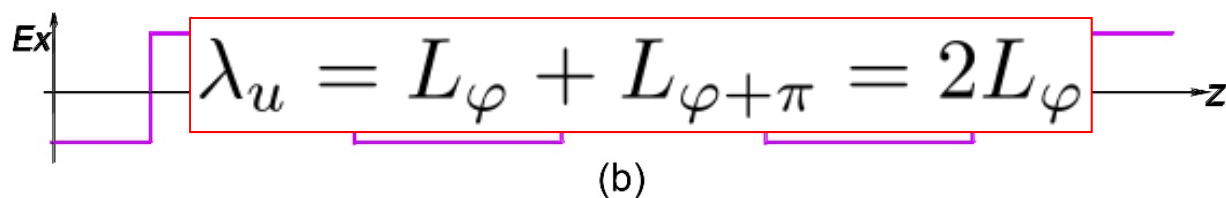
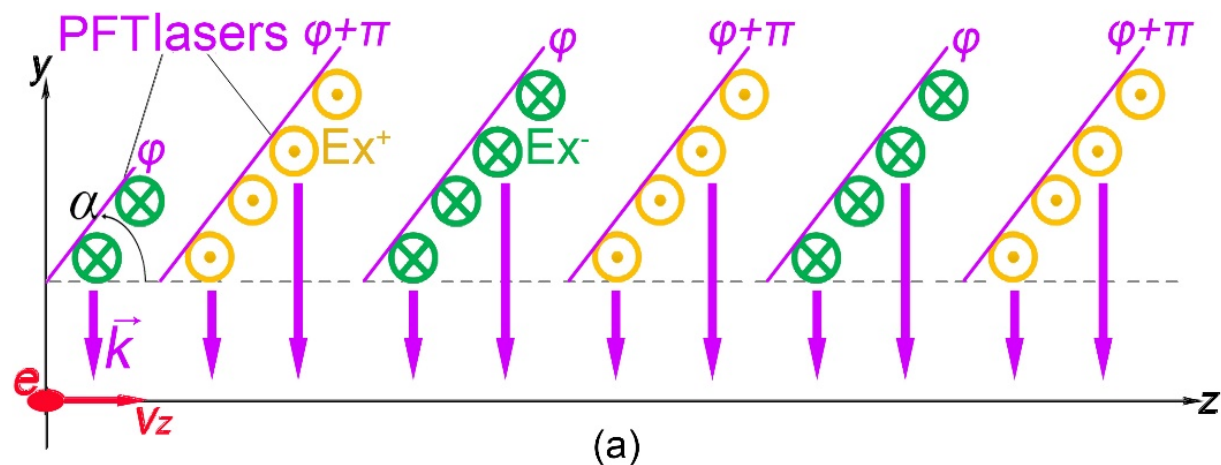


$$x(z) = -\frac{eE_x}{m_e\gamma} \frac{z^2}{2v_z^2} + \frac{v_0}{v_z} z + x_0$$



II. Description of scheme

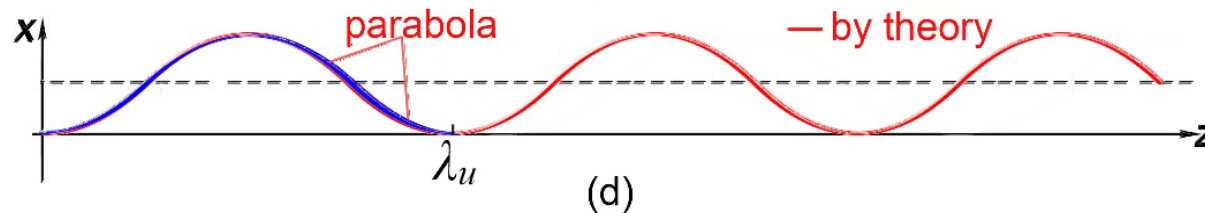
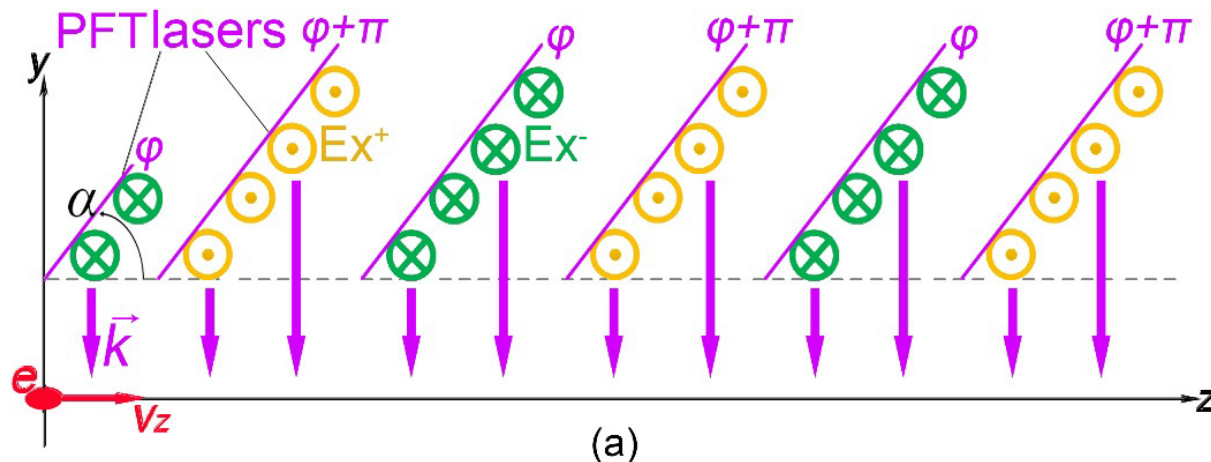
1. Model description





III. FEL performance

2. analyses



$$X(z) = \sum_{n=1}^{+\infty} S(n) \frac{K_n}{\gamma \beta_z k_n} \cos k_n z$$

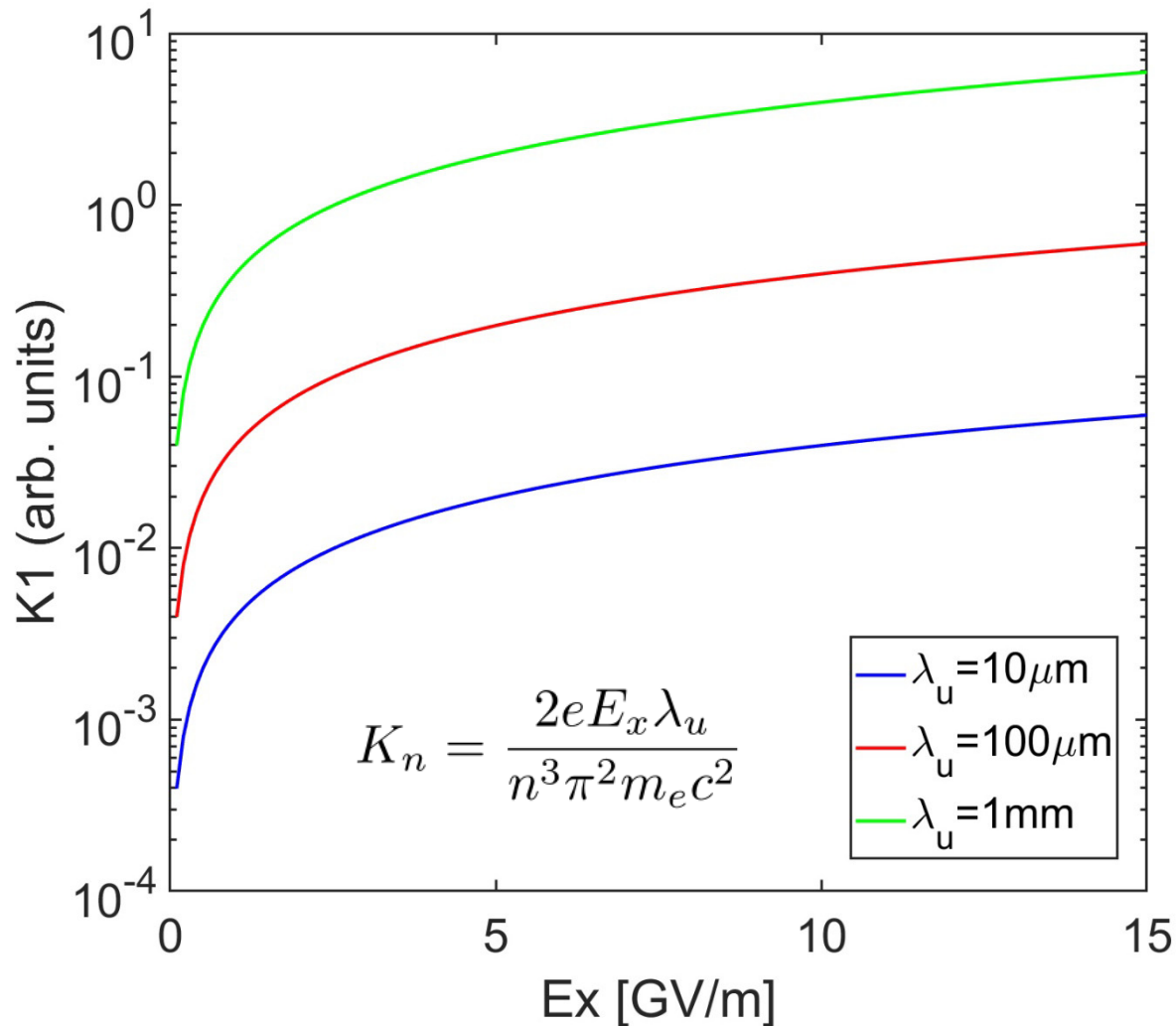
$$X(z) = x(z) + e E_x L^2 / 32 \gamma \beta_z^2 m_0 c^2$$

$$K_n = \frac{2e E_x \lambda_u}{n^3 \pi^2 m_e c^2}$$



III. FEL performance

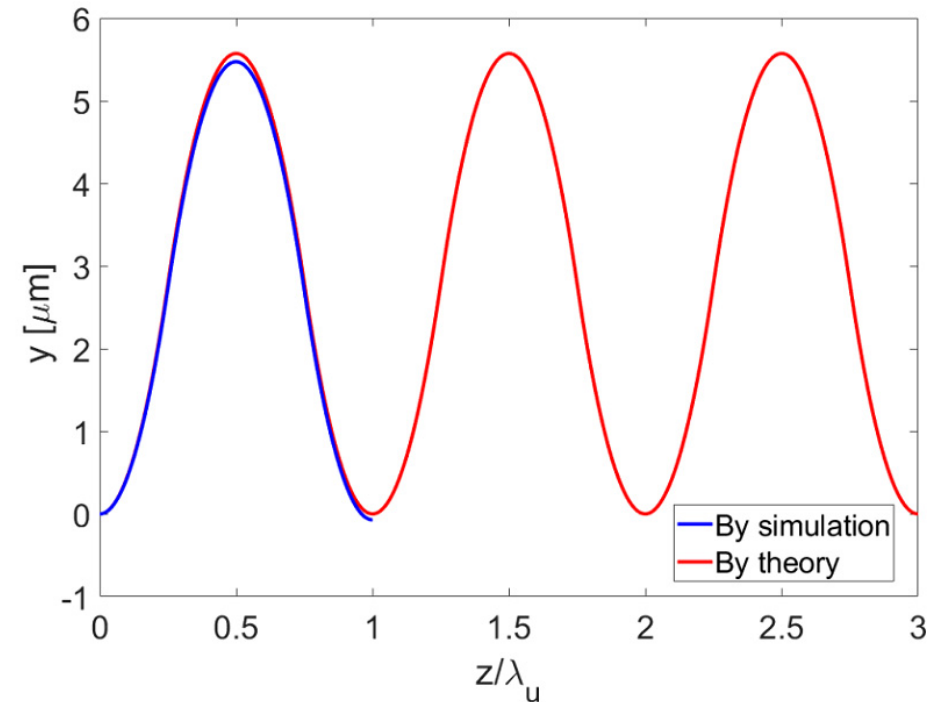
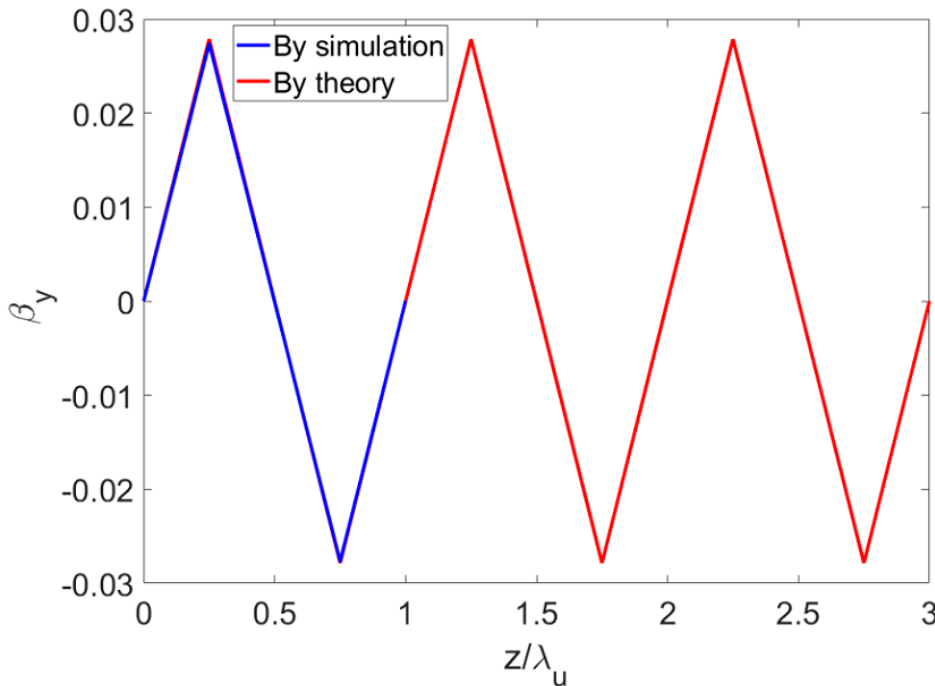
2. analyses





III. FEL performance

2. analyses



Beam energy: 35 MeV

Incident Laser wavelength: 10 μm

$\lambda_u = 0.1\text{mm}$

$$\lambda_r = 10\text{nm}$$



III. FEL performance

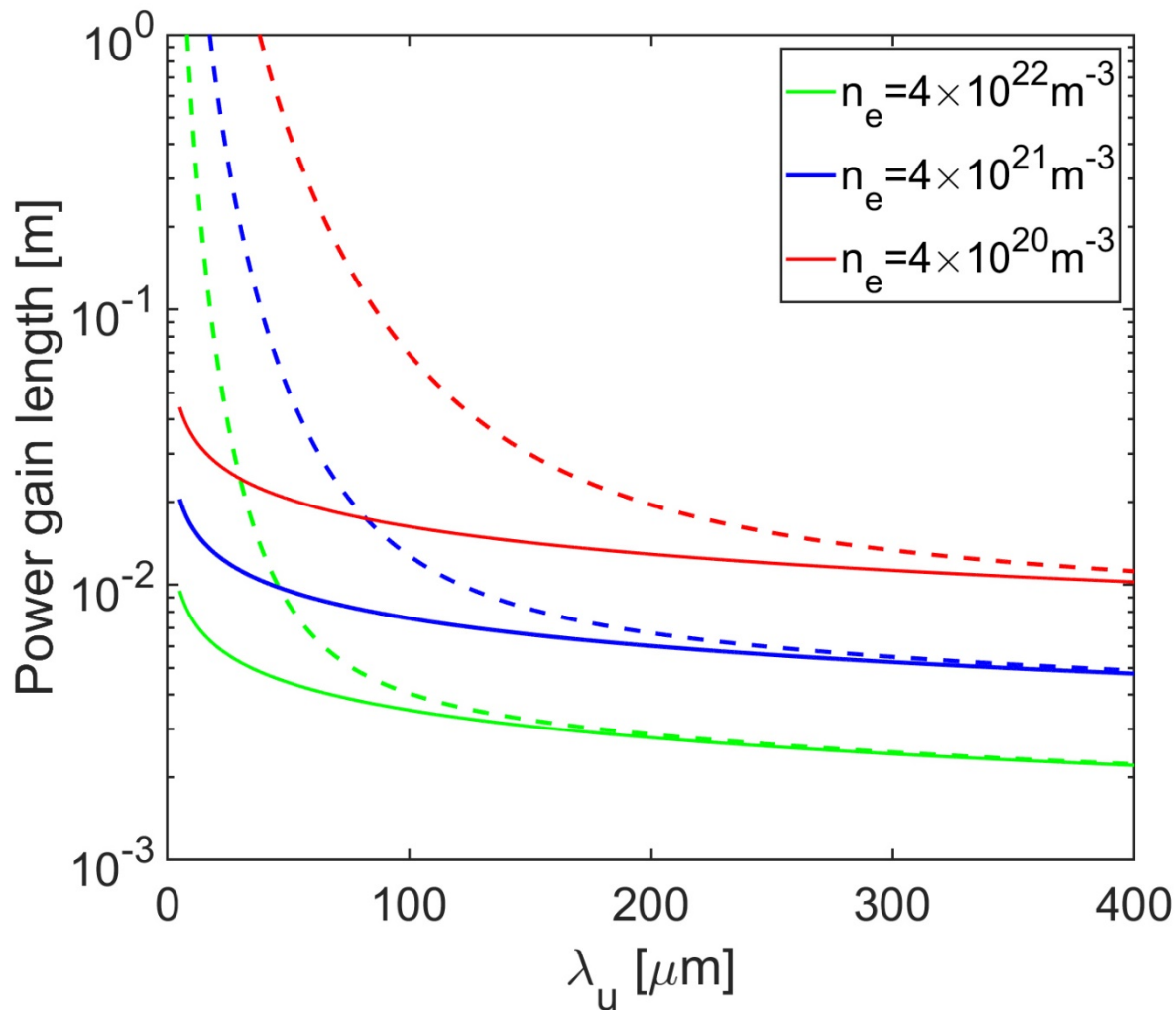
2. analyses

$$L_{G0} = \frac{1}{\sqrt{3}} \left[\frac{4\gamma^3 m_e}{\mu_0 K^2 e^2 k_u n_e} \right]^{1/3}$$

Ming Xie formula:

$$\varepsilon = 10^{-7} \text{ m} \cdot \text{rad}$$

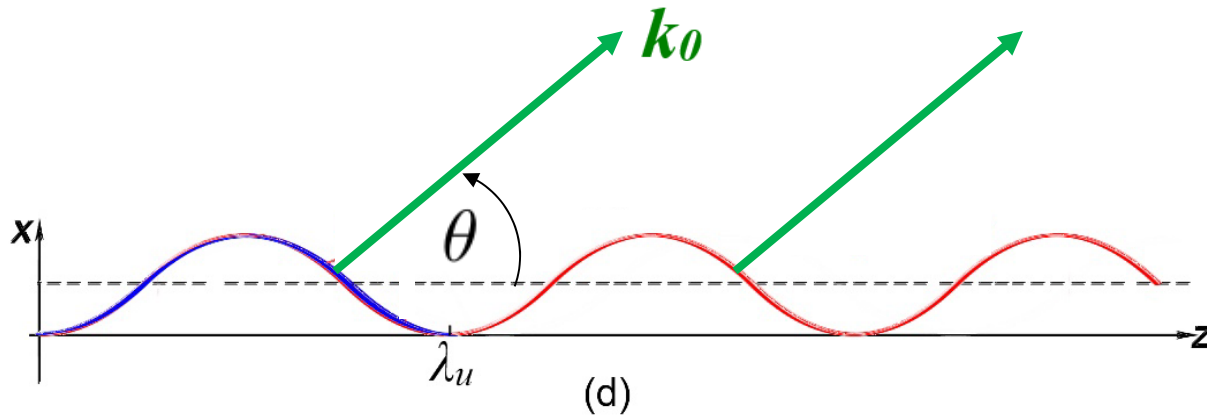
$$\Delta\gamma/\gamma = 5 \times 10^{-4}$$





III. FEL performance

3. notings



$$\frac{\omega}{c} - \frac{\omega}{v_z} \cos \theta = k_0 - k_z \cos \theta = 2n\pi \longrightarrow \lambda_n = \frac{\lambda_u}{n} \left(\frac{1}{\beta_z} - \cos \theta \right)$$

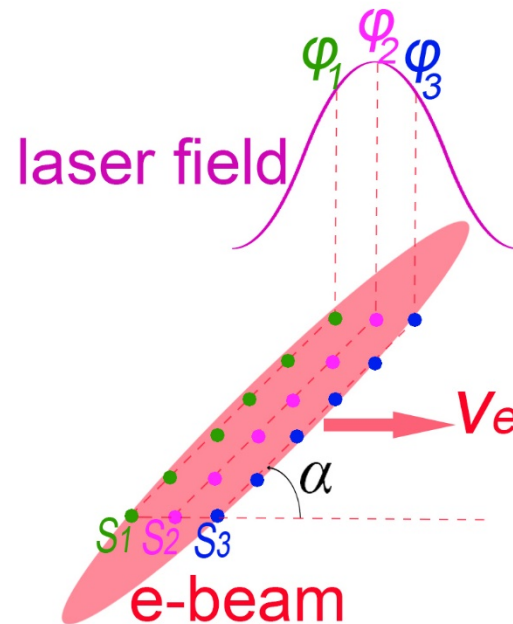
In the forward direction with small angle θ :

$$\lambda_n = \frac{\lambda_u}{2n\gamma^2} (1 + \gamma^2 \theta^2)$$



III. FEL performance

3. notings



$$K_i = K_0 \sin \varphi_i$$



III. FEL performance

3. notings

- ◆ Using the optical paths to distribute a single laser beam into an array of beams with phase controlled [1];
- ◆ By folding one or two laser beams by using well designed optical paths formed by reflectors.

IV. Conclusion



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An option for developing compact undulator with adjustable undulating period and strength.



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