

# TOWARDS BEAM-BEAM SIMULATIONS FOR FCC-EE

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Special thanks to:

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(eeFACT2022)**

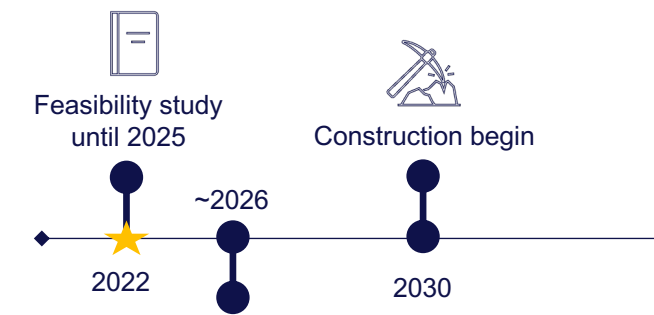
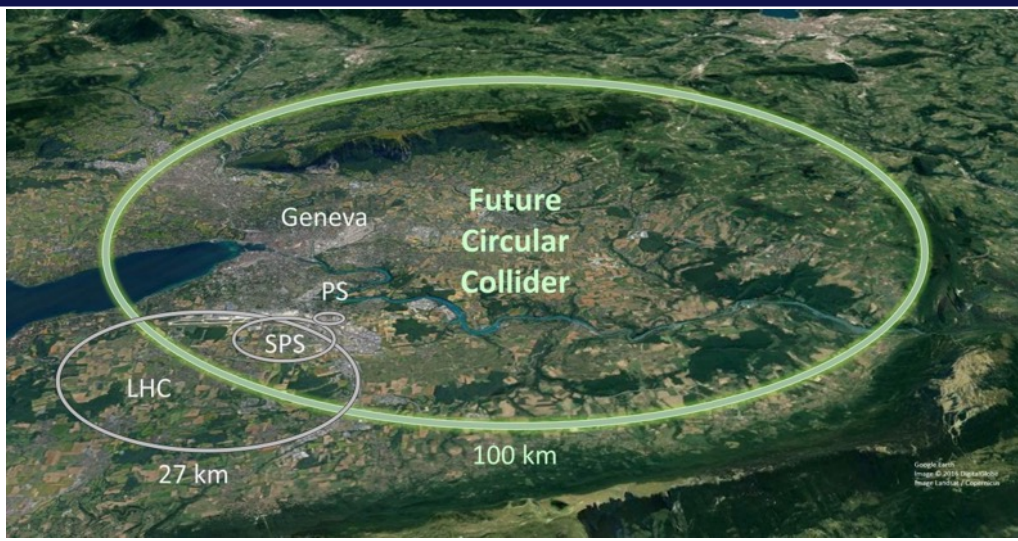
14<sup>th</sup> September 2022

# Overview

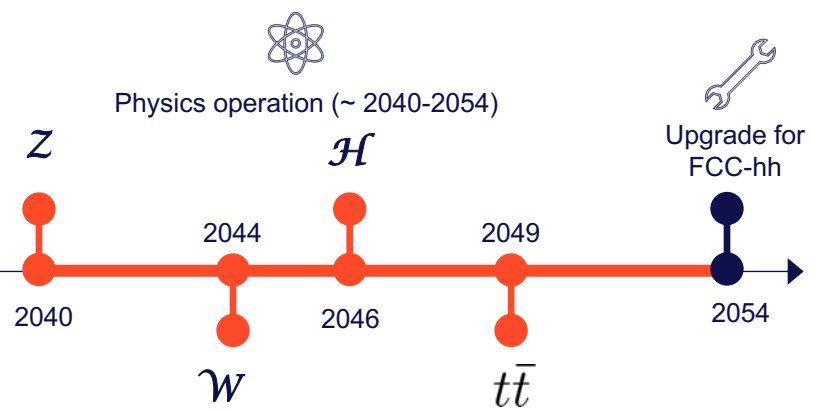
1. Introduction to FCC-ee
2. Beam-beam effects in FCC-ee
3. Overview of existing simulation tools for circular machines
4. Beam-beam models
5. First studies
6. Summary & next steps

# FCC-ee

- The FCC-ee (Future Circular Collider): currently one of the most favored next colliders at CERN
- Study properties of standard model particles with unprecedented precision, up to 350 GeV
- A first stage towards a possible 100 TeV hadron collider (FCC-hh)
- Feasibility study ongoing

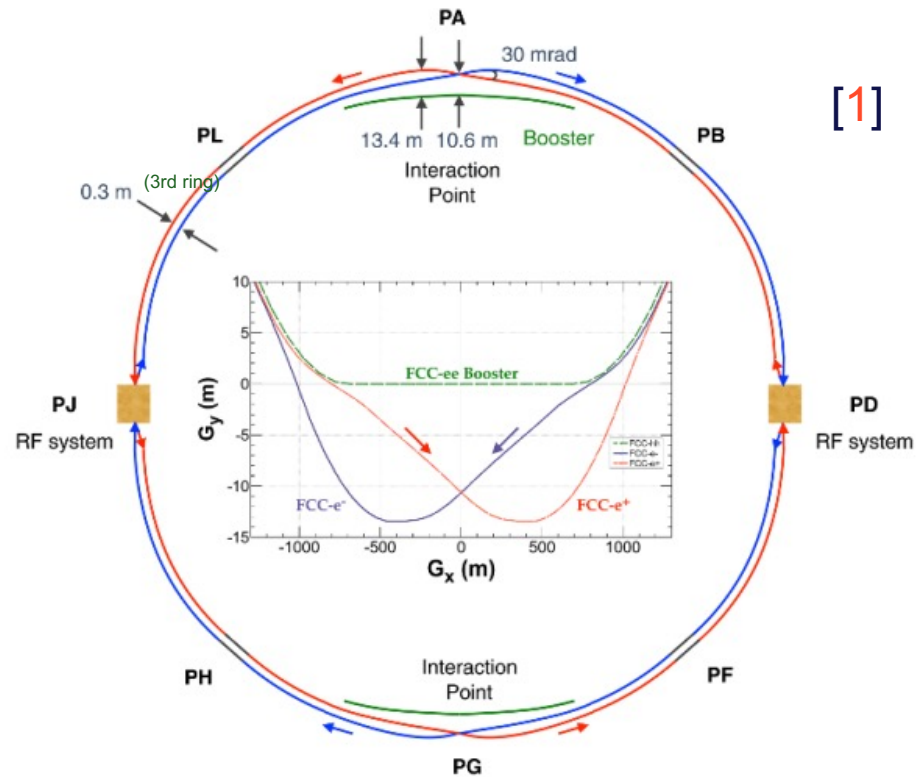


If approved: infrastructure design & preparation



# Layout

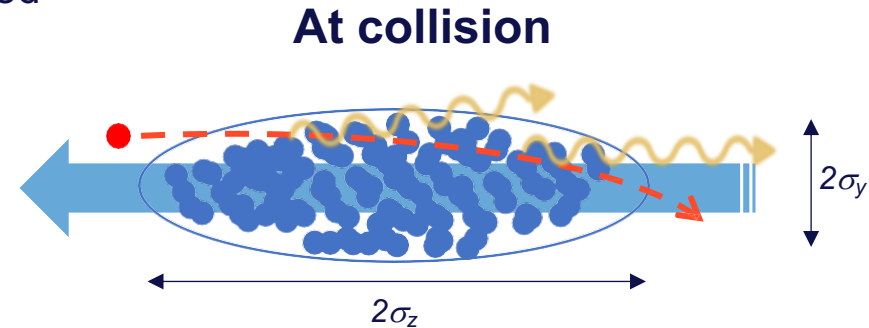
- Baseline with 2 IP
- 4 IP configuration under study
- Accelerator design aims to maximize luminosity and reduce beam-beam effects



[1]

# Beam-beam effects in FCC-ee

- Nonlinear kick
- No complete theory, simulations have to be used
- Beamstrahlung:
  - Increases bunch length ( $\sigma_z$ ) & energy spread ( $\sigma_\delta$ )
  - Decreases luminosity & beam lifetime
- Proposed setup to increase luminosity [1]:
  1. Large Piwinski angle + crab waist scheme [2]
    - Small beam size, crossing angle, crab sextupoles
- 1. Top-up injection scheme: continuous injection of new bunches
  - Maintains luminosity levels & compensates for decreased beam lifetime



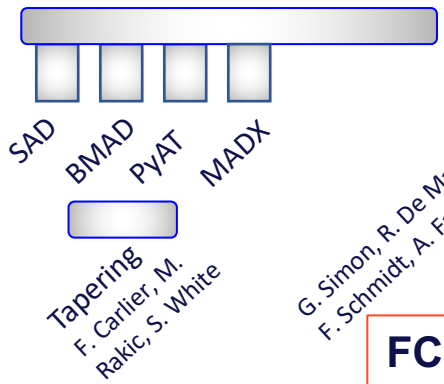
[1] <https://cds.cern.ch/record/2651299/files/CERN-ACC-2018-0057.pdf>

[2] <https://arxiv.org/pdf/1608.06150.pdf>



Swiss Accelerator Research and Technology

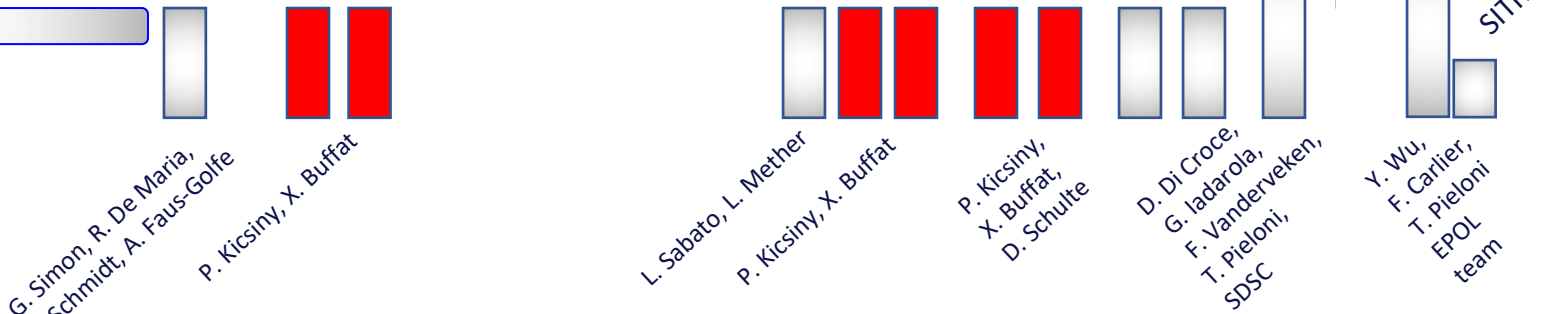
Xsequence, Xconverter (F. Carlier)



	Full lattice description	Dynamic effects (trims, noise)	Beam beam 4d (weak strong)	Beam beam 6d (weak strong)	e-cloud incoherent	Space charge frozen	Advanced collimation features	Impedances	Transverse feedbacks	Space charge PIC	e-cloud self-consistent	Beam beam 4d (strong strong)	Beam beam 6d (strong strong)	Synchrotron radiation	Beamsstrahlung	Available on BOINC	Runs on GPU
MAD-X track	Green	Green	Green	Red	Red	Green	Red	Red	Red	Red	Red	Red	Red	Green	Red	Red	Red
Sixtrack	Green	Green	Green	Green	Green	Green	Red	Red	Red	Red	Red	Red	Red	Red	Red	Green	Red
Sixtracklib	Green	Red	Green	Green	Green	Green	Red	Red	Yellow	Red	Red	Red	Red	Red	Red	Green	Red
PyHEADTAIL	Red	Green	Green	Red	Green	Green	Red	Red	Green	Red	Red	Red	Red	Green	Red	Red	Yellow
COMBI	Red	Green	Green	Green	Red	Green	Red	Red	Green	Green	Green	Green	Green	Green	Red	Red	Red
Xsuite	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green	Green

[1,2]

ML for DA optimization

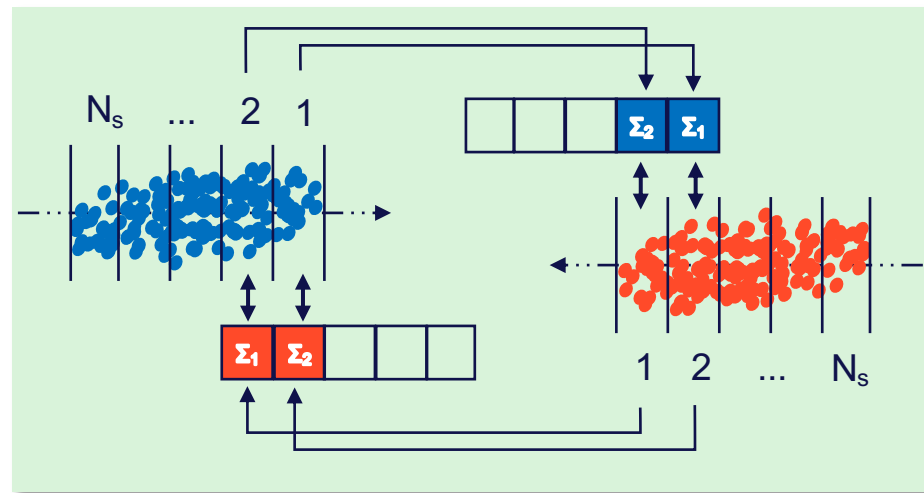


**FCC-ee high complexity: need to simulate interplay of different effects**

[1] G. Iadarola [https://indico.cern.ch/event/1066779/contributions/4485729/attachments/2301867/3915592/019\\_Xsuite.pdf](https://indico.cern.ch/event/1066779/contributions/4485729/attachments/2301867/3915592/019_Xsuite.pdf)  
 [2] T. Pieloni <https://indico.cern.ch/event/1064327/contributions/4893328/attachments/2454297/4206242/FCC%20Software%20framework%20developments.pdf>

# Beam-beam models

- $\sim 10^4$ - $10^7$  particles per bunch
- Longitudinal slicing (simplecticity)
- Interaction of slice pairs
  - Compute kick using slice moments ( $\Sigma$ )
  - Update dynamical variables



multi-turn effects

low disruption parameter

high disruption parameter

single particle effects

slow instabilities

fast instabilities, wakefields

**fastest & least accurate**

**slowest & most accurate**

**never**

**periodically**

**after each slice-slice**

weak-strong [WS]

quasi strong-strong [QSS]

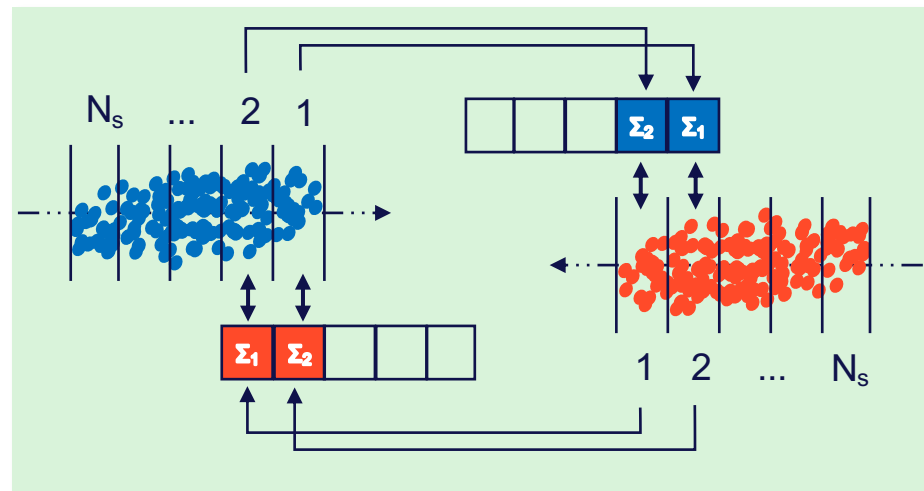
**interaction**

**Frequency of recomputing slice moments**

strong-strong [SS]

# Beam-beam models

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  - Update dynamical variables

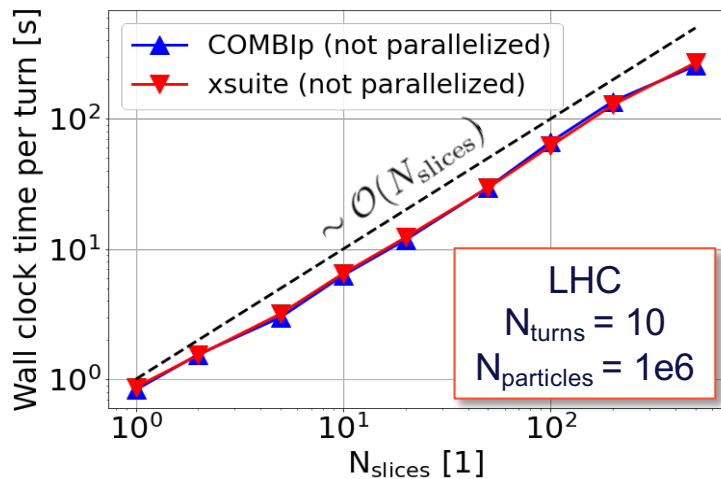


## In xsuite:

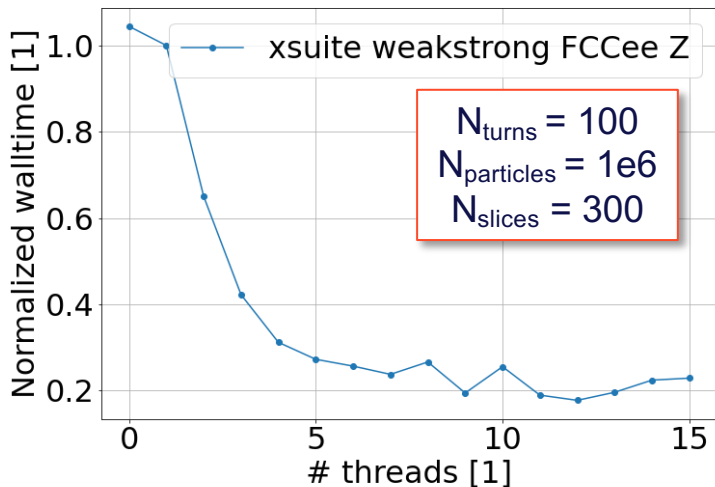
- Core algorithm: single slice-slice interaction
- Flexible choice of model
- Force: soft-Gaussian kick by Bassetti-Erskine formula [1] (field solvers to be tested in future)
- Extendible: e.g. Beamstrahlung, Bhabha scattering

[1] <https://cds.cern.ch/record/122227/files/198005132.pdf>





- Benchmark of computation time for beam-beam (**strong-strong**) + linear tracking against reference code COMBIp [1]
- Time per turn scales approximately with the number of longitudinal slices



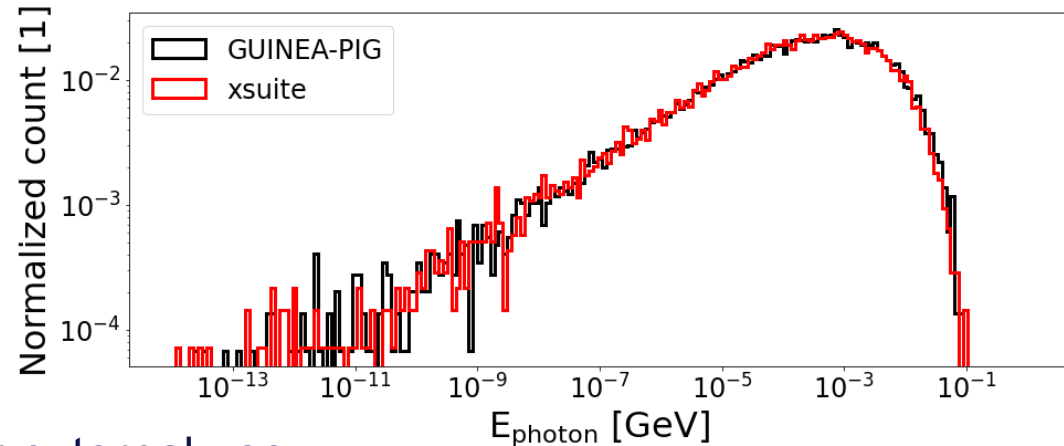
- Multithreading:  $\sim x5$  speedup
- GPU acceleration is available in xsuite
  - To be tested
  - Will be needed for full scale simulations

# Beamstrahlung benchmark

- Benchmark against reference code GUINEA-PIG [1]

- FCC-ee flat beams
- Crossing angle:  $15\text{e-}3$  [rad]
- Beamstrahlung model OK
- xsuite: **weak-strong**
- GUINEA-PIG: **strong-strong**

## Beamstrahlung photon spectrum / coll.



- Possibility to generate photons for external use (collimation, MDI) [2]

- **TODO:** come up with an efficient model of Bhabha scattering

[1] <https://twiki.cern.ch/twiki/bin/view/ABPCComputing/Guinea-Pig>

[2] [https://xsuite.readthedocs.io/en/latest/internal\\_record.html#internal-record-for-elements-used-in-standalone-mode](https://xsuite.readthedocs.io/en/latest/internal_record.html#internal-record-for-elements-used-in-standalone-mode)

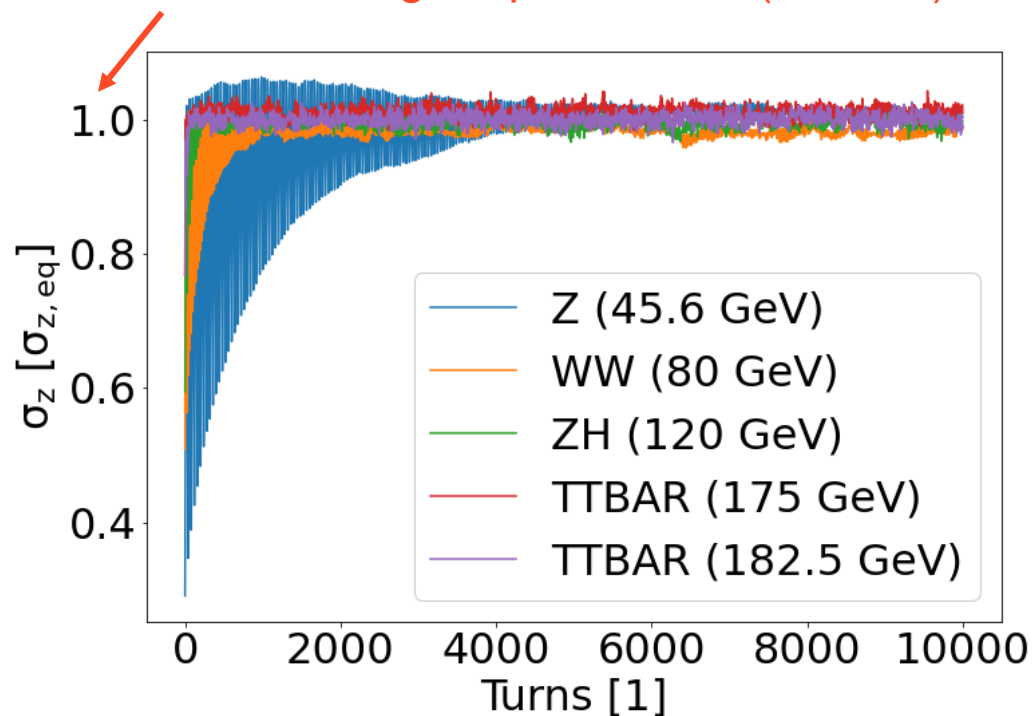
# Simplified tracking simulations with xsuite

- Exploit superperiodicity of machine (2 IP case)
- In code:
  - 1 IP + tracking over half arc with linear transfer matrix
  - Arc split into 3 segments
  - 2 crab sextupoles between arc segments
  - A «turn» begins in front of the right sextupole:
    - Observation point for emittances (by stat. definition from normalized coordinates)
    - Observation point for raw coordinates is before IP
  - Effective radiation (damping+noise) in arc, beamstrahlung in beam-beam



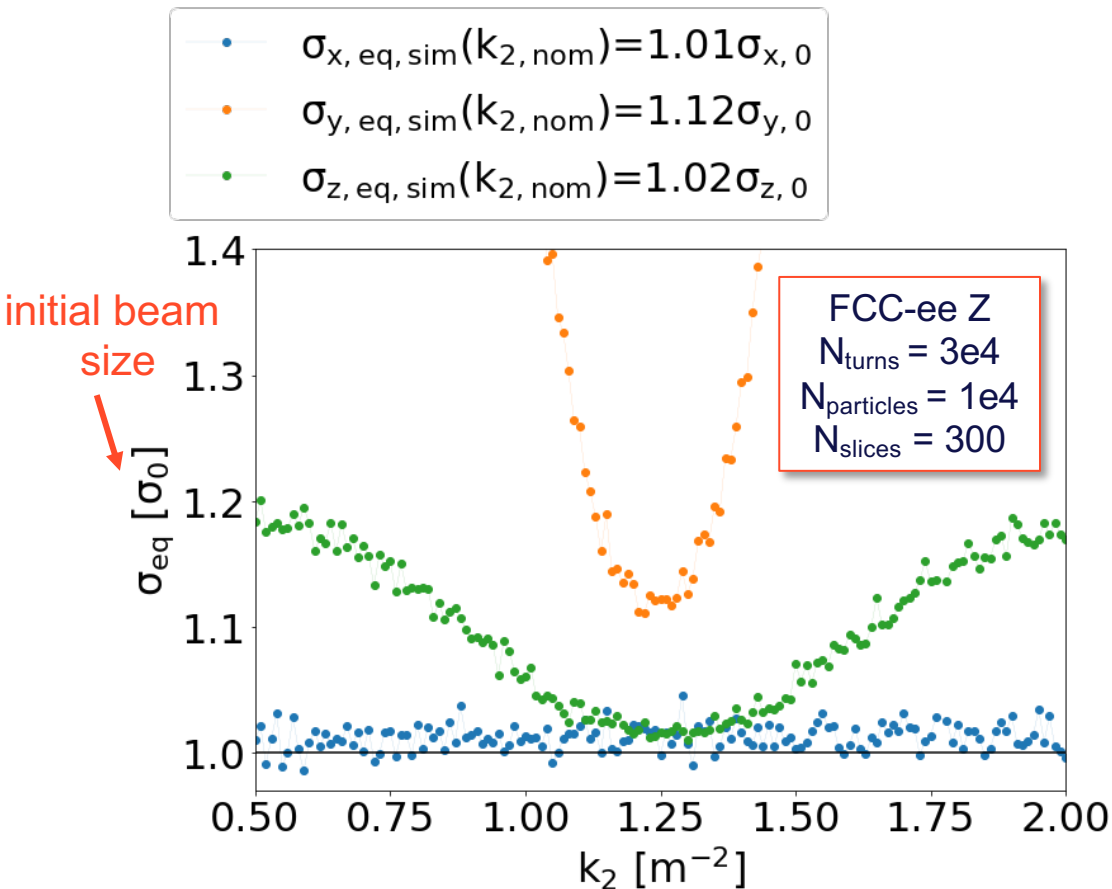
# Equilibrium bunch length

normalized to design report values (SR+BS)



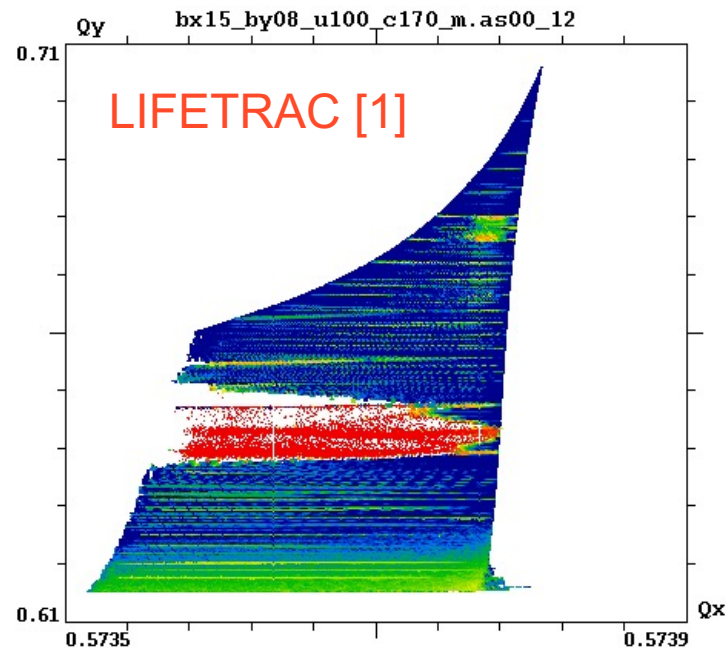
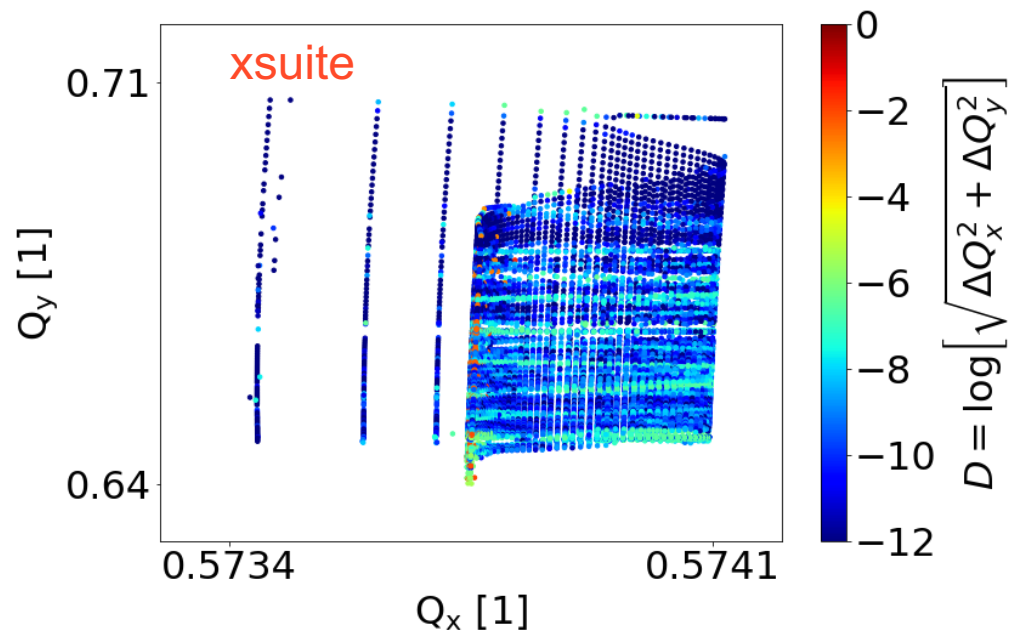
- **Weak-strong** model (1e4 particles)
- Equilibrium bunch length agrees with design report value for all resonances

# Crab waist & transverse blowup



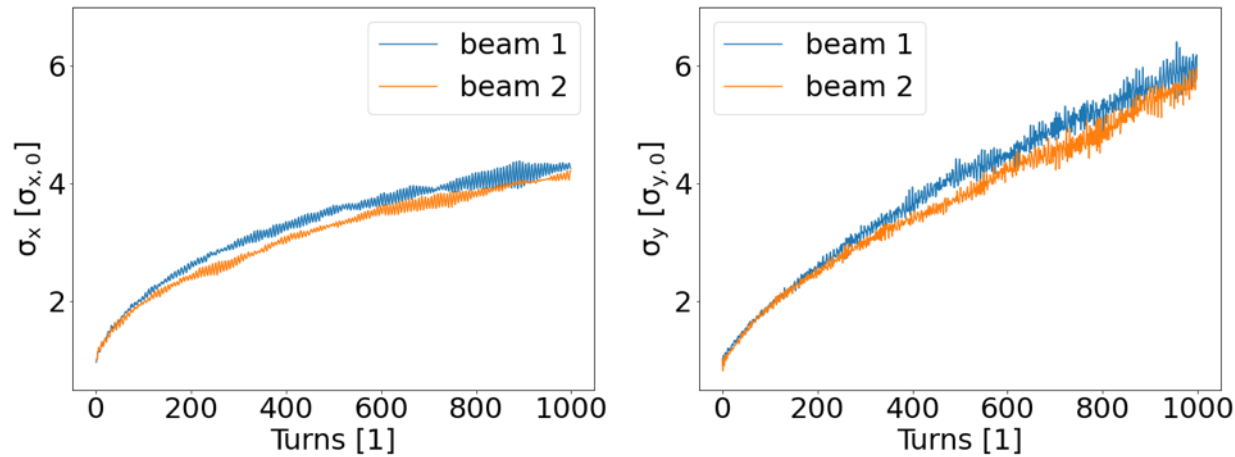
- **Weak-strong** model
- Optimum  $k_2$  close to nominal value ( $\sim 0.97 \cdot k_{2, nom}$  for Z resonance)
- $\sim 10\%$  blowup of vertical beam size (stat. errors  $\sim 1\%$ )
- Not observed in other codes
- Investigation in progress

# Understanding transverse blowup & benchmarking



- FCCee Z tune footprint
- Differences to be understood

# Strong-strong simulations



FCC-ee Z  
 $N_{\text{turns}} = 3e4$   
 $N_{\text{particles}} = 1e4$   
 $N_{\text{slices}} = 300$

- Fast blowup in x and y size (not observed in other codes)
- Coherent beam-beam instability? [1]
- Investigation in progress

# Summary

*Work so far: xsuite code development & benchmarks for FCC-ee*

- Flexible beam-beam models (weak-strong, quasi strong-strong, strong-strong)
- Beamstrahlung: photon generation available
- Weak-strong benchmarks (understanding vertical blowup, FMA benchmark)
- Strong-strong benchmarks (understanding blowup, reproduce coherent instability)

*Work ongoing*

- Bhabha scattering
- 3D flip-flop
- Top-up injection

*Other xsuite features targeted*

- Impact of lattice imperfections
- Interplay with real lattice model
- Multiple IPs
- Monochromation
- Wakefields

## Thank you!

This work was performed under the auspices and with support from the Swiss Accelerator Research and Technology (CHART) program ([www.chart.ch](http://www.chart.ch)).