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The magnetic field analysis of CS-30

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Cyclotrons 2022

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contents

- 01** Backgrounds
- 02** Progress and details
- 03** Conclusion



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01

Backgrounds

Status of CS-30 in SCU



From: 2003

Particles: P, α

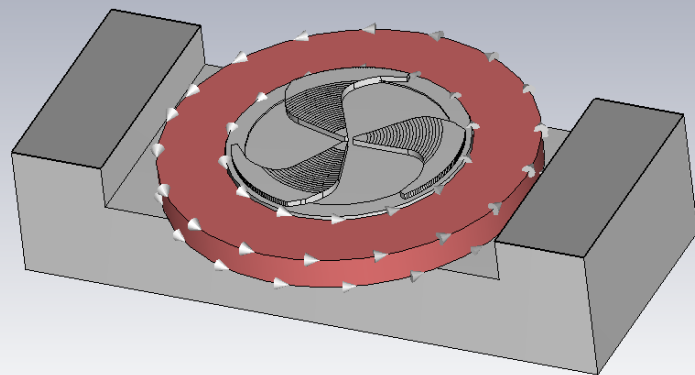
Operation time: 800h

Status: Production of isotopes
Study on irradiation effect of materials
Teaching demonstration device

Purpose: extraction!



Status of CS-30 in SCU



Particle	Energy (MeV)	Current intensity (uA)		Divergence (fwhm)	Emittance of the outer beam (mm-mrad)
		Internal beam	Outer beam		
P	26	200	60	<1%	<50
d	15	300	100	<1%	<50

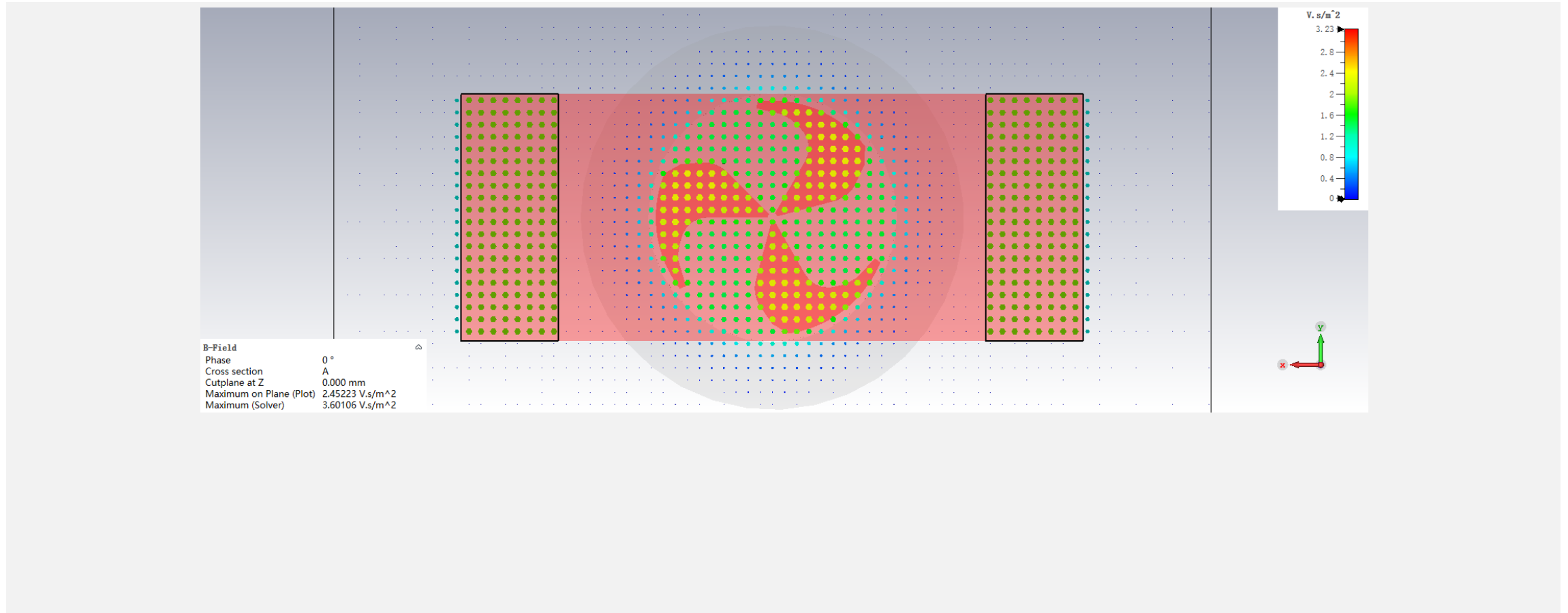


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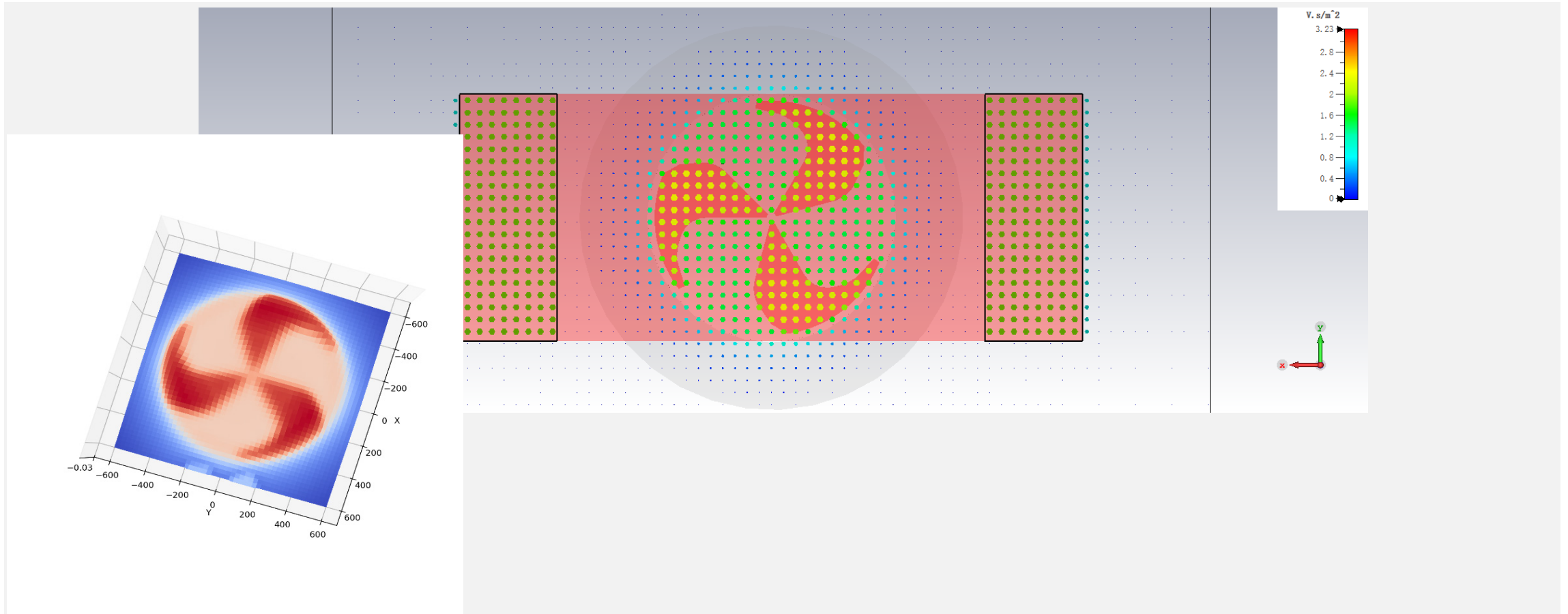
02

Progress and Details

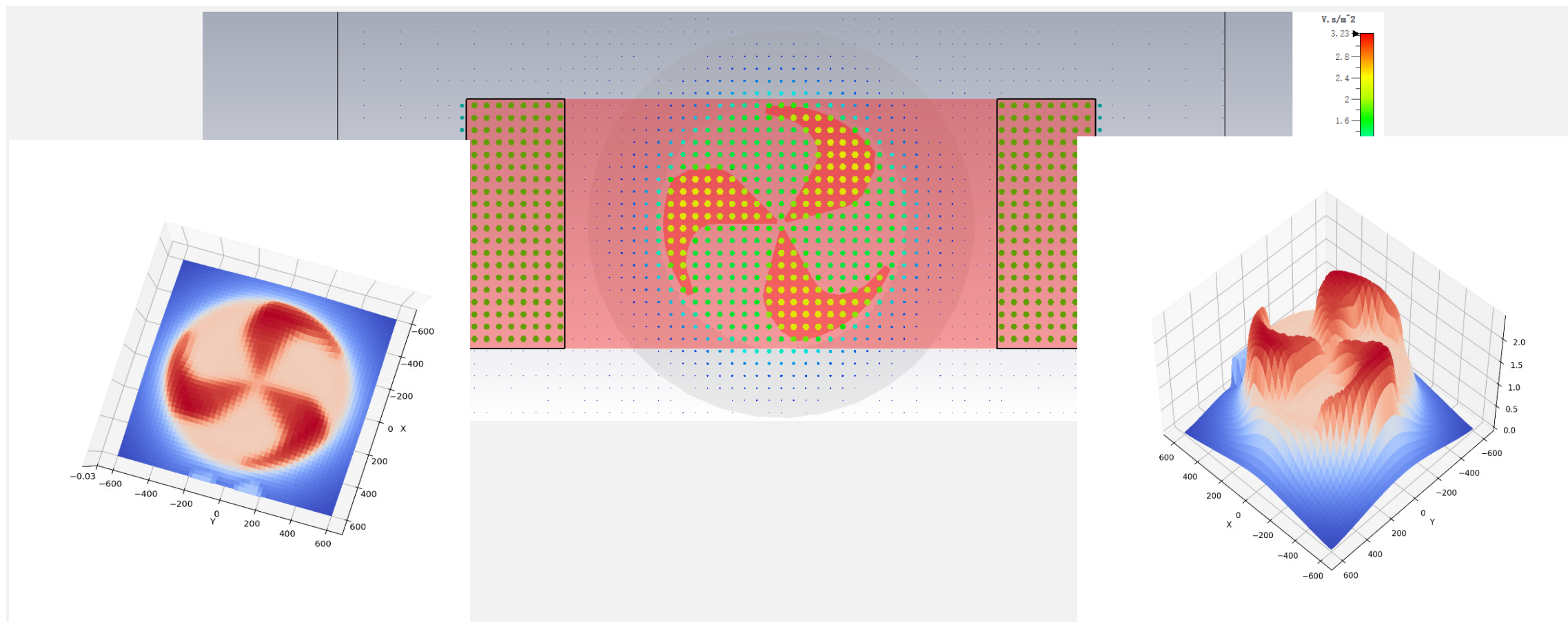
Magnetic field calculation



Magnetic field calculation



Magnetic field calculation



Magnetic field analysis



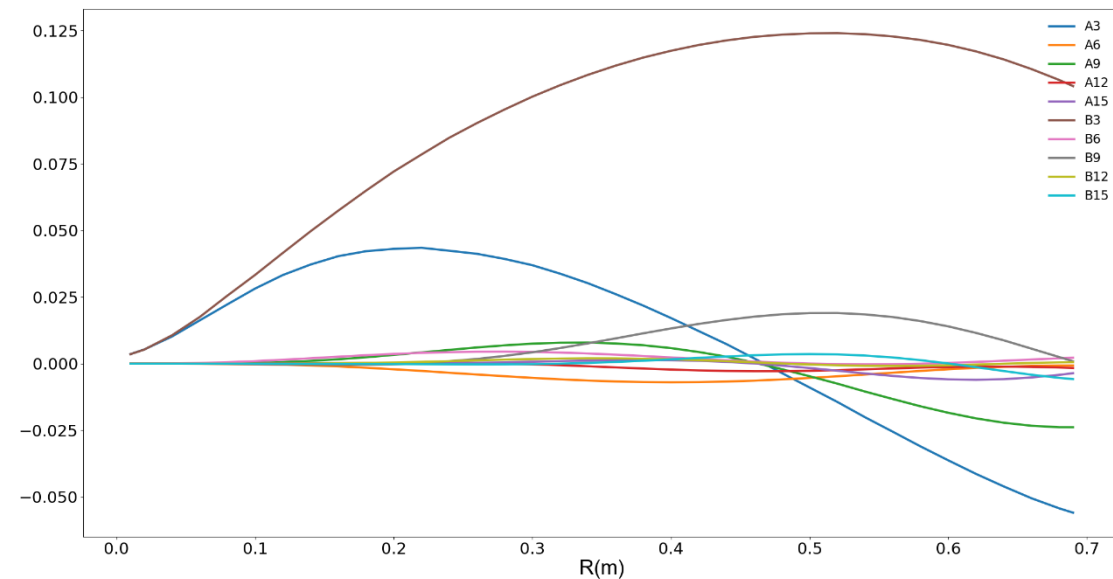
The central plane of the synchrotron:

$$B(r, \theta) = \bar{B}(r)[1 + F(r, \theta)]$$

Fourier expansion:

$$F(r, \theta) = \sum_n A_n(r) \cos n\theta + B_n(r) \sin n\theta$$

introduce $x = \frac{r-r_0}{r_0}$, $u(x, \theta) = B(r, \theta) / \bar{B}(r_0)$



Magnetic field analysis



$$\begin{aligned} u(x, \theta) &= \left(1 + \bar{\mu}'x + \frac{1}{2}\bar{u}''x^2 + \frac{1}{6}\bar{\mu}'''x^3 + \dots \right) \\ &+ \sum_n \left(A_n + A'_n x + \frac{1}{2}A_n''x^2 + \dots \right) \cos n\theta + \sum_n \left(B_n + B'_n x + \frac{1}{2}B_n''x^2 + \dots \right) \sin n\theta \end{aligned}$$

$$\begin{aligned} A_n &= A_n(r_0), A'_n = \left[\frac{r dA_n(r)}{dr} \right]_{r=r_0}, A''_n = \left[\frac{r^2 d^2 A_n(r)}{dr^2} \right] \\ B_n &= A_n(r_0), B'_n = \left[\frac{r dB_n(r)}{dr} \right]_{r=r_0}, B''_n = \left[\frac{r^2 d^2 B_n(r)}{dr^2} \right] \end{aligned}$$

Magnetic field analysis



Equation of motion:

$$\begin{aligned}\frac{dr}{d\theta} &= r \frac{p_r}{q} \\ \frac{dp_r}{d\theta} &= q - \frac{Ze}{p} r B_z \\ p &= mv \\ q &= \sqrt{1 - p_r^2}\end{aligned}$$

The Hamiltonian function

$$H = -r(1 - p_r^2)^{\frac{1}{2}} + \frac{Ze}{p} \int^r r B_z dr$$

introduce $x = \frac{r-r_0}{r_0}$, $u(x, \theta) = B(r, \theta)/\bar{B}(r_0)$

And let the momentum of the particle
 $p_\theta = Ze r_0 \bar{B}(r_0)$

New Hamiltonian function could be

$$H = -(1+x)(1 - p_r^2)^{\frac{1}{2}} + \int (1+x) \mu(x, \theta) dx$$

p_x is the regular conjugate of x

Equilibrium orbits



static equilibrium orbits:

$$r_e = r_0(1 + x_e)$$

Fourier expansion:

$$x_e = \gamma + \sum_n \alpha_n \cos n\theta + \beta_n \sin n\theta$$

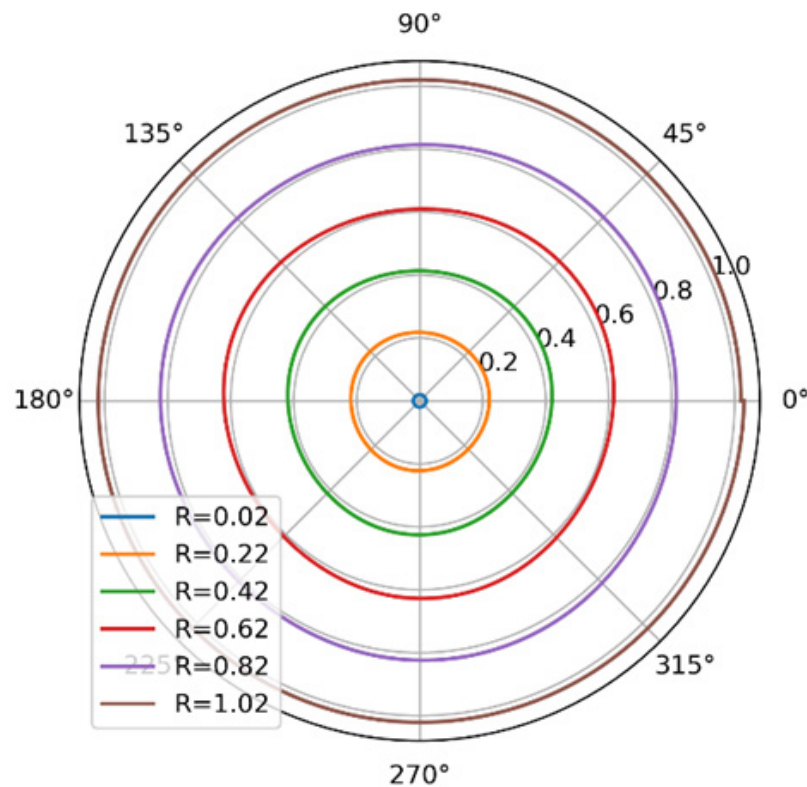


$$x_e = \gamma + \sum_n \frac{A_n}{n^2 + 1} \cos n\theta + \frac{B_n}{n^2 + 1} \sin n\theta$$

$$\gamma = - \sum_n \frac{3n^2 - 2}{4(n^2 - 1)^2} (A_n^2 + B_n^2) + \frac{1}{2(n^2 - 1)^2} (A_n A'_n + B_n B'_n)$$

★
$$r_e = r_0 \left(1 + \gamma + \sum_n \frac{A_n}{n^2 + 1} \cos n\theta + \frac{B_n}{n^2 + 1} \sin n\theta \right)$$

Equilibrium orbits

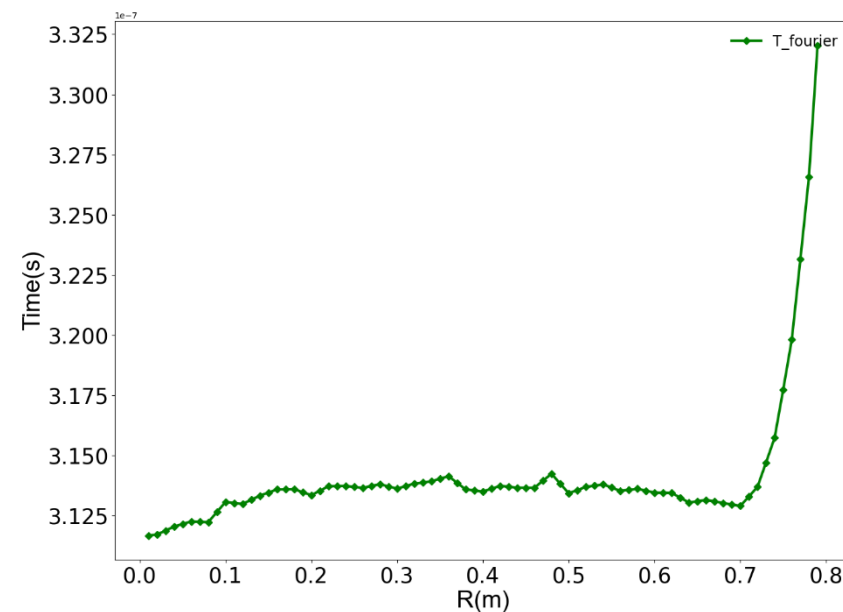
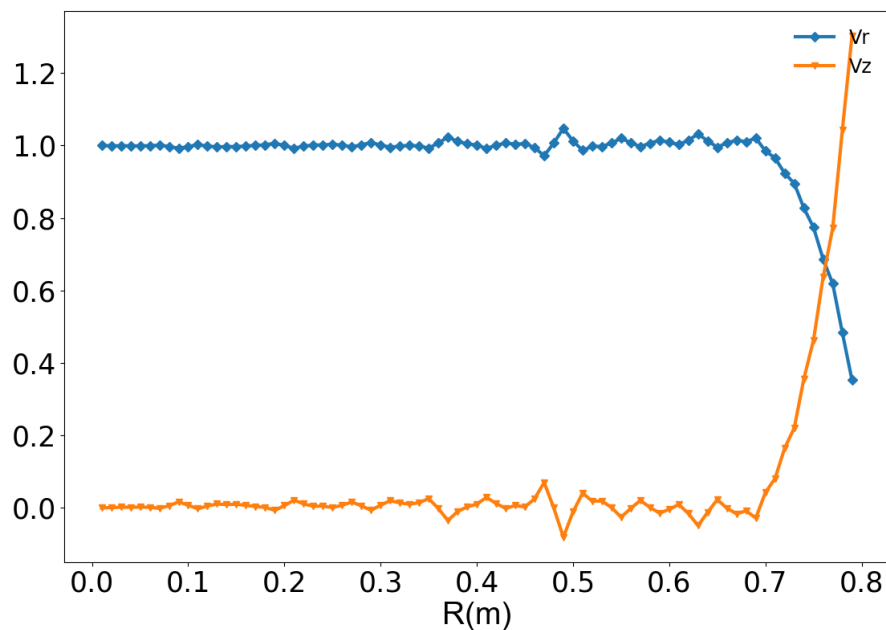


Equilibrium orbits



Radial oscillation frequency:
$$v_r^2 = 1 + \frac{1}{2}\bar{u}' + \sum_n \frac{3n^2}{4(n^2 - 1)(n^2 - 4)} (A_n^2 + B_n^2)$$

Axial oscillation frequency:
$$v_z^2 = -\bar{u}' + \sum_n \frac{n^2}{2(n^2 - 1)} (A_n^2 + B_n^2)$$

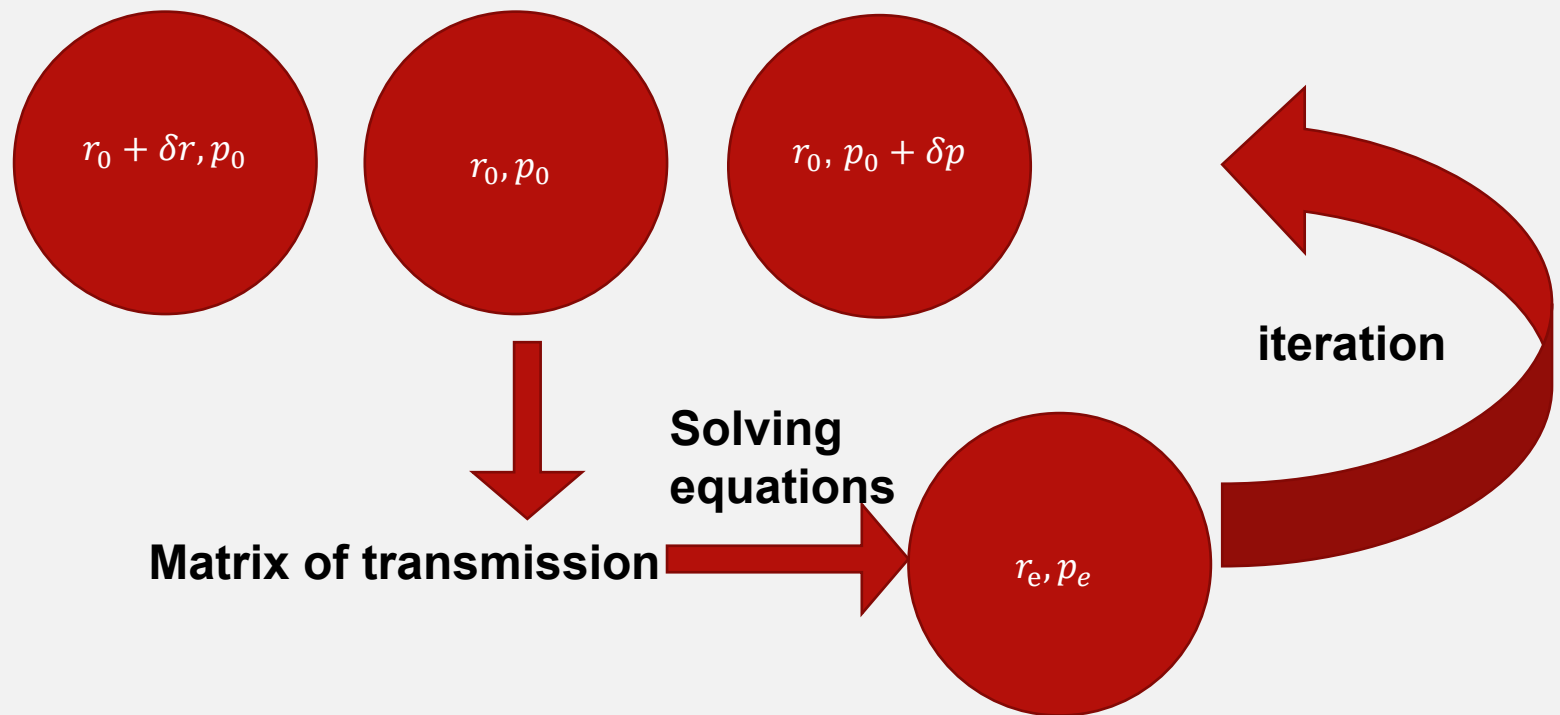


Equilibrium orbits

Equation of motion:

$$\begin{aligned}\frac{dr}{d\theta} &= r \frac{p_r}{q} \\ \frac{dp_r}{d\theta} &= q - \frac{Ze}{p} r B_z \\ p &= mv \\ q &= \sqrt{1 - p_r^2}\end{aligned}$$

Matrix method:

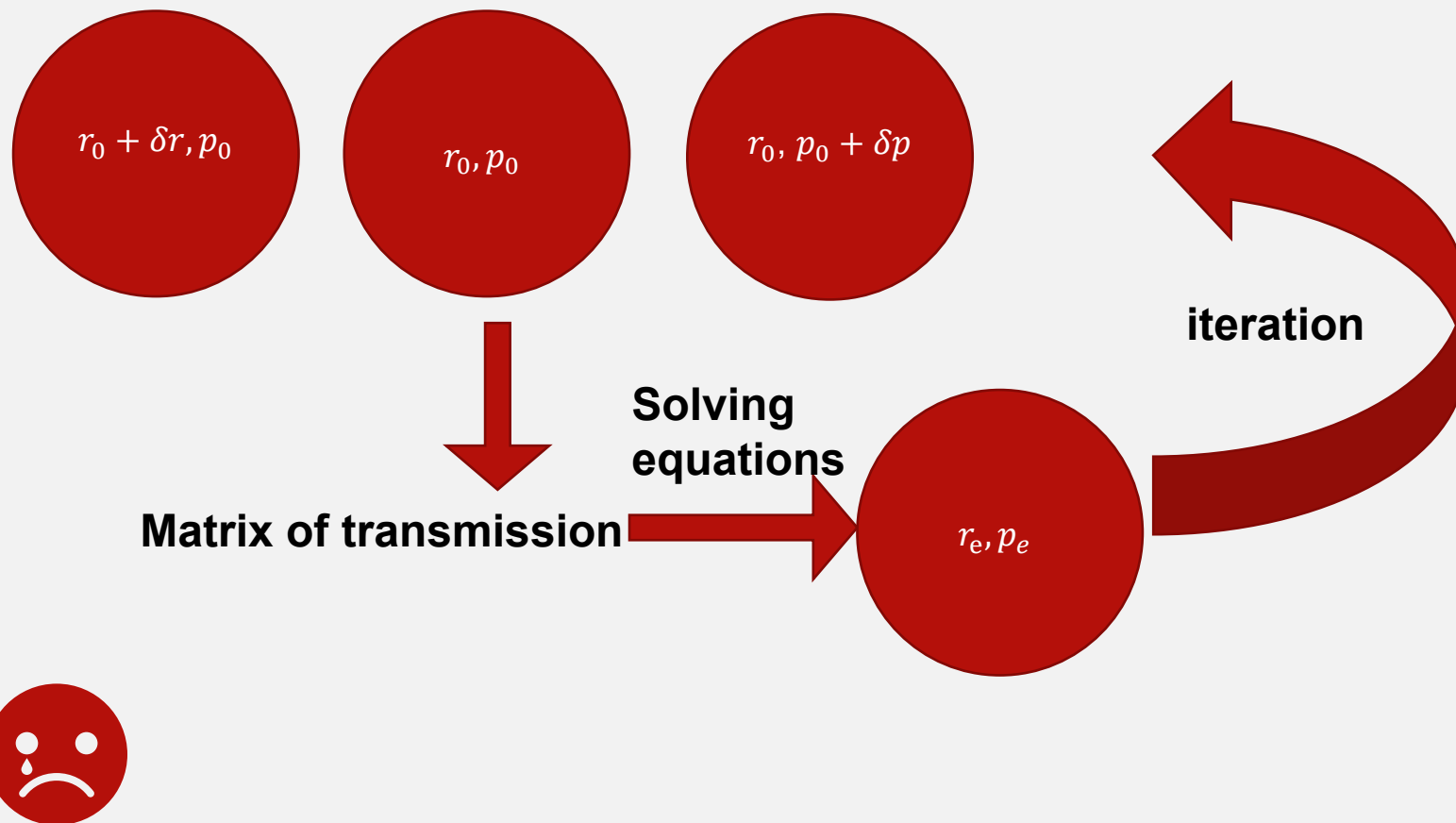


Equilibrium orbits

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Matrix method:

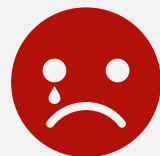
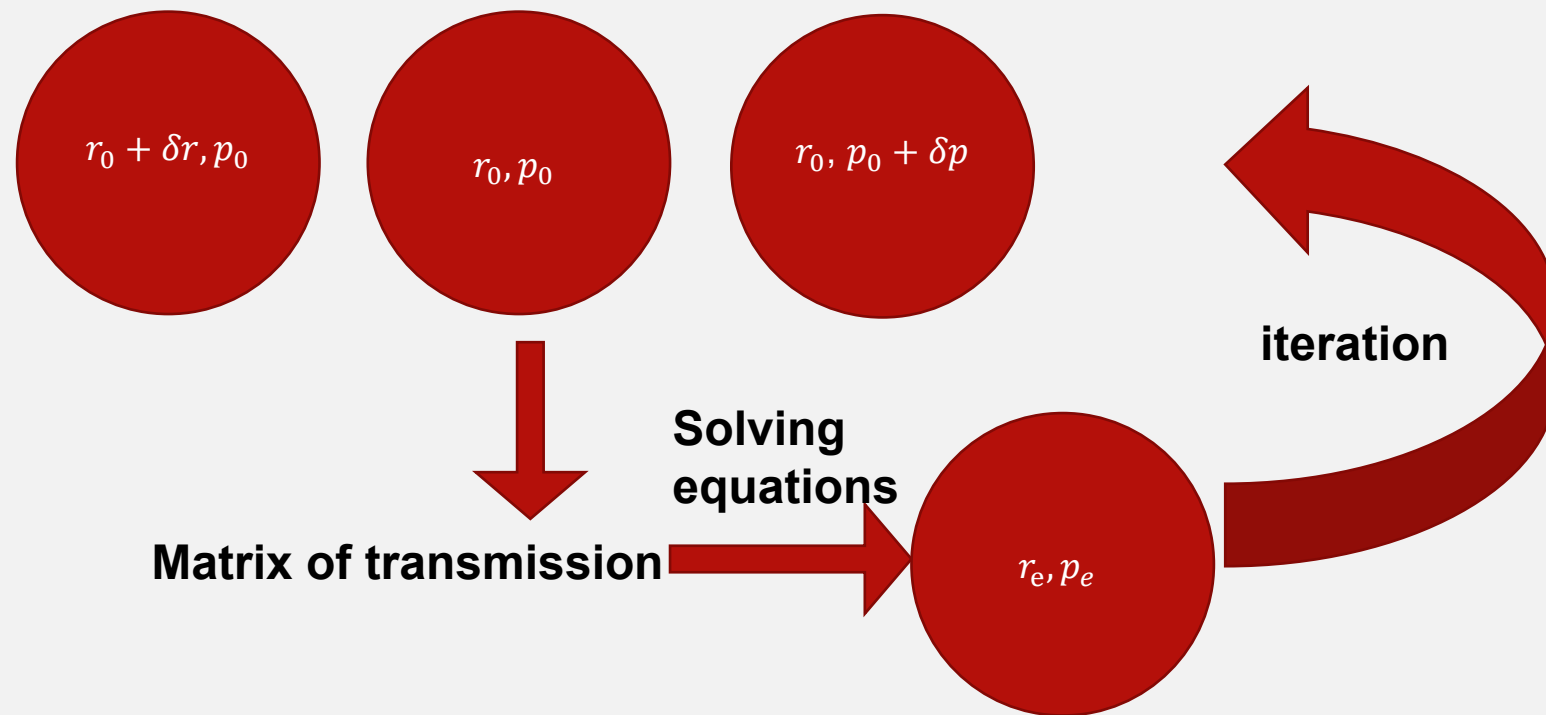


Equilibrium orbits

Equation of motion:

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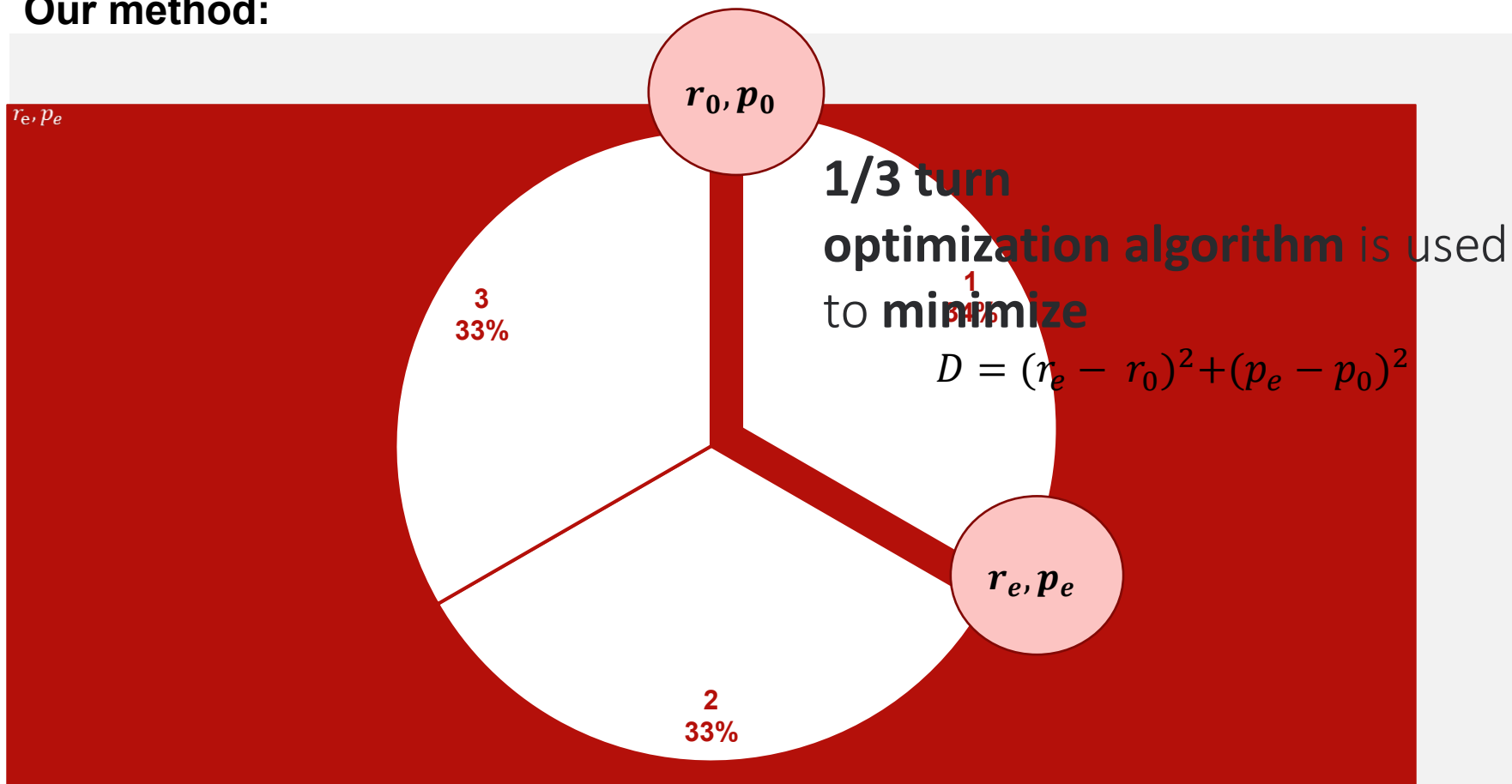
Matrix method:



Strict requirements for initial values

Equilibrium orbits

Our method:



$$\frac{dr}{d\theta} = r \frac{p_r}{q}$$
$$\frac{dp_r}{d\theta} = q - \frac{Ze}{p} r B_z$$
$$p = mv$$
$$q = \sqrt{1 - p_r^2}$$

Equilibrium orbits



Why 1/3?

$B/\bar{B}_0$

$B/\bar{B}_0$

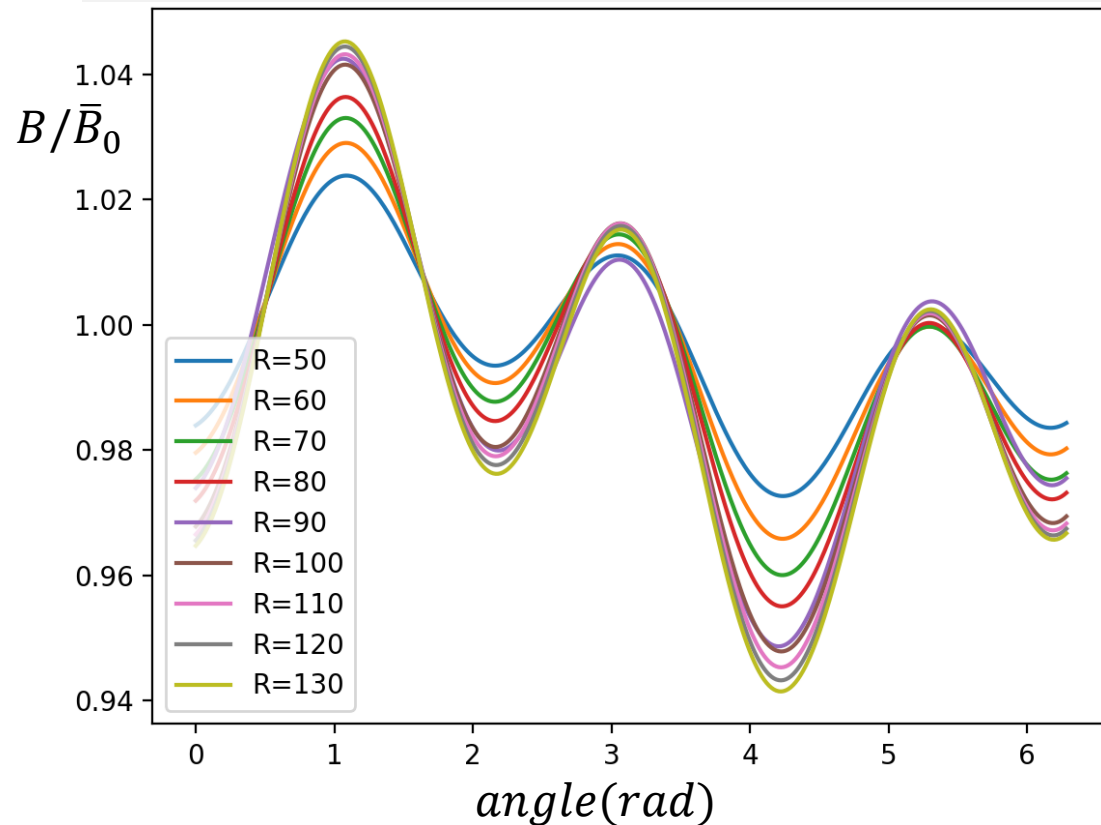
$angle(rad)$

$angle(rad)$

Equilibrium orbits



Why 1/3?



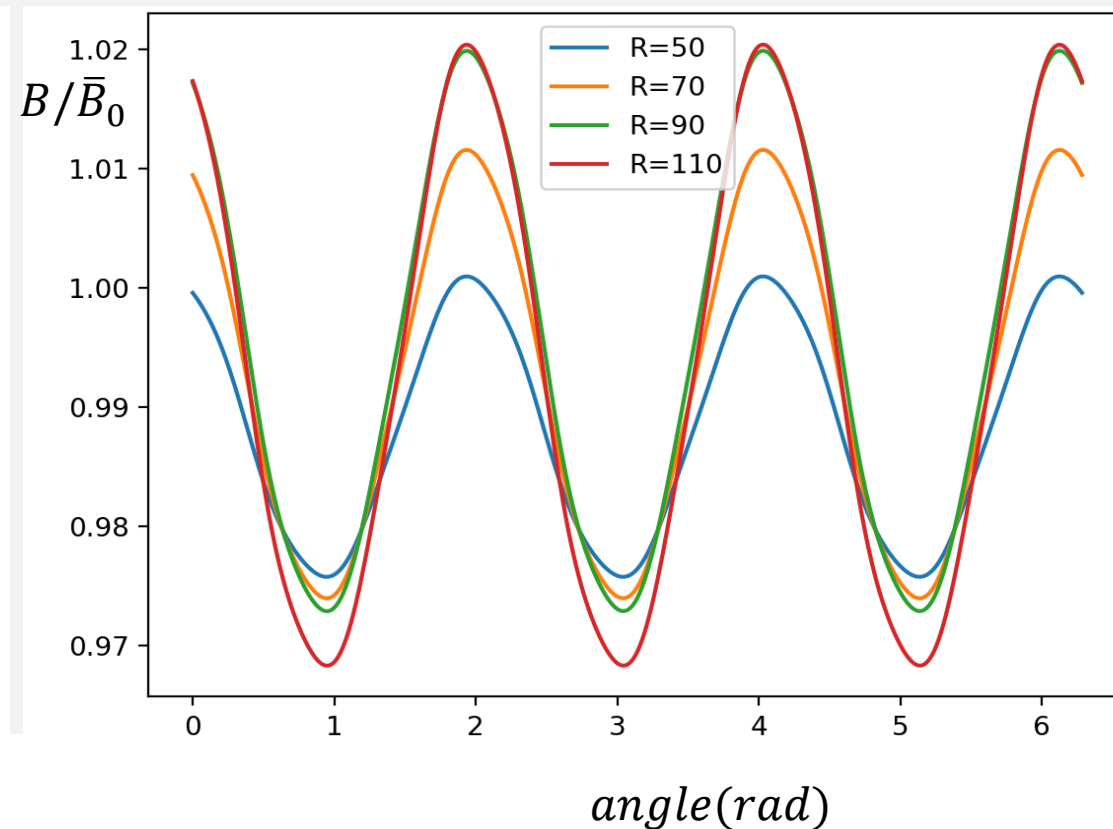
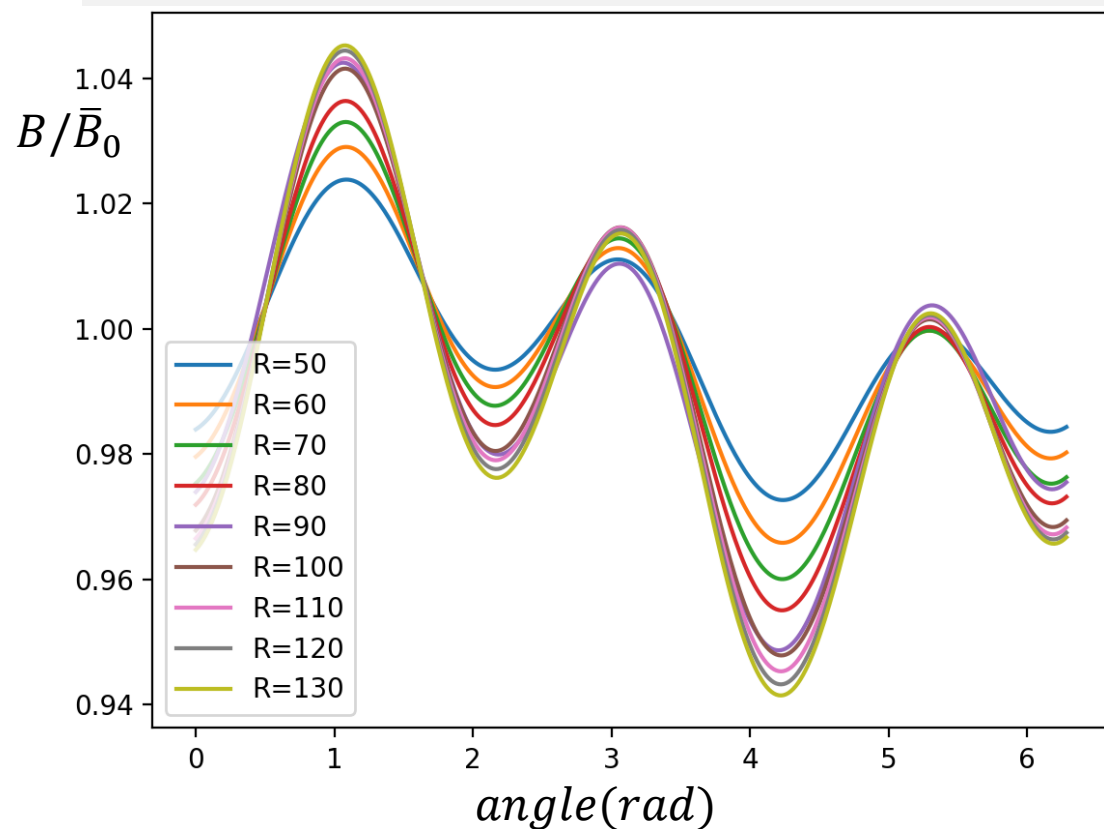
$B/\bar{B}_0$

$angle(rad)$

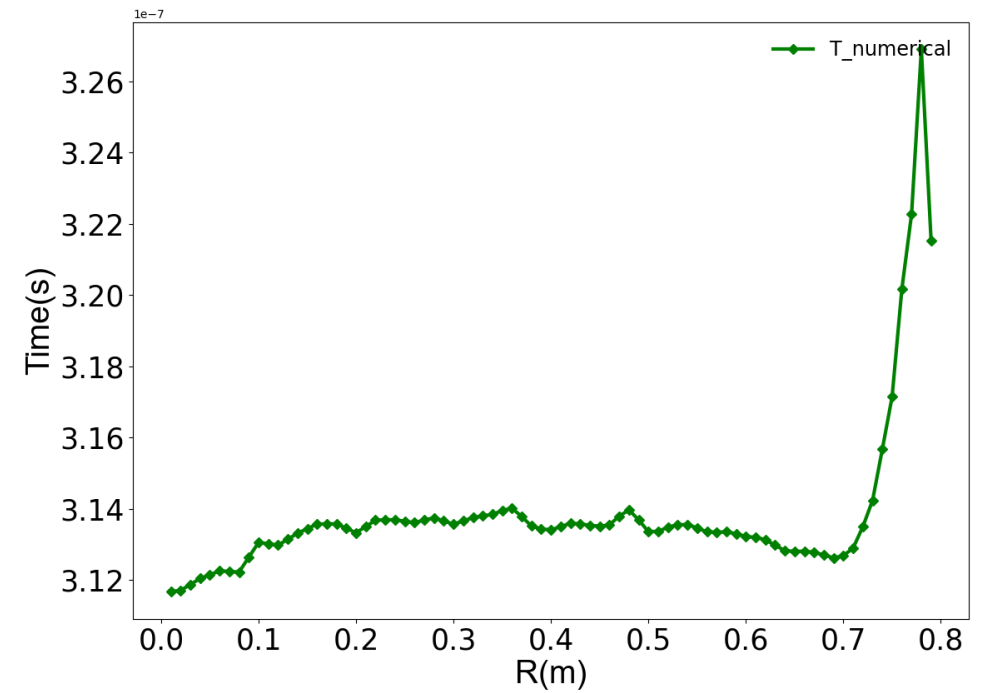
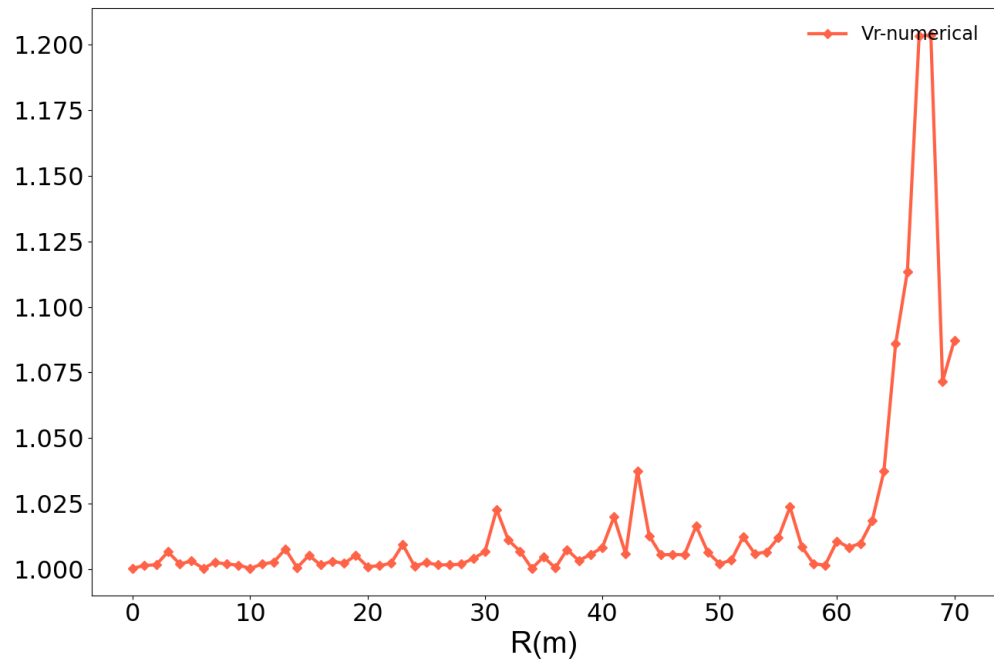
Equilibrium orbits



Why 1/3?



Equilibrium orbits



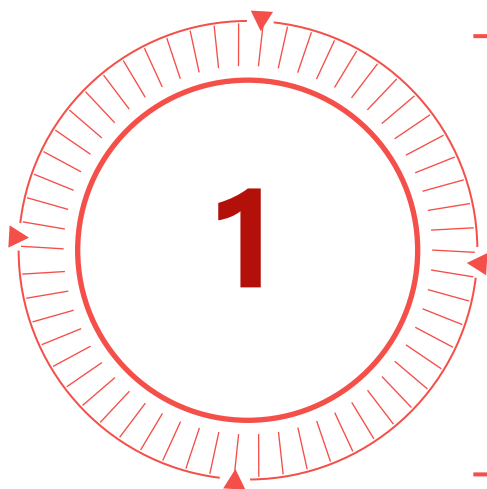


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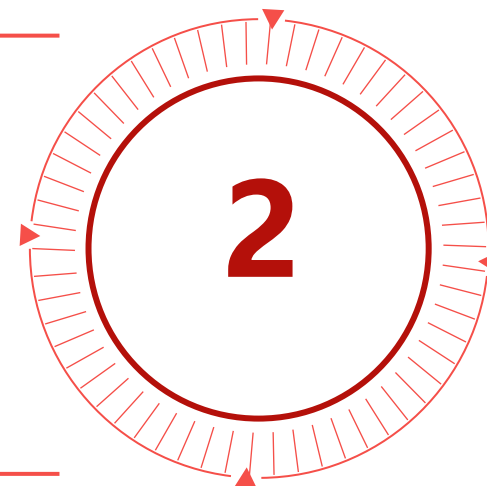
Conclusion

Conclusion



Model

Material





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Thanks for your attention

