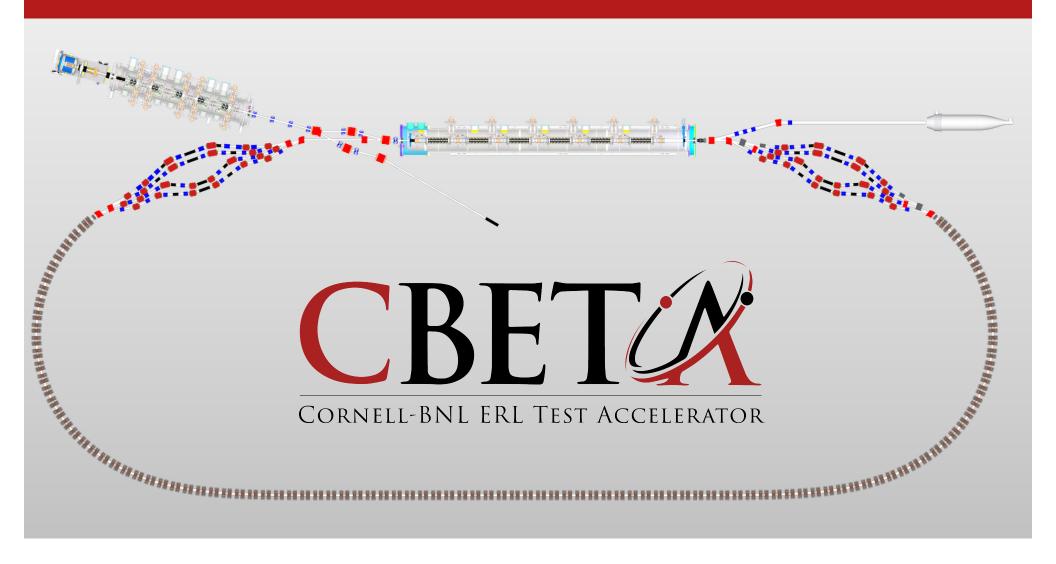




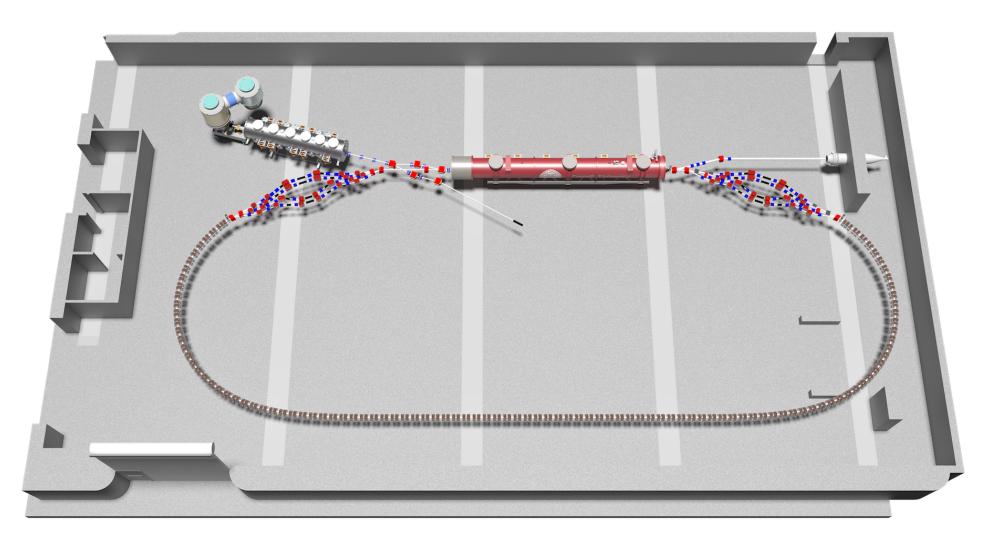
# CBETA Multipass Lattice Design







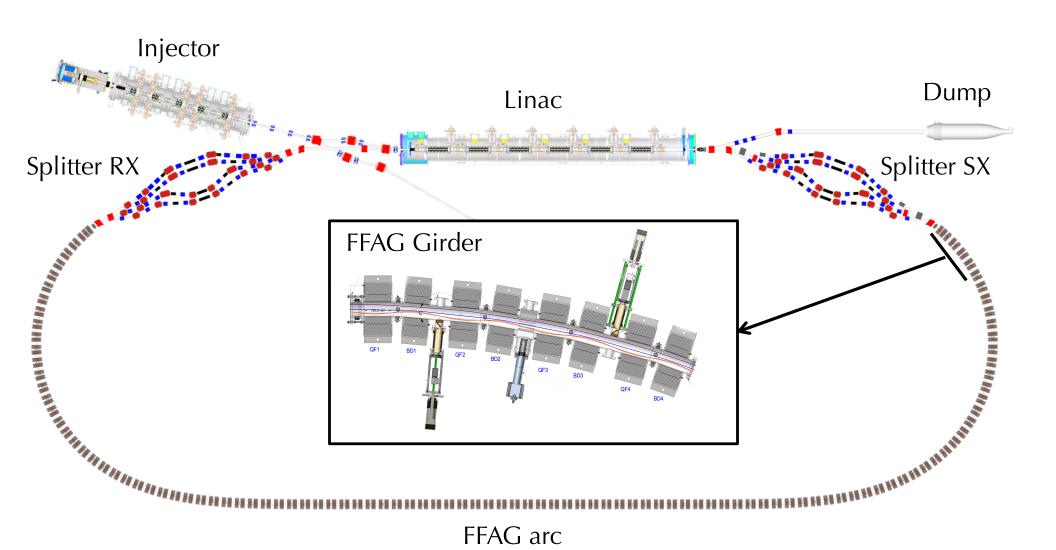






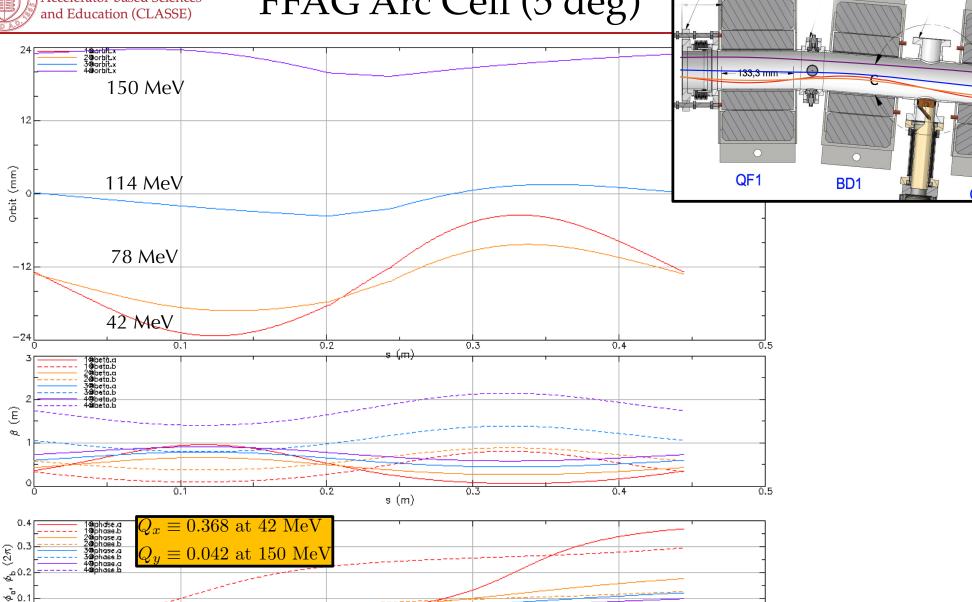
## CBETA Layout in L0E







# FFAG Arc Cell (5 deg)



BD

s (m)

**BPM** 

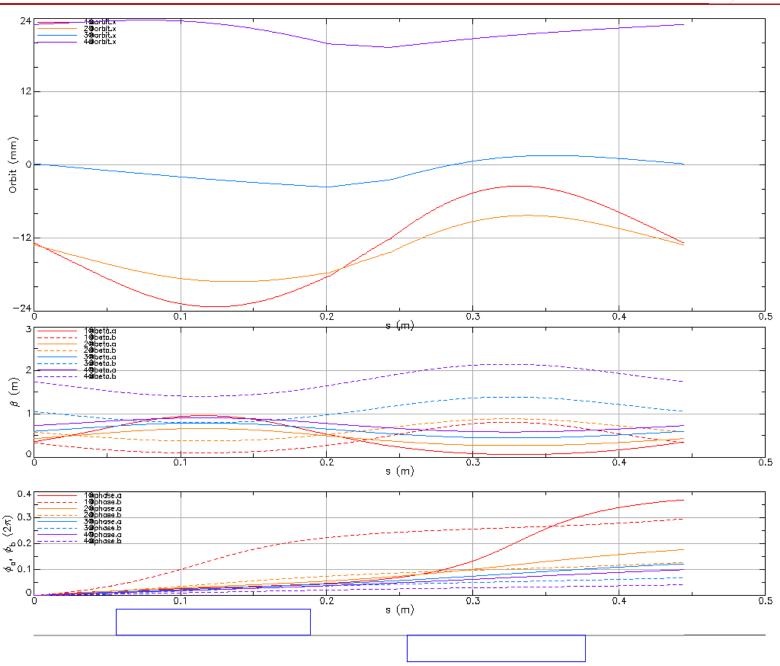
0.4

QF



# Cell designed with fieldmaps

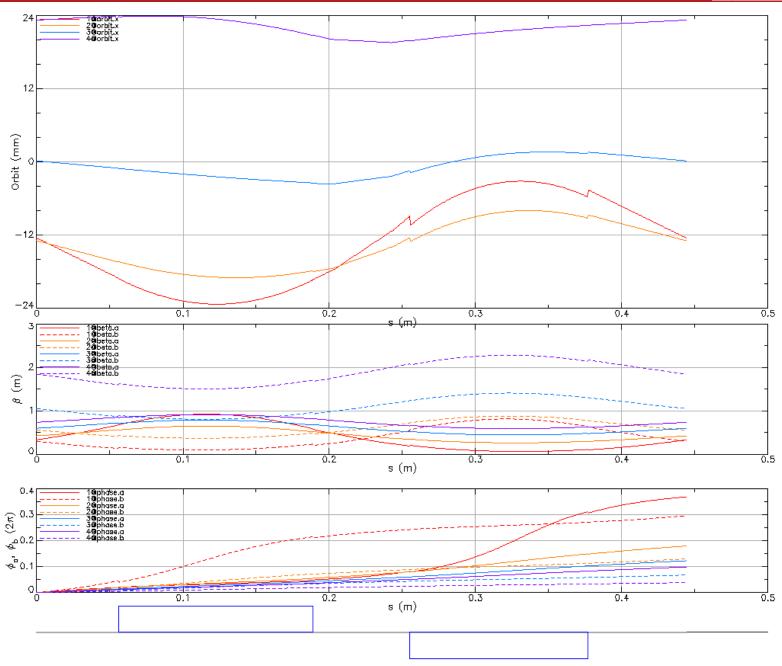






# Cell modeled with Bmad\_standard BROOKHAVEN

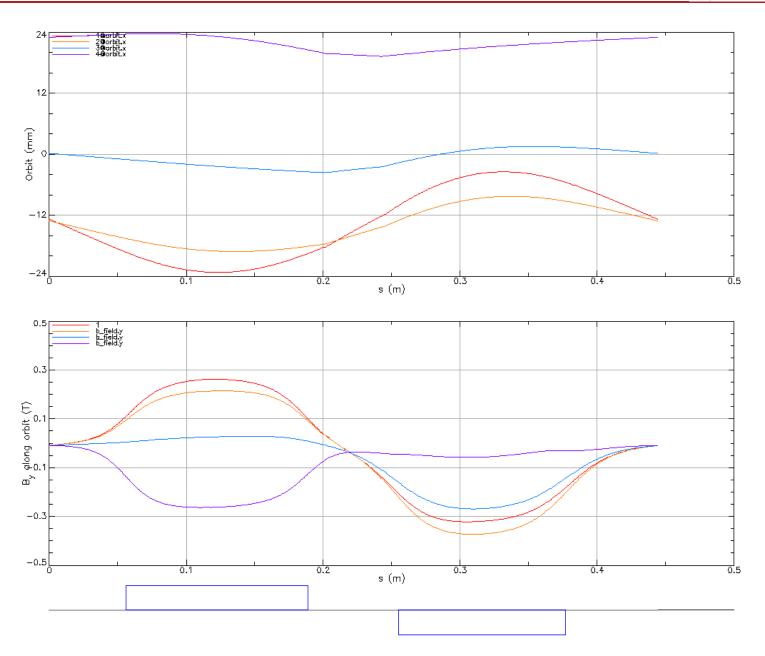






# Fields seen: fieldmaps

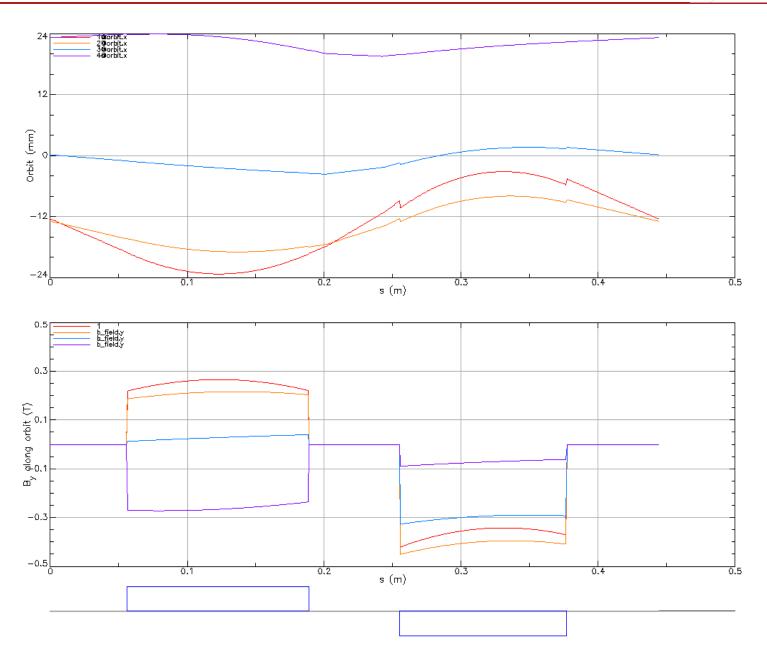






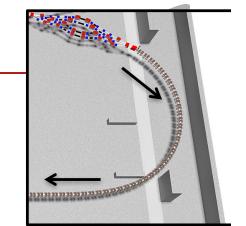
## Fields seen: bmad\_standard

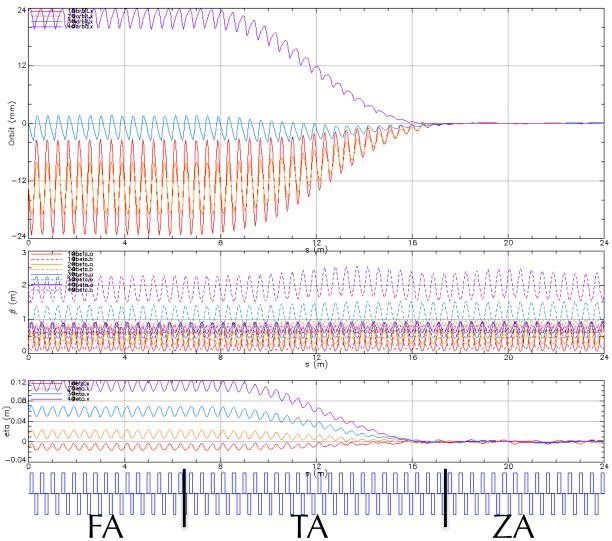






### Designed FFAG Arc, transition, straight





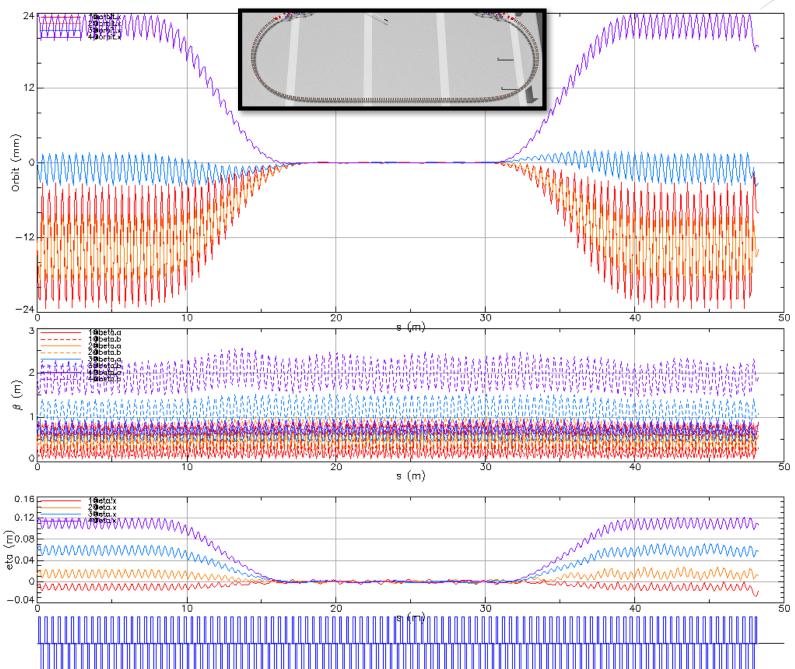
Offsets, angles scaled by factor:

$$f(x) = 1 - x + (1/2 - x)x(1 - x)[1.788 + 3.954x(1 - x) + 6.58x^{2}(1 - x)^{2}]$$



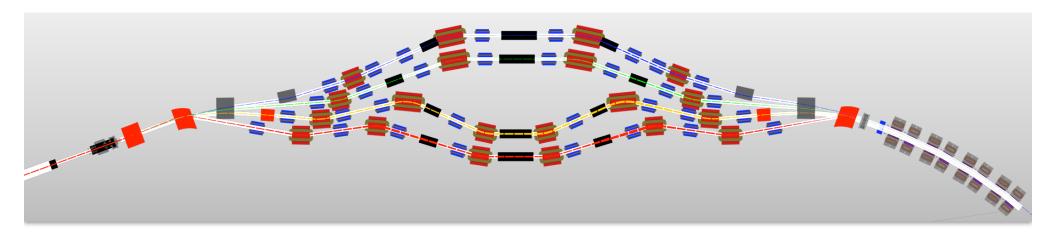
#### Full FFAG Arc







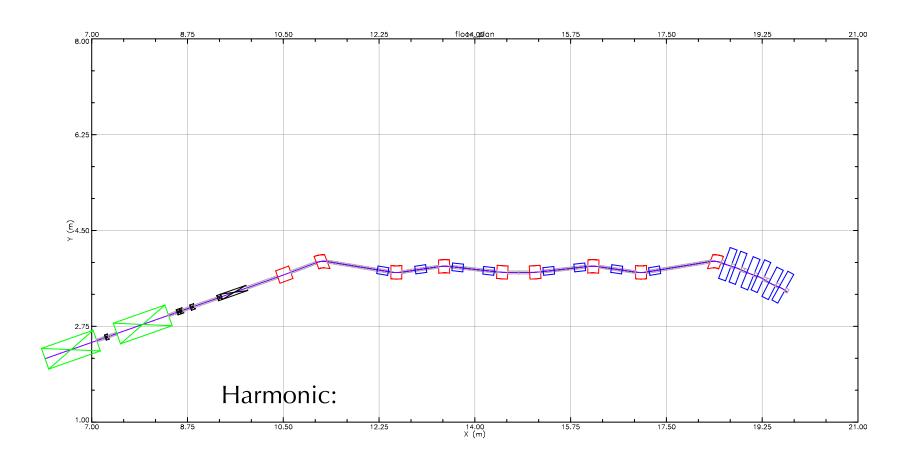




- Receive beams on-axis from the linac
- Match each energy beam onto its stable orbit in the FFAG arg
- Match optics for each energy beam into the FFAG arc
- Momentum compaction (r56) adjustment
- Path lengths: (S1 + FA pass 1) = (S2 + FA pass 2) = (S3 + FA pass 3)
- Allow path length adjustment by sliding joints, ±10 deg rf phase adjustment
- Dipole fields < 0.6 T
- Quad fields < 4 T/m</li>
- Realistic transverse element sizes

## Path length: 1-pass ERL

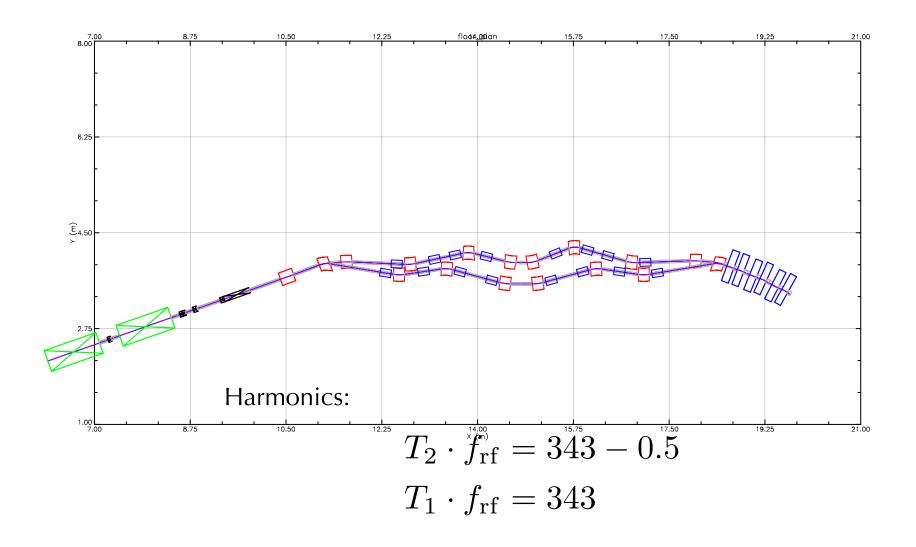




$$T_1 \cdot f_{\rm rf} = 343 - 0.5$$

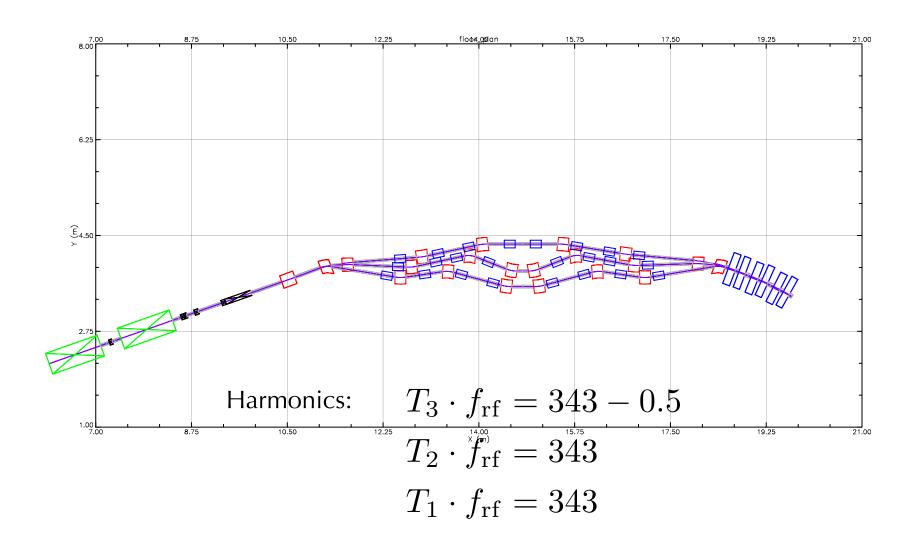
## Path length: 2-pass ERL





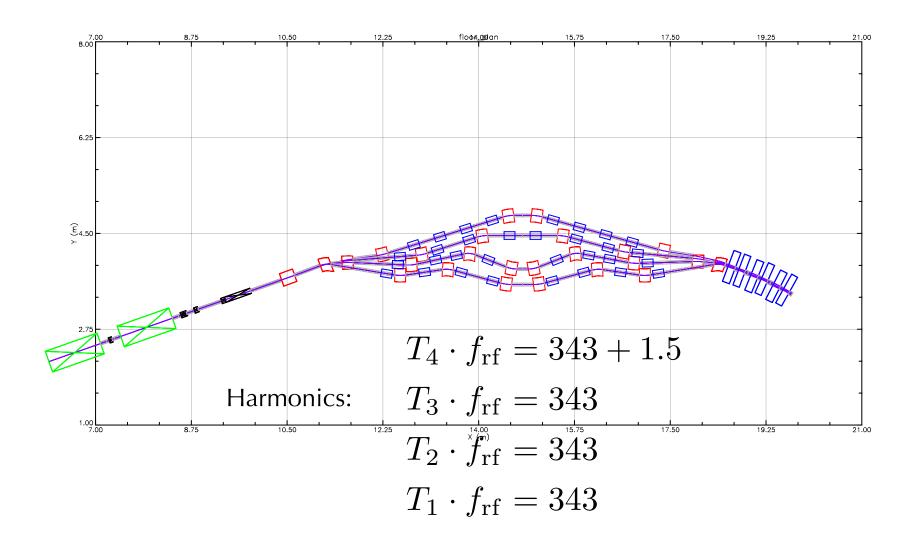
#### Path length: 3-pass ERL





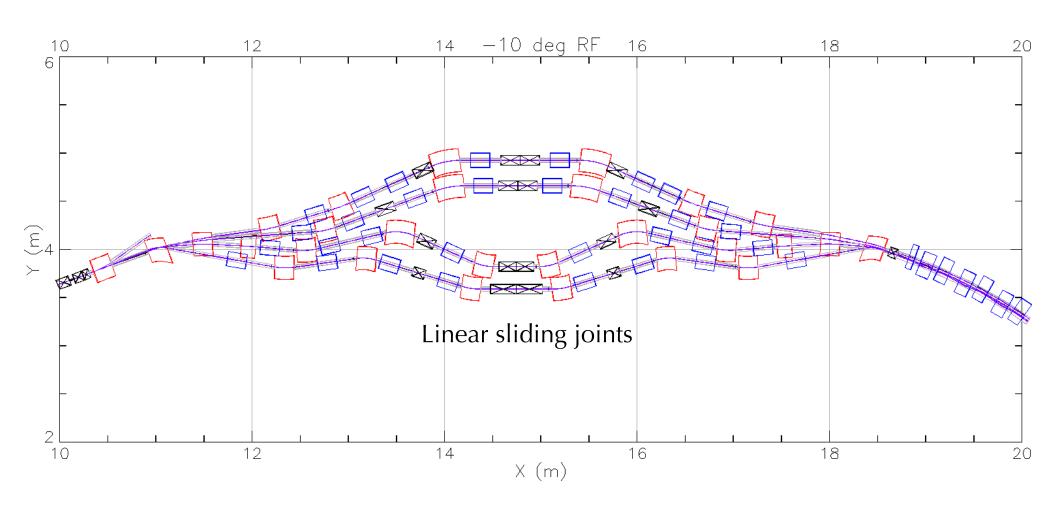
### Path length: 4-pass ERL





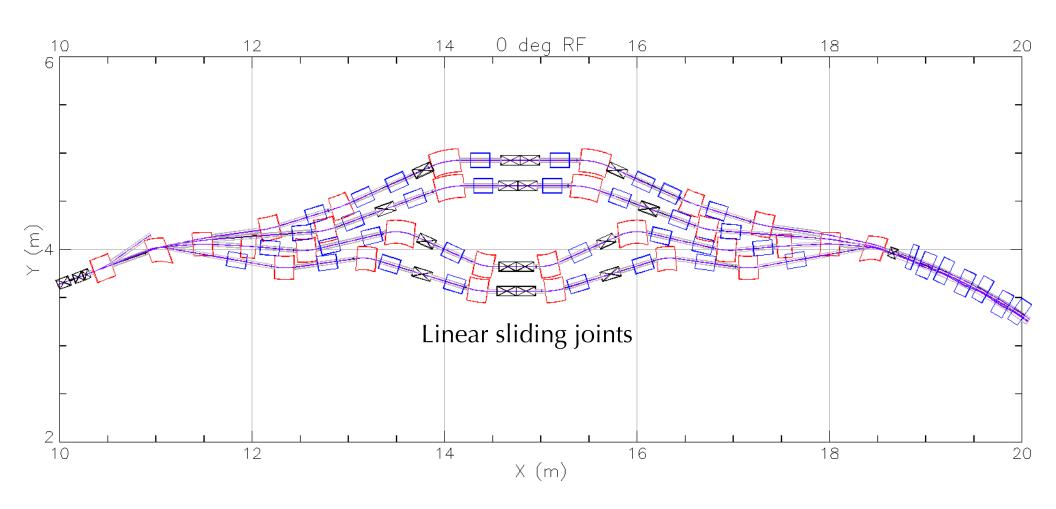
## Pass 1 length adjustment





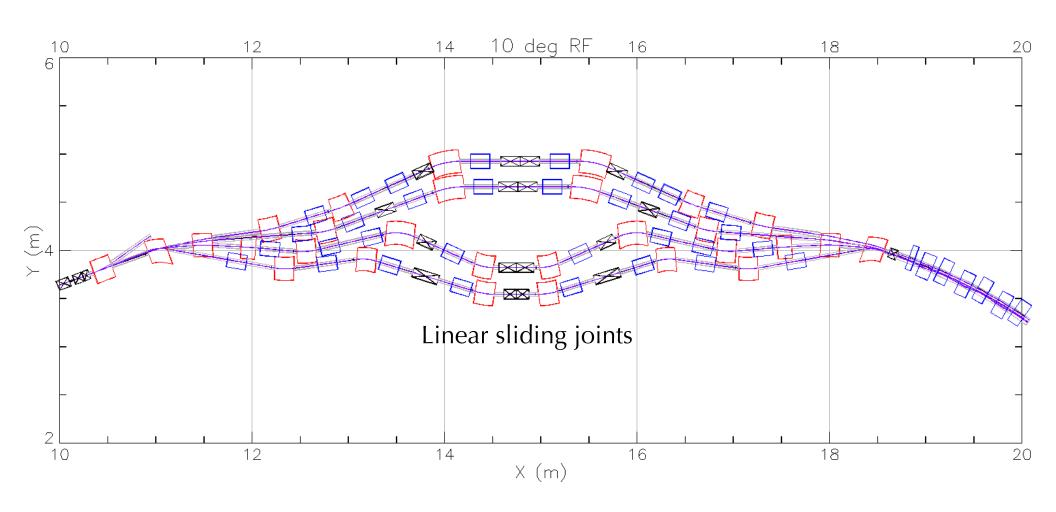
## Pass 1 length adjustment





## Pass 1 length adjustment

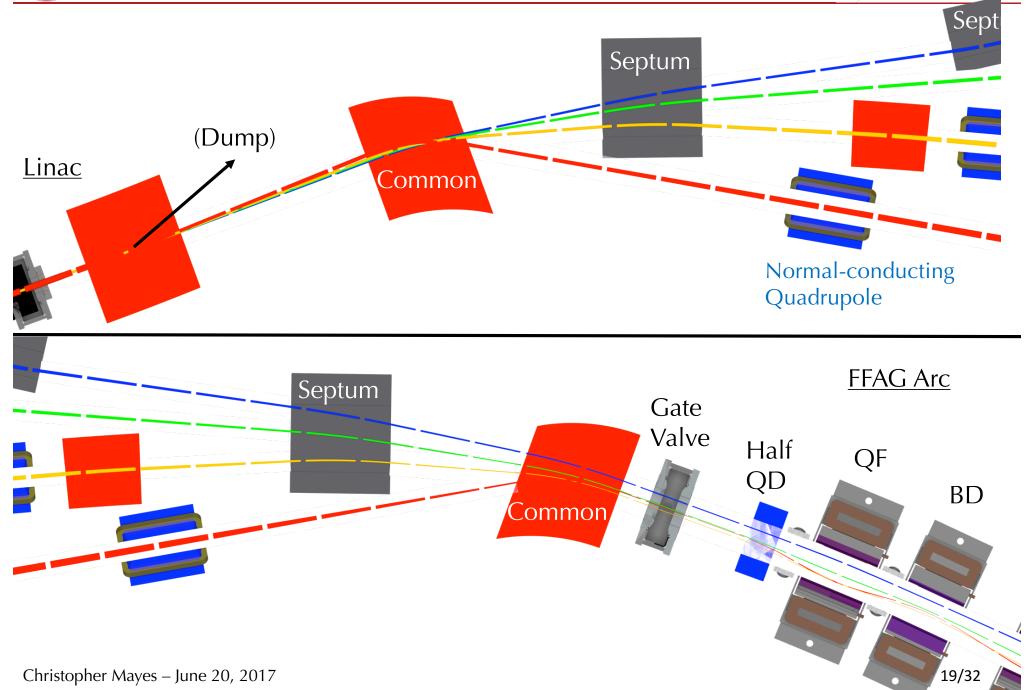






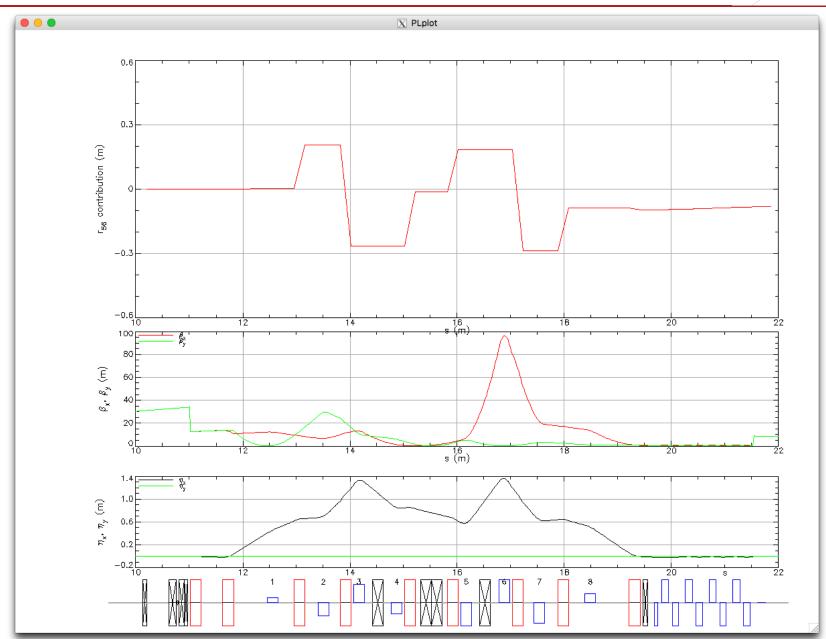
#### Splitter entrance and exit detail





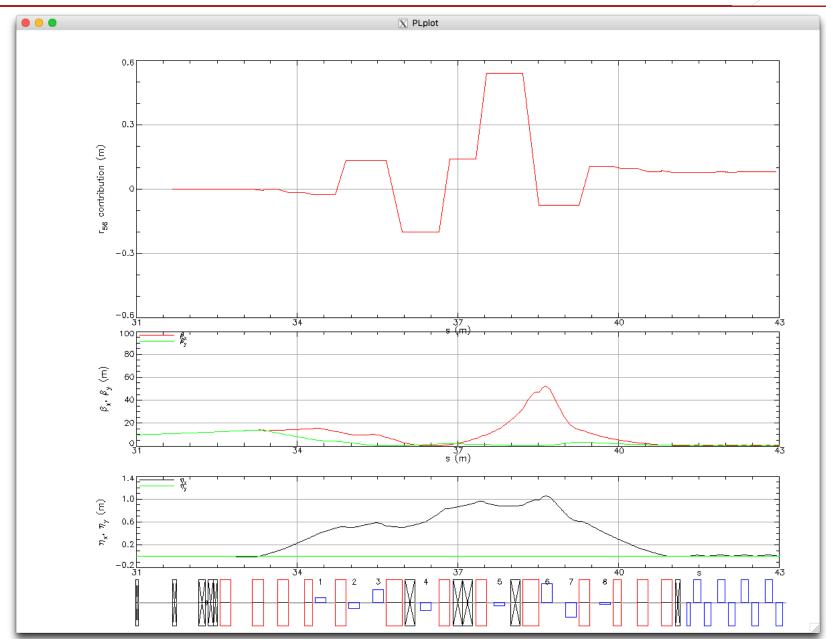
## S1 optics (42 MeV)





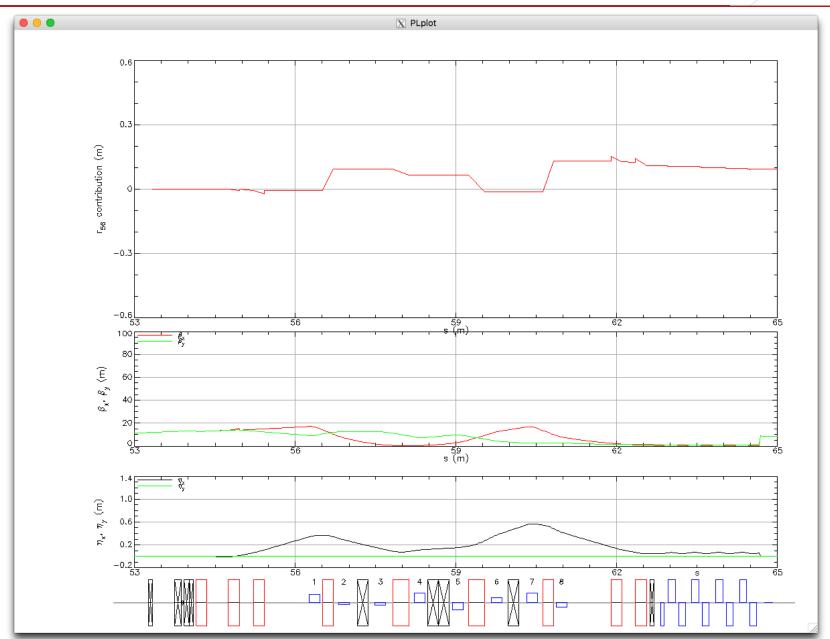
## S2 optics (78 MeV)





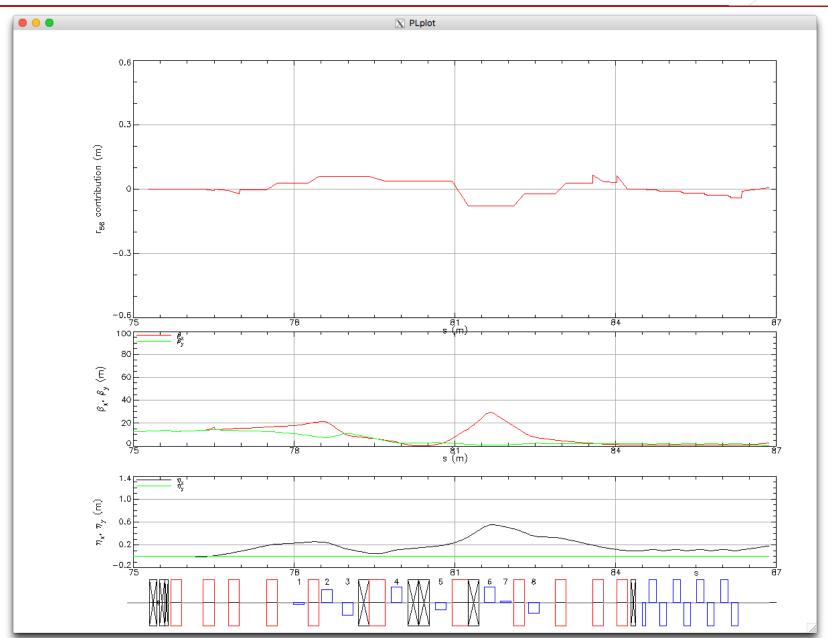
## S3 optics (114 MeV)





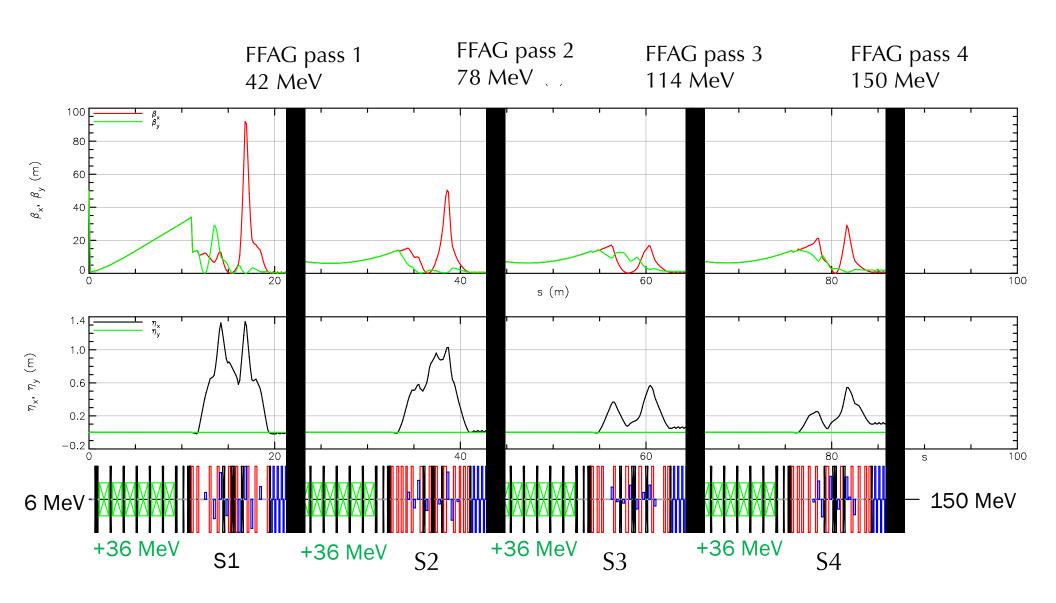
## S4 optics (150 MeV)





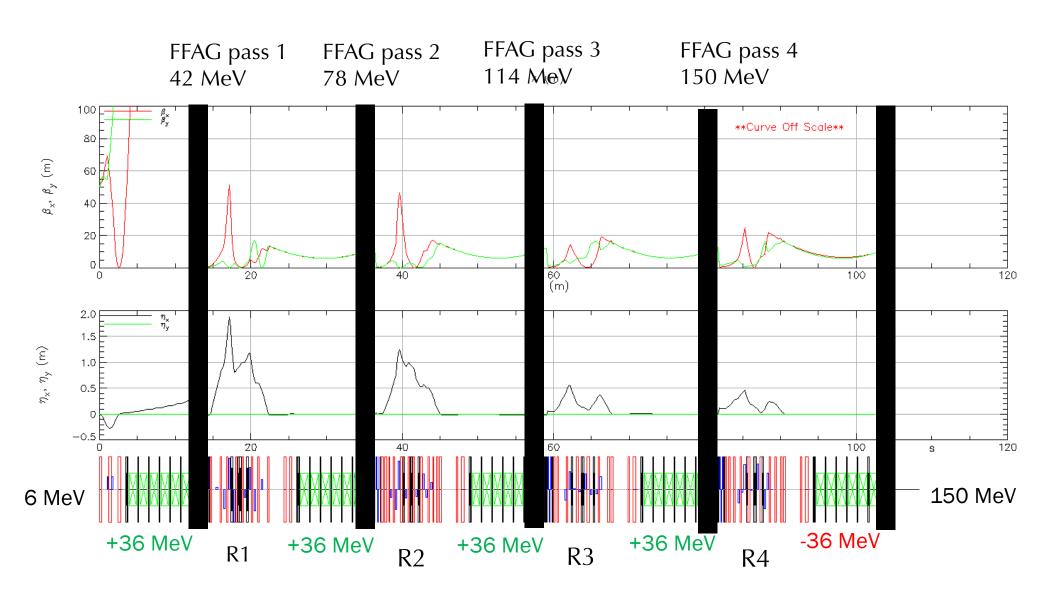
### SX optics for each pass





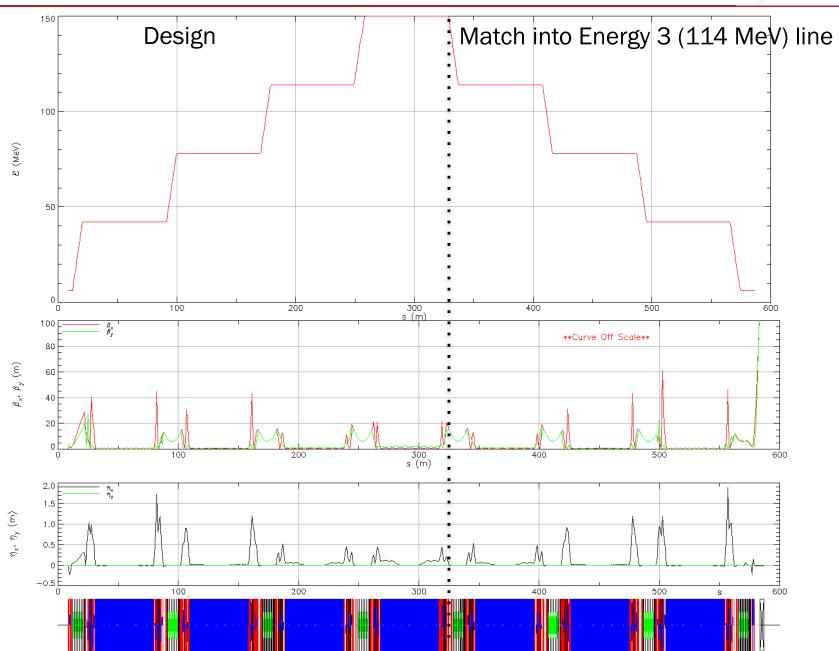
#### RX optics for each pass





## 4-pass Optics Design

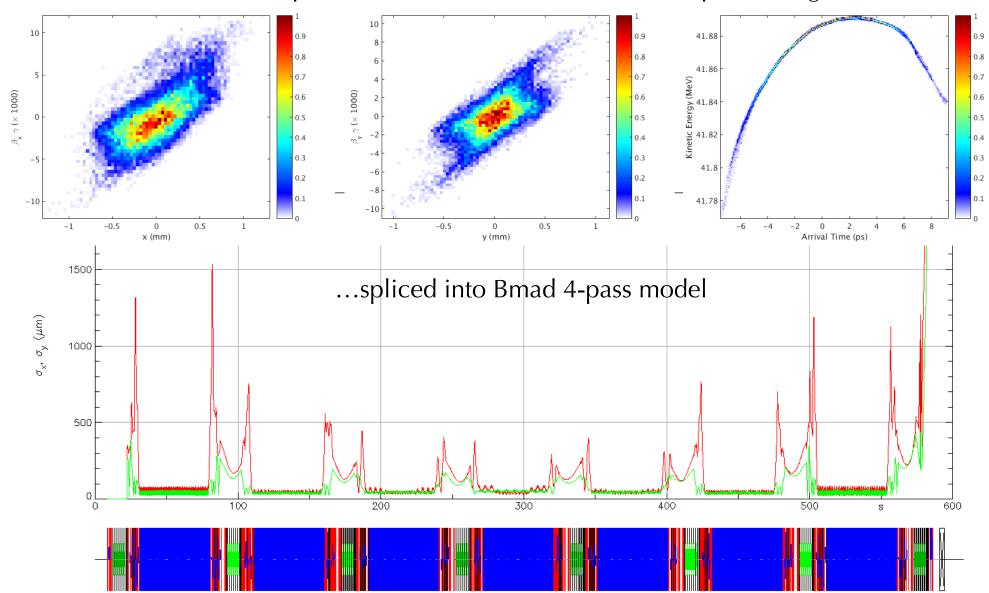




### Start-to-End tracking



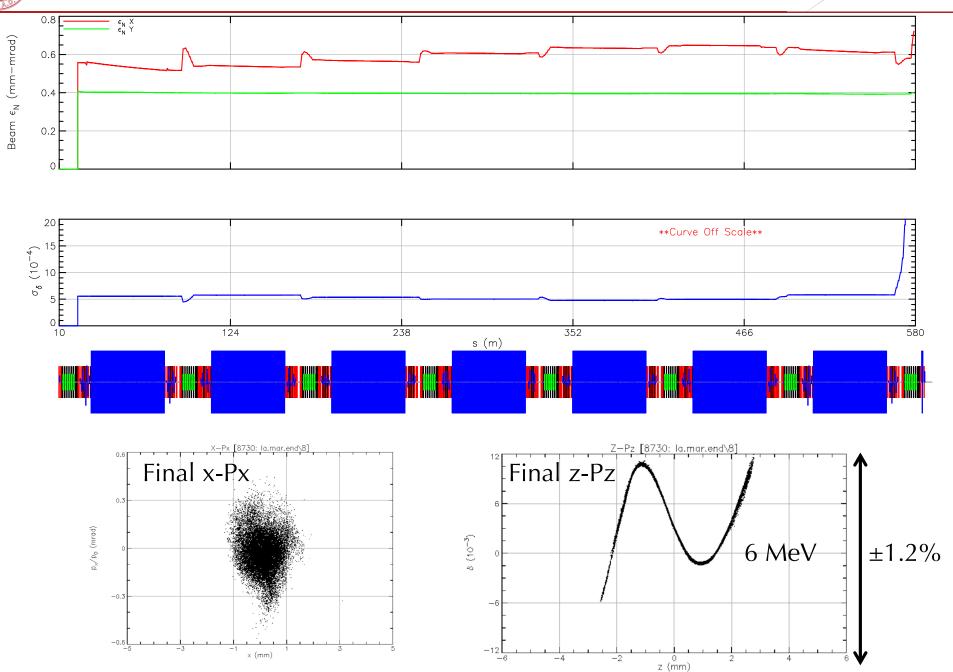
#### 100 pC bunch calculated from GPT with space charge





#### Start-to-End tracking

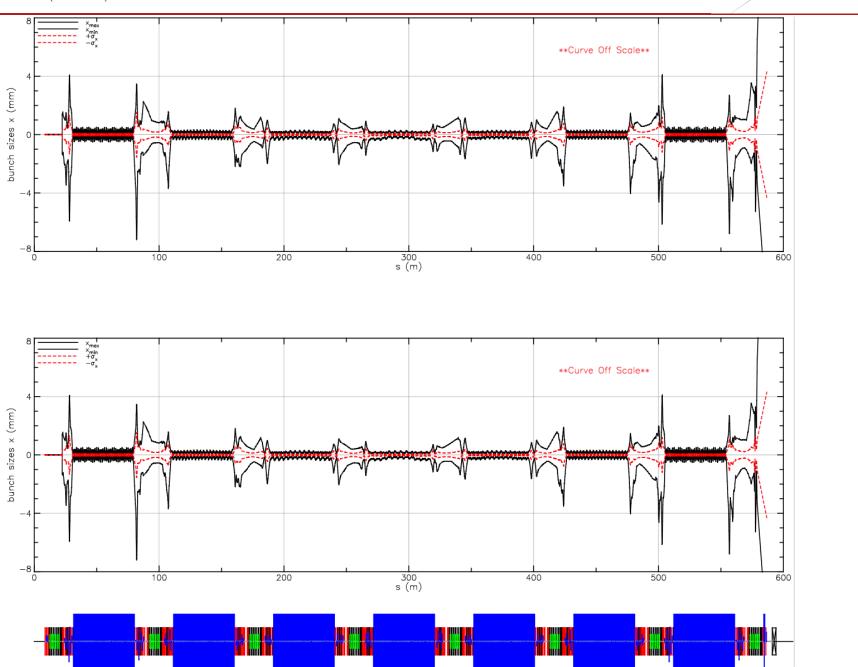






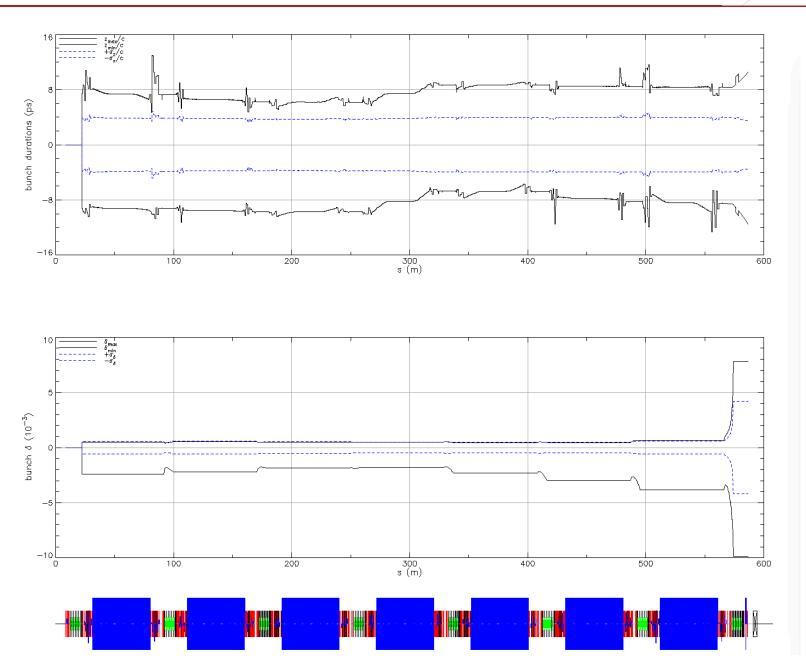
### Start-to-End tracking envelopes





## Start-to-End tracking







#### Summary



- CBETA Lattice is finalized
- FFAG designed with fieldmaps, well-modeled in Bmad for fast tracking.
- Splitters designed for:
  - possible 1,2,3,4-pass ERL configuration
  - Match orbit and linear optics into FFAG arc for each beam
  - ±10° RF phase shift adjustment via linear sliding joints.
- 4-pass start-to-end ERL tracking:
  - Negligible emittance growth
  - Well-controlled RMS and full (100%) beam envelope (both transverse and longitudinal)
  - Excellent energy at the dump ±1%



#### **END**





