



COOL 2019

Dielectronic Recombination spectroscopy of Na-like Kr^{25+} at the cooler storage ring CSRm

Zhongkui HUANG & DR collaboration



Institute of Modern Physics, Chinese Academy of Sciences



Budker INP, Novosibirsk, Sep-23, 2019

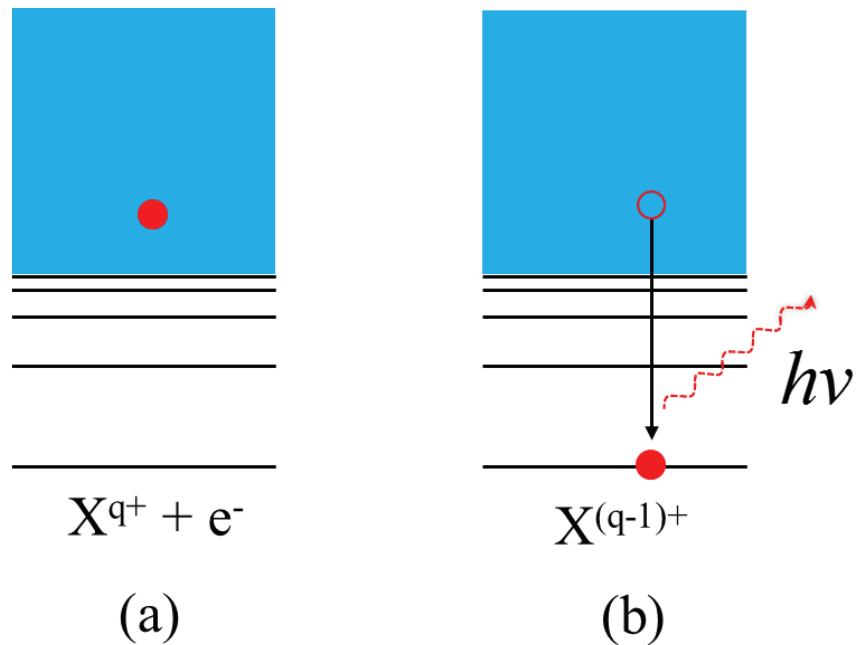
Content

- 1. Introduction and motivation**
- 2. Experimental setup and technique**
- 3. DR experiment of Na-like Krypton at the CSRm**
- 4. Summary and outlook**

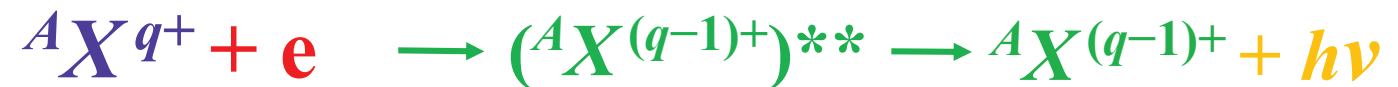
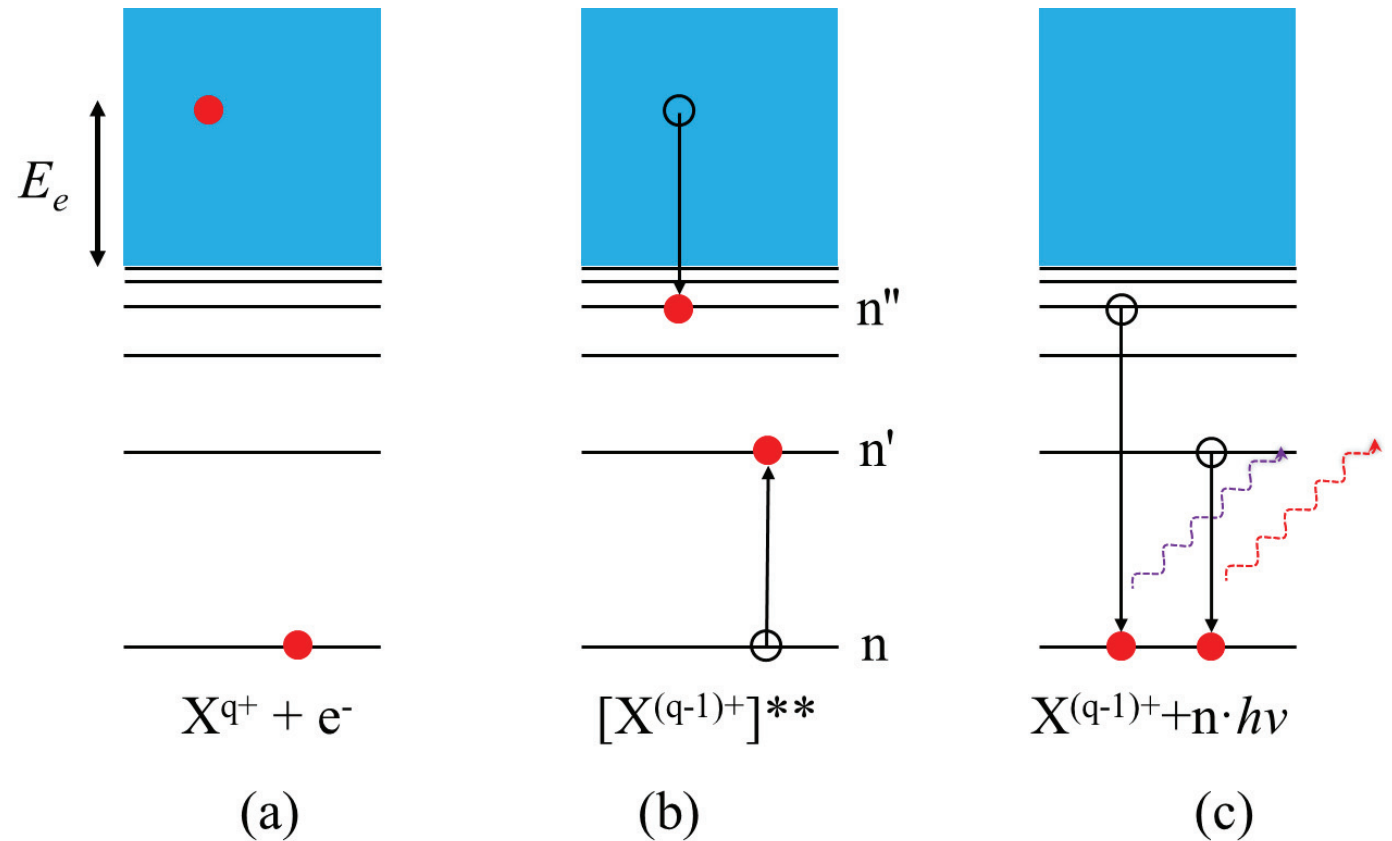
1.Introduction and motivation

Introduction-RR and DR

Radiative Recombination(RR)



Dielectronic Recombination(DR)

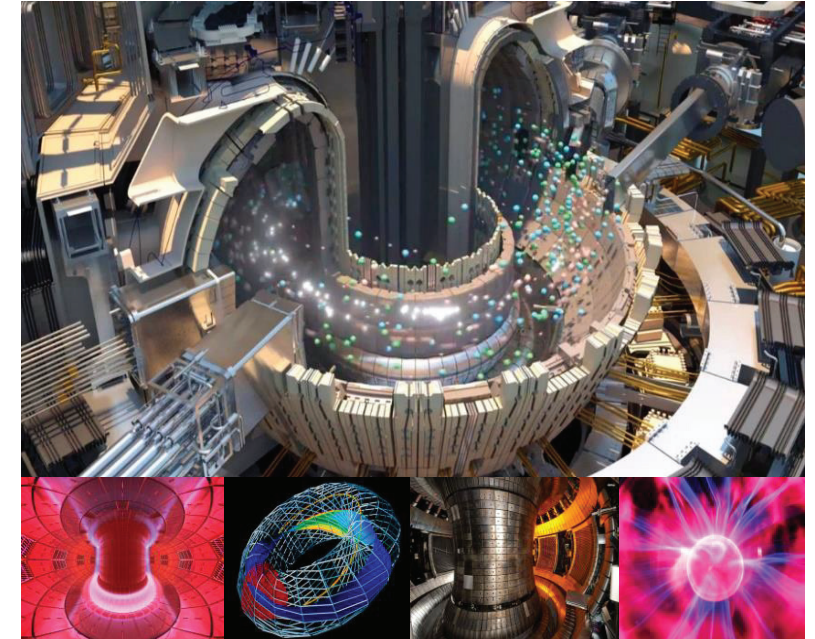
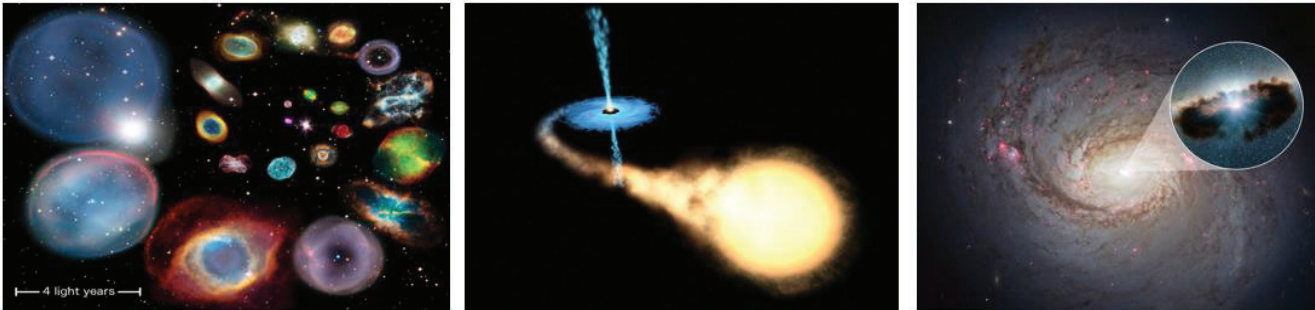


Motivation 1: astrophysical and fusion plasma

Collisionally ionized plasma formed in stars, supernova remnants, and galaxies



photoionized plasmas formed in planetary nebulae, X-ray binaries, and AGN



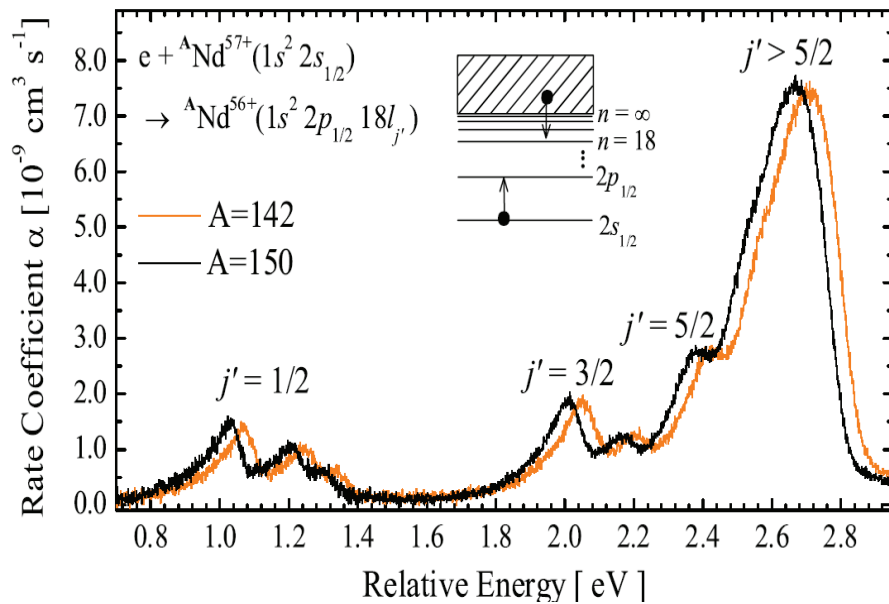
ITER

- ❑ Diagnose status (T_e and n_e) of natural and man-made plasmas;
- ❑ Interpret the spectra from cosmic sources
- ❑ Benchmark the theory and model;

Motivation 2: precision spectroscopy tool

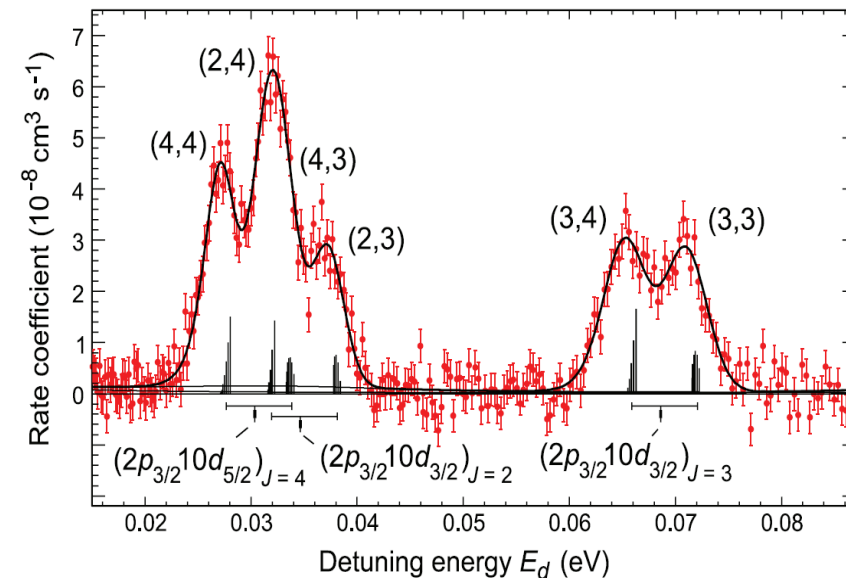
- Test QED in strong field (Au^{76+} , Pb^{79+} , U^{89+});
- Measure Isotope shift ($^{142,150}Nd^{57+}$, $^{207,208}Pb^{53+}$) and hyperfine splitting (Sc^{18+});

Isotope shift of DR resonances in $^{142,150}Nd^{57+}$



C. Brandau et al., PRL 100, 073201(2008)

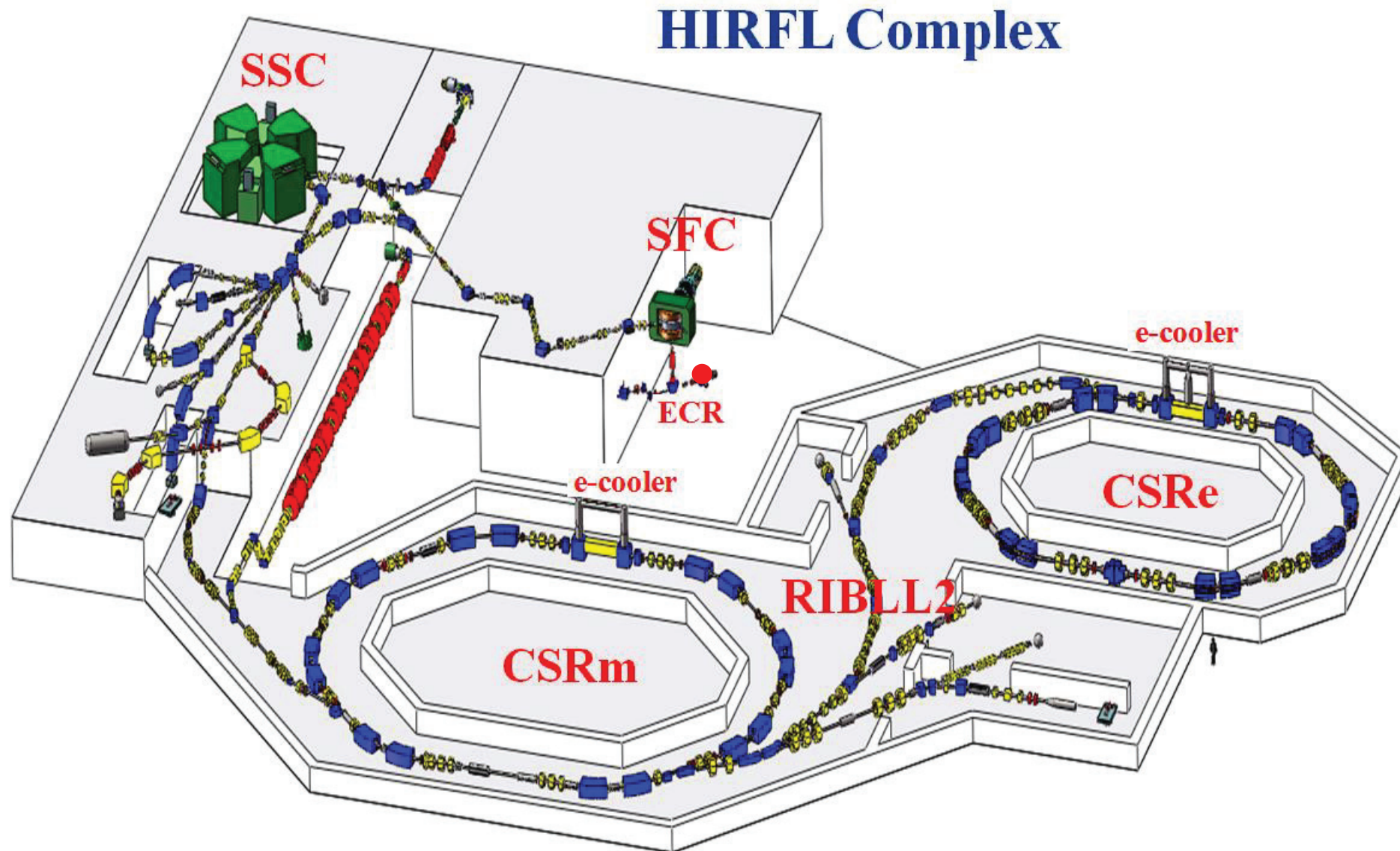
Hyperfine splitting of DR resonances in Sc^{18+}



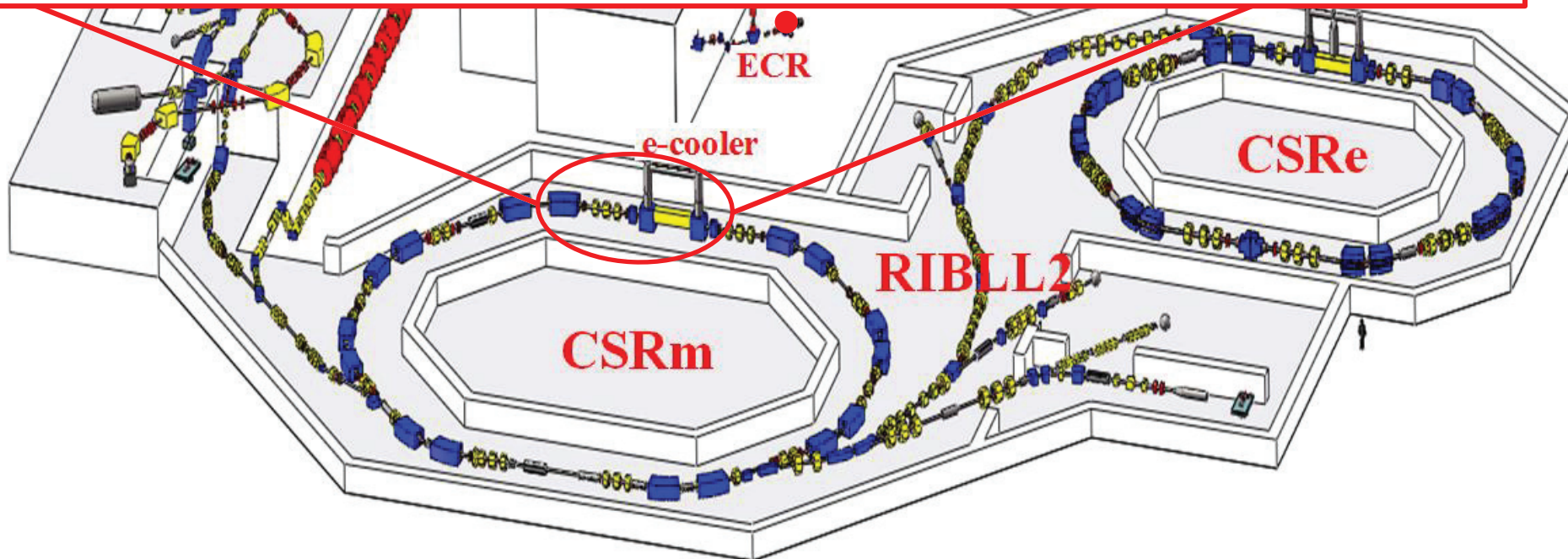
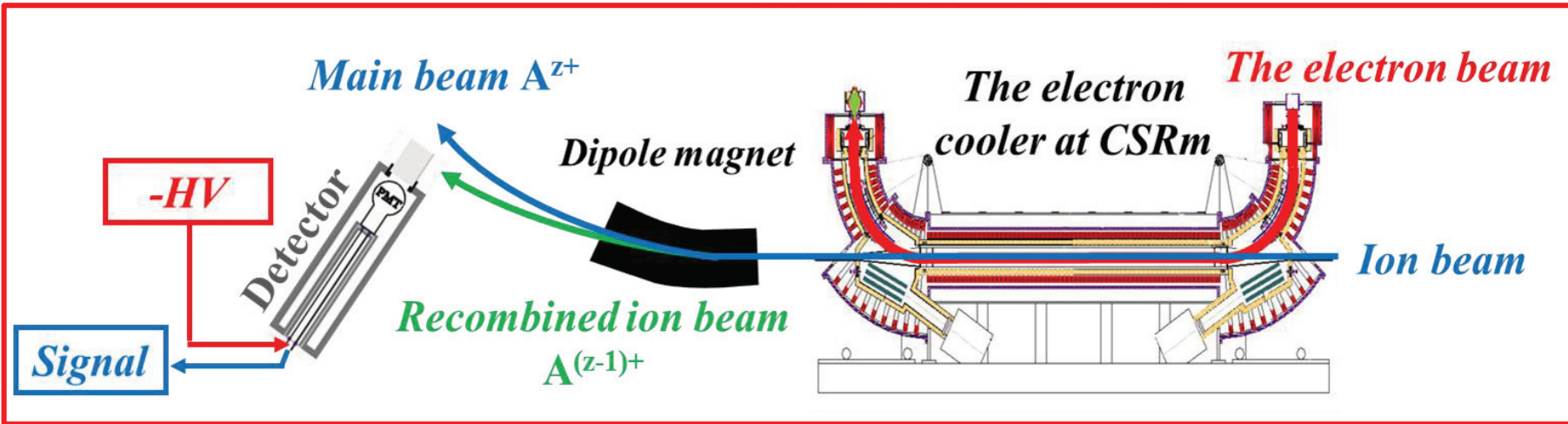
M. Lestinsky et al., PRL 100, 033001(2008)

2. Experimental setup and technique

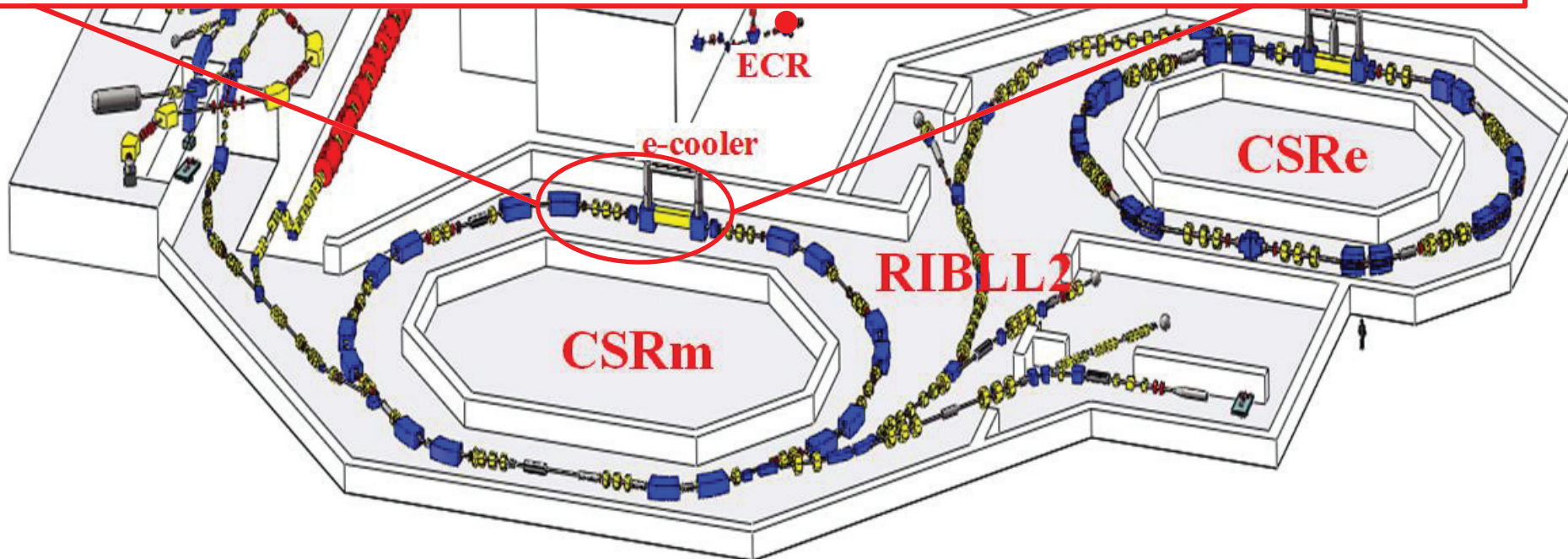
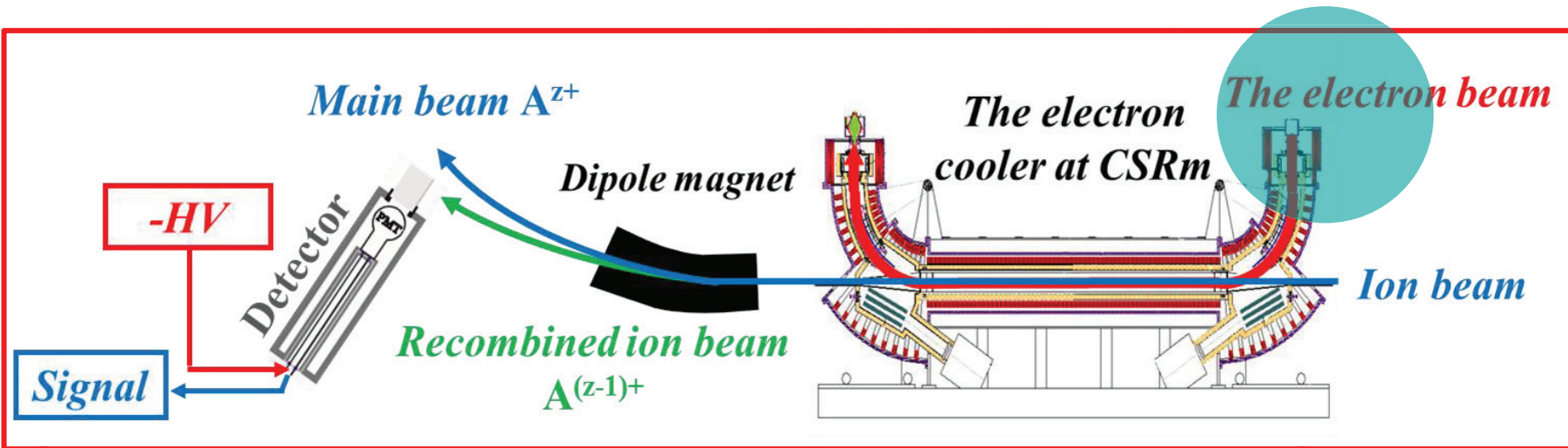
DR experimental setup at the HIRFL-CSRm



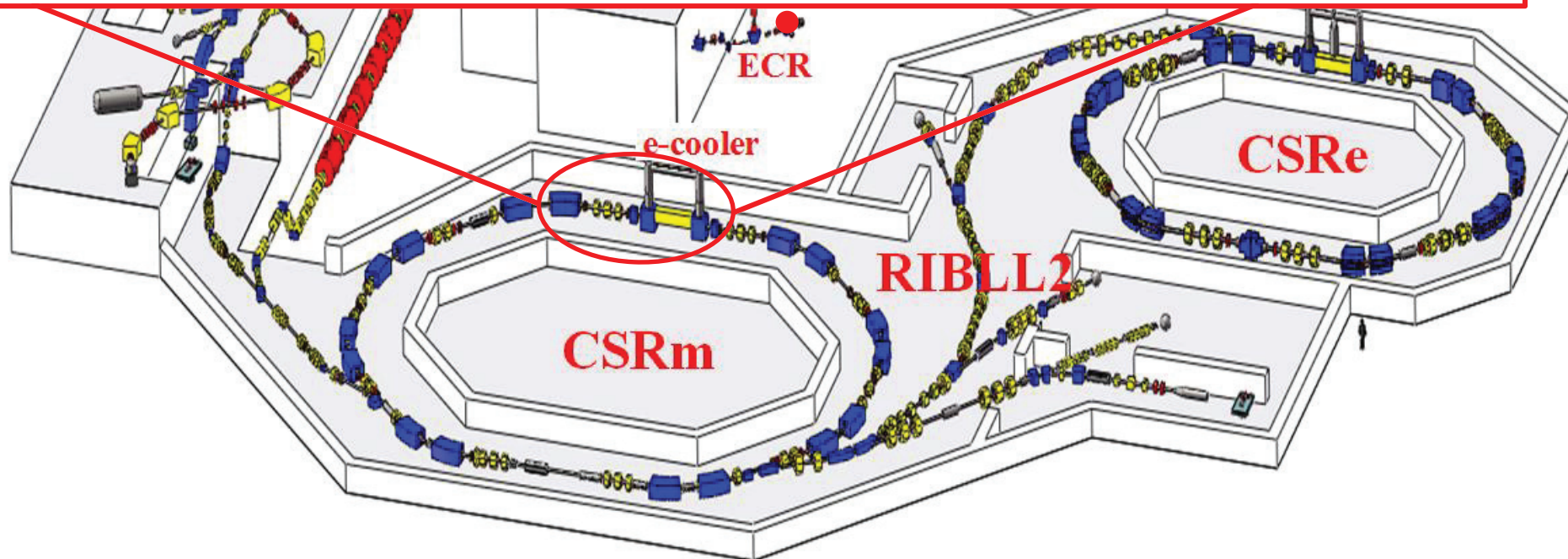
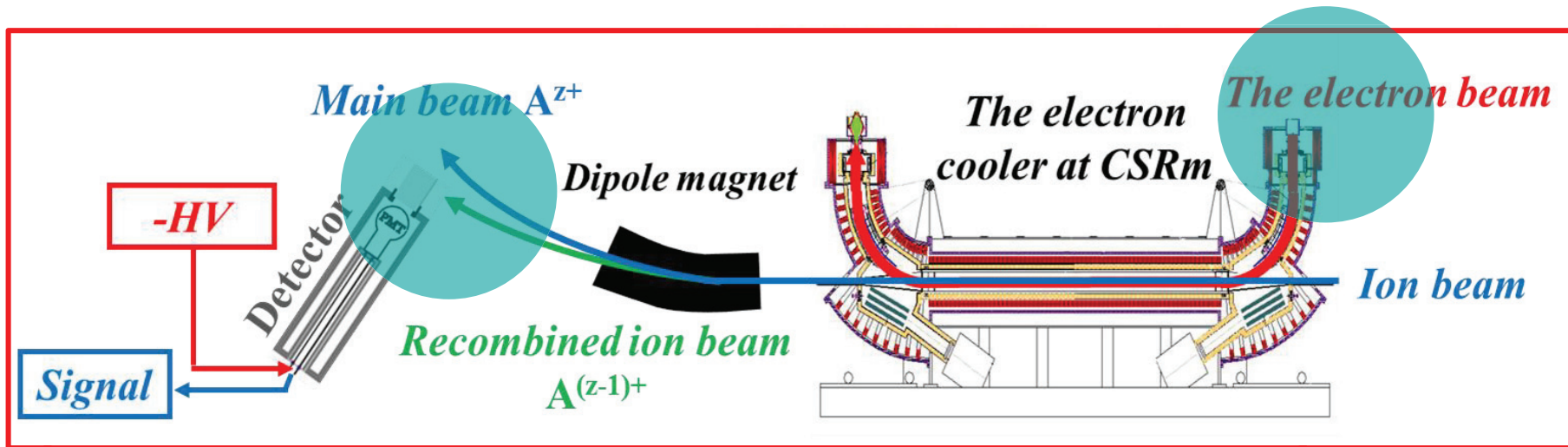
DR experimental setup at the HIRFL-CSRm



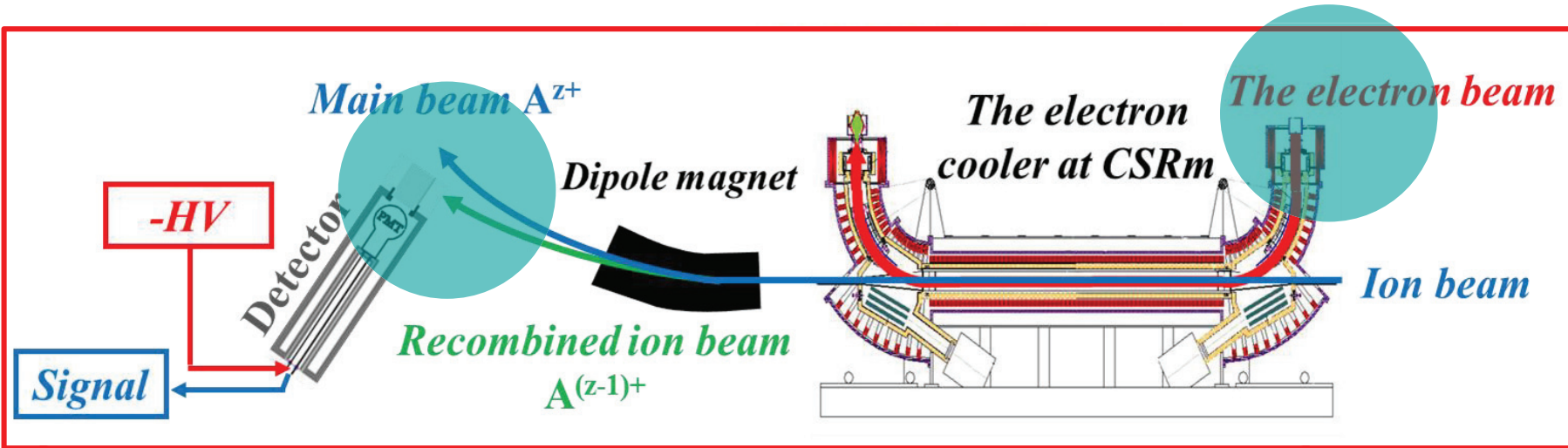
DR experimental setup at the HIRFL-CSRm



DR experimental setup at the HIRFL-CSRm



DR experimental setup at the HIRFL-CSRm



$$\alpha(E_{rel}) = \frac{R}{N_i n_e (1 - \beta_e \beta_i)} \frac{C}{L}$$

R : counts of recombined ions

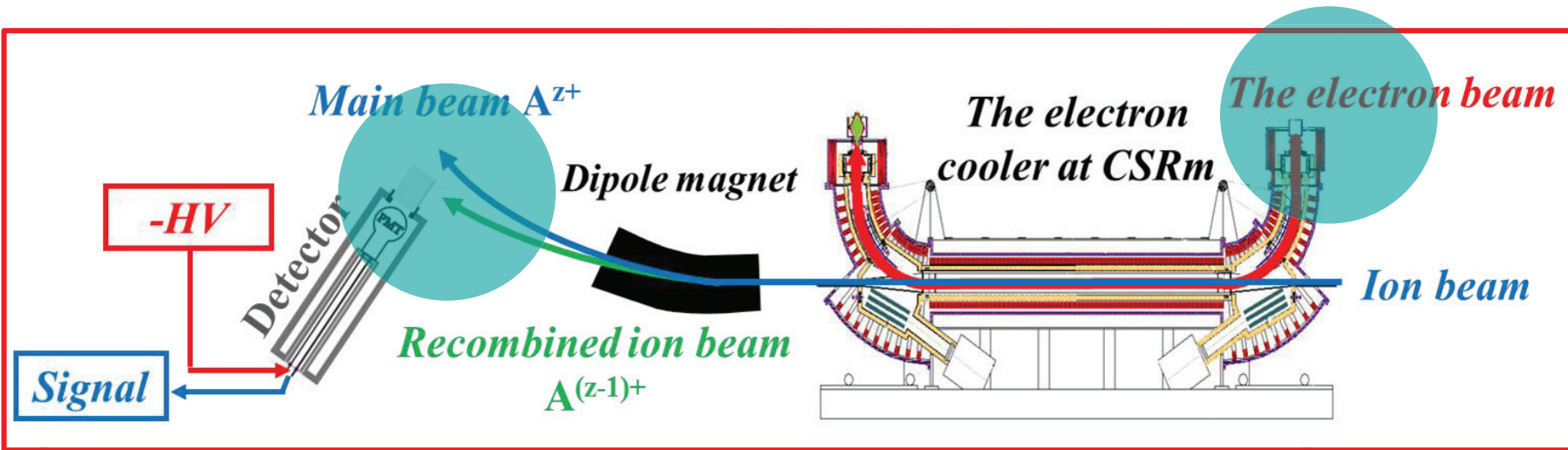
N_i : stored ion beam in storage ring

n_e : electron density

L : effective interaction length

C : the circumstance of CSRm

DR experimental setup at the HIRFL-CSRm



-----Advantages-----

- *High vacuum*
Low background
- *Broad detuning energy-range*
- *Ultra-high precision*
- *~100% detection efficiency*
- *Absolute rate coefficients*

$$\alpha(E_{rel}) = \frac{R}{N_i n_e (1 - \beta_e \beta_i)} \frac{C}{L}$$

***R** : counts of recombined ions*

***N_i** : stored ion beam in storage ring*

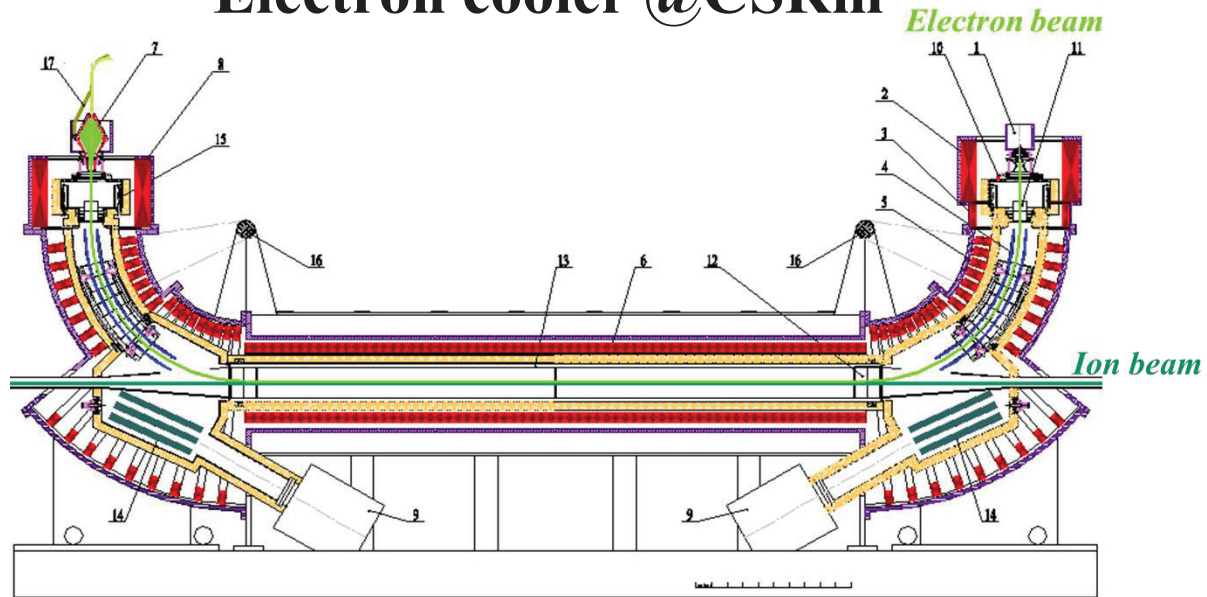
***n_e** : electron density*

***L** : effective interaction length*

***C** : the circumstance of CSRm*

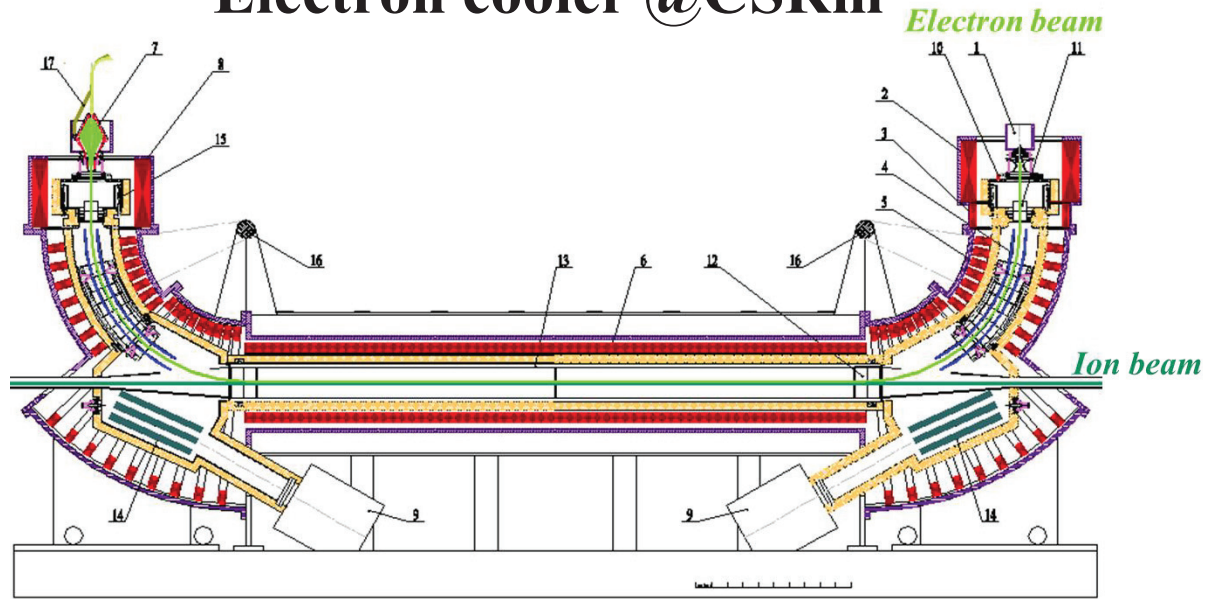
Electron cooler and beam cooling

Electron cooler @CSRm



Electron cooler and beam cooling

Electron cooler @CSRm



Electron-cooler:

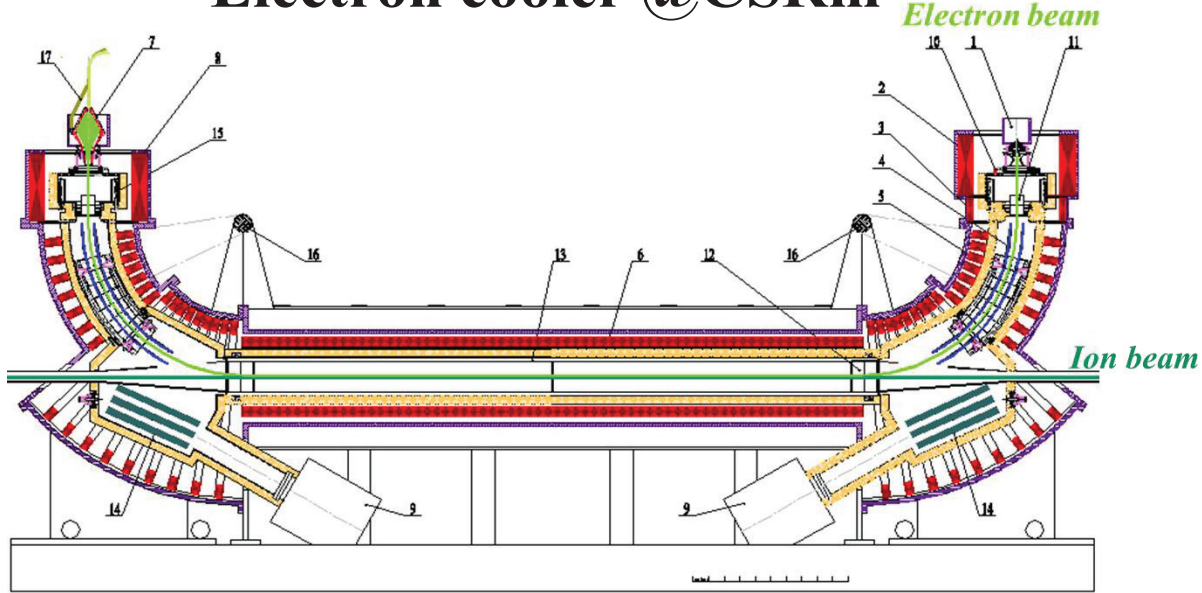
decrease the momentum spread, improve beam quantity;

Electron-target:

provide low-temperature electron beam;

Electron cooler and beam cooling

Electron cooler @CSRm



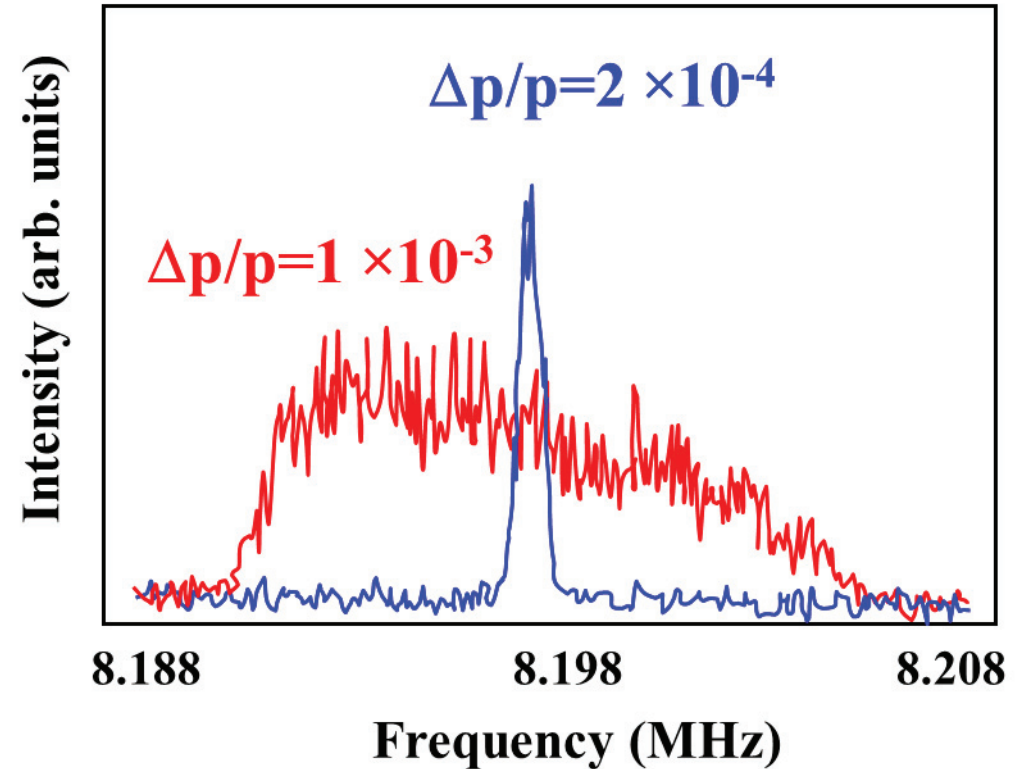
Electron-cooler:

decrease the momentum spread, improve beam quantity;

Electron-target:

provide low-temperature electron beam;

8.37 MeV $^{36}\text{Ar}^{15+}$ @CSRm



Schottky noise spectrum analysis

Adiabatic transverse expansion of the electron beam

Flattened Maxwellian electron energy distribution [**Storage Ring**]

$$f(\nu_{rel}, \vec{\nu}) = \left(\frac{m_e}{2\pi k T_{\parallel}}\right)^{\frac{1}{2}} \exp\left[-\frac{m_e(\nu_{\parallel} - \nu_{rel})^2}{2k T_{\parallel}}\right] \times \frac{m_e}{2\pi k T_{\perp}} \exp\left(-\frac{m_e \nu_{\perp}^2}{2k T_{\perp}}\right)$$

Adiabatic transverse expansion of the electron beam

Flattened Maxwellian electron energy distribution [**Storage Ring**]

$$f(\nu_{rel}, \vec{\nu}) = \left(\frac{m_e}{2\pi k T_{\parallel}}\right)^{\frac{1}{2}} \exp\left[-\frac{m_e(\nu_{\parallel} - \nu_{rel})^2}{2k T_{\parallel}}\right] \times \frac{m_e}{2\pi k T_{\perp}} \exp\left(-\frac{m_e \nu_{\perp}^2}{2k T_{\perp}}\right)$$

Adiabatic transverse expansion of the electron beam

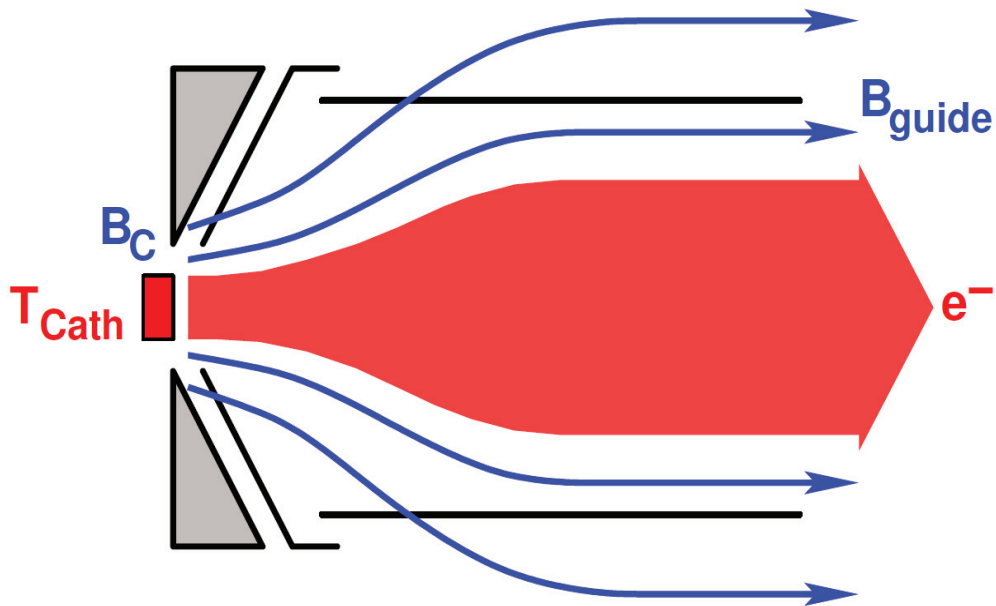
Flattened Maxwellian electron energy distribution [**Storage Ring**]

$$f(v_{rel}, \vec{v}) = \left(\frac{m_e}{2\pi k T_{\parallel}} \right)^{\frac{1}{2}} \exp\left[-\frac{m_e (v_{\parallel} - v_{rel})^2}{2k T_{\parallel}} \right] \times \frac{m_e}{2\pi k T_{\perp}} \exp\left(-\frac{m_e v_{\perp}^2}{2k T_{\perp}} \right)$$

Adiabatic transverse expansion of the electron beam

Flattened Maxwellian electron energy distribution [**Storage Ring**]

$$f(\nu_{rel}, \vec{\nu}) = \left(\frac{m_e}{2\pi k T_{\parallel}} \right)^{\frac{1}{2}} \exp\left[-\frac{m_e (\nu_{\parallel} - \nu_{rel})^2}{2k T_{\parallel}} \right] \times \frac{m_e}{2\pi k T_{\perp}} \exp\left(-\frac{m_e \nu_{\perp}^2}{2k T_{\perp}} \right)$$

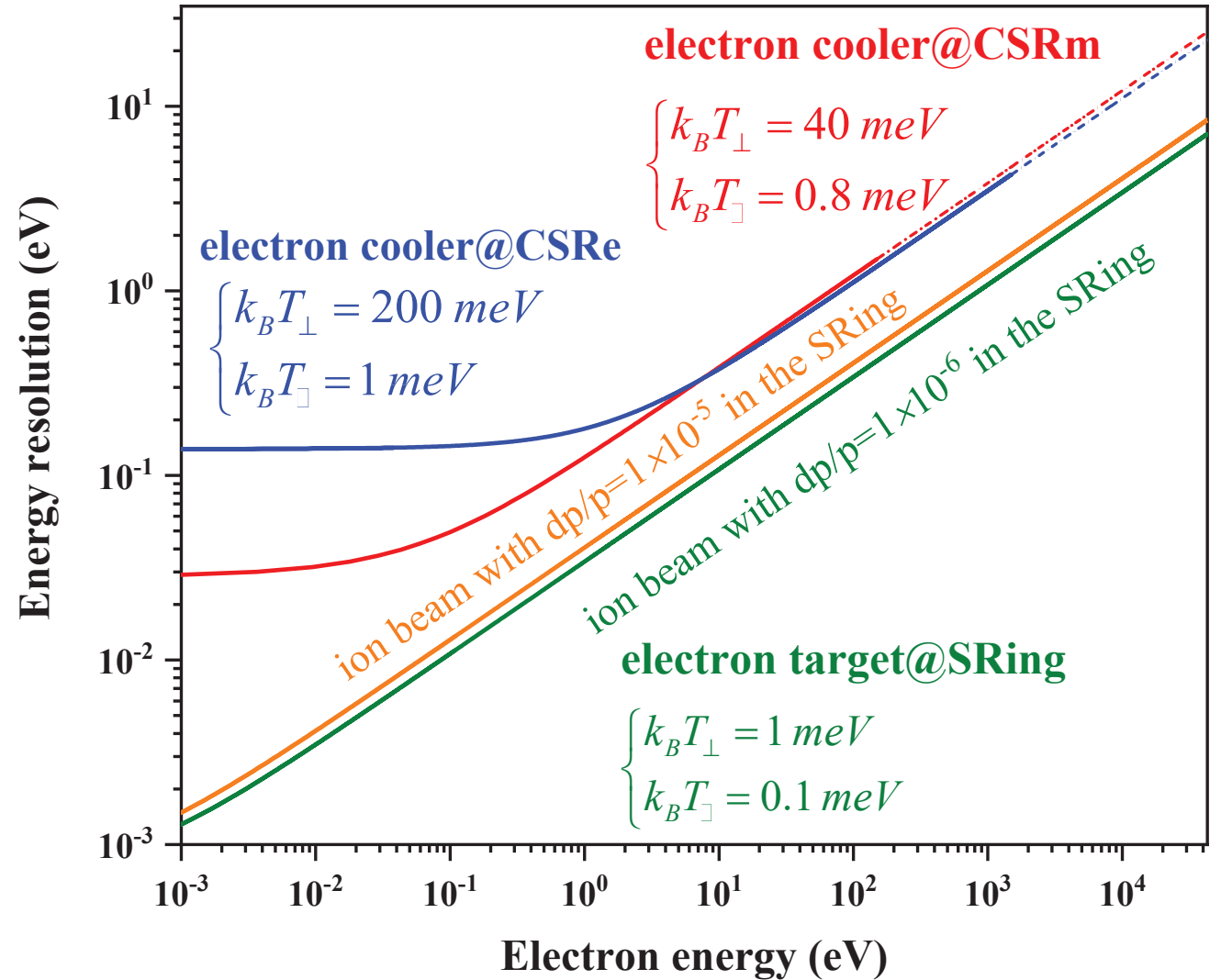


$$k_B T_{\perp} = \frac{k_B T_{\text{cath}}}{\xi} \quad \xi = B_c / B_{\text{guide}}$$

$$k_B T_{\parallel} = k_B T_{\parallel}^{\text{kin}} + \frac{\partial \Delta E_{\text{TLR}}}{\partial x} dx + \Delta E_{\text{LLR}}$$

Energy resolution of DR resonances

$$\Delta E = \sqrt{(K_B T_{\perp} \cdot \ln 2)^2 + 16 \ln 2 \cdot K_B T_{\parallel} \cdot E_{rel}} + \frac{\Delta p}{p} \cdot (\beta_{ion} - \beta_e) \gamma_{ion} \gamma_e$$



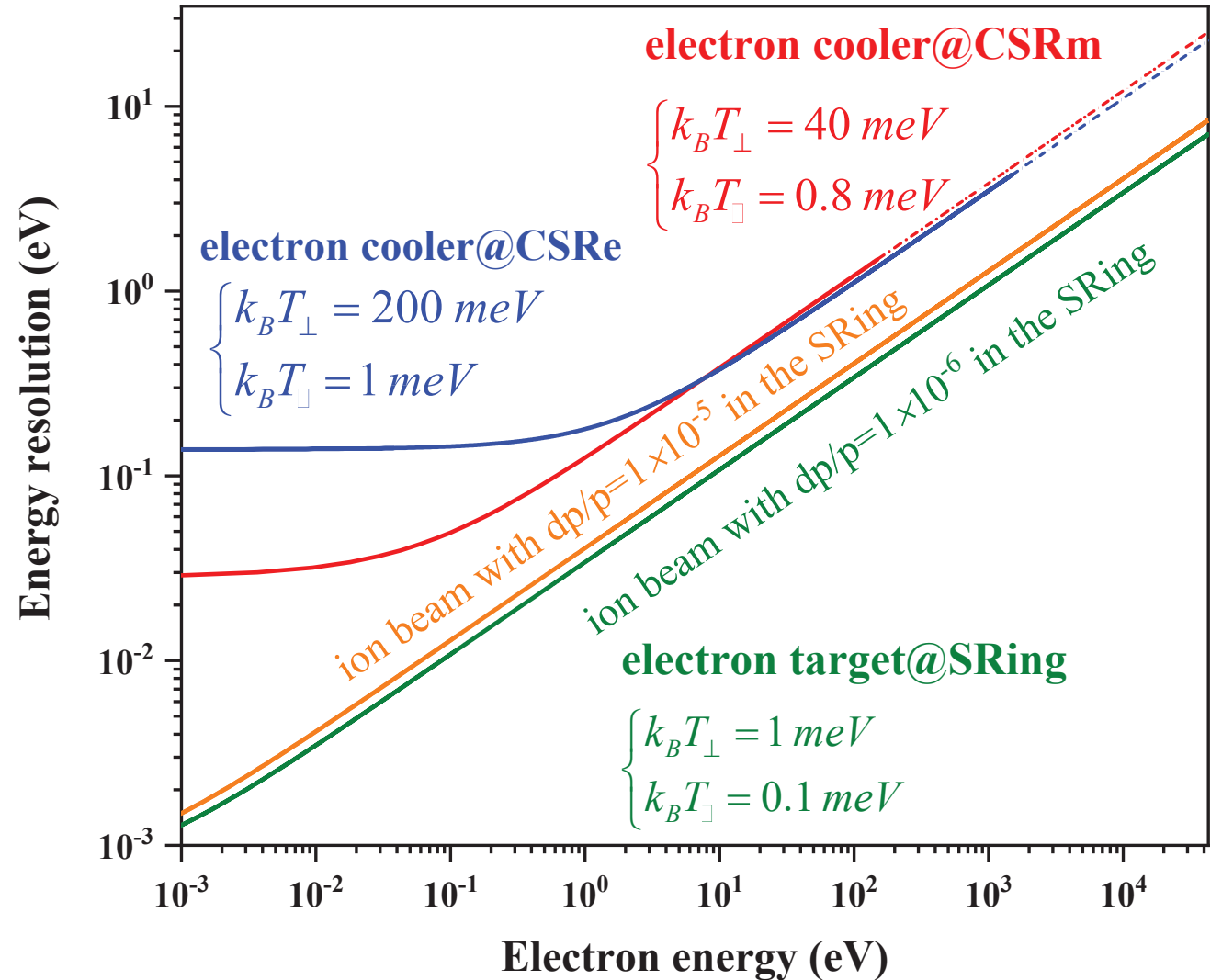
Energy resolution of DR resonances

$$\Delta E = \sqrt{(K_B T_{\perp} \cdot \ln 2)^2 + 16 \ln 2 \cdot K_B T_{\parallel} \cdot E_{rel}} + \frac{\Delta p}{p} \cdot (\beta_{ion} - \beta_e) \gamma_{ion} \gamma_e$$

Lower electron temperature
Lower momentum spread

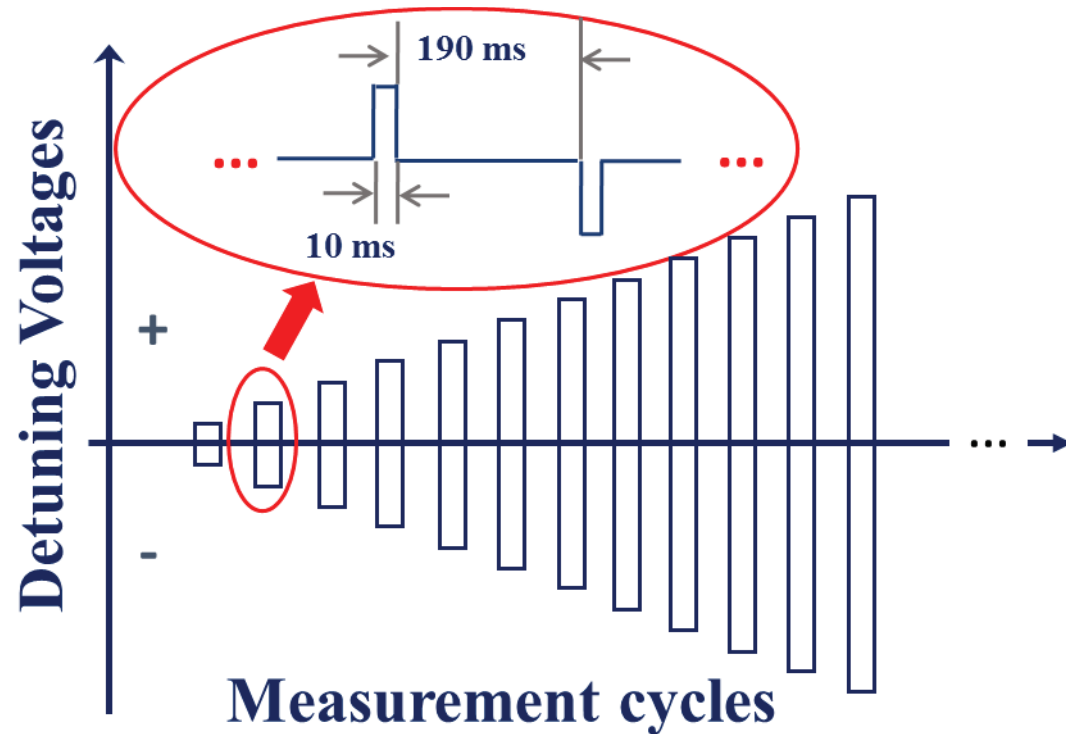


Higher energy resolution



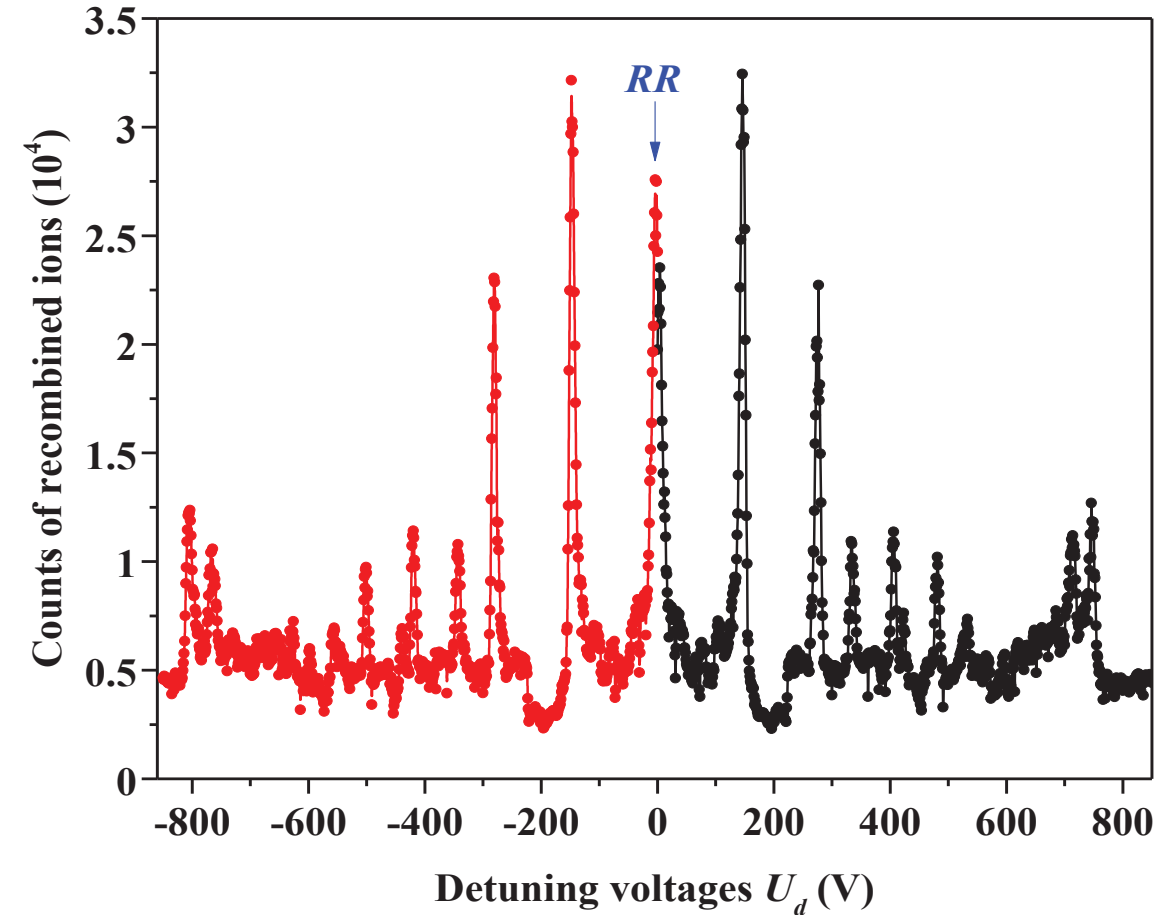
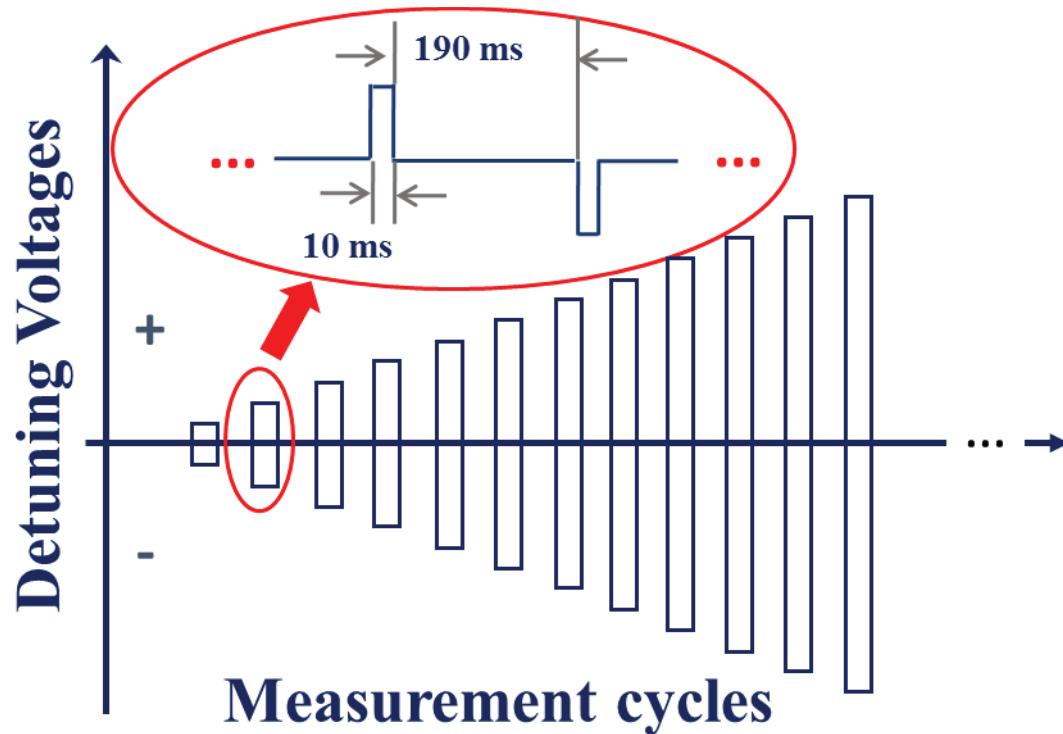
Detuning timing sequence

Detuning timing scheme for DR experiments at the CSRm



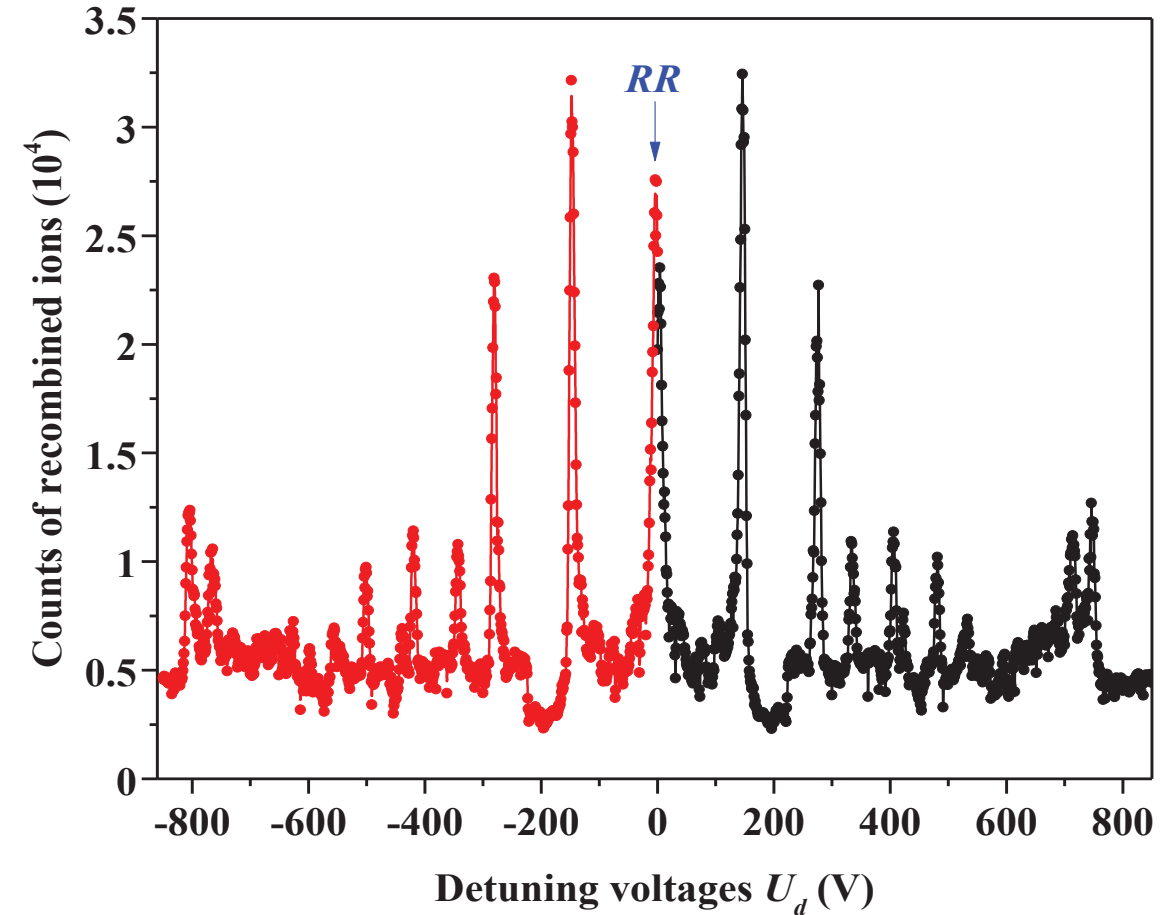
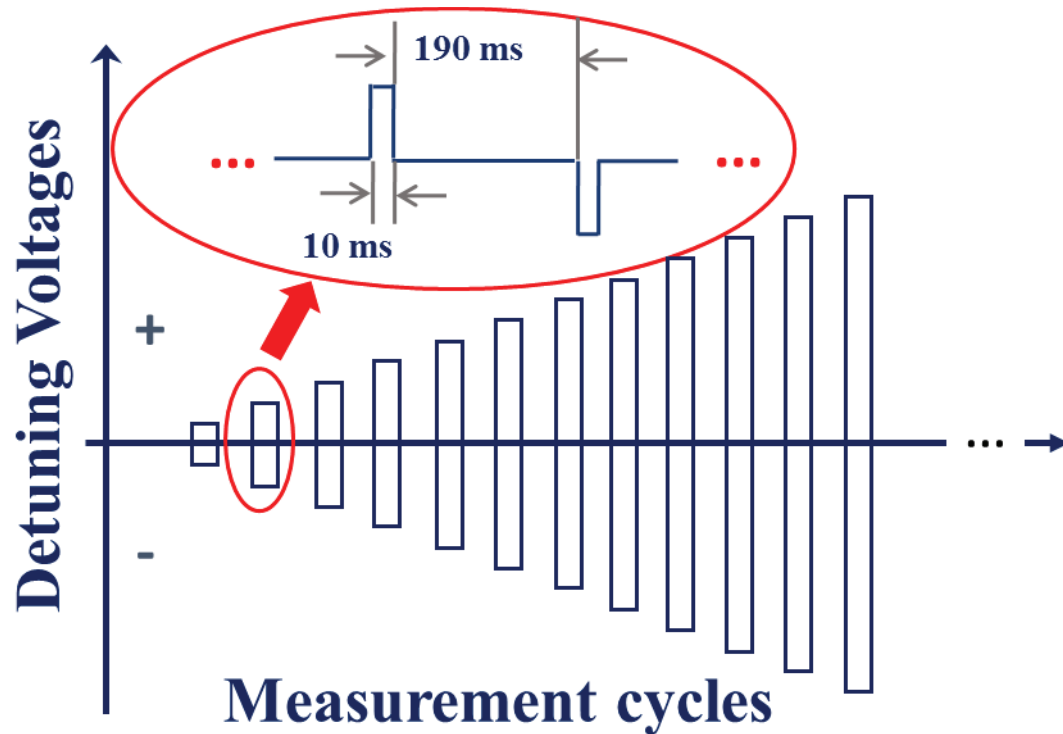
Detuning timing sequence

Detuning timing scheme for DR experiments at the CSRm



Detuning timing sequence

Detuning timing scheme for DR experiments at the CSRm



Counts of recombined
ions vs. detuning voltages



DR spectrum

Data analysis

1. X axis : Detuning voltages → Electron –ion collision energy ;

$$E_{rel} = \sqrt{m_e^2 c^4 + m_{ion}^2 c^4 + 2m_e m_{ion} \gamma_e \gamma_{ion} c^4 (1 - \beta_e \beta_{ion} \cos \theta)} - m_e c^2 - m_{ion} c^2$$

Under cooling: $\gamma_e = \gamma_i$

Detuning:
$$\gamma_e = 1 + \frac{E_{e-0} + \Delta E_e}{m_e c^2} = \gamma_i + \frac{\Delta E_e}{m_e c^2}$$

2. Y axis : Counts of recombined ion → Rate coefficients ;

$$\alpha(E_{rel}) = \frac{R}{N_i n_e (1 - \beta_e \beta_i)} \frac{C}{L} = q e^2 c^2 \pi r_e^2 \cdot \frac{\beta_e \beta_i}{1 - \beta_e \beta_i} \cdot \frac{RL}{I_{ion} I_e}$$

Data analysis

1. X axis : Detuning voltages → Electron –ion collision energy ;

$$E_{rel} = \sqrt{m_e^2 c^4 + m_{ion}^2 c^4 + 2m_e m_{ion} \gamma_e \gamma_{ion} c^4 (1 - \beta_e \beta_{ion} \cos \theta)} - m_e c^2 - m_{ion} c^2$$

Under cooling: $\gamma_e = \gamma_i$

Detuning + Correlation

Detuning:
$$\gamma_e = 1 + \frac{E_{e-0} + \Delta E_e}{m_e c^2} = \gamma_i + \frac{\Delta E_e}{m_e c^2}$$

2. Y axis : Counts of recombined ion → Rate coefficients ;

$$\alpha(E_{rel}) = \frac{R}{N_i n_e (1 - \beta_e \beta_i)} \frac{C}{L} = q e^2 c^2 \pi r_e^2 \cdot \frac{\beta_e \beta_i}{1 - \beta_e \beta_i} \cdot \frac{RL}{I_{ion} I_e}$$

Data analysis

1. X axis : Detuning voltages → Electron –ion collision energy ;

$$E_{rel} = \sqrt{m_e^2 c^4 + m_{ion}^2 c^4 + 2m_e m_{ion} \gamma_e \gamma_{ion} c^4 (1 - \beta_e \beta_{ion} \cos \theta)} - m_e c^2 - m_{ion} c^2$$

Under cooling: $\gamma_e = \gamma_i$

Detuning + Correlation

Detuning:
$$\gamma_e = 1 + \frac{E_{e-0} + \Delta E_e}{m_e c^2} = \gamma_i + \frac{\Delta E_e}{m_e c^2}$$

2. Y axis : Counts of recombined ion → Rate coefficients ;

$$\alpha(E_{rel}) = \frac{R}{N_i n_e (1 - \beta_e \beta_i)} \frac{C}{L} = q e^2 c^2 \pi r_e^2 \cdot \frac{\beta_e \beta_i}{1 - \beta_e \beta_i} \cdot \frac{RL}{I_{ion} I_e}$$

Data analysis

1. X axis : Detuning voltages → Electron –ion collision energy ;

$$E_{rel} = \sqrt{m_e^2 c^4 + m_{ion}^2 c^4 + 2m_e m_{ion} \gamma_e \gamma_{ion} c^4 (1 - \beta_e \beta_{ion} \cos \theta)} - m_e c^2 - m_{ion} c^2$$

Under cooling: $\gamma_e = \gamma_i$

Detuning + Correlation

Detuning:
$$\gamma_e = 1 + \frac{E_{e-0} + \Delta E_e}{m_e c^2} = \gamma_i + \frac{\Delta E_e}{m_e c^2}$$



2. Y axis : Counts of recombined ion → Rate coefficients ;

$$\alpha(E_{rel}) = \frac{R}{N_i n_e (1 - \beta_e \beta_i)} \frac{C}{L} = q e^2 c^2 \pi r_e^2 \cdot \frac{\beta_e \beta_i}{1 - \beta_e \beta_i} \cdot \frac{RL}{I_{ion} I_e}$$

Data analysis

1. X axis : Detuning voltages → Electron –ion collision energy ;

$$E_{rel} = \sqrt{m_e^2 c^4 + m_{ion}^2 c^4 + 2m_e m_{ion} \gamma_e \gamma_{ion} c^4 (1 - \beta_e \beta_{ion} \cos \theta)} - m_e c^2 - m_{ion} c^2$$

Under cooling: $\gamma_e = \gamma_i$

Detuning + Correlation

Detuning:
$$\gamma_e = 1 + \frac{E_{e-0} + \Delta E_e}{m_e c^2} = \gamma_i + \frac{\Delta E_e}{m_e c^2}$$



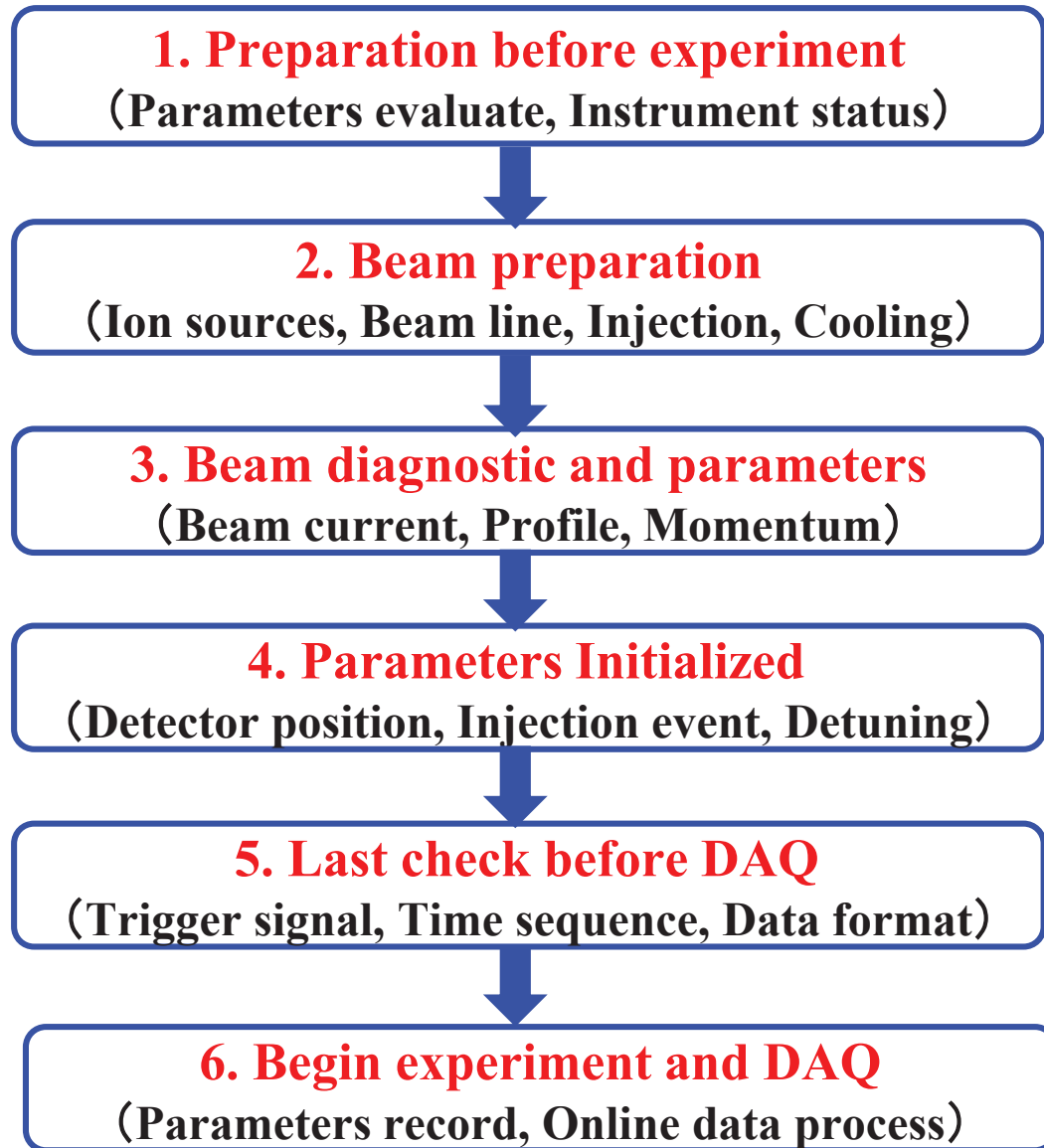
DR Spectrum

2. Y axis : Counts of recombined ion → Rate coefficients ;

$$\alpha(E_{rel}) = \frac{R}{N_i n_e (1 - \beta_e \beta_i)} \frac{C}{L} = q e^2 c^2 \pi r_e^2 \cdot \frac{\beta_e \beta_i}{1 - \beta_e \beta_i} \cdot \frac{RL}{I_{ion} I_e}$$

3. DR experiment of Na-like Kr^{25+} at the CSRm

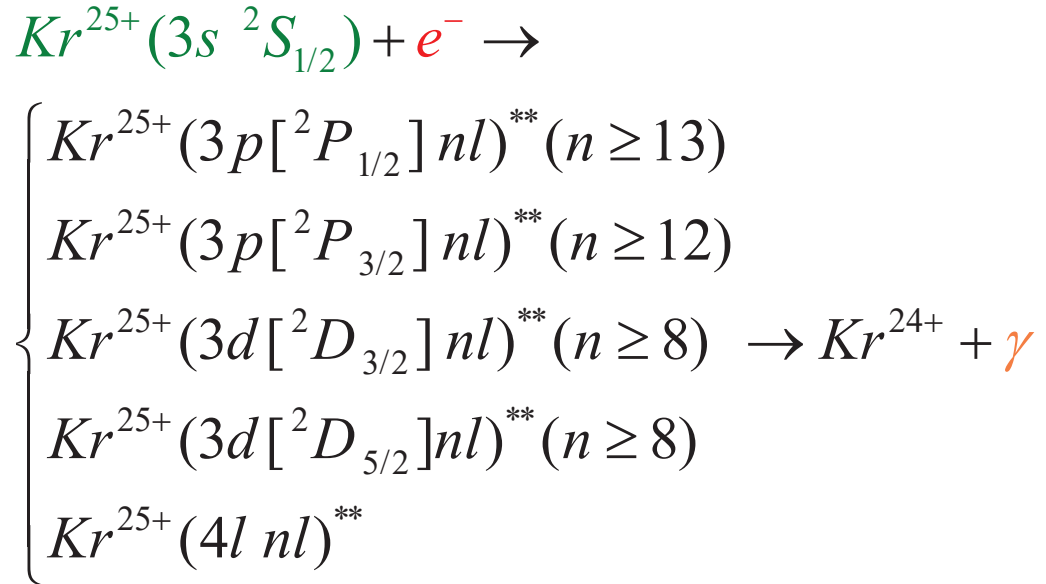
Program and parameters



Parameters (unit)	value
CSRm circumstance (m)	161.00
Length of cooling section (m)	4.0
Radii of beam tube (cm)	25
Beam energy (MeV/u)	4.98
Max beam current (μA)	200
Momentum spread (dp/p)	2.2×10^{-4}
Beam life time (s)	50
Cooling point (kV)	-2.732
Electron beam current (mA)	~ 120
Electron density (cm^{-3})	3.85×10^5
Radii of electron beam (cm)	2.60
Magnet in cooling section (GS)	390
Magnet in gun section (GS)	1250

Atomic structure of Na-like Kr²⁵⁺

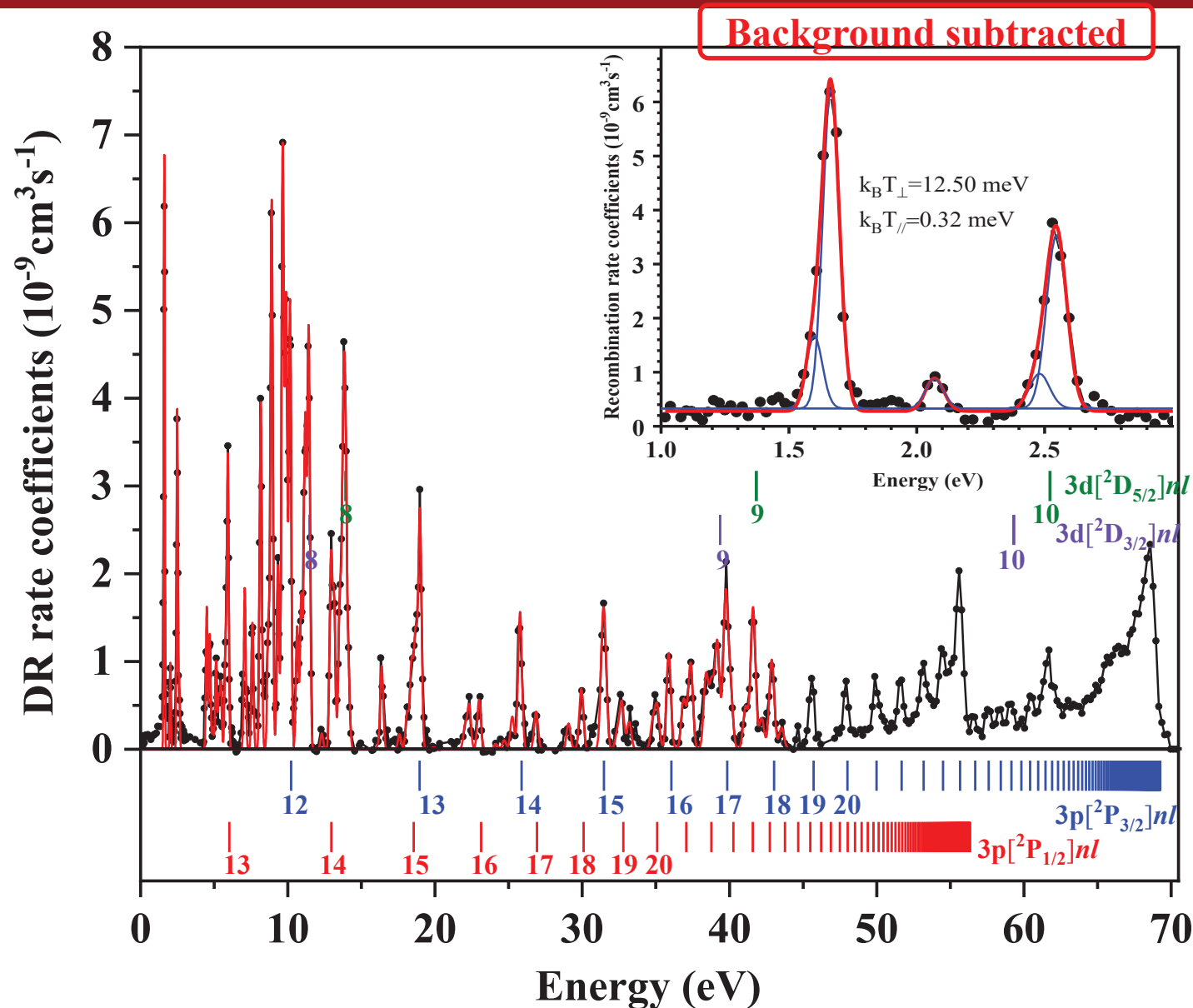
Dominant channels for DR of Na-like Kr²⁵⁺



Energy levels for Na-like Kr²⁵⁺ ions

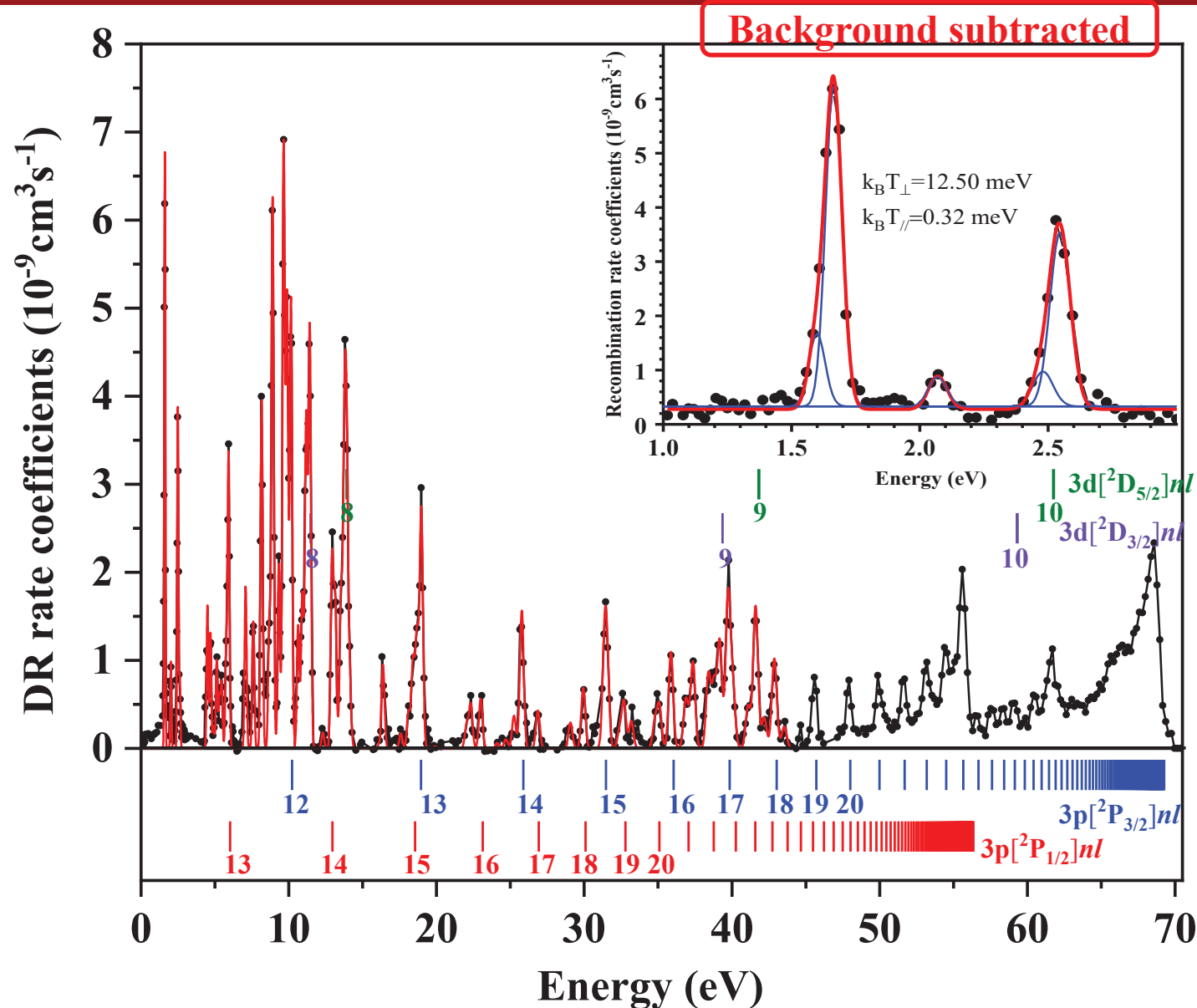
Level configuration	Excitation energy(eV) ^a
1s ² 2s ² 2p ⁶ 3s [² S _{1/2}]	0
1s ² 2s ² 2p ⁶ 3p [² P _{1/2}]	56.340
1s ² 2s ² 2p ⁶ 3p [² P _{3/2}]	69.267
1s ² 2s ² 2p ⁶ 3d [² D _{3/2}]	144.340
1s ² 2s ² 2p ⁶ 3d [² D _{5/2}]	146.796
1s ² 2s ² 2p ⁶ 4s [² S _{1/2}]	557.147
1s ² 2s ² 2p ⁶ 4p [² P _{1/2}]	580.175
1s ² 2s ² 2p ⁶ 4p [² P _{3/2}]	585.285
1s ² 2s ² 2p ⁶ 4d [² D _{3/2}]	613.368
1s ² 2s ² 2p ⁶ 4d [² D _{5/2}]	614.463
1s ² 2s ² 2p ⁶ 4f [² F _{5/2}]	628.266
1s ² 2s ² 2p ⁶ 4f [² F _{7/2}]	628.708

Experimental results: Na-like Kr^{25+}



- The energy scale was recalibrated by a factor of 1.022 to achieve agreement with $3p[{}^2P_{3/2}]nl$ series limit at 69.267 eV.
- By fitting the resolved DR resonances with a flattened Maxwellian, electron temperatures of $k_B T_{\parallel} = 0.32 \text{ meV}$ and $k_B T_{\perp} = 12.50 \text{ meV}$ were obtained.

Experimental results: Na-like Kr²⁵⁺



The vertical bar indicated in the figure is estimated by Rydberg formula :

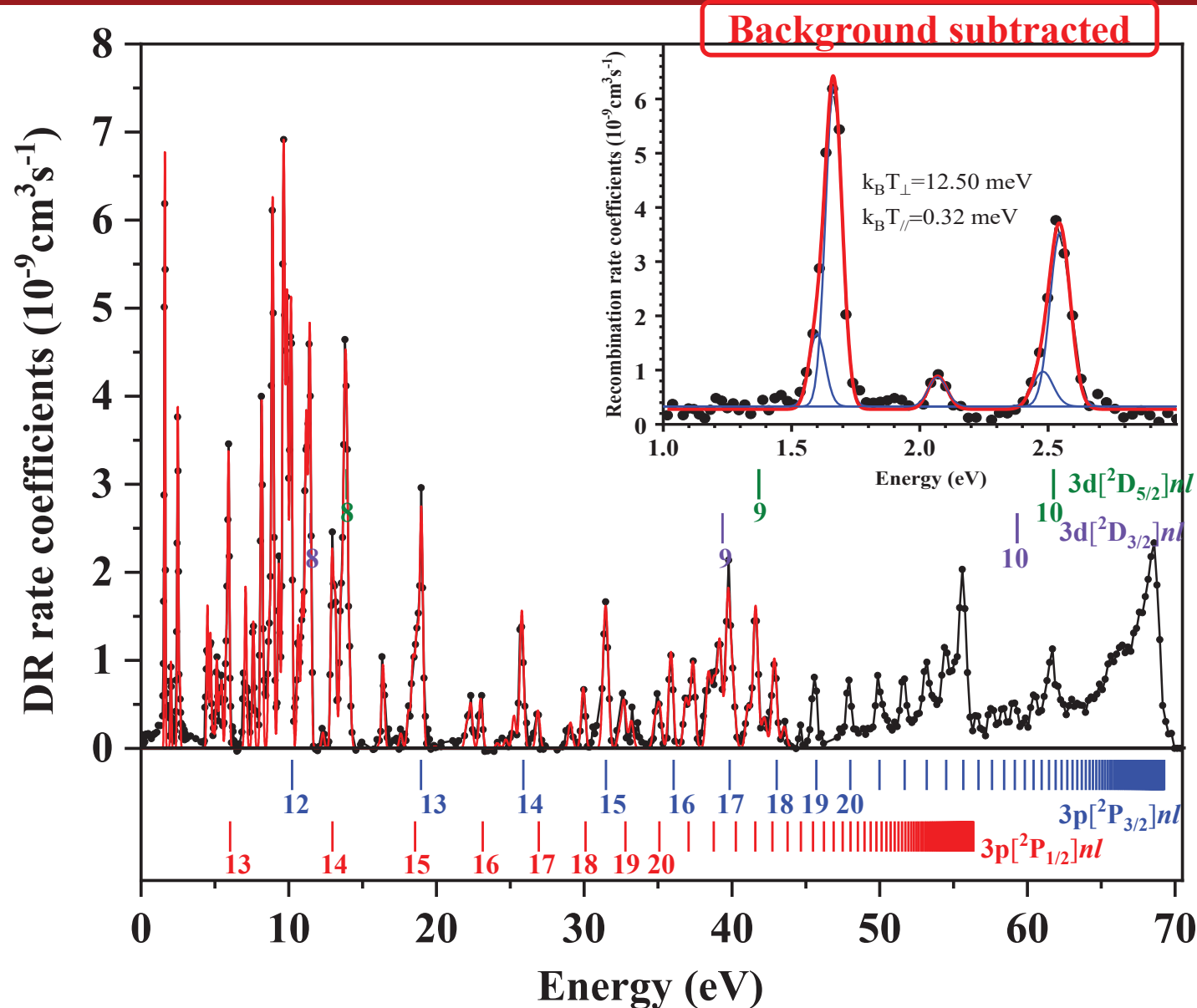
E_{exc} donates the core excitation energy

R donates the Rydberg constant

Z_{eff} donates the charge state of ion

- The energy scale was recalibrated by a factor of 1.022 to achieve agreement with $3p[{}^2P_{3/2}]nl$ series limit at 69.267 eV.
- By fitting the resolved DR resonances with a flattened Maxwellian, electron temperatures of $k_B T_{\parallel} = 0.32 \text{ meV}$ and $k_B T_{\perp} = 12.50 \text{ meV}$ were obtained.

Experimental results: Na-like Kr²⁵⁺



The vertical bar indicated in the figure is estimated by Rydberg formula :

$$E_{\text{res}} = E_{\text{exc}} - \frac{RZ_{\text{eff}}}{n^2}$$

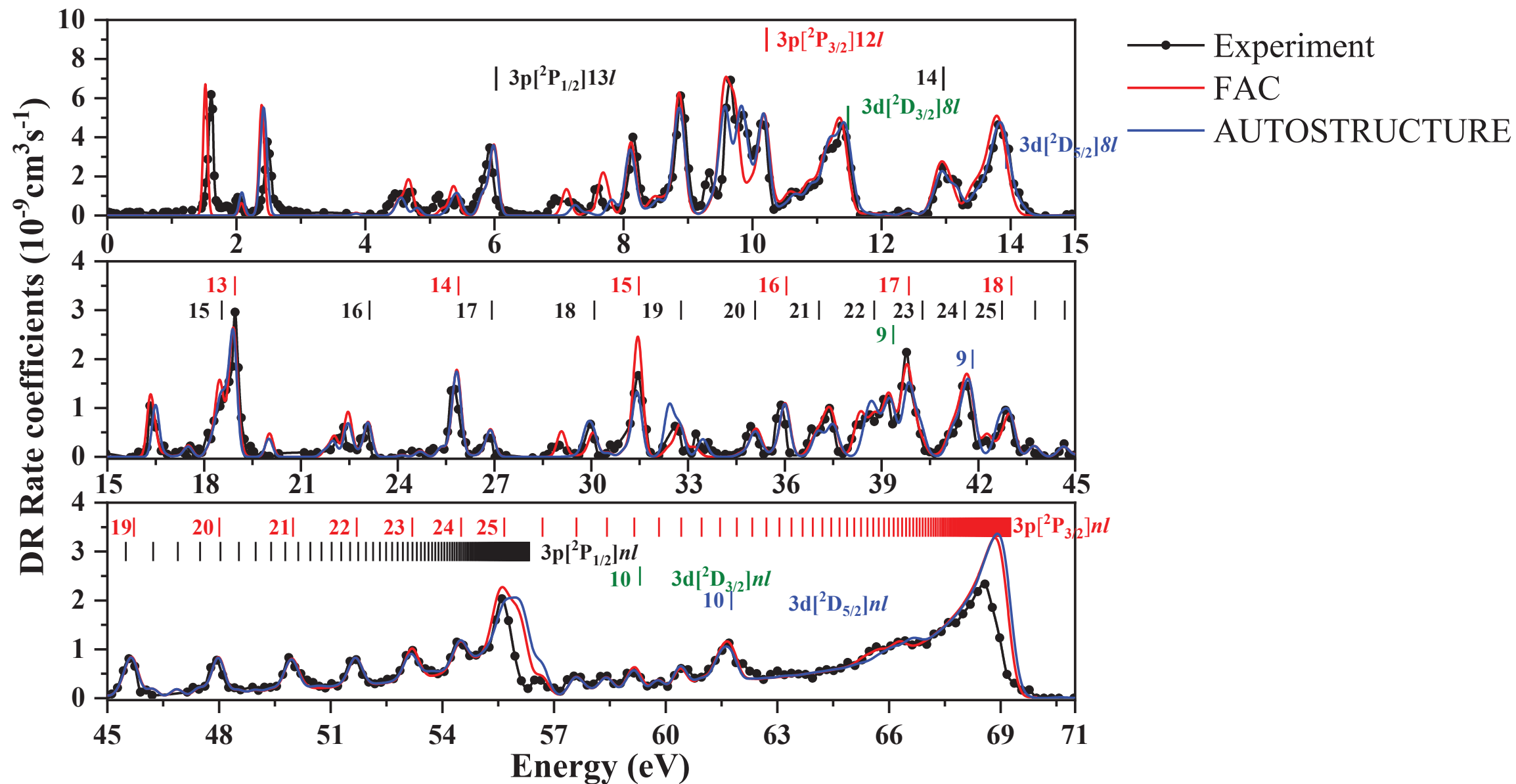
E_{exc} donates the core excitation energy

R donates the Rydberg constant

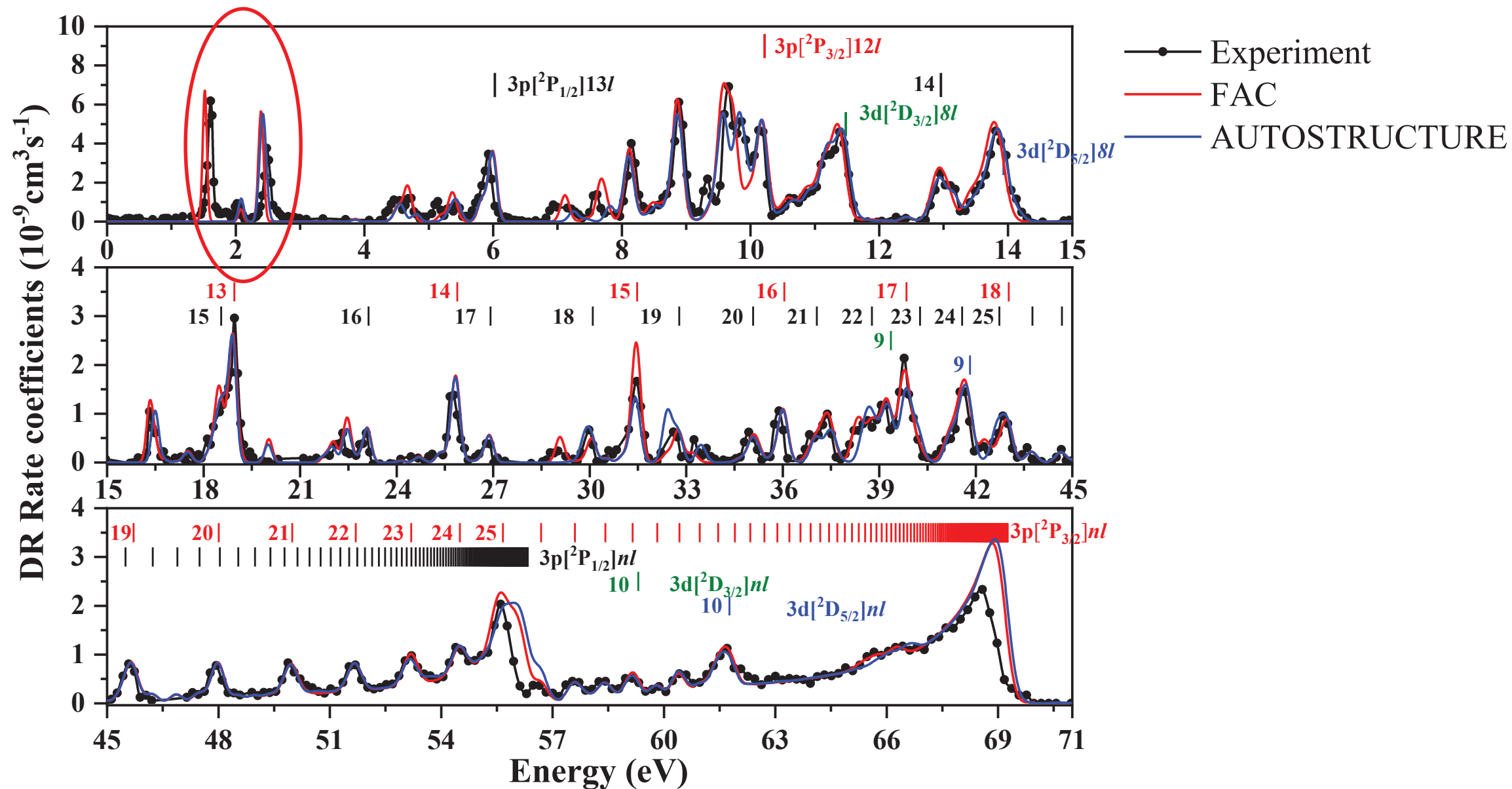
Z_{eff} donates the charge state of ion

- The energy scale was recalibrated by a factor of 1.022 to achieve agreement with $3p[{}^2P_{3/2}]nl$ series limit at 69.267 eV.
- By fitting the resolved DR resonances with a flattened Maxwellian, electron temperatures of $k_B T_{\parallel} = 0.32 \text{ meV}$ and $k_B T_{\perp} = 12.50 \text{ meV}$ were obtained.

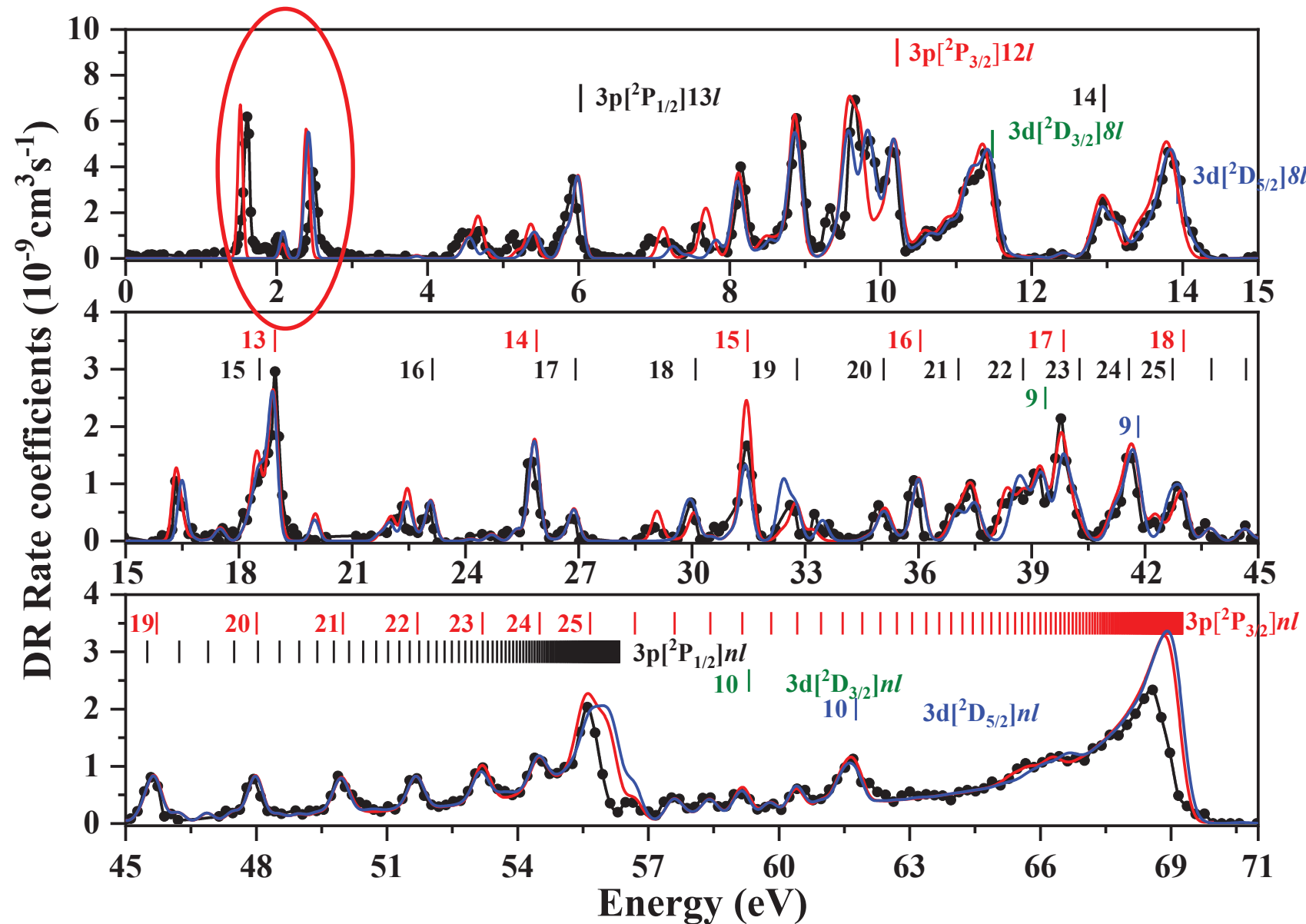
Experimental results: Na-like Kr^{25+}



Experimental results: Na-like Kr^{25+}



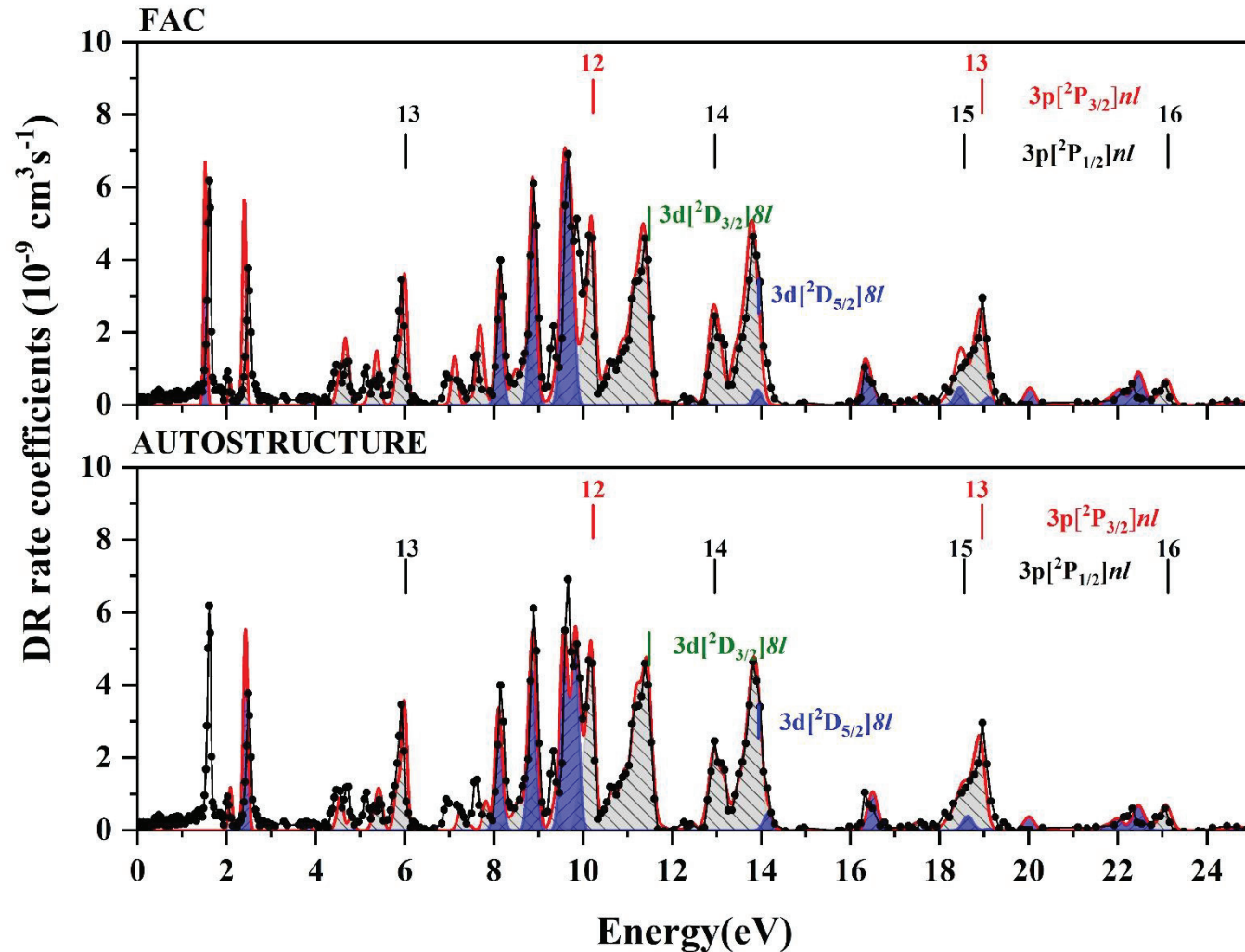
Experimental results: Na-like Kr^{25+}



—●— Experiment
— FAC
— AUTOSTRUCTURE

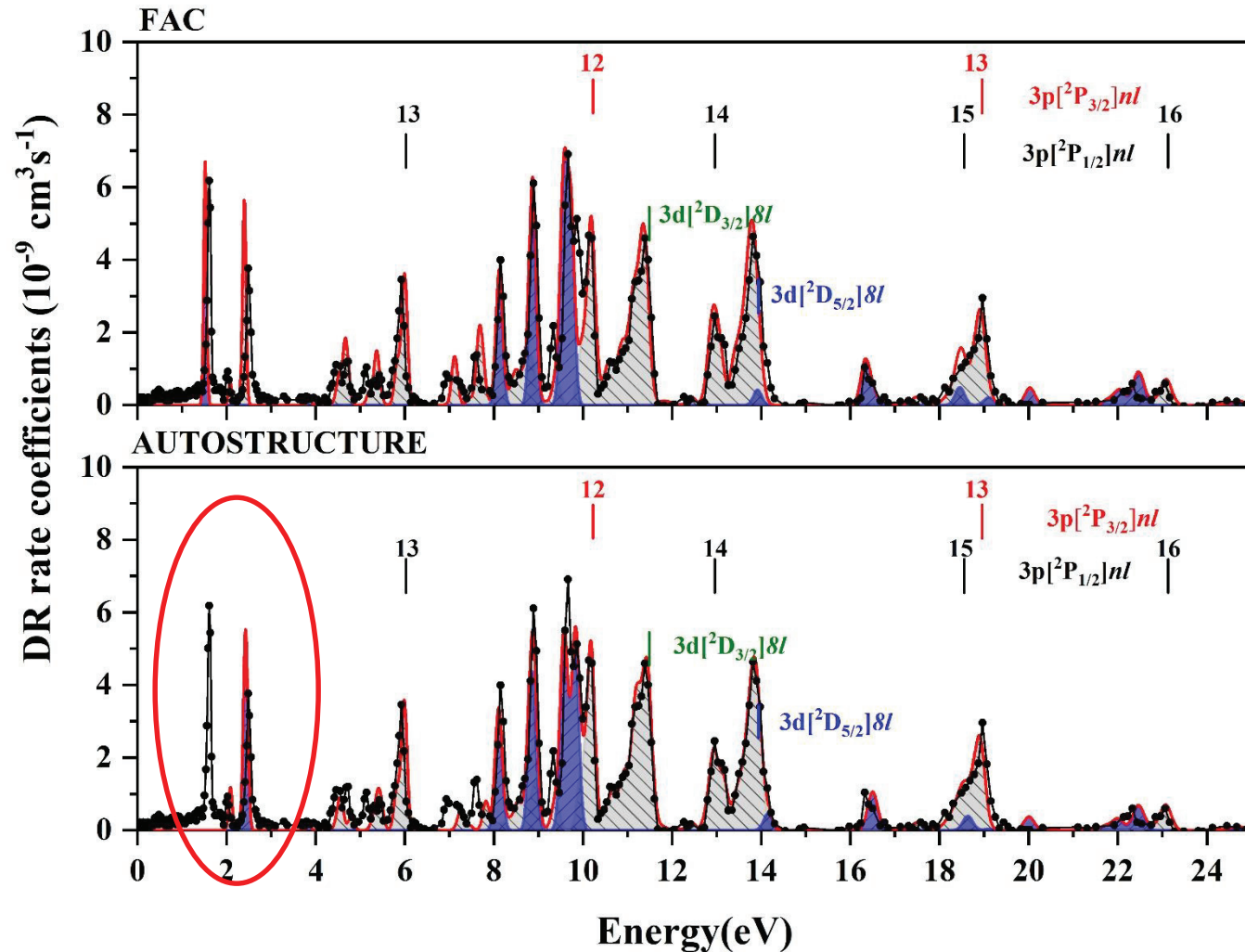
Note: in the present spectra, the DR resonances associated with 3-4 core transition were shifted with - 1.54 eV for AUTOSTRUCTURE Calculation.

Experimental results: Na-like Kr²⁵⁺



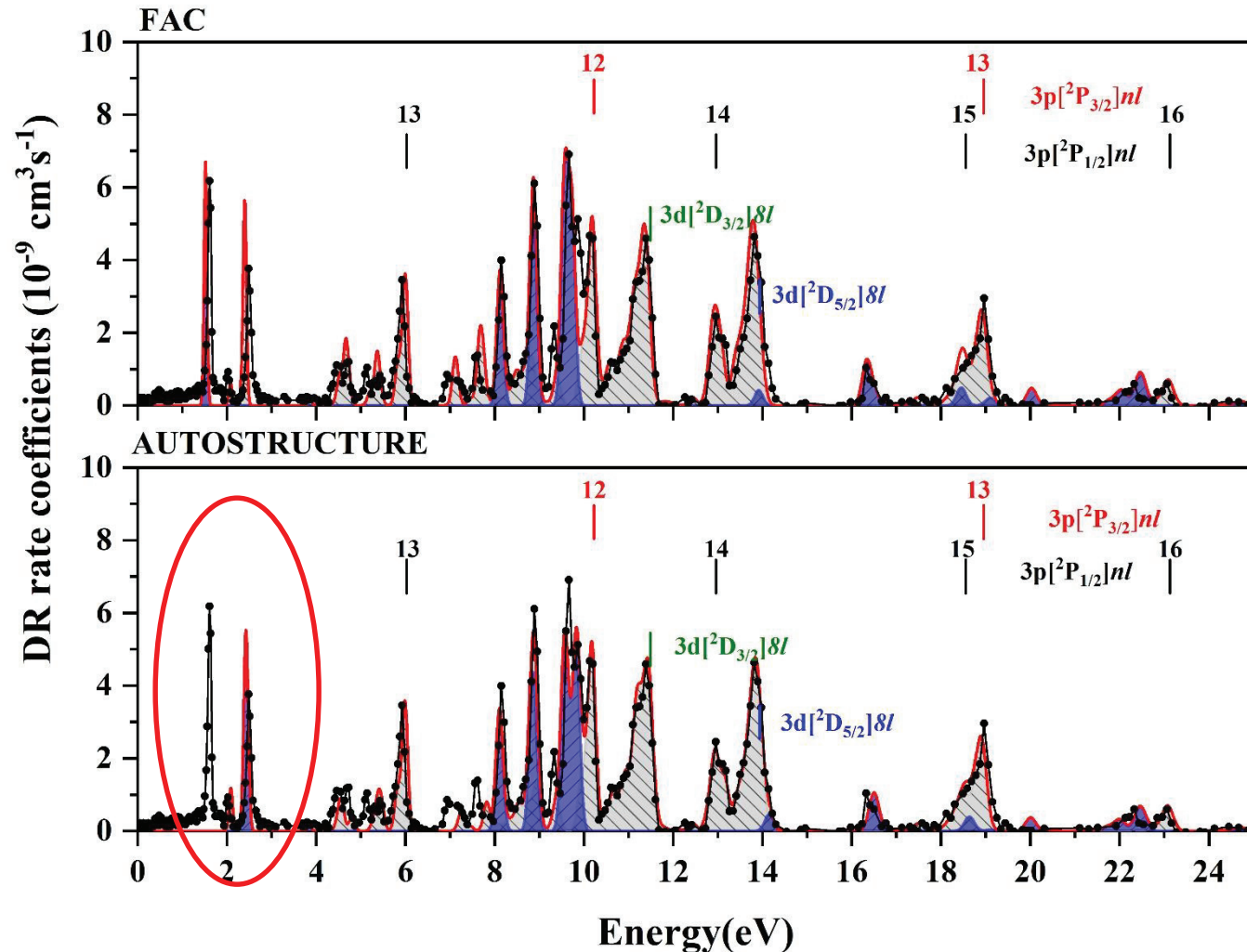
- The connected black dotted curve donates the measured background-subtracted DR spectrum.
- The red solid curve donates the FAC AUTOSTRUCTURE calculated total DR rate coefficient in each graph.
- The grey areas donate the DR rate coefficient associated with $3l \rightarrow 4l$ ($\Delta N=1$) core excitation.
- The blue areas donate the DR rate coefficient associated with $3s \rightarrow 3l$ ($\Delta N=0$) core excitation.

Experimental results: Na-like Kr²⁵⁺



- The connected black dotted curve donates the measured background-subtracted DR spectrum.
- The red solid curve donates the FAC AUTOSTRUCTURE calculated total DR rate coefficient in each graph.
- The grey areas donate the DR rate coefficient associated with 3l → 4l (ΔN=1) core excitation.
- The blue areas donate the DR rate coefficient associated with 3s → 3l (ΔN=0) core excitation.

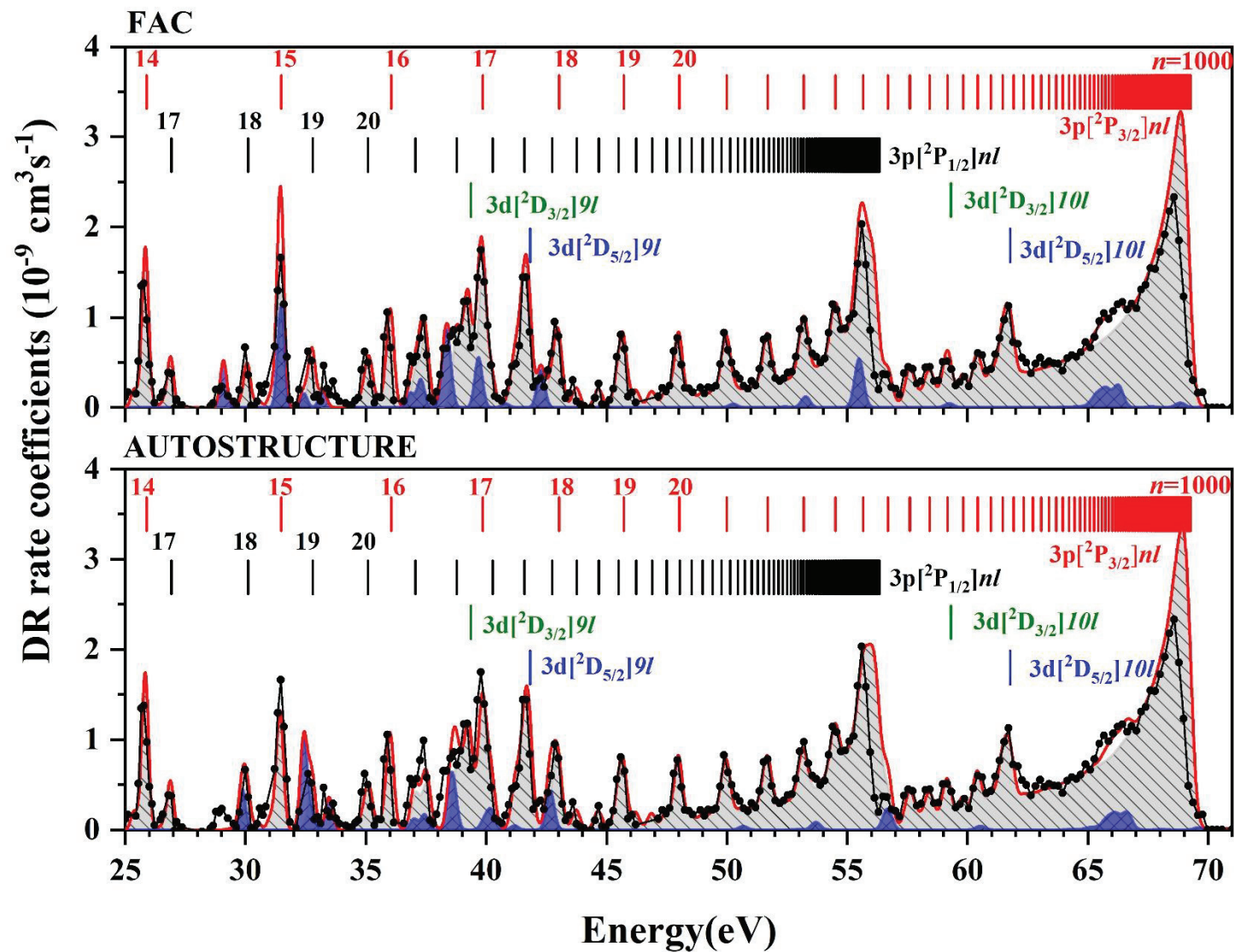
Experimental results: Na-like Kr²⁵⁺



- The connected black dotted curve donates the measured background-subtracted DR spectrum.
- The red solid curve donates the FAC AUTOSTRUCTURE calculated total DR rate coefficient in each graph.
- The grey areas donate the DR rate coefficient associated with 3l→4l (ΔN=1) core excitation.
- The blue areas donate the DR rate coefficient associated with 3s→3l (ΔN=0) core excitation.

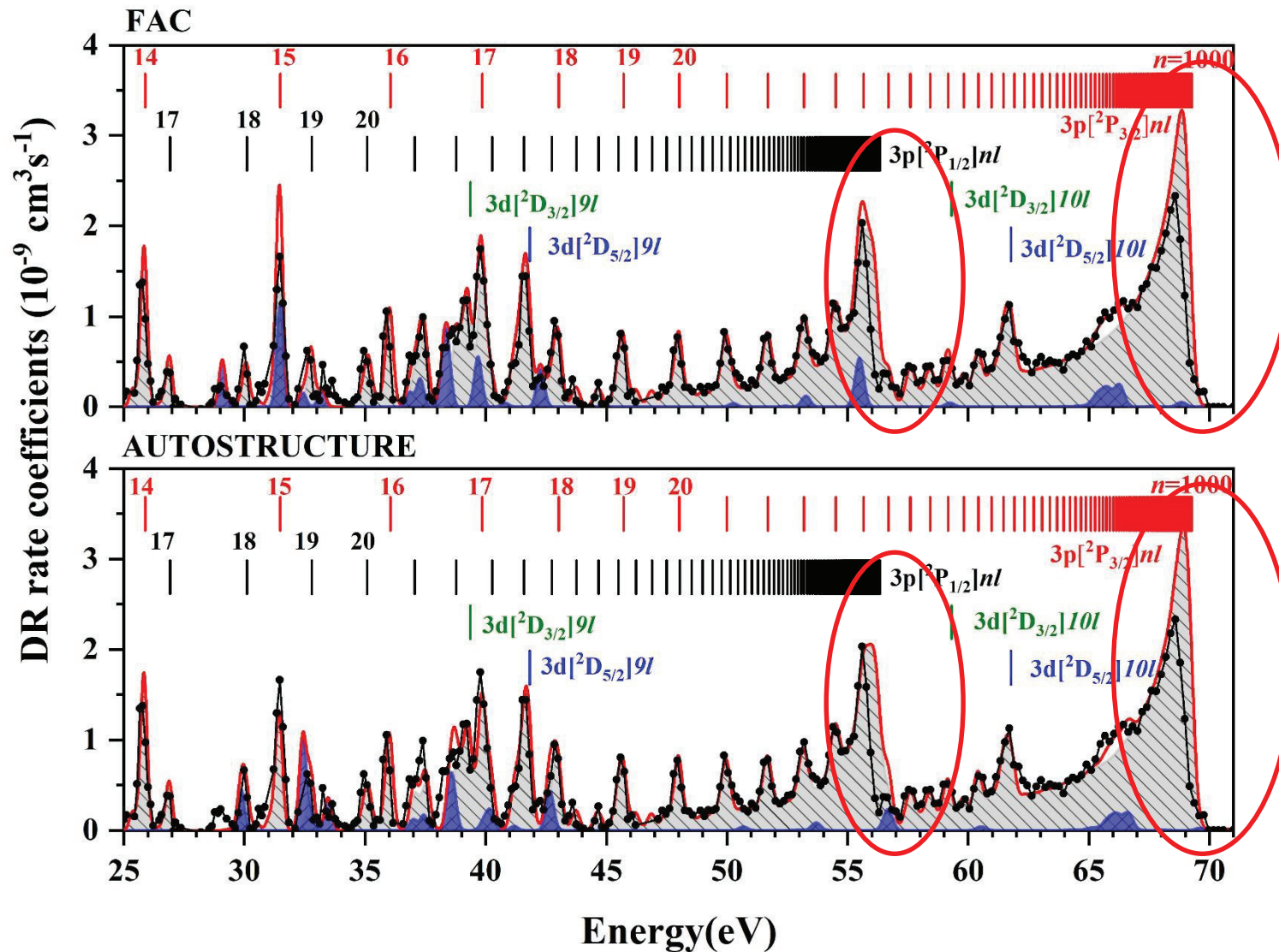
Note: the DR resonances associated with 3-4 core transition were shifted with -1.54 eV [AUTOSTRUCTURE]

Experimental results: Na-like Kr^{25+}



- Same as last figure, but for the energy range of 25-70 eV.

Experimental results: Na-like Kr²⁵⁺



Field- ionization

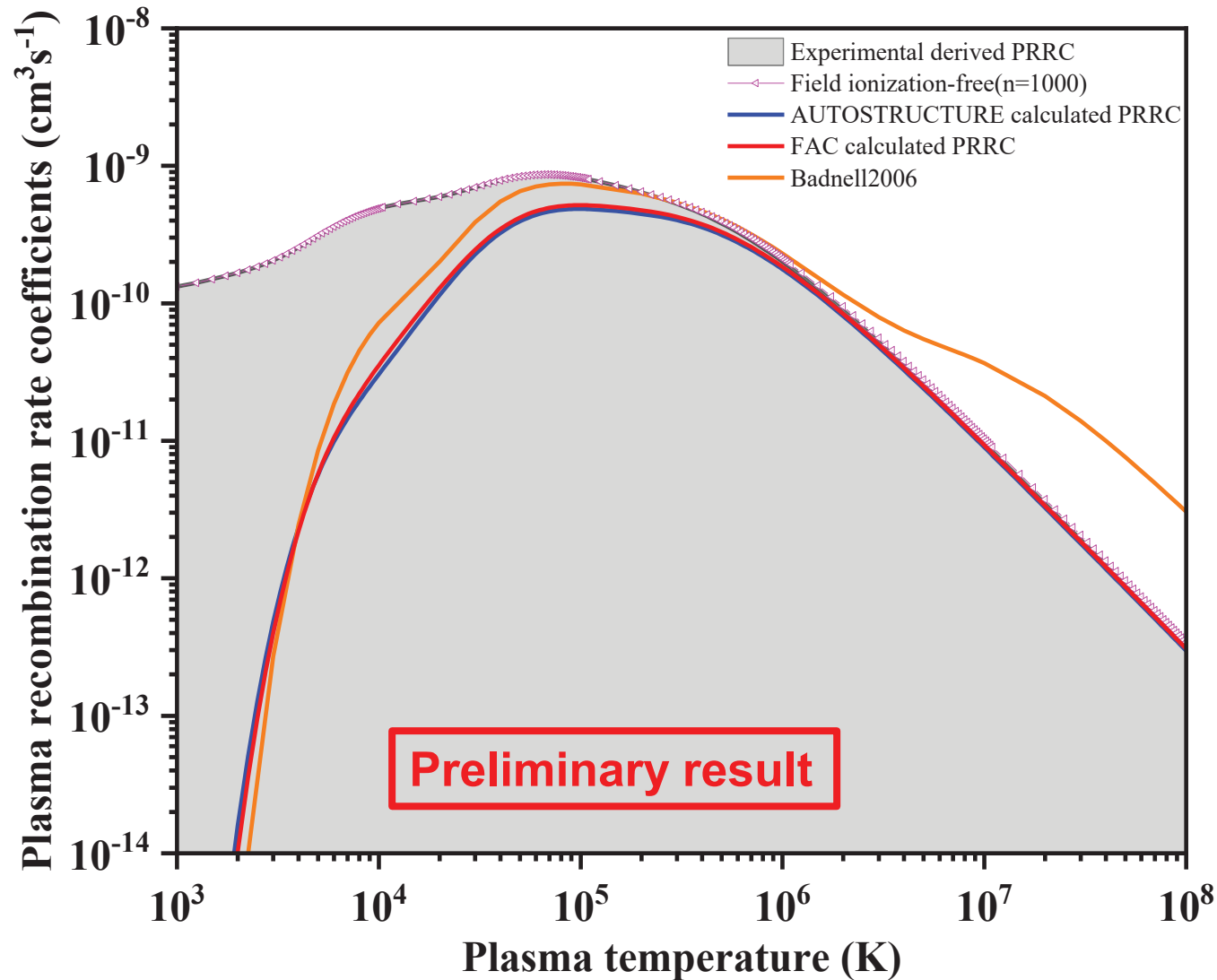
Field ionization of the loosely bound high Rydberg electron in the recombined ions can result from the **motional electric fields** that the ions experience inside the storage ring bending magnets

$$n_{cutoff} \approx \left[6.2 \times 10^8 \left(\frac{v}{cm} \right) \frac{q^3}{v_i \times B} \right]^{1/4}$$

q is the charge state of ion beam;
 v_i donates the mean velocity of ion beam;
 B is the magnet filed strength;

- Same as last figure, but for the energy range of 25-70 eV.

Experimental results: Na-like Kr^{25+}



- The solid red curve denotes the plasma DR rate coefficients derived from the presently FAC code calculated DR rate coefficients.
- The solid blue curve denotes the plasma DR rate coefficients derived from the presently AUTOSTRUCTURE calculated DR rate coefficients.
- The solid orange denotes the previous data calculated by Badnell et al., which included both $\Delta N=0$ and $\Delta N=1$ DR rate coefficients.
- The pink triangle solid line is the field-ionization-free resonant plasma DR rate coefficients.

Experimental results: Na-like Kr²⁵⁺

In order to facilitate the plasma modelers and astrophysicists to use our data, the presently experimentally derived and the theoretical calculated PRRC have been parameterized.

$$\alpha(T_e) = T_e^{-3/2} \sum_i^n c_i \cdot \exp\left(-\frac{E_i}{kT_e}\right)$$

No. <i>i</i>	<i>n</i> _{cutoff}		<i>n</i> _{max} =1000	
	<i>c_i</i>	<i>E_i</i>	<i>c_i</i>	<i>E_i</i>
1	0.173[0]	60.922[0]	1.454 [-4]	0.535[0]
2	0.071[0]	33.311[0]	1.702[-5]	0.127[0]
3	0.023[0]	7.562[0]	0.024[0]	7.627[0]
4	0.002[0]	1.539[0]	0.074[0]	33.806[0]
5	0.029[00]	3.101[0]	0.193[0]	61.738[0]
6	1.445[-4]	0.533[0]	0.003[0]	3.128[0]
7	0.048[0]	12.817[0]	0.048[0]	12.932[0]
8	1.692[0]	0.127[0]	0.002[0]	1.543[0]

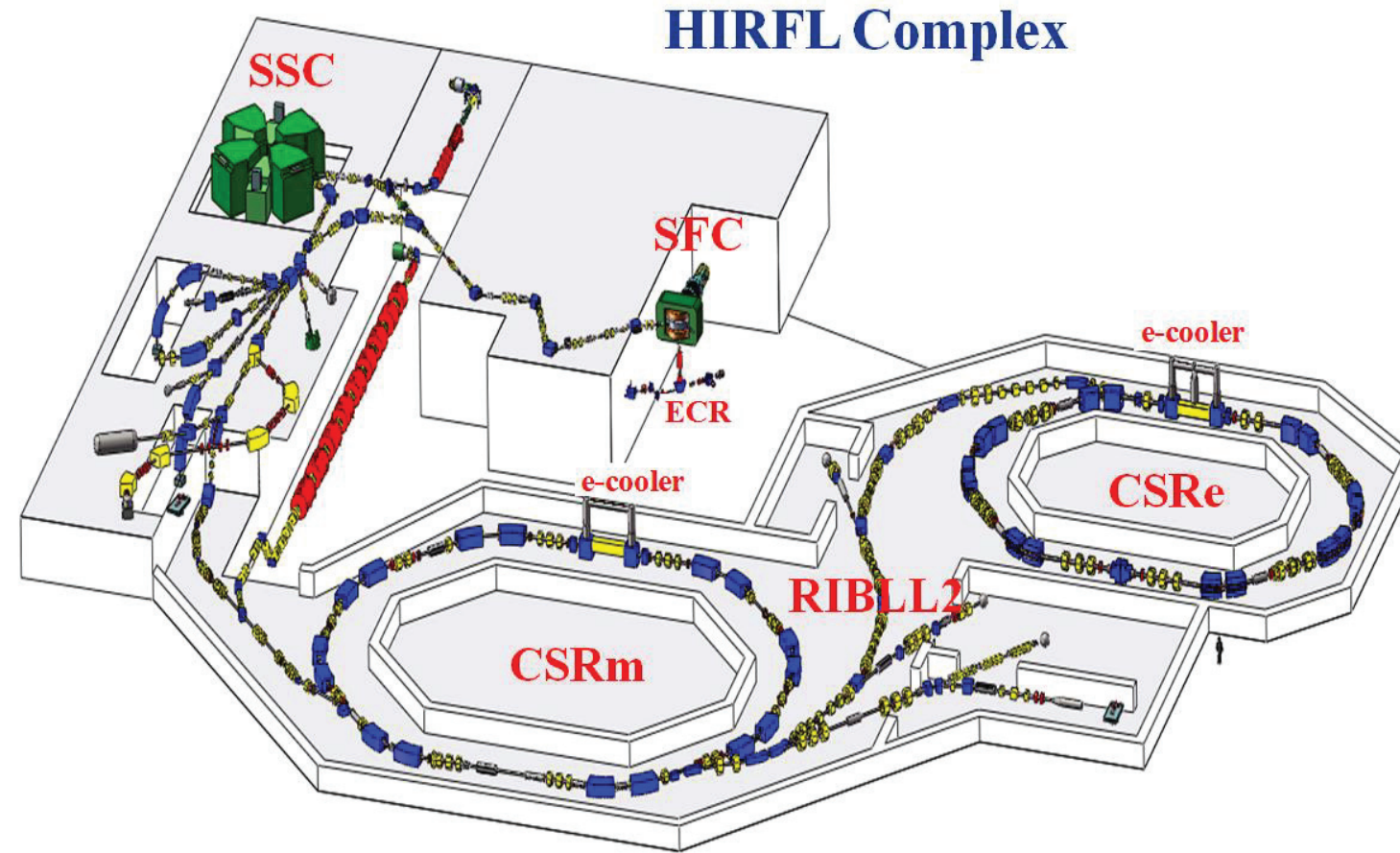
Note: Numbers in the squared brackets are powers of 10.

4. Summary and outlook

Summary

- ❑ DR spectrum of Na-like Krypton was measured first time;
- ❑ Both $\Delta N=0$ and $\Delta N=1$ resonances were observed in the measured spectrum;
- ❑ This work renewed the calculation of DR spectra for Na-like Kr^{25+} by AUTOSTRUCTURE.
- ❑ The plasma rate coefficients was derived and compared with the available theoretical calculation;
- ❑ The DR experiments at the CSRm pave the way for our upcoming DR experiments at the CSRe and also on the future facility HIAF;

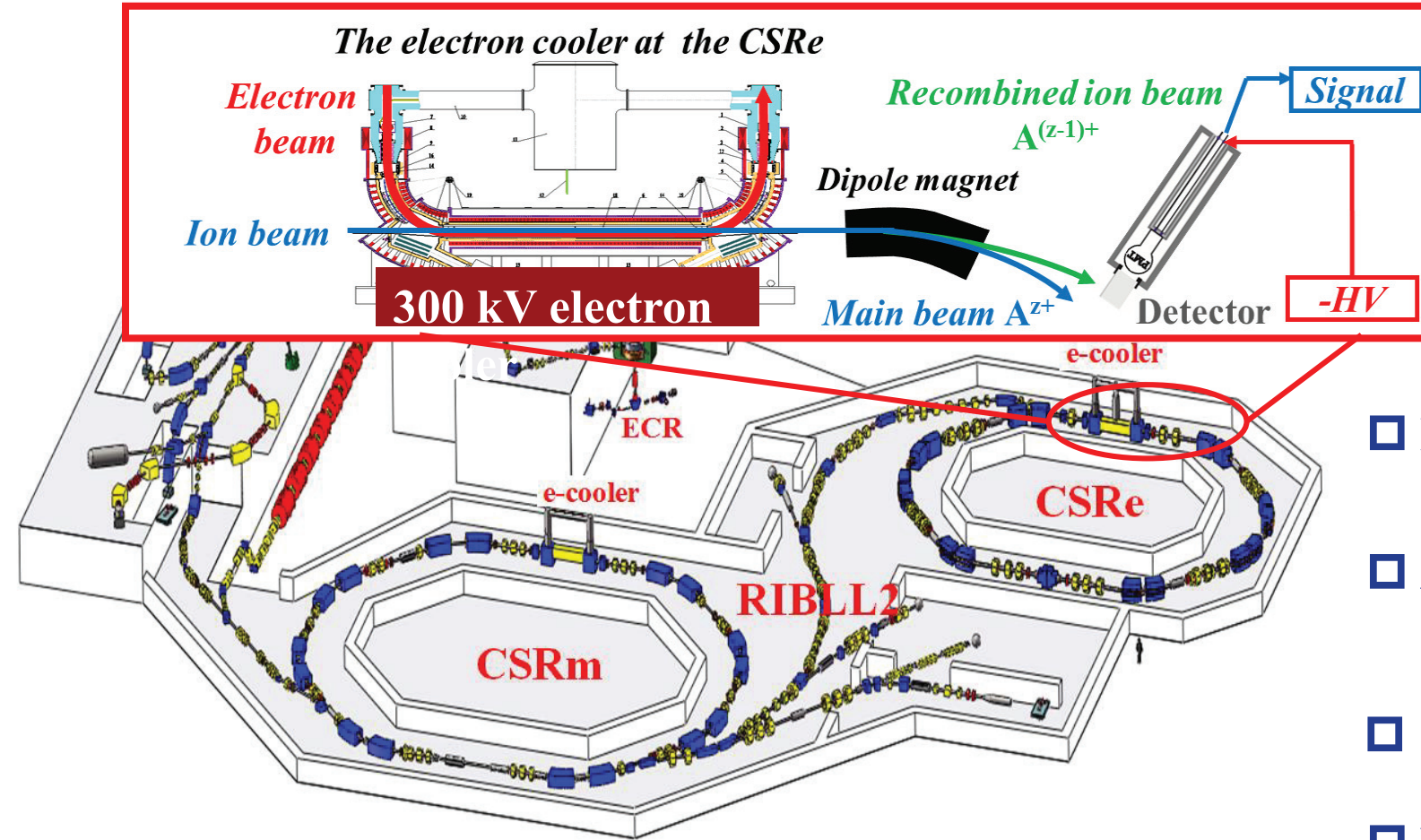
Outlook-upcoming DR experiment at the CSRe



Sketch view of DR experiment at the CSRe

- ❑ Much broader detuning energy range
[± 30 kV~1500 eV ($U^{89+}@250\text{MeV/u}$)]
- ❑ Astrophysics relevant DR spectroscopy
[H-like, He-like, Li-like, Be-like]
- ❑ DR data of W^{q+} for the ITER project
- ❑ DR research on radioactive ion beams
[CSRm + RIBLL2 + CSRe]

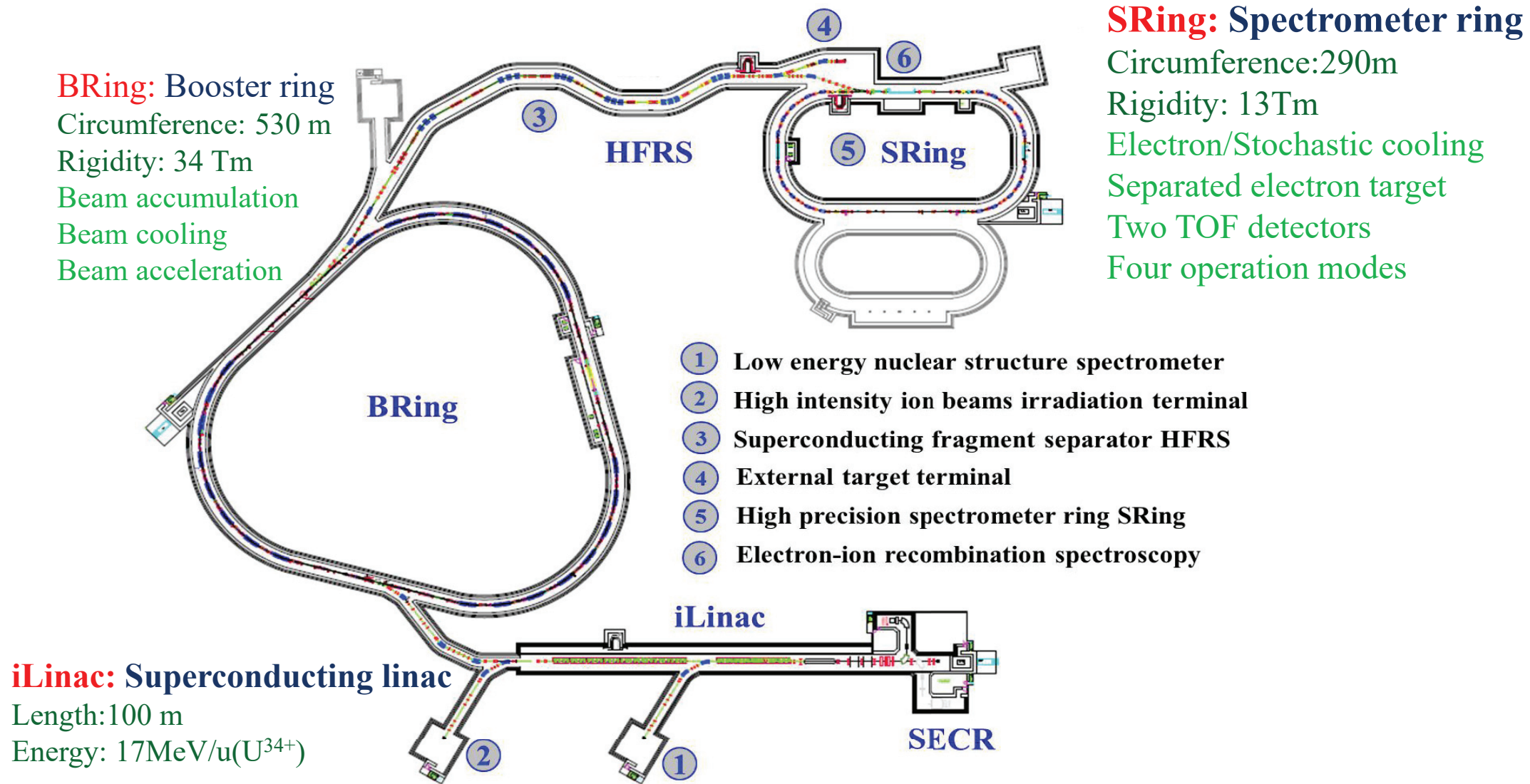
Outlook-upcoming DR experiment at the CSRe



- ❑ Much broader detuning energy range
[± 30 kV~1500 eV (U^{89+} @250MeV/u)]
- ❑ Astrophysics relevant DR spectroscopy
[H-like, He-like, Li-like, Be-like]
- ❑ DR data of W^{q+} for the ITER project
- ❑ DR research on radioactive ion beams
[CSRm + RIBLL2 + CSRe]

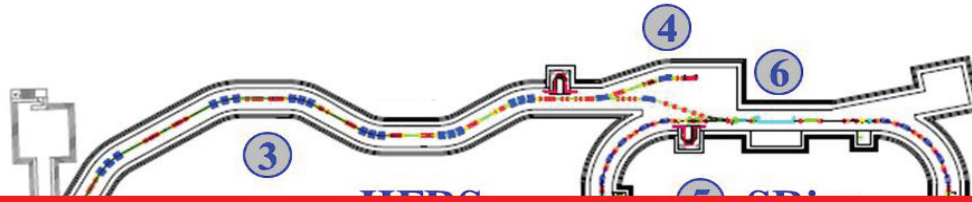
Sketch view of DR experiment at the CSRe

Outlook-future DR experiment at the HIAF-SRing



Outlook-future DR experiment at the HIAF-SRing

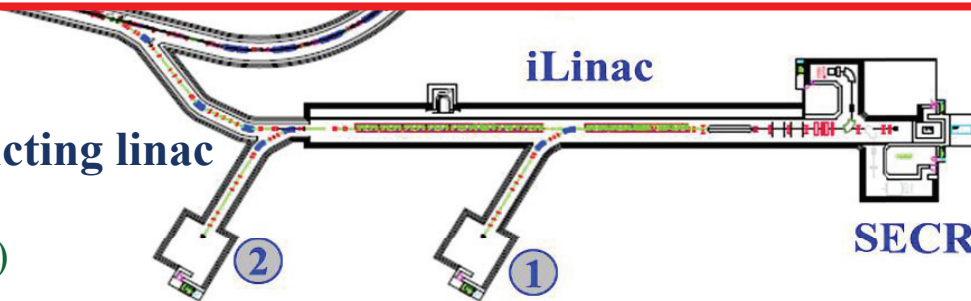
BRing: Booster ring
Circumference: 530 m



SRing: Spectrometer ring
Circumference: 290m
Rigidity: 13Tm
Electron/Stochastic cooling

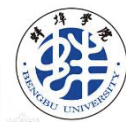
The highlight of DR experiments at HIAF
electron-cooler & an ultra-cold electron-target
a unique research platform
electron-ion recombination spectroscopy!

iLinac: Superconducting linac
Length: 100 m
Energy: 17MeV/u(U^{34+})



DR international cooperation group

IMPCAS, Lanzhou	Z. K. Huang, W. Q. Wen, H. B. Wang, S. Mahmood, N. Khan, X. Y. Chai, L. J. Dou, X. L. Zhu, D. M. Zhao, L. J. Mao, Y. J. Yuan, J. Li, X. M. Ma, J. C. Yang, X. Ma;
USTC, Hefei	X. Xu, S. X. Wang, W. Q. Xu, L. F. Lin;
Uni. Fudan, Shanghai	T.H. Xu, K. Yao, Y. Yang;
GSI, Darmstadt	Th. Stöhlker, C. Brandau, A. Gumberidze, Yu. Litvinov, M. Steck;
Uni. Giessen	A. Müller, S. Schippers;
BINP, Novosibirsk	V. V. Parkhomchuk, V. B. Reva;
IAPCM, Beijing	C. Y. Li, X. Y. Han, J. G. Wang;
NWNU, Lanzhou	C. Z. Dong, L. Y. Xie;
Uni. Strathclyde	N. R. Badnell, Simon Preval;



Thanks for your kind attention!



Thank You!

Thanks for your kind attention!