



Optical Beam Quality Analysis of the Clara Test Facility using Second Moment Analysis

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Abstract

- ◆ We studied and characterised the FEL optical radiation in simulations of the CLARA FEL test facility under development at Daresbury Laboratory in the UK [1].
- ◆ We determined the radiation source properties corresponding to the long bunch operation mode via wave-front propagation in free space using OPC (Optical Propagation Code), [2], and second moment analysis.
- ◆ We found the shortest undulator module length suitable for schemes to be carried out in CLARA, without degrading the beam quality.
- ◆ We studied the way that different properties of the electron bunches (emittance, peak current, bunch length) affect the optical beam.
- ◆ We are now able to understand how the optical beam will propagate from the end of the undulator and through the photon transport system to the experimental stations.

SECOND MOMENT ANALYSIS

Radiation source properties are found by fitting the evolution of the beam profile ($\sigma_i^2(z) = C_2 z^2 + C_1 z + C_0$) to the measured values of the second moments profile,[4]

$$M_i^2 = \frac{2\pi}{\lambda} \sqrt{4C_0 C_2 - C_1^2}, \quad z_0 = -\frac{C_1}{2C_2} \quad \sigma_{i0} = \sqrt{C_0 - \frac{C_1^2}{4C_2}} \quad (1)$$

With M^2 being beam quality coefficient, σ_{i0} , rms size at the beam waist and z_0 the waist position.

CLARA LONG BUNCH MODE

- E_{beam} = 150-250 MeV.
- Bunch charge = 250 pC.
- $\sigma_t = 800$ fs.
- Peak current = 125 A.
- $\bar{\epsilon} = 0.5$ mm-mrad.
- E spread = 25 keV.
- $\lambda_U = 2.5$ cm.
- $\lambda_r = 100 - 400$ nm.
- Maximum rms (undulator parameter) = 1.4

PRELIMINARY STUDY

Table 1: Comparison between optical beam parameters obtained from steady state and time-dependent simulations

Parameter	Steady state		Time-dependent	
	x	y	x	y
M^2	3.8	3.6	3.6	3.5
z_0 (m)	-1.85	-1.93	-1.27	-1.27
σ_{z_0} (μ m)	283	273	274	278

Preliminary study

- ◆ **Goal:** Comparison between steady state and time-dependent simulations in GENESIS 1.3 to demonstrate the validity of time-dependent approach for beam quality calculations.
- ◆ $\lambda_r = 266$ nm

Results of the simulations (Table 1)

- ◆ M^2 parameters for the steady state and time-dependent simulations are quite close to each other (relative difference of 5.2% and 2.8% in x and y, respectively).
- ◆ The M^2 parameters in x and y are large compared to the ideal TEM₀₀ Gaussian mode propagating in free space ($M^2 = 1$).

IMPACT OF UNDULATOR MODULE LENGTH

Table 2: Undulator parameters for the preliminary study in last section and each proposed undulator module. There are 1.5 undulator periods (λ_U) end pieces for all cases, per end.

Parameter	Previous Undulator module length study			
	0.5 m	0.75 m	1 m	
λ_U (m)	0.0275	0.025	0.025	0.025
Active periods	28	17	27	37
Break sections (m)	0.4125	0.5	0.5	0.5
x/y quad. grad. (T/m)	8/10	13/13	10/10	9/9

Goal: Choose the undulator module length (proposed: 0.5, 0.75 and 1 m) with the highest beam quality (**Minimum M^2 at maximum brightness**).

Comparison of M^2 for different modules (Table 3)

- ◆ M^2 at maximum brightness for the 0.5 m module (in Table 3) has the largest M^2 of all modules (1.9 times larger than the M^2 obtained for the 0.75 m module in x and y). **Not considered further as alternative.**
- ◆ Fluctuation of $\Delta M_{x,y}^2 = |M_x^2 - M_y^2|$, (in Fig. 1) around a non-zero value due to the difference in focusing of the electron beam for both transversal directions while traversing the FODO cell (**asymmetry in beam quality**).
- ◆ The 0.75 and 1 m modules have **similar beam quality** (relative difference between M^2 of both modules less than 1% in x and 3.1% in y). **0.75 m module** chosen as it is compatible with proposed schemes **without degrading beam quality**.

Table 3: Comparison between source properties at n_{sec} at maximum brightness for the proposed modules.

L (m)	M_x^2	M_y^2	z_{0x} (m)	z_{0y} (m)	$\sigma_{z_{0x}}$ (μ m)	$\sigma_{z_{0y}}$ (μ m)
0.5	8.32	7.29	-1.99	-2.1	509	471
0.75	4.40	3.80	-1.41	-1.50	300	287
1	4.41	3.92	-1.86	-1.97	348	329

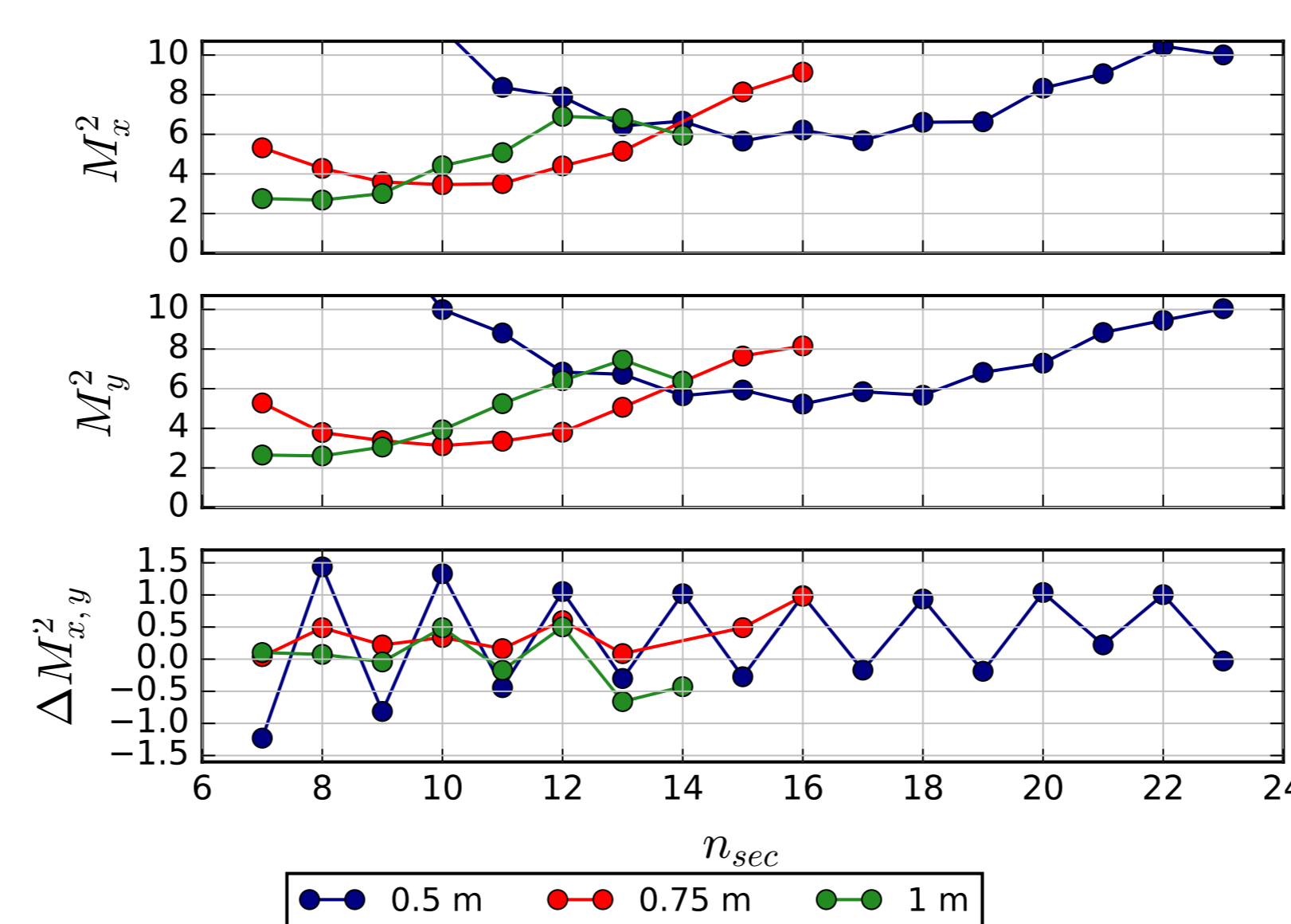


Figure 1: M^2 in x (top) and y (middle) and their difference $\Delta M_{x,y}^2 = M_x^2 - M_y^2$ (bottom) in terms of n_{sec} (for 0.5, 0.75 and 1 m modules).

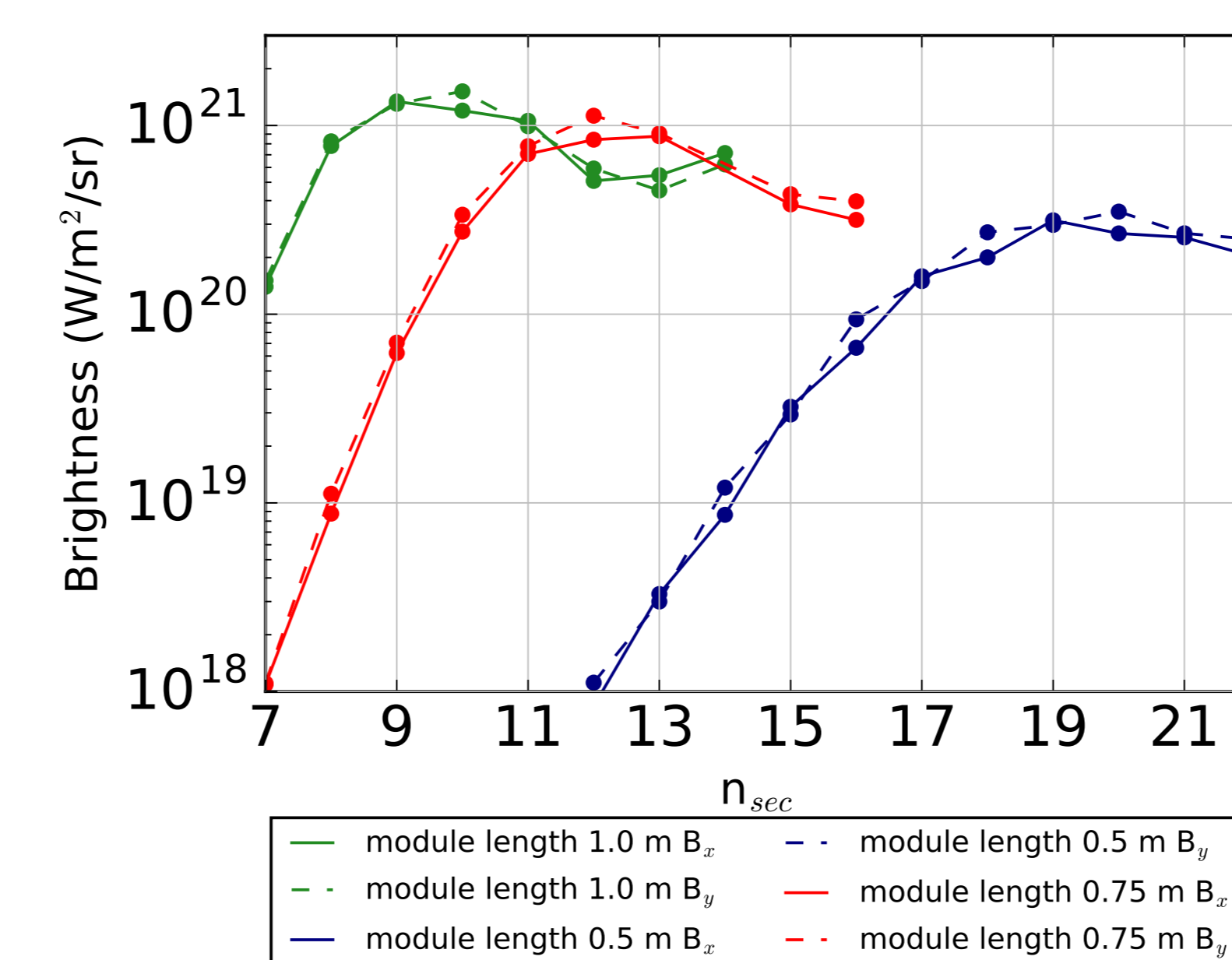


Figure 2: Brightness for the modules as a function of n_{sec} .

IMPACT OF BEAM PARAMETERS

Electron beam scenarios

Goal: Study the impact of electron beam properties on optical beam quality.

Scenarios

- ◆ (A) Increased emittance bunch (0.8 mm-mrad).
- ◆ (B) Reduced quad strength (from 10 to 2 T/m, e-beam bigger in one plane).
- ◆ (C) Symmetric undulator focusing.
- ◆ (D) Bunch with double peak current and half the bunch length.

Table 4: Beam quality coefficient at n_{sec} corresponding to minimum M^2 and maximum brightness for all scenarios.

Scenario	Minimum M^2		Maximum Brightness	
	M_x^2	M_y^2	M_x^2	M_y^2
Scenario (A)	3.61	3.34	4.65	3.86
Scenario (B)	3.67	2.31	4.76	2.77
Scenario (C)	3.54	3.57	4.41	4.11
Scenario (D)	3.04	2.69	3.38	3.21

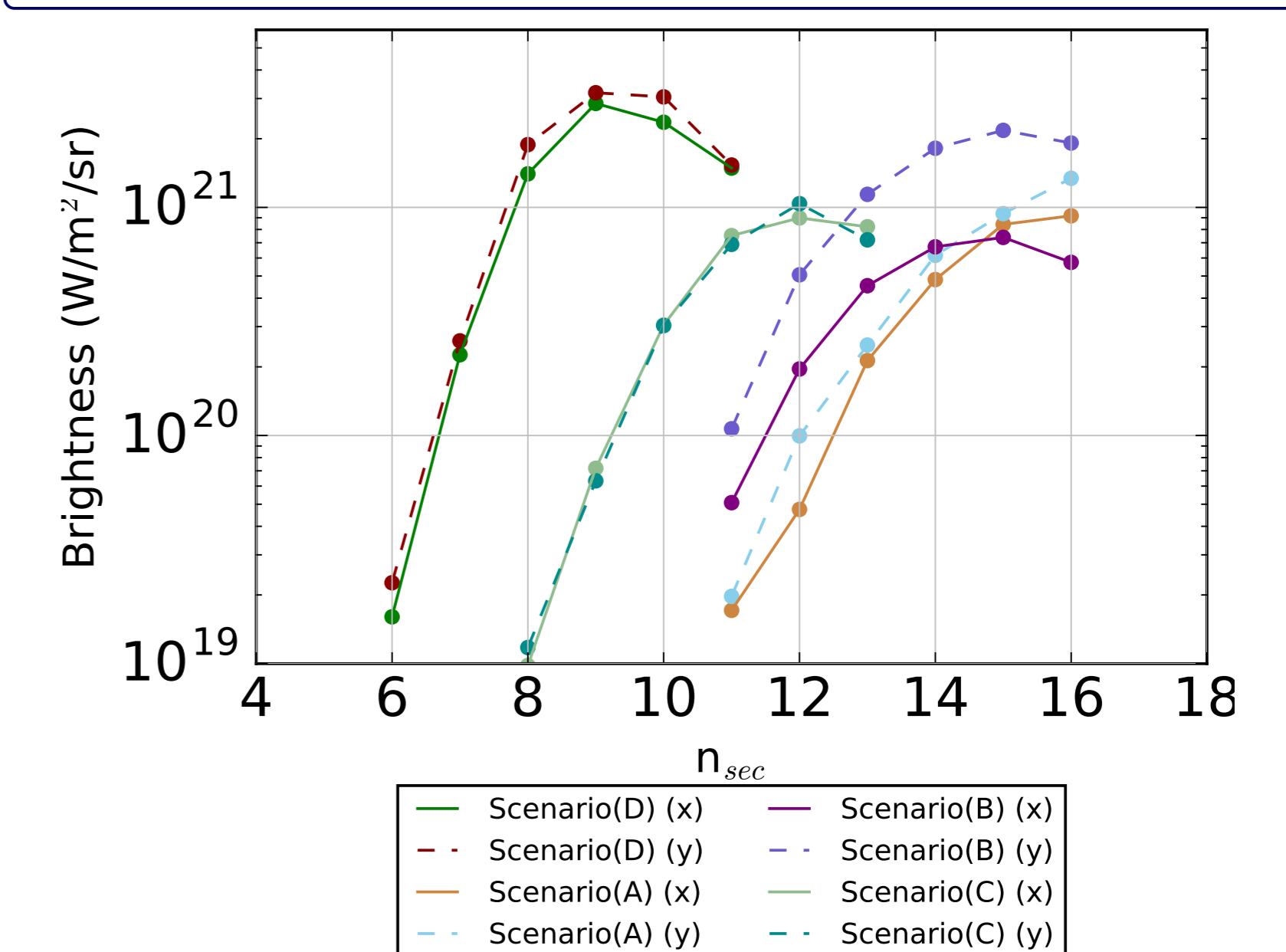


Figure 3: Brightness as a function of n_{sec} (for the electron beam scenarios).

 M^2 (Table 4) compared to 0.75 m module (Table 3)

- ◆ Scenario (A): **Degradation** of beam quality compared to the nominal 0.75 m module (relative difference of M^2 in x around 5.7% and 1.5% in y).
- ◆ Scenario (B): **Vast improvement** of beam quality in y (relative difference compared to nominal 0.75 m module: 27%). **Degradation** in x (relative difference of 8.2% compared to the same nominal case).
- ◆ Scenario (C): **No improvement of beam quality** in either of the planes. Relative difference of 8% in y.
- ◆ Scenario (D): **Minimum M^2 of all proposed cases**. **Improvement** in beam quality in both transversal planes (M^2 reduced to 0.77 and 0.84 of the nominal case in x and y, respectively).

Summary

- ◆ Three different module lengths (0.5, 0.75 and 1 m) were assessed to determine the impact of the undulator design on the beam quality.
- ◆ The 0.75 m undulator module was chosen, optimum for the different R&D topics proposed (mode-locking and HB SASE), without degrading the beam quality compared to longer modules.

References

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