

# Electro-Optic Longitudinal Bunch Profile Measurements at FLASH: Experiment, Simulation, and Validation

Bernd Steffen, DESY

FEL 2007

Novosibirsk, August 29th 2007

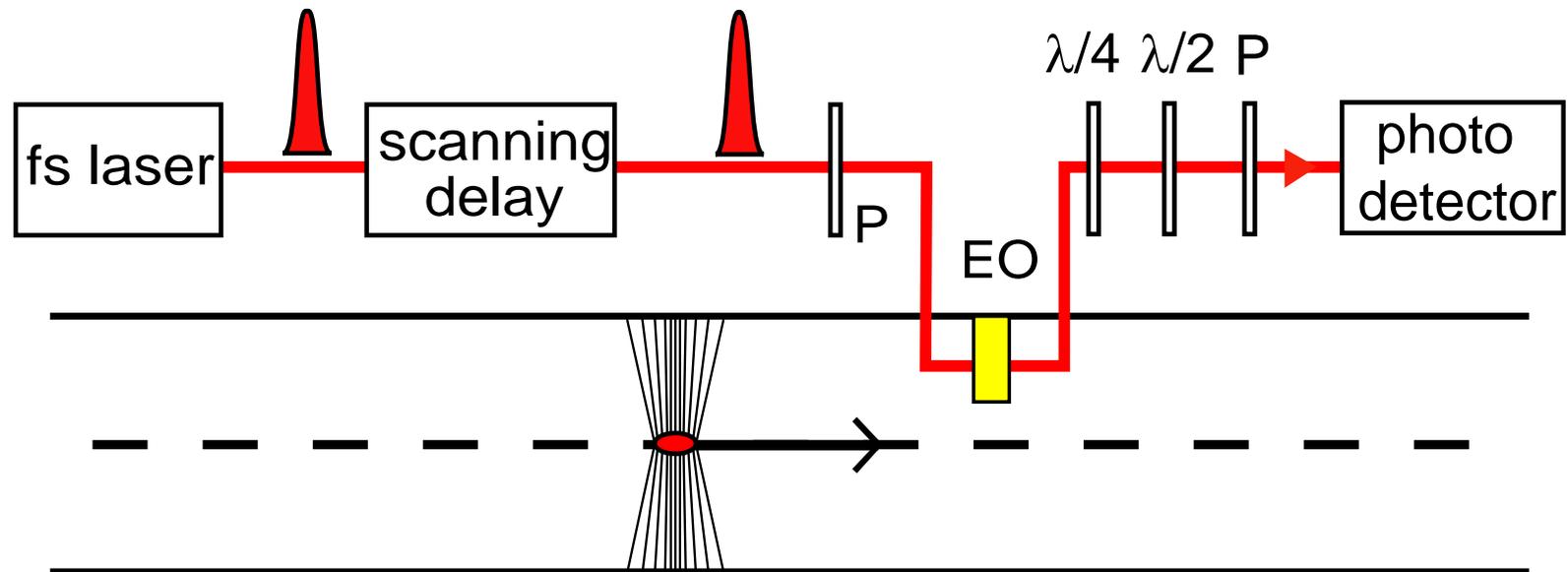
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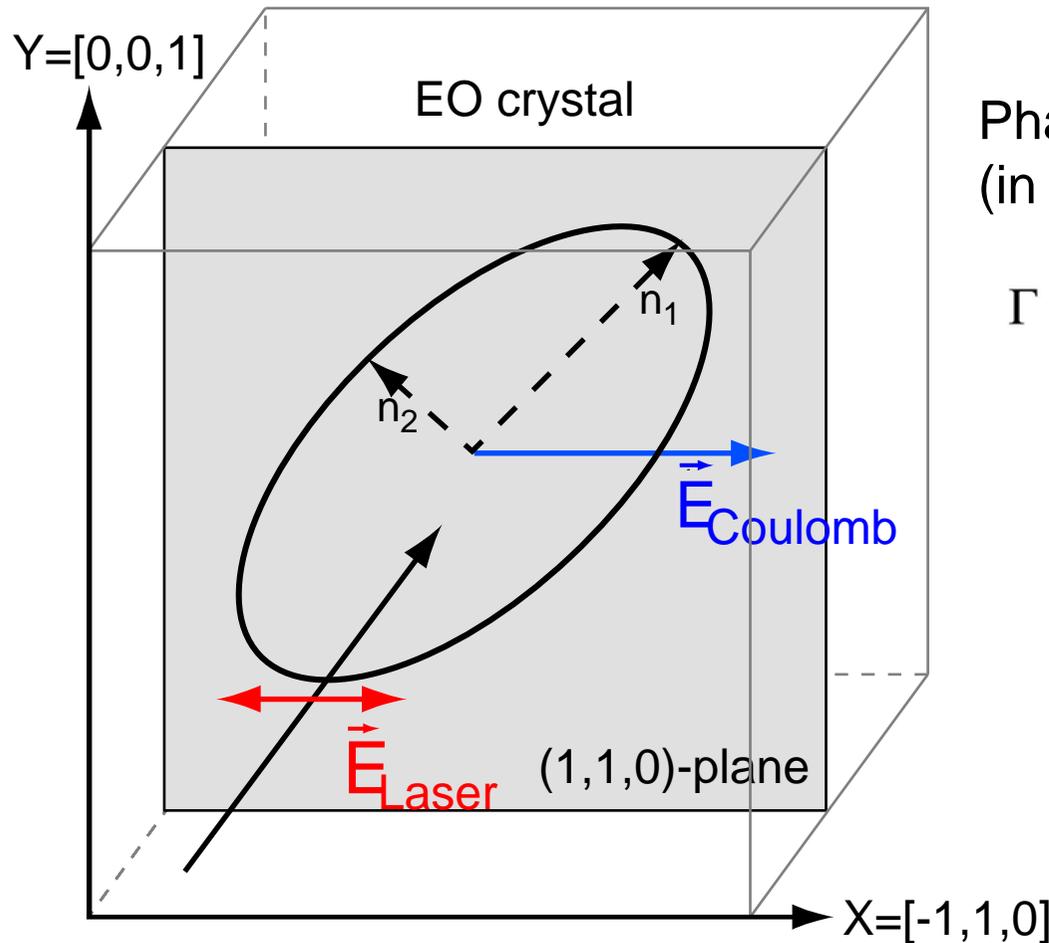
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# Electro-Optic Bunch Length Detection



- Coulomb field of electron bunch induces birefringence in EO crystal.
- birefringence is sampled by Ti:Sa laser pulse.

# The Electro-Optic Effect: Coulomb Field induced Birefringence



Phase retardation  
(in the small signal limit):

$$\begin{aligned}\Gamma &= \frac{\omega d}{c}(n_1 - n_2) \\ &= \frac{\omega d}{c}n_0^3 r_{41} E_{\text{Coulomb}}\end{aligned}$$

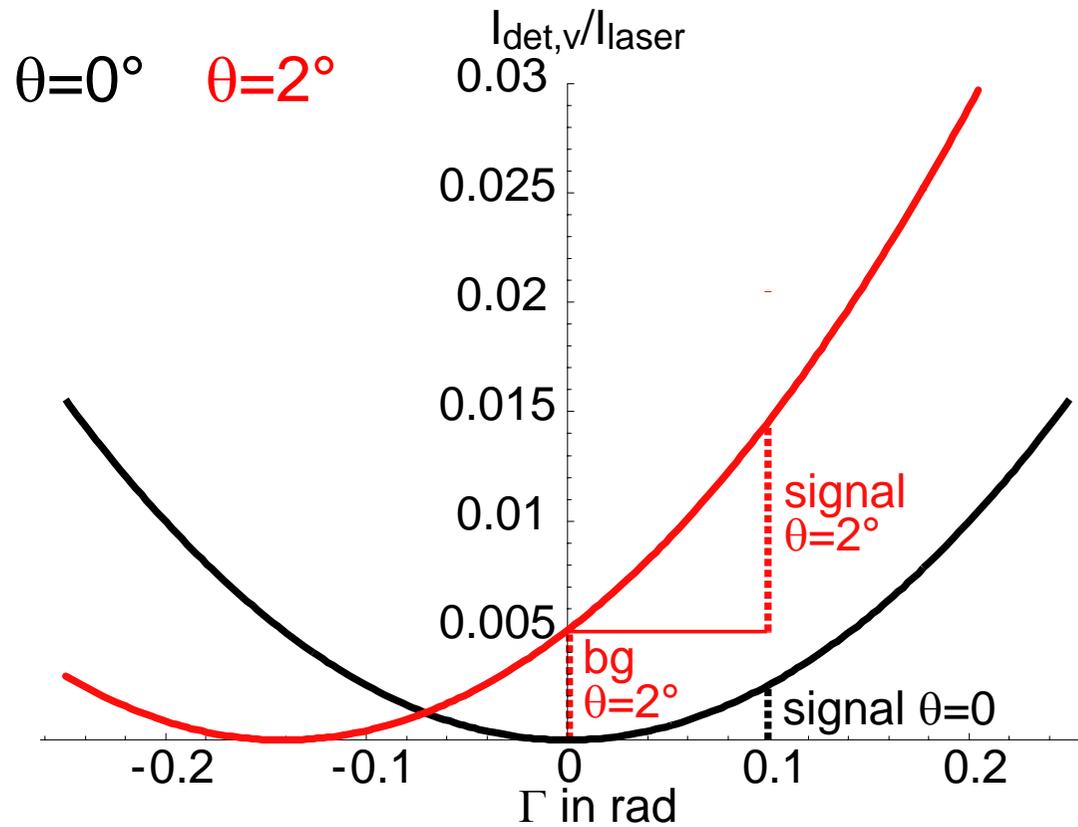
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# Effect of the half wave plate



$$I_{\text{det}}(\theta, 0, \Gamma) = \frac{I_{\text{laser}}}{2} [1 - \cos(\Gamma + 4\theta)]$$

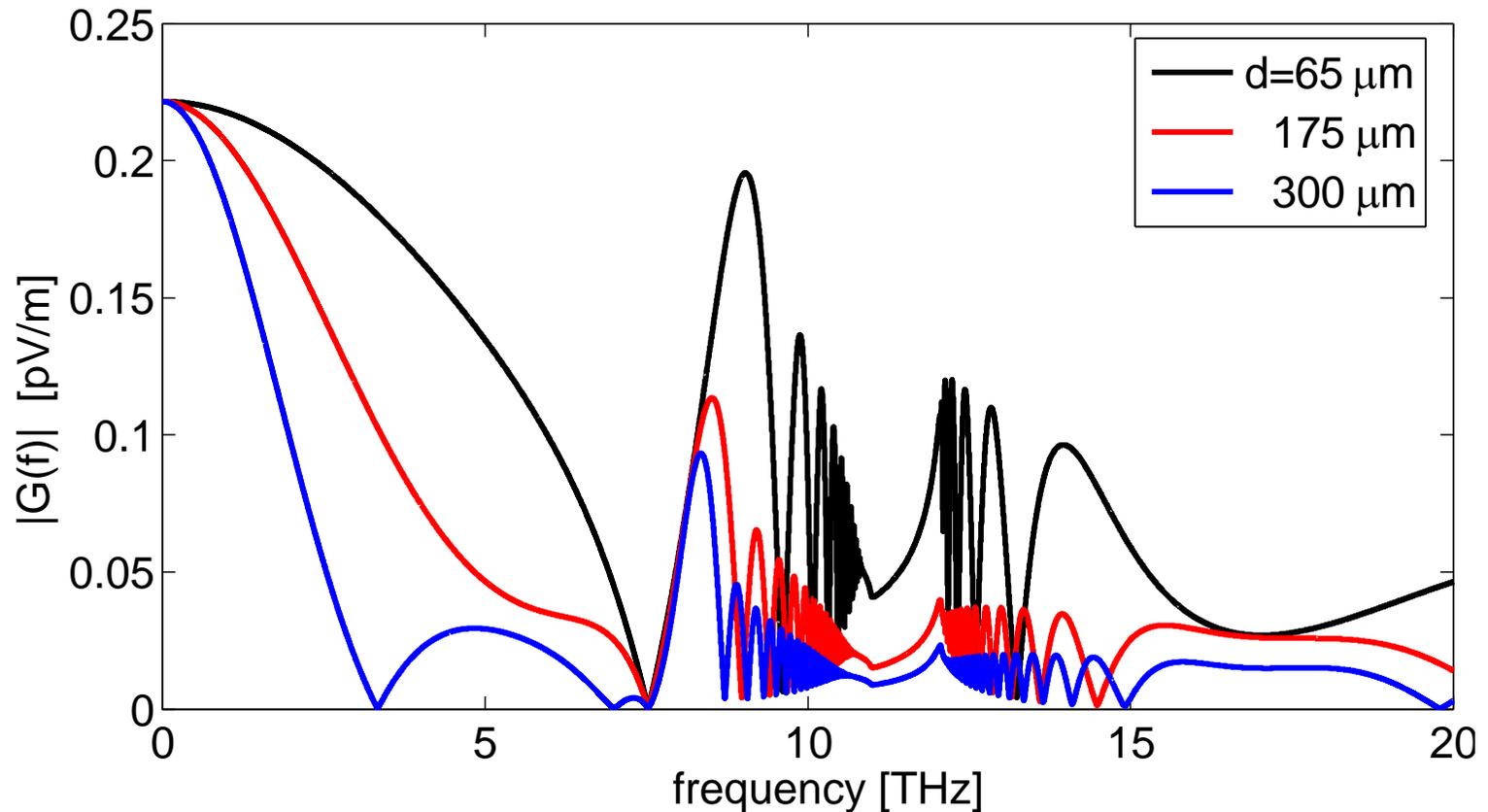
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# Response function of the GaP crystal



$$G(f, d) = r_{41}(f) \frac{2}{1 + n(f) + ik(f)} \frac{1}{d} \int_0^d \exp \left[ i 2\pi f z \left( \frac{1}{v_{\text{ph}}(f)} - \frac{1}{v_g} \right) \right] dz$$

EO coeff., transmission, velocity matching

**Signal distortion esp. for thick crystals !**

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# The simulation program

- Effective Coulomb pulse calculated from electron bunch profile and EO response function
- Phase retardation  $\Gamma$  from effective THz pulse
- Complex electric field of the modulated stretched laser pulse calculated according to:

$$\begin{aligned} E_{\text{det}}(\theta, \phi, \Gamma) &= \begin{pmatrix} 0 & 1 \end{pmatrix} \cdot \mathbf{H}(\theta) \cdot \mathbf{Q}(\phi) \cdot \mathbf{EO} \cdot \begin{pmatrix} 1 \\ 0 \end{pmatrix} \cdot E_{\text{laser}} \\ &= \frac{E_{\text{laser}}}{\sqrt{2}} [\cos(2\theta) \sin(\Gamma/2) - \sin(2\phi - 2\theta) \cos(\Gamma/2) \\ &\quad -i(\sin(2\theta) \cos(\Gamma/2) + \cos(2\phi - 2\theta) \sin(\Gamma/2))] \end{aligned}$$

- Temporal and spectral intensity in both polarisations can be calculated.

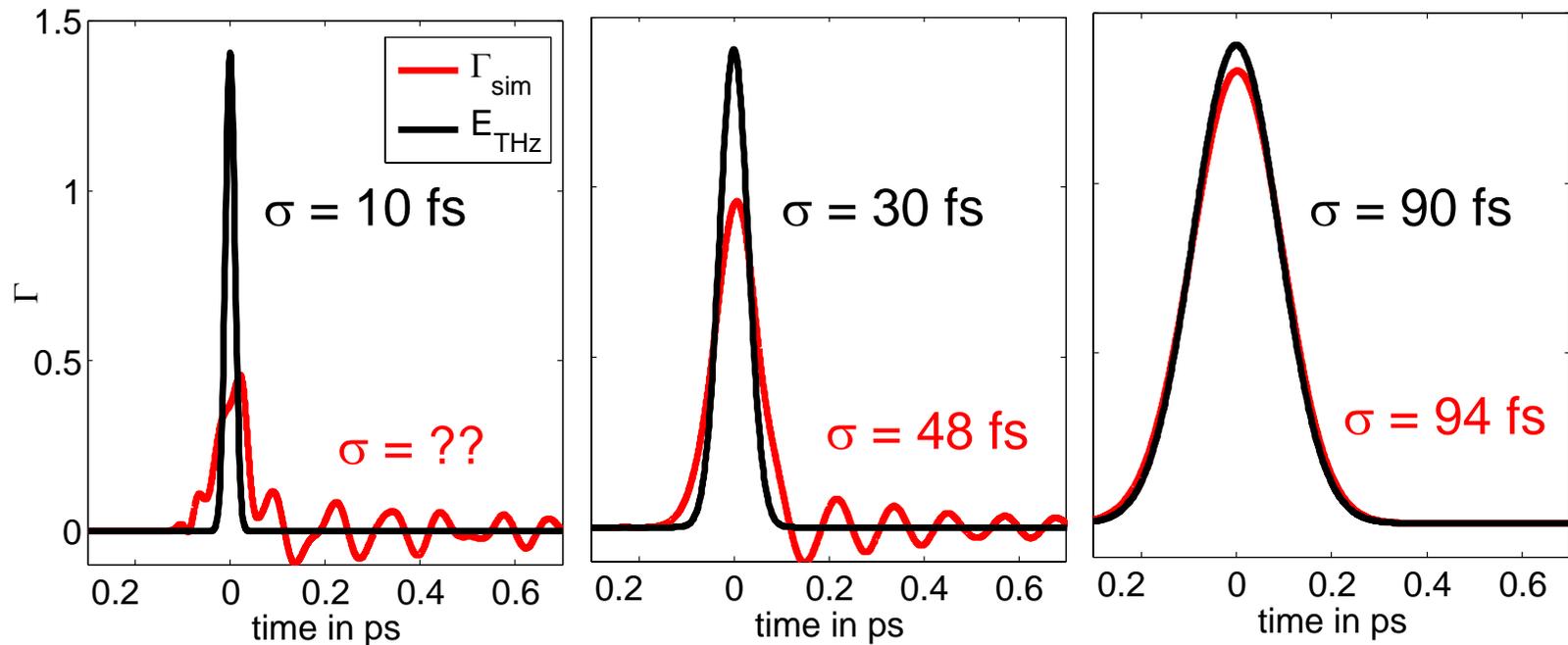
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# Simulated EOTD signals of Gaussian THz pulses in 65 $\mu\text{m}$ GaP



All pulse length:  
 $\sigma$  of a fitted  
Gaussian

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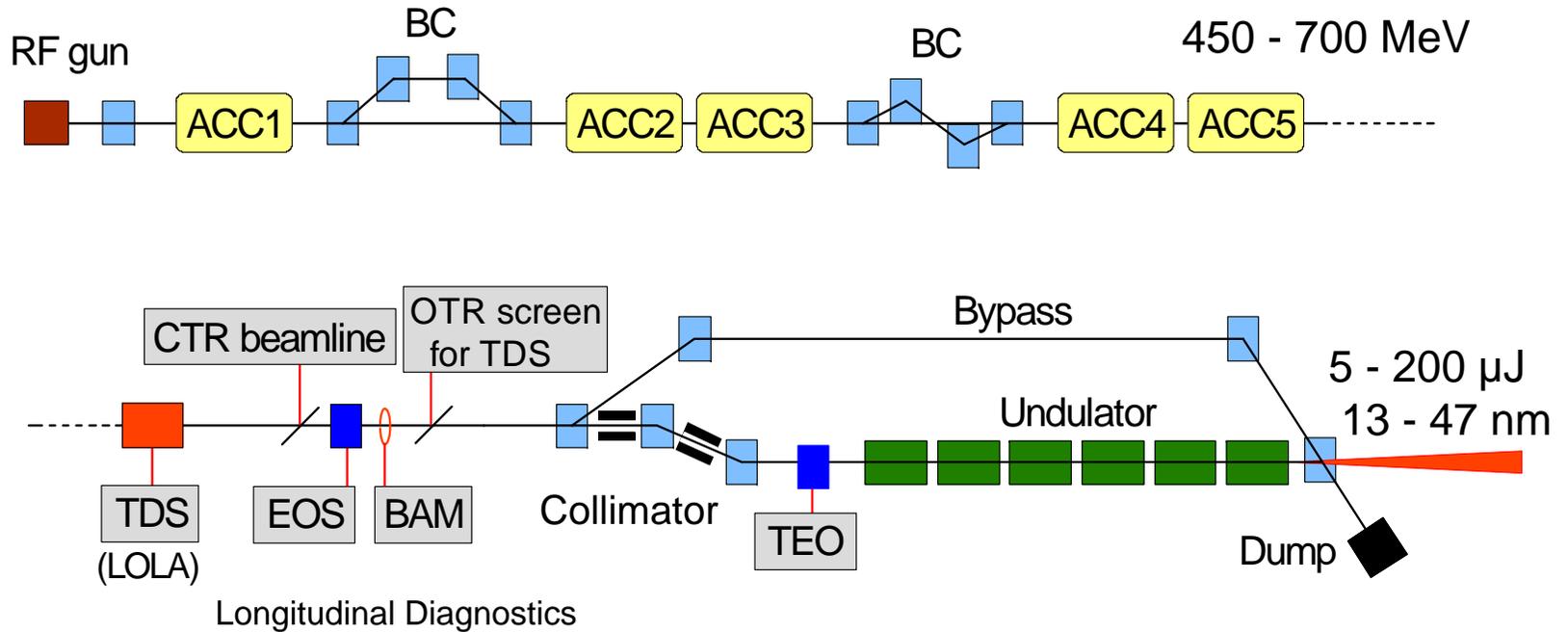


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## Free-Electron Laser in Hamburg



Electron bunches:  $\approx 30$  fs duration  
 $\approx 700$  MeV electron energy  
 $\approx 0.5 - 1$  nC charge  
 $\approx 1$  kA peak current

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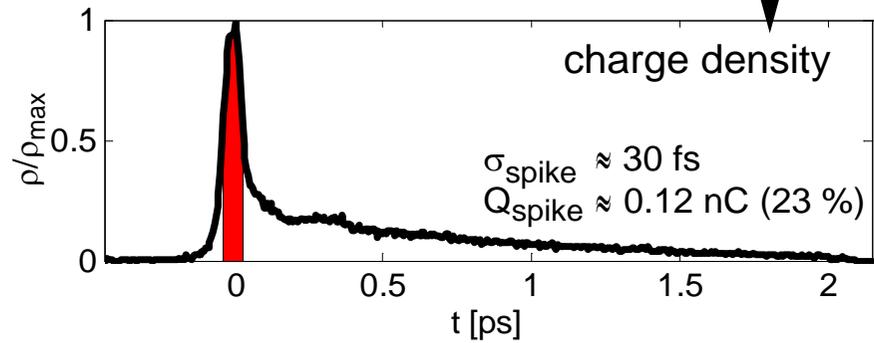
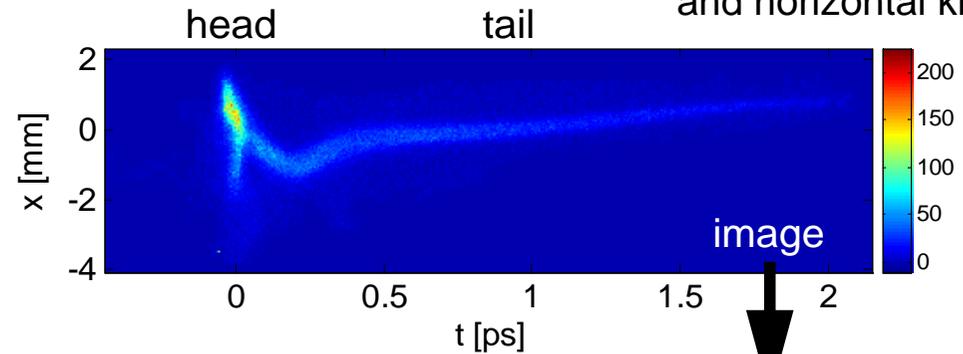
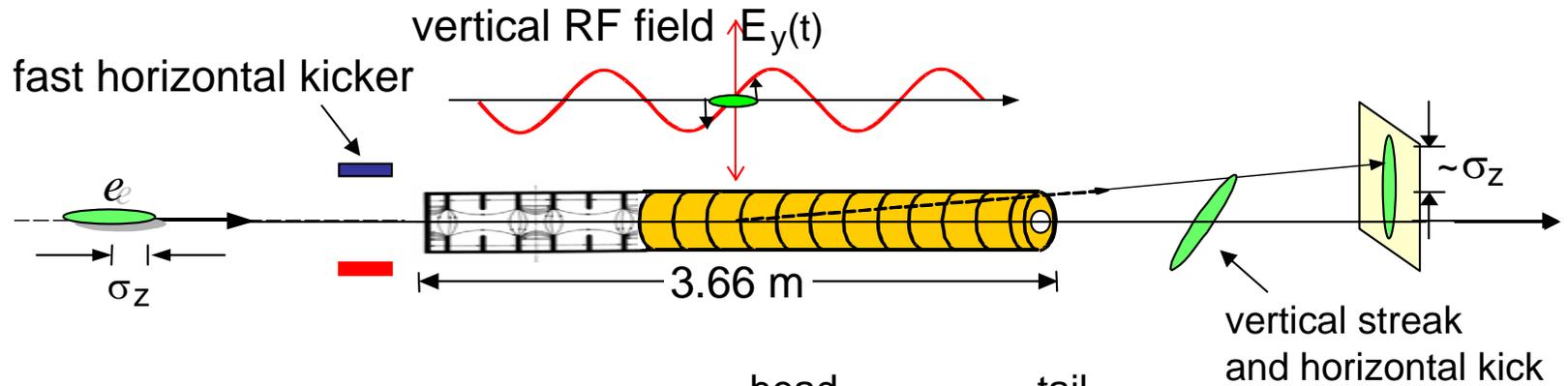
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# Bunch length measurements using the transverse deflecting structure (TDS)



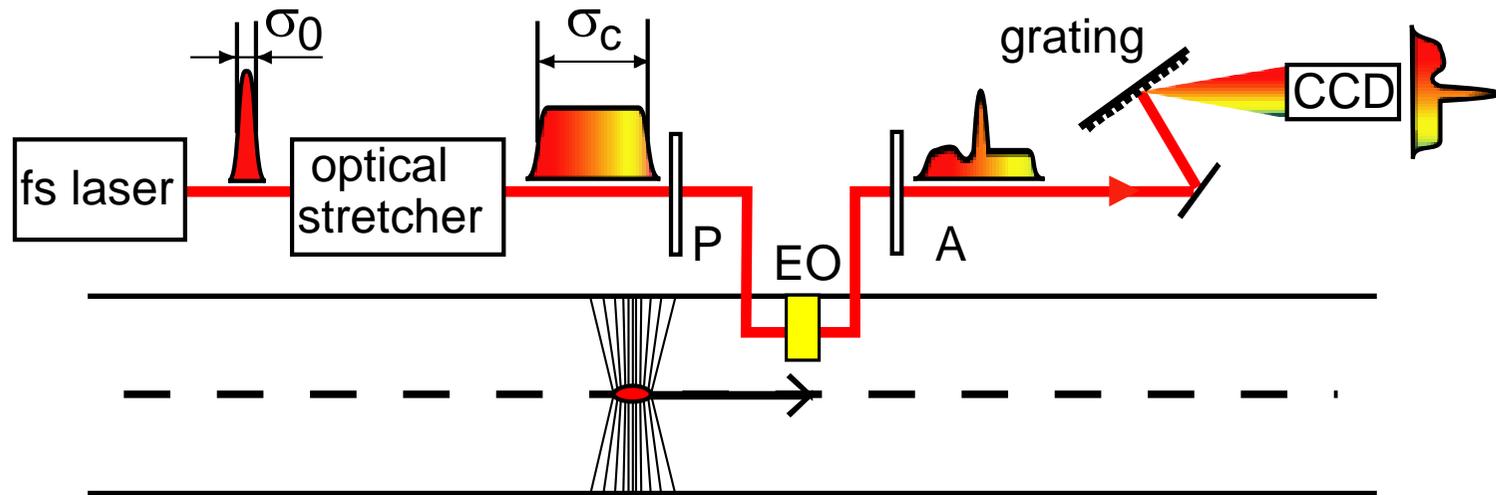
Resolution:  
approx. 20 fs  
at a time window of 2 ps

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# EO Spectral Detection



- Linear relationship between wavelength and long. position in laser pulse (“linear chirp“)
- Bunch profile is transferred to spectral profile of the laser pulse

- Problem: Frequency mixing with Coulomb field creates new frequency components:

⇒ Distortions at large chirp  $\alpha \approx 1/\sqrt{\sigma_0 \sigma_c}$

$$\sigma_{\min} \approx 2.6\sqrt{\sigma_0 \sigma_c} \approx 200 \text{ fs} \quad (\text{for Gaussian pulses!})$$

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# Spectrally resolved detection: Comparison of measured to simulated Signals

5 consecutive bunches,  
corrected for different  
arrival times

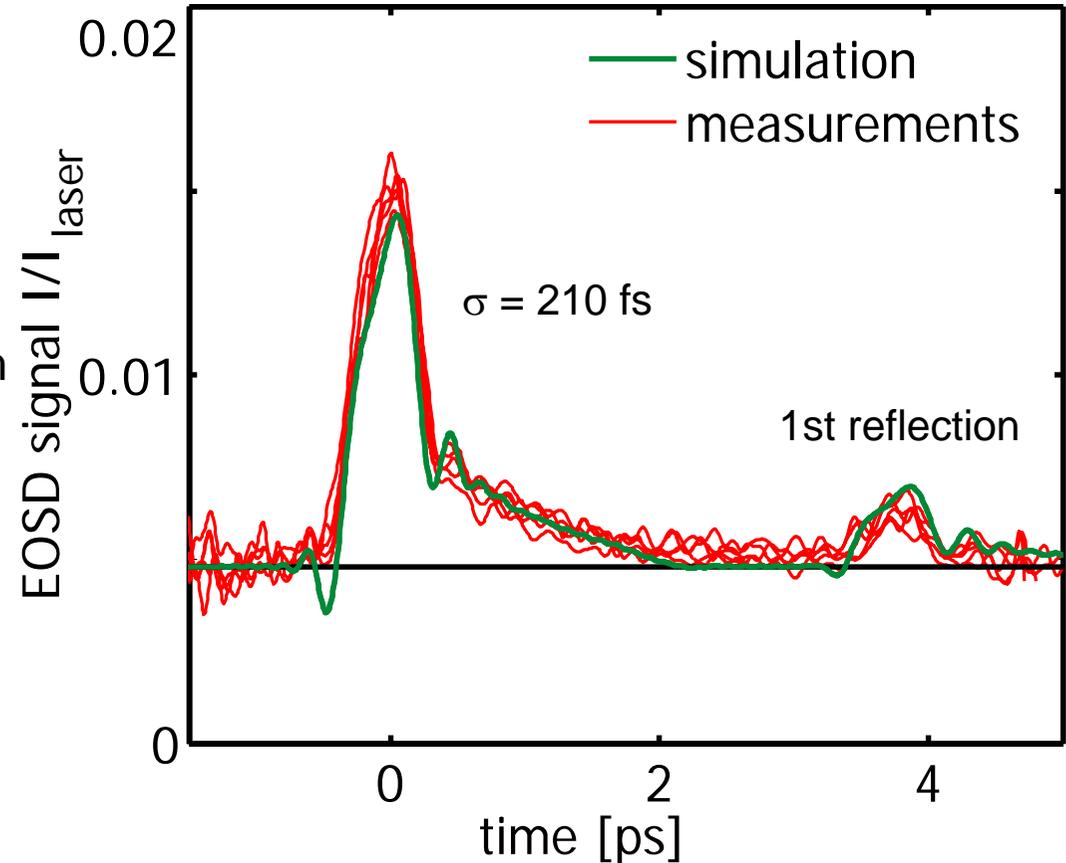
Simulation:  
EOSD signal of a bunch  
measured with TDS

GaP 175  $\mu\text{m}$

$\theta=2^\circ$

$\sigma_0=6$  fs

$\sigma_c=1.5$  ps



**Excellent agreement with simulation in shape and amplitude,**  
but much wider than electron bunch due to response function and  
frequency mixing

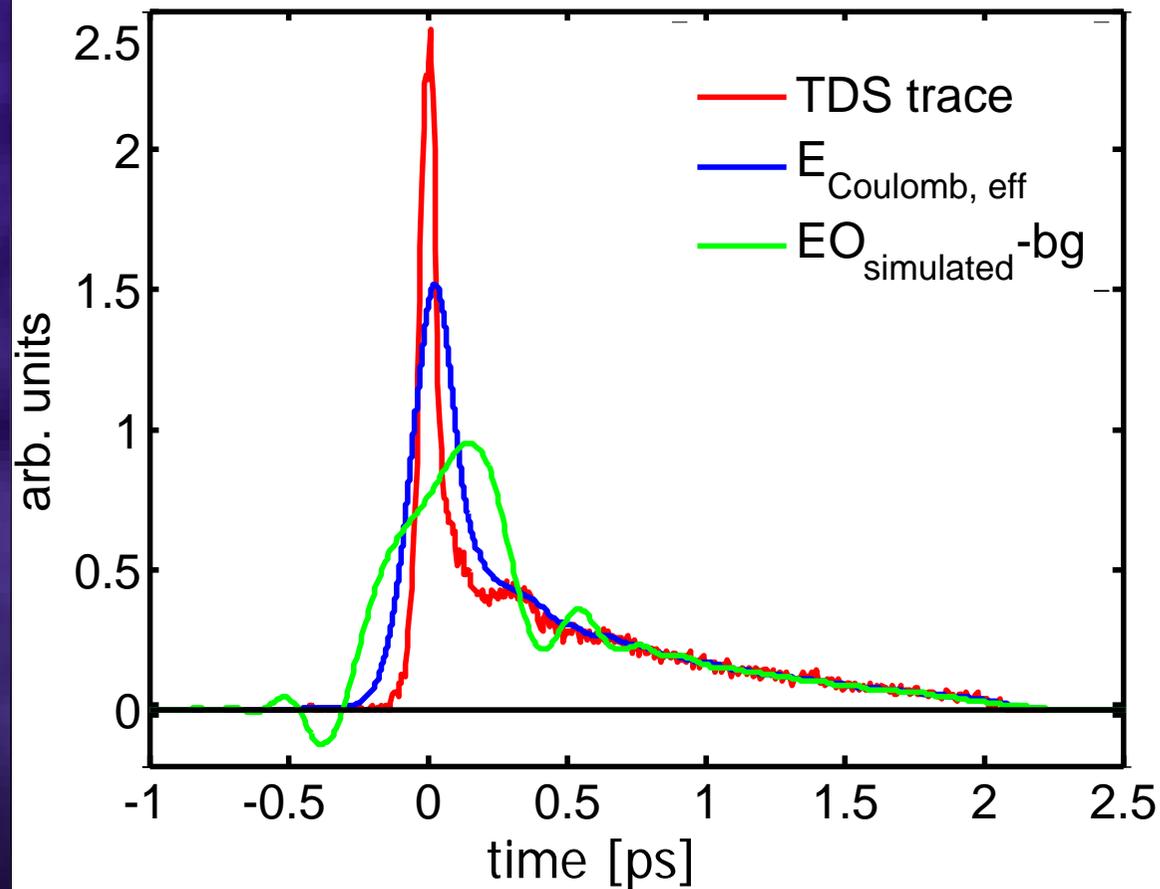
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# EOSD: Distortions due to frequency mixing for thin crystal and large chirp



GaP 175  $\mu\text{m}$  thick

Laser  $\sigma_0=6$  fs  
chirped to:  $\sigma_c=1.5$  ps

$\theta=2^\circ$

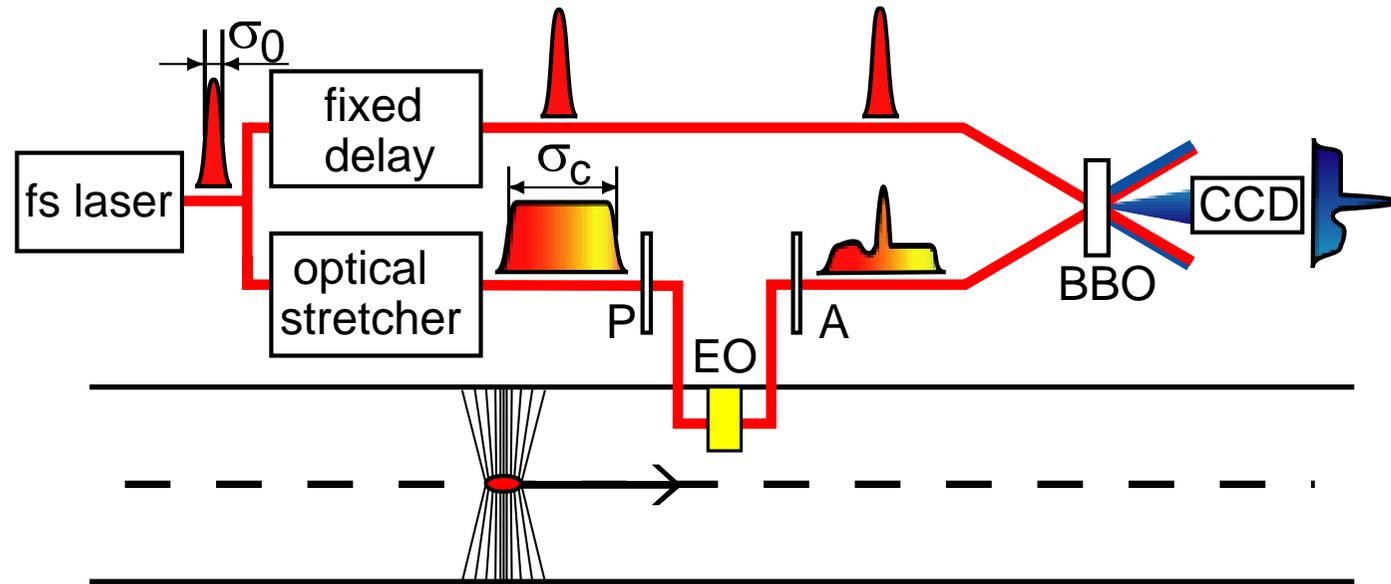
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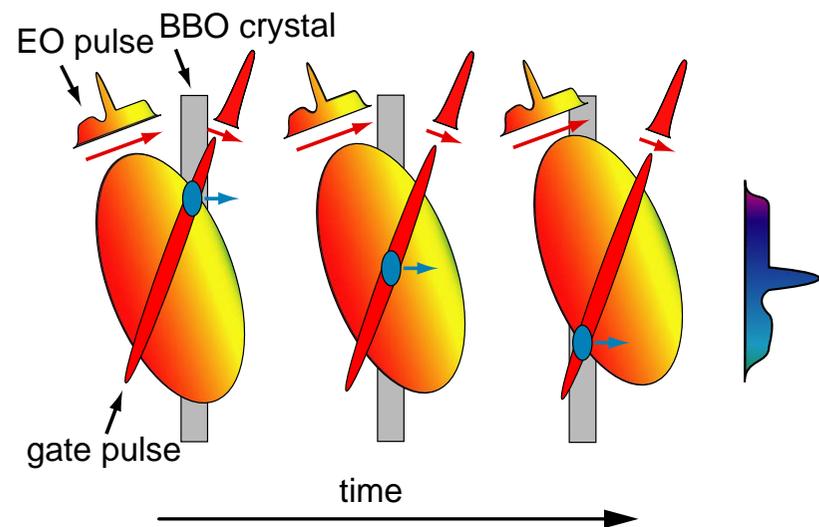
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# EO Temporal Detection



- Single shot cross-correlation with fs pulse in a frequency doubling crystal (BBO)
- approx. 100  $\mu\text{J}$  pulse energy necessary for 10 ps time window



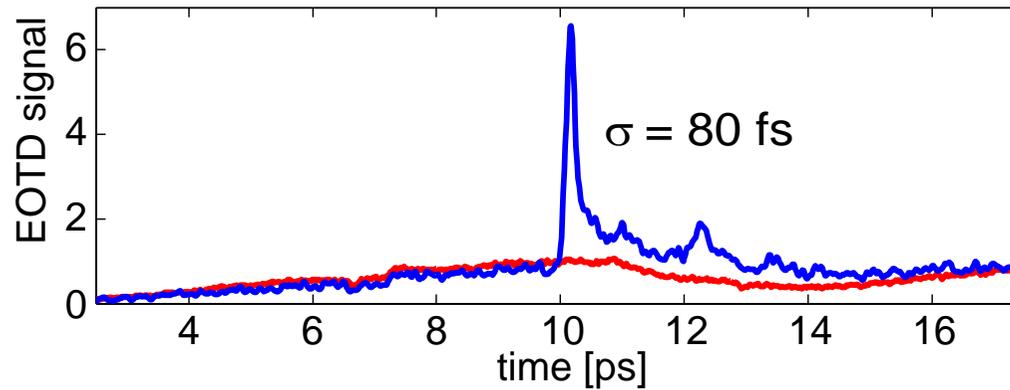
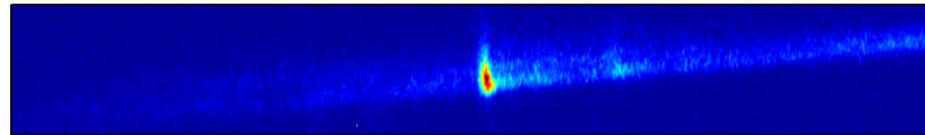
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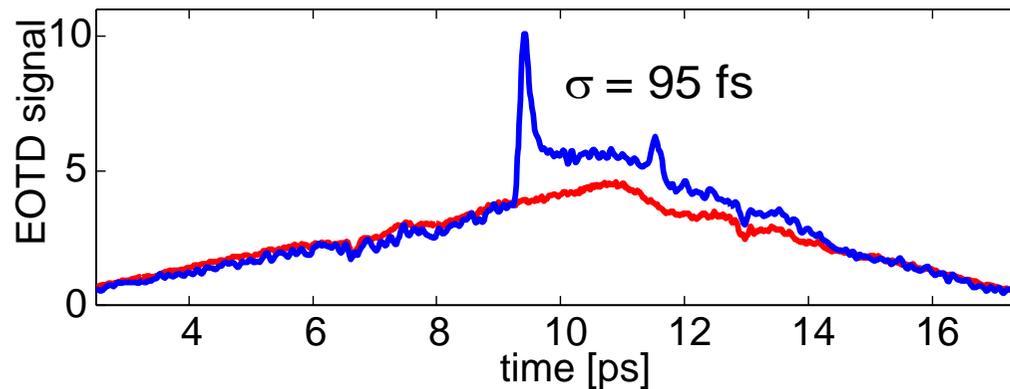
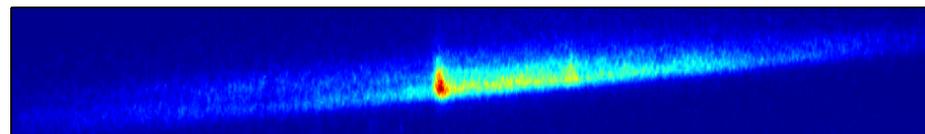
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# EO Temporal Detection



$\theta = 0$

EO signal  $\propto E_{\text{Coul}}^2$



$\theta = 1^\circ$

EO signal  $\propto E_{\text{Coul}}$

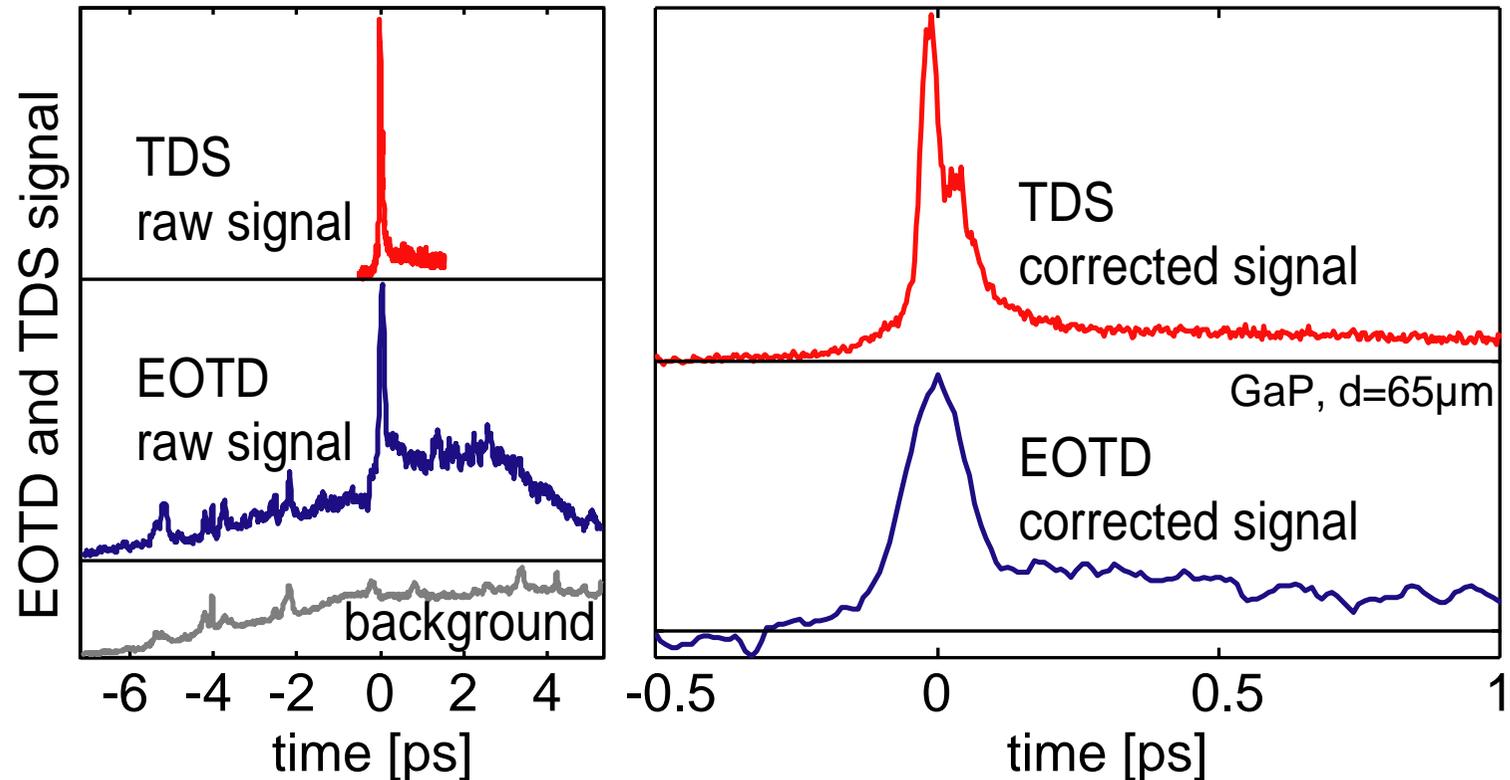
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# Comparison of EOTD vs. TDS measurements



- 10th bunch in bunch train: electro-optic detection
- 11th bunch: TDS

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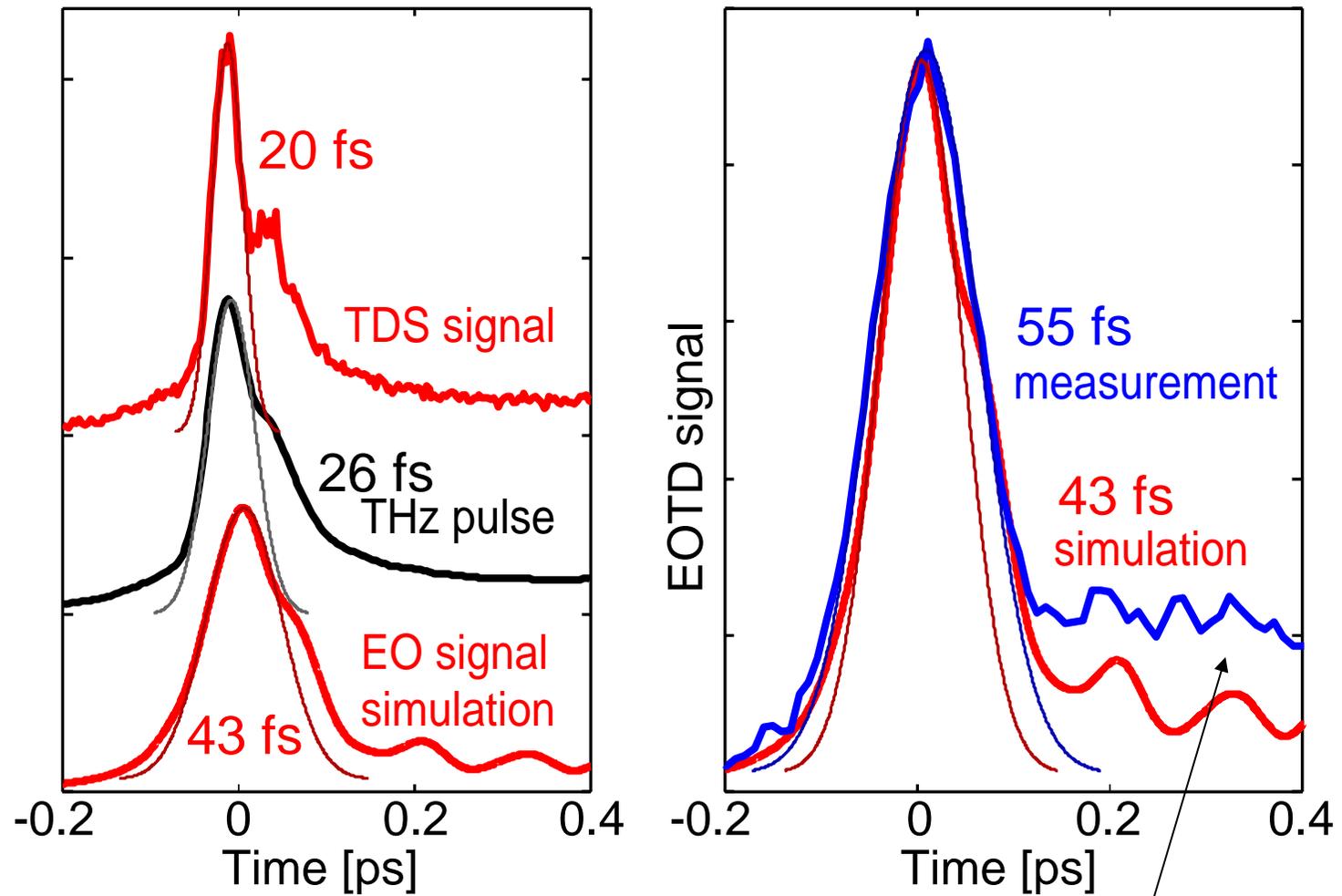
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# Comparison of EOTD vs. TDS measurements



- **Good agreement between measurement and simulation**
- **close to the resolution limit of GaP**

Signal due to wake fields?

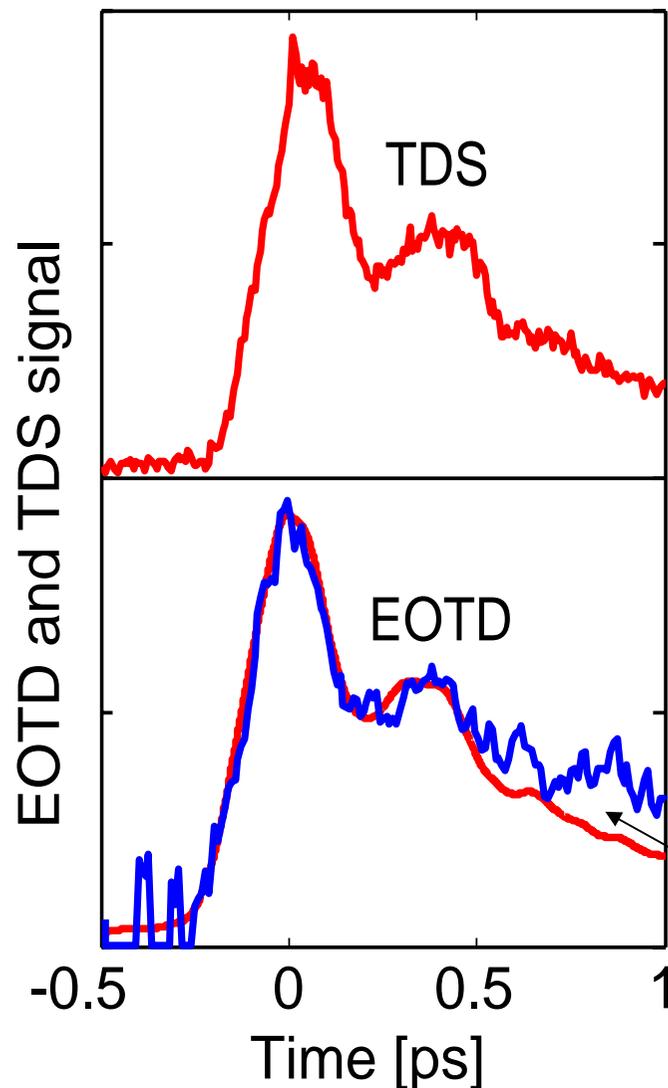
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# TDS and EOTD measurement of overcompressed bunches



In good agreement with  
the electron bunch shape

Signal due to wake fields?

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# Conclusions

- Benchmarked EO detection against TDS
- Simulations based on published material data are consistent in shape and amplitude with measured signals for GaP
- EOTD signals measured with of 55 fs (rms) length (linear in field and without deconvolution!) are close to the resolution limit of GaP

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