

Latest Results of Experimental Approach to Ultra-cold Beam at S-LSR



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Contents

1. Electron Cooling

1D Ordering of 7 MeV proton beam

Bio-medical Vertical Irradiation Port with Short Bunch

2. Experimental Demonstration of **Active Multi-dimensional** Laser Cooling of 40 keV $^{24}\text{Mg}^+$ ion beam

3. Improvement of Laser Cooling Efficiency by **suppression** **of IBS** with Scraping

4. Comparison of Attained Temperatures



Compact Cooler Ring S-LSR

– Circumference 22.56m

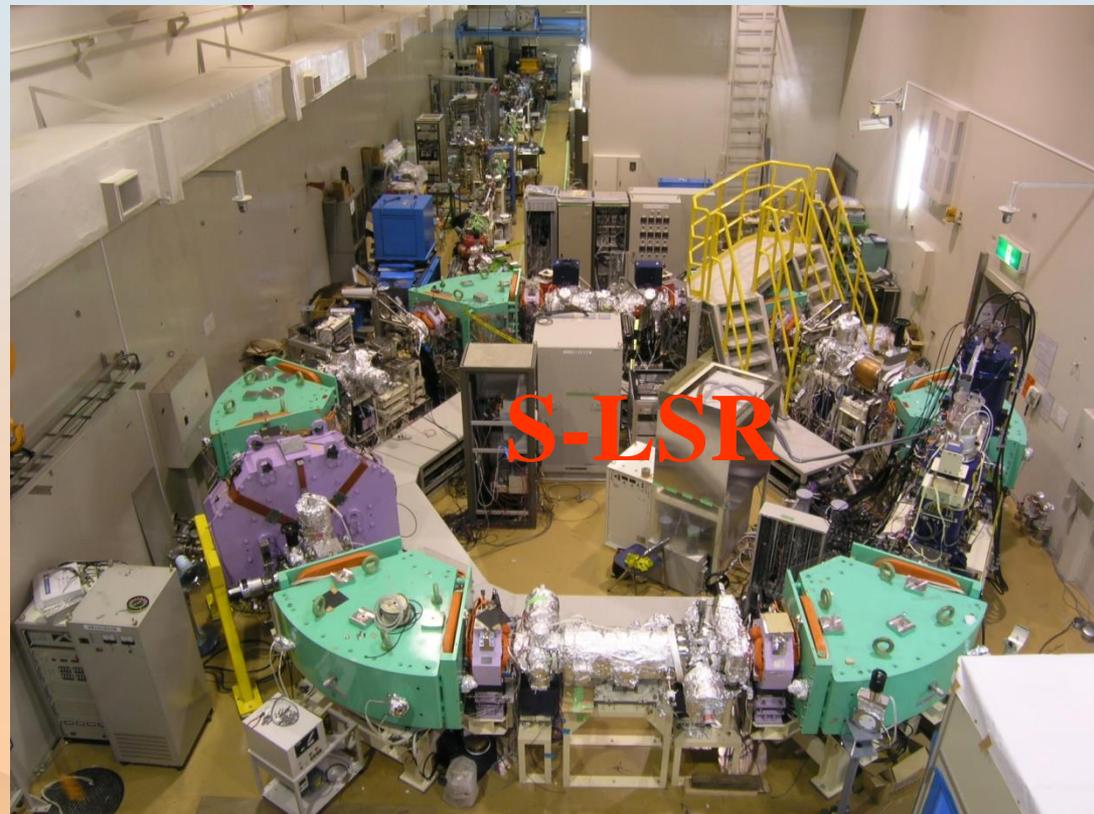
– Straight Section Length 1.86m

E-cooling modes

– Protons 7MeV
($E_e=3.8\text{keV}$)

⚙ Laser cooling

– $^{24}\text{Mg}^+$ 40 keV
($\lambda=282\text{ nm}$)



In operation since October, 2005

Main Parameters of S-LSR

Circumference	22.557 m
Average radius	3.59 m
Length of straight section	1.86 m
Number of periods	6
Betatron Tune	
Crystalline Mode	Normal Operation Mode
1.45 (H), 1.44 (V)	1.872(H), 0.788 (V): EC
	2.068(H), 1.105, 1.070 (V): LC
Bending Magnet	(H-type)
Maximum field	0.95 T
Curvature radius	1.05 m
Gap height	70 mm
Pole end cut	Rogowski cut+Field clamp
Deflection Angle	60°
Weight	4.5 tons
Quadrupole Magnet	
Core Length	0.20 m
Bore radius	70 mm
Maximum field gradient	5 T/m

ESR at GSI, by M. Steck

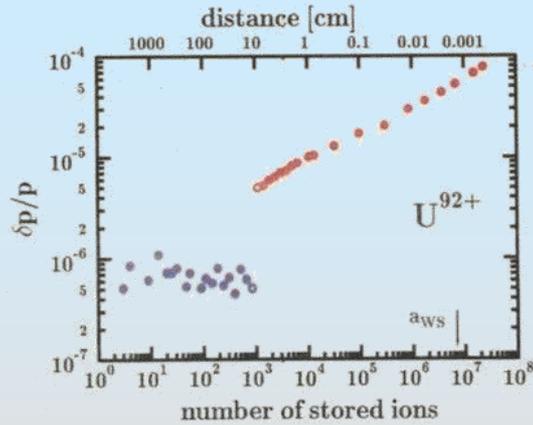


Figure 2. Experimental momentum spreads from Schottky signals vs. number of stored ions in the ESR for electron cooled U^{92+} ions at 240 MeV/u. a_{WS} indicates the Wigner-Seitz radius of eq.(3). (after ref. ⁹)

CRYRING at Stockholm, by H. Danared

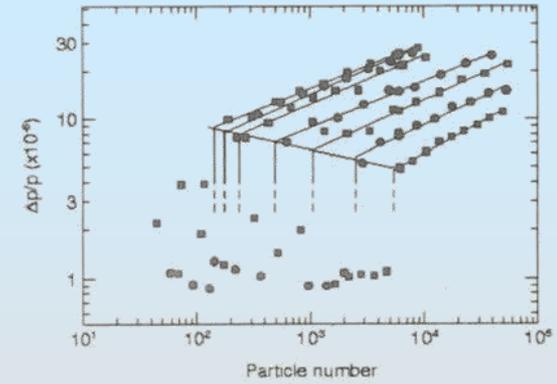


Fig. 5: Relative momentum spread as a function of particle number for the lowest seven electron densities represented in Fig. 2. The density increases from the upper left to the lower right. For each density, a line is fitted to the data points. A line is also drawn through the points corresponding to the transition to the ordered state. (The use of different symbols is just to help identifying which points belong to same electron density.)

ESR at GSI, by M. Steck

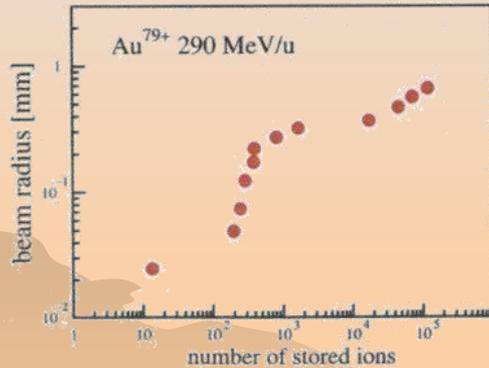


Figure 3. Beam radius measured with a beam scraper vs. number of stored ions in the ESR for electron cooled Au^{79+} ions at 290 MeV/u (from ref. ¹⁰).

NAP-M at BINP, Novosibirsk by V.V. Parkhomchuk

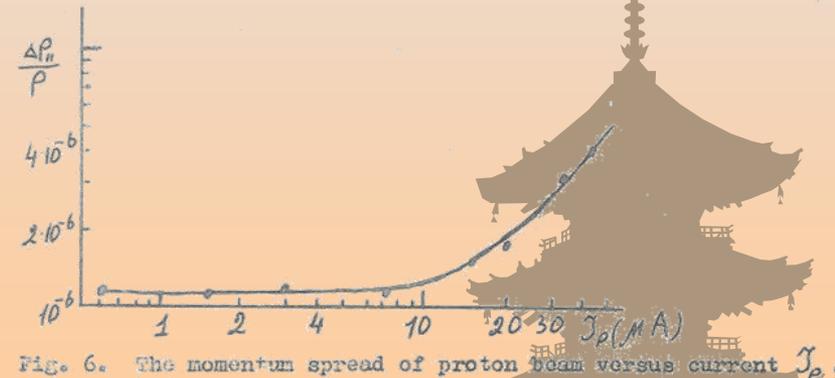


FIG. 6. The momentum spread of proton beam versus current I_p .

Ring Layout

Induction Accelerator

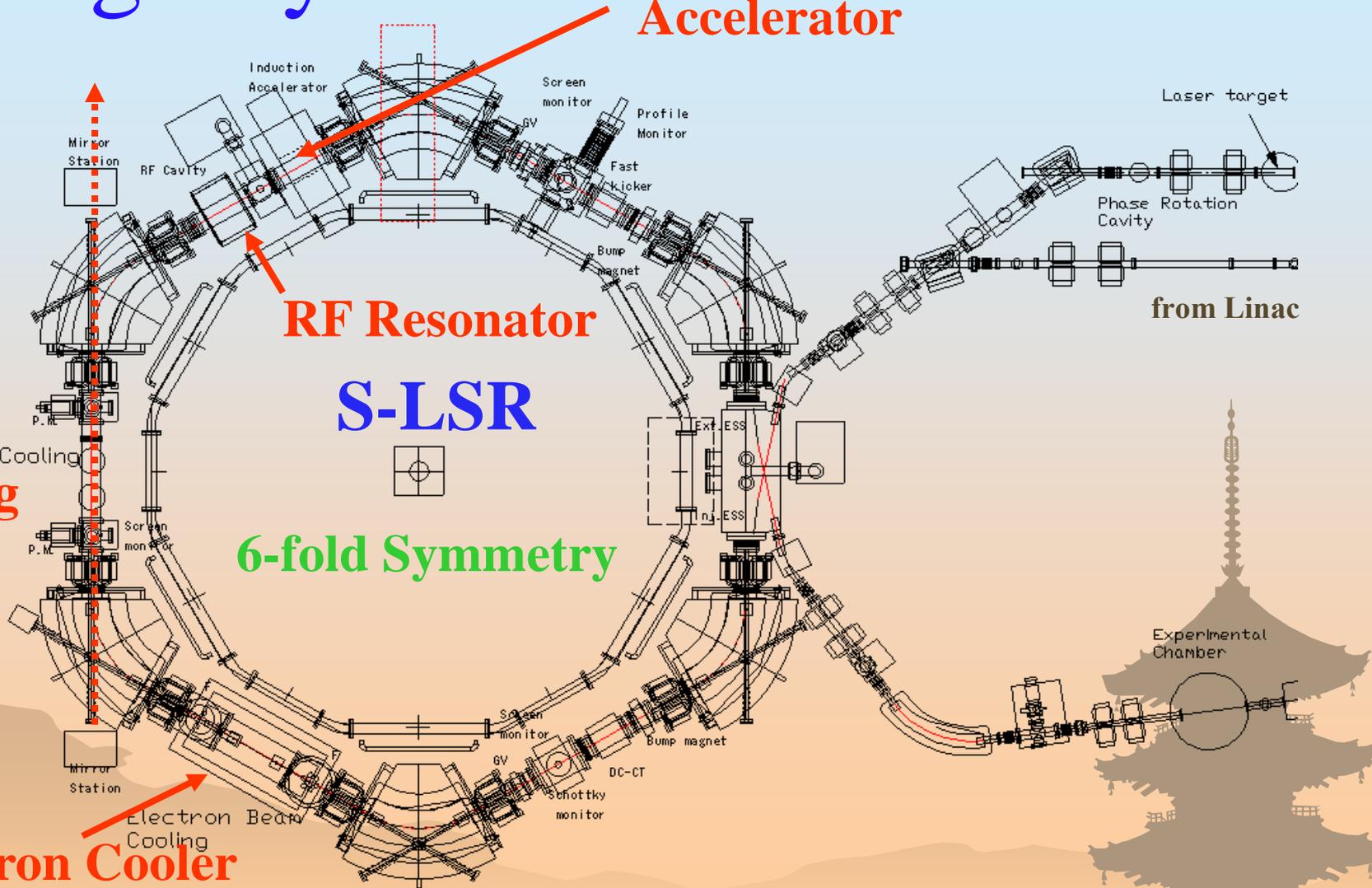
Laser Cooling

RF Resonator

S-LSR

6-fold Symmetry

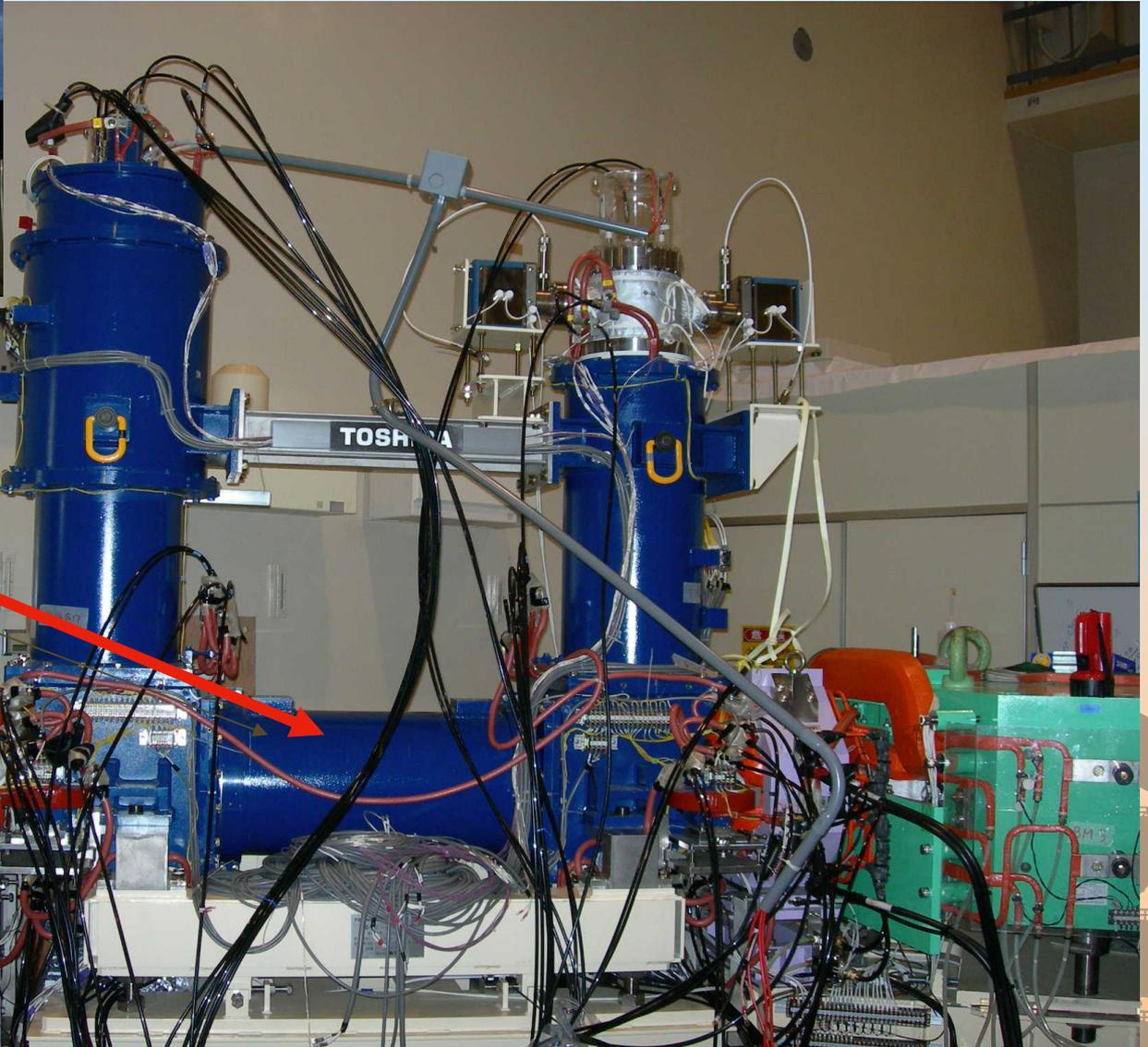
Electron Cooler



Electron Cooler installed in S-LSR

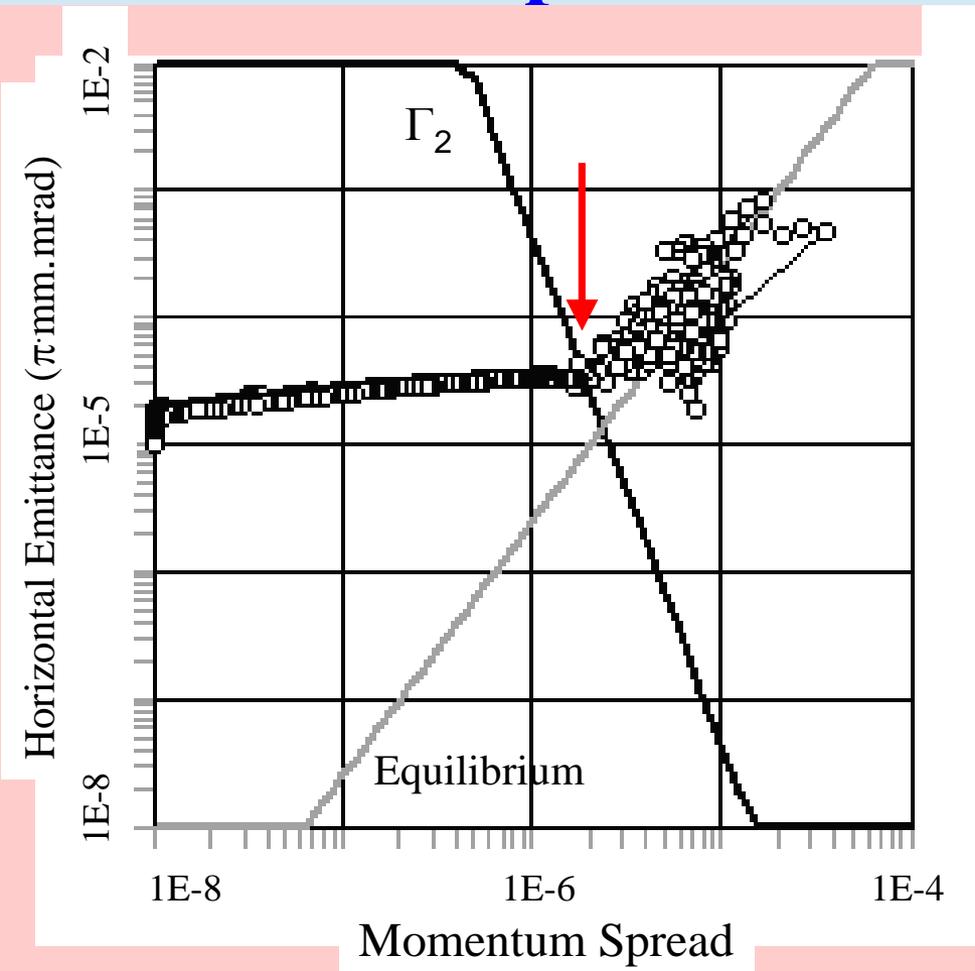


Dr. Hicham Fadil



Cooler Solenoid

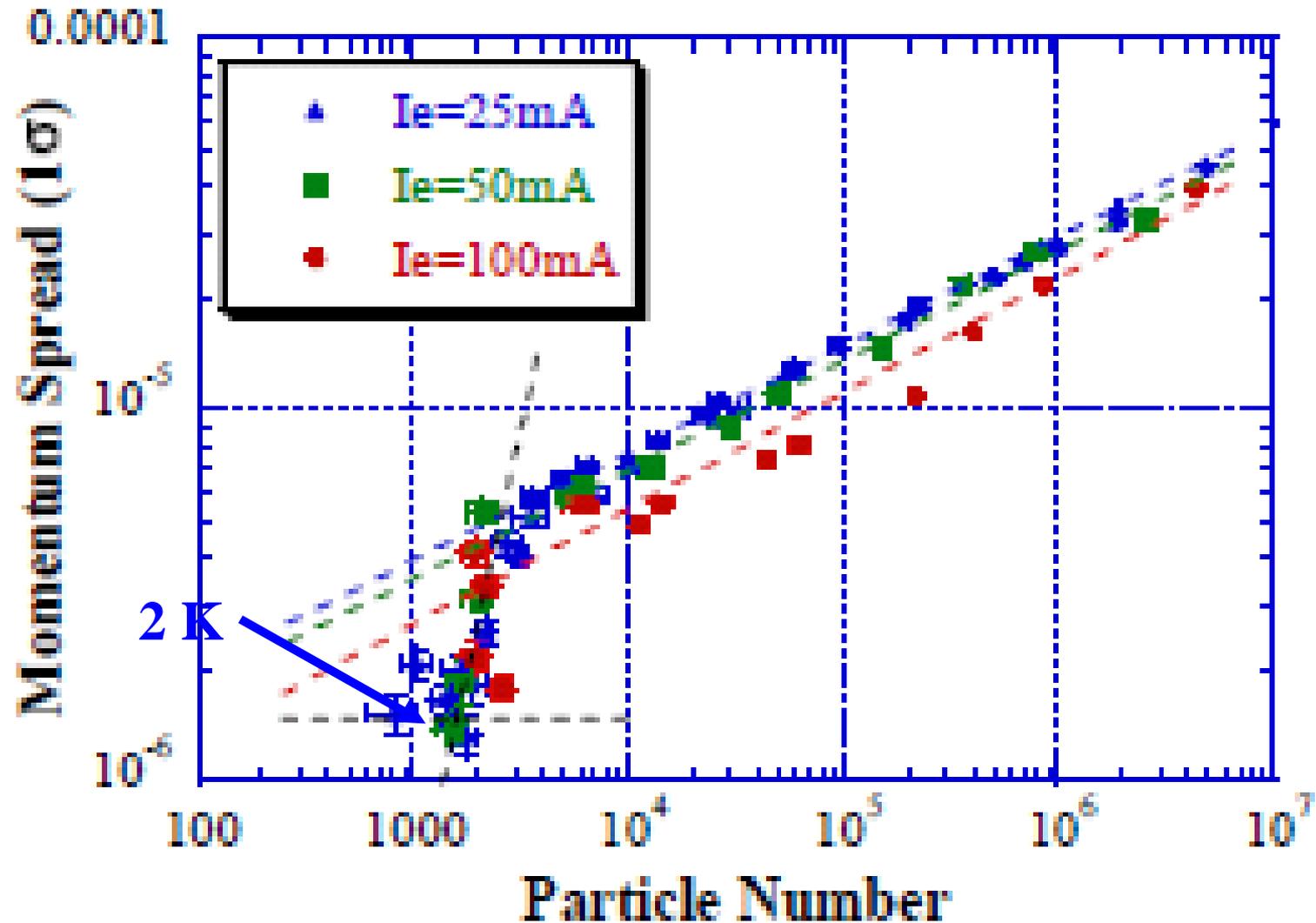
Simulation with Betacool predicts 1D ordering of 7 MeV proton at S-LSR -particle number of 3000-



$$\Gamma_2 \equiv \frac{Z^2 e^2}{4\pi\epsilon_0 \sigma_{\perp} k_B T_{\parallel}}$$

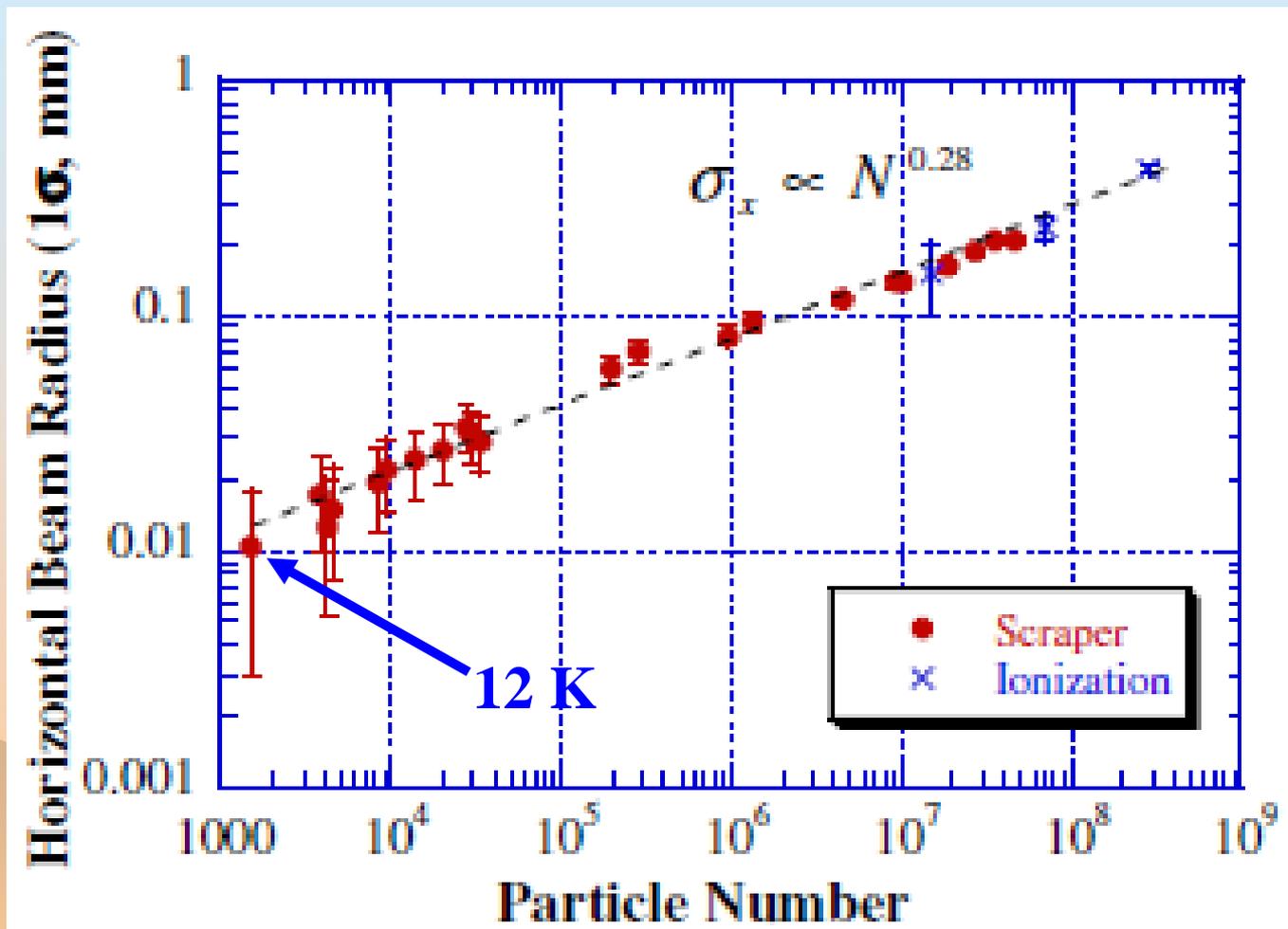
Collaboration with JINR, Dubna
by Prof. I. Meshkov
and Dr. A. Smirnov et al.

Phase Transition to 1D Ordered State

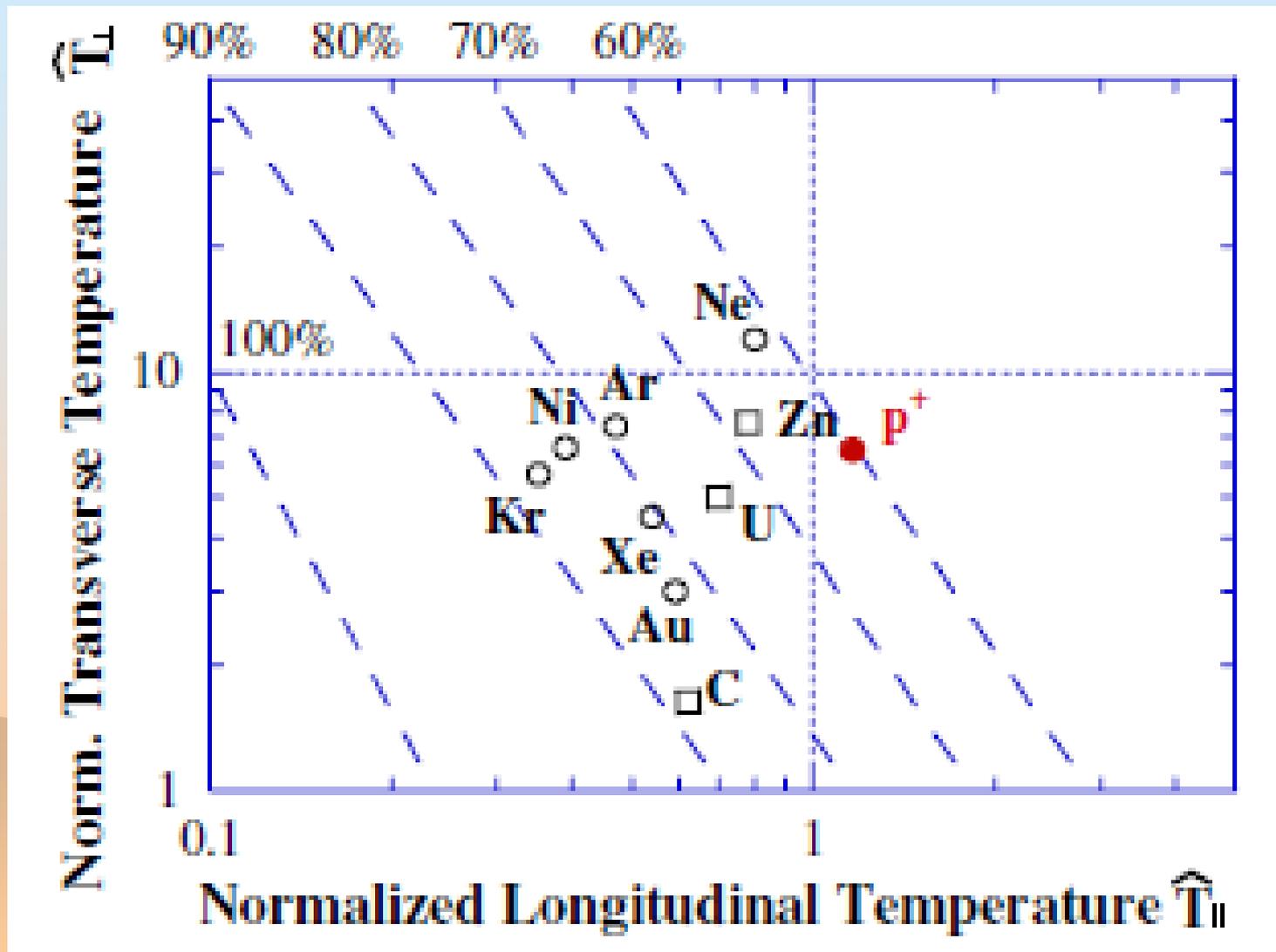


T. Shirai et al., PRL, 98 (2007) 204801

Horizontal Beam Size Reduction by Electron Cooling



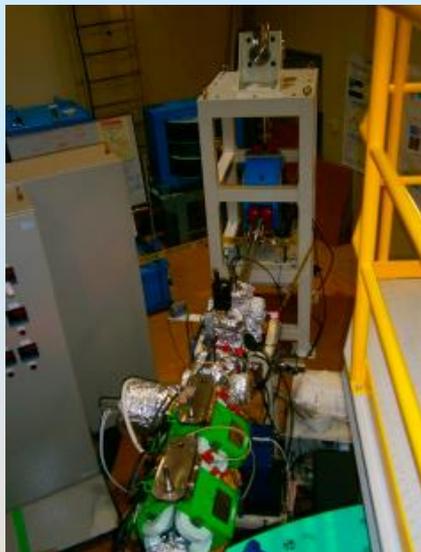
Reflection Probability of Ions made Phase Transition



Construction of Vertical Beam Irradiation Port



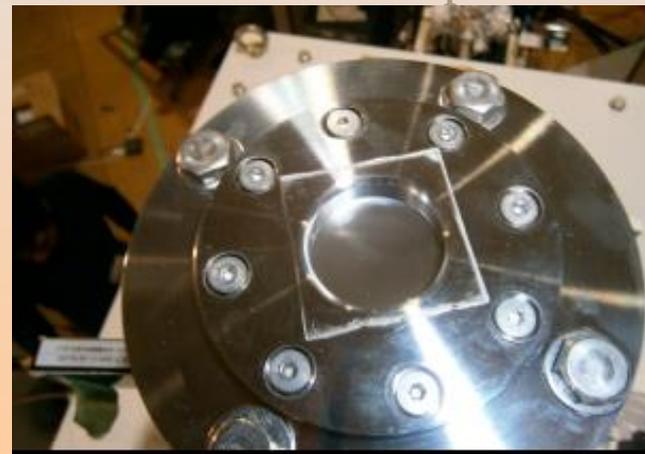
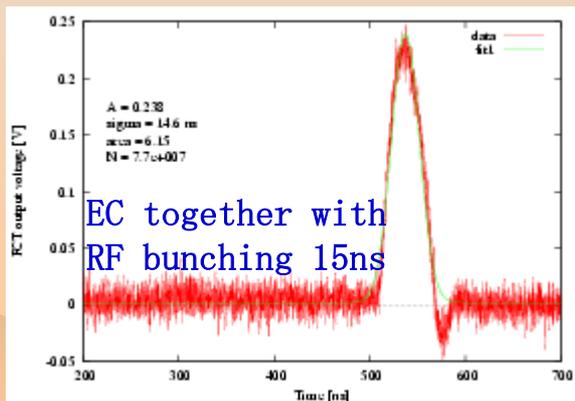
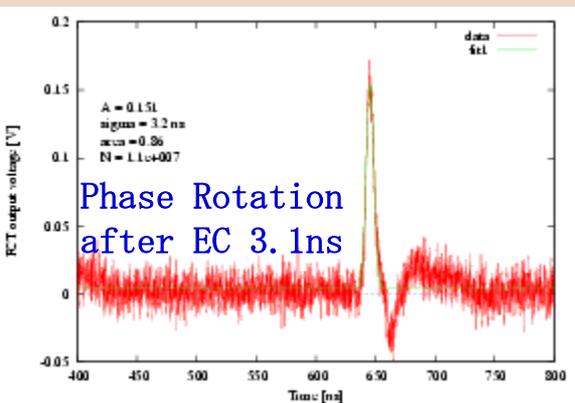
Completed Beam Line



Profile measurement after extraction into air through havar foil



Irradiation Strength Analysis by CR39
Irradiation strength 26200 proton/mm²
7115 pits are detected

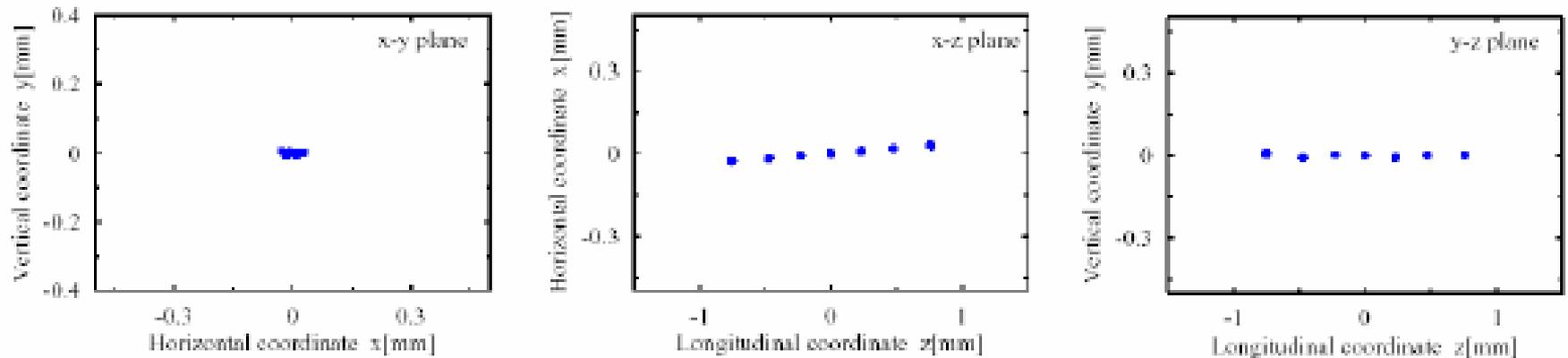


Extracted into air through havar foil of 10μm thickness

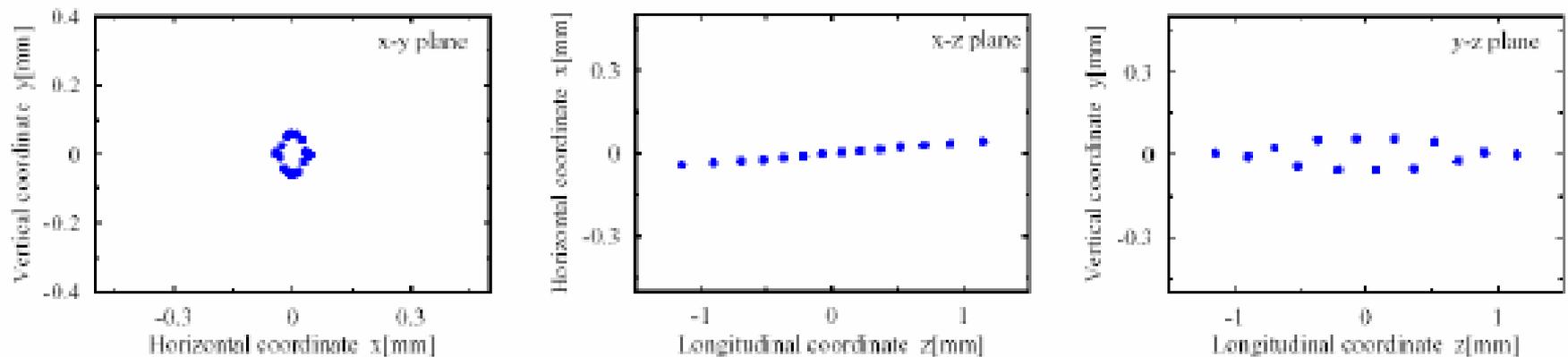
Approach to much Lower Temperature
by Laser Cooling Applied for
40 keV $^{24}\text{Mg}^+$ Ion Beam



Expectation from Simulation



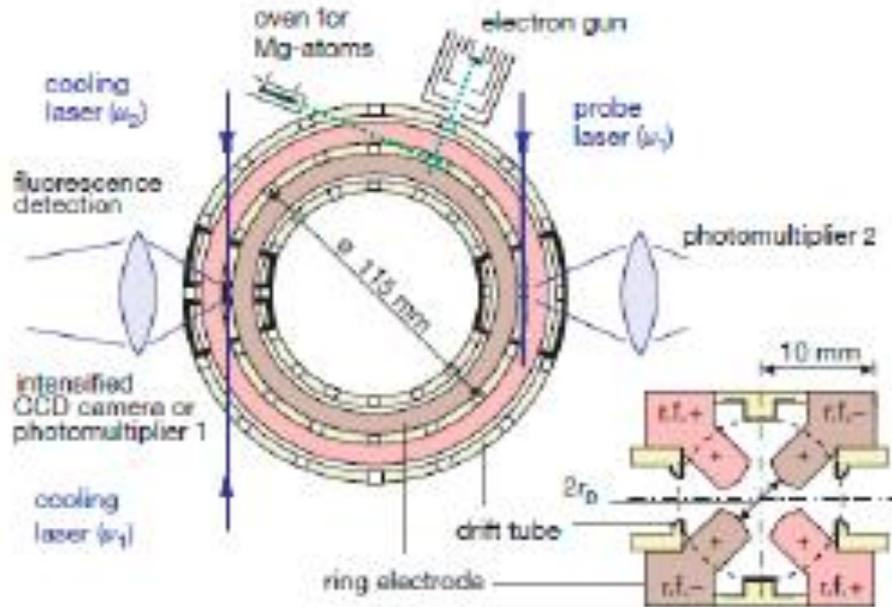
(a) 1D ordering



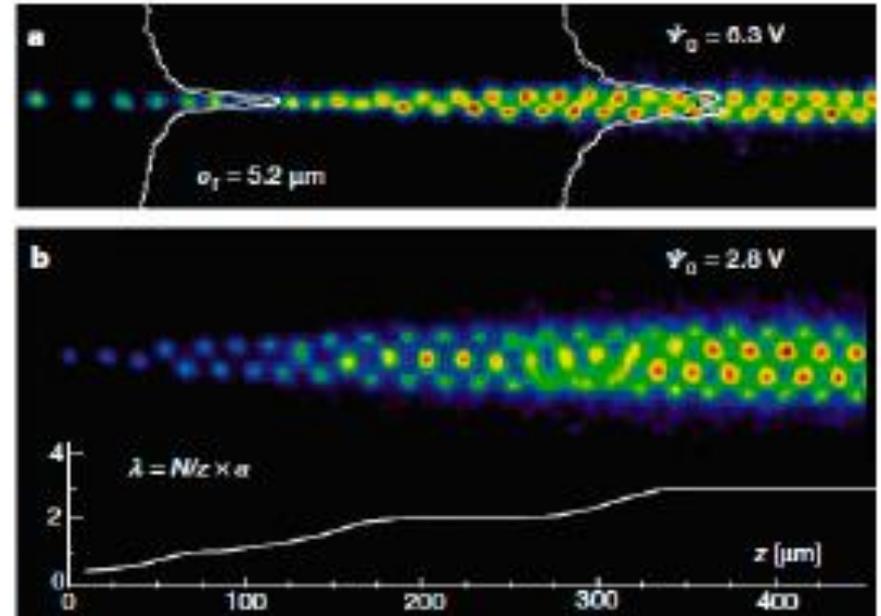
(b) 2D zigzag structure

Crystalline Beam in Circular RFQ, PALLAS

T. Schatz, U. Schramm, D. Habs: *Nature*, 412, 717 (2001)

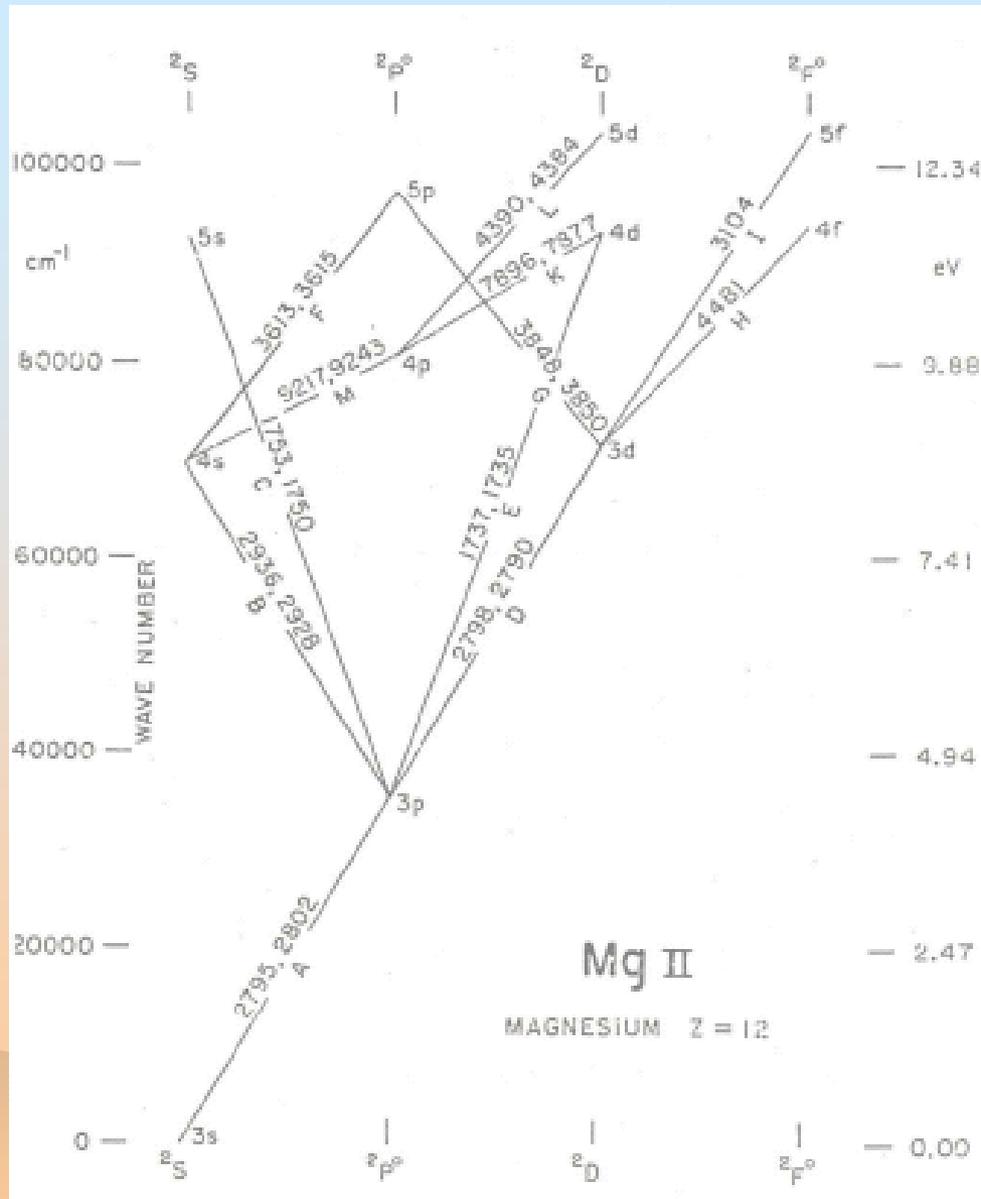


Structure of Circular RFQ, PALLAS

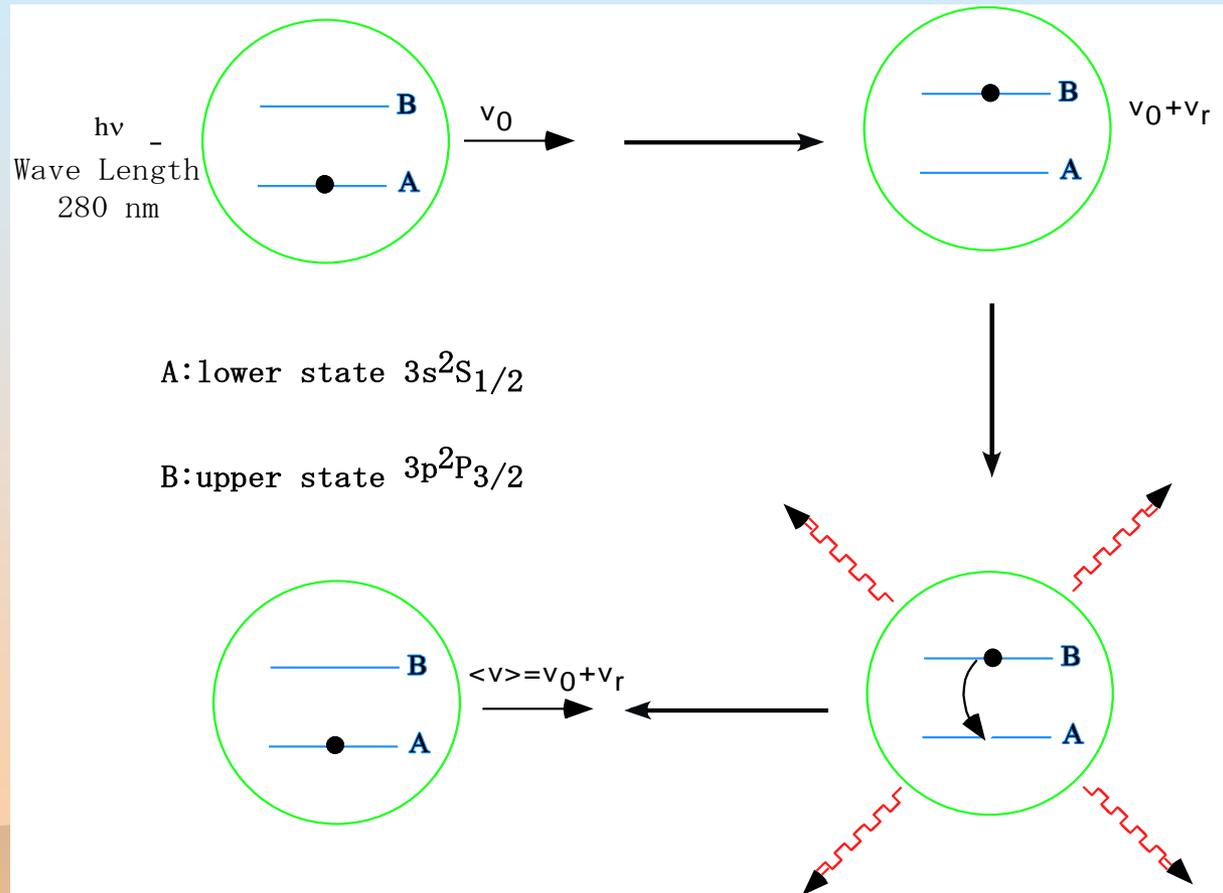


Images of ion crystals at rest in PALLAS

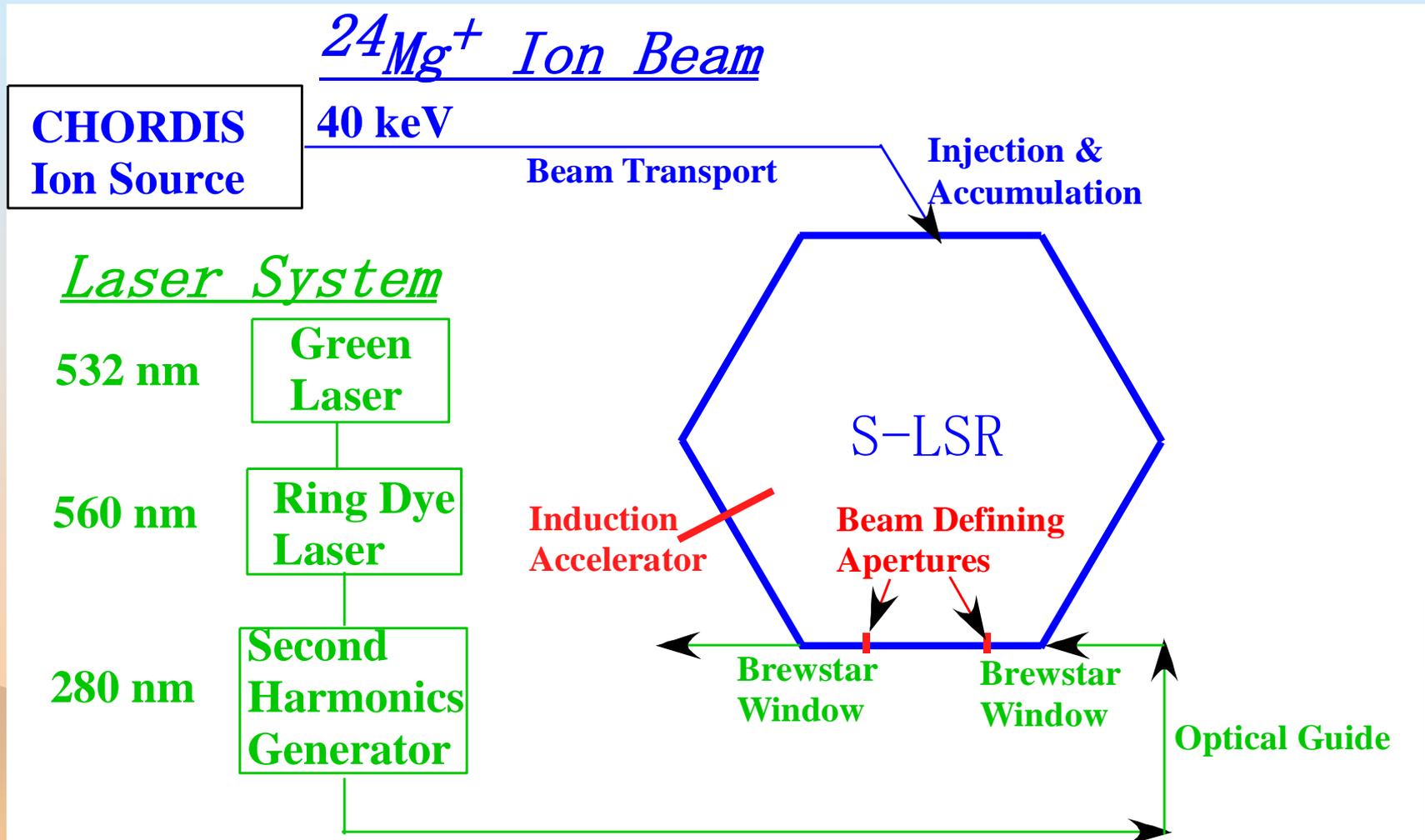
Excited States of Mg Ion



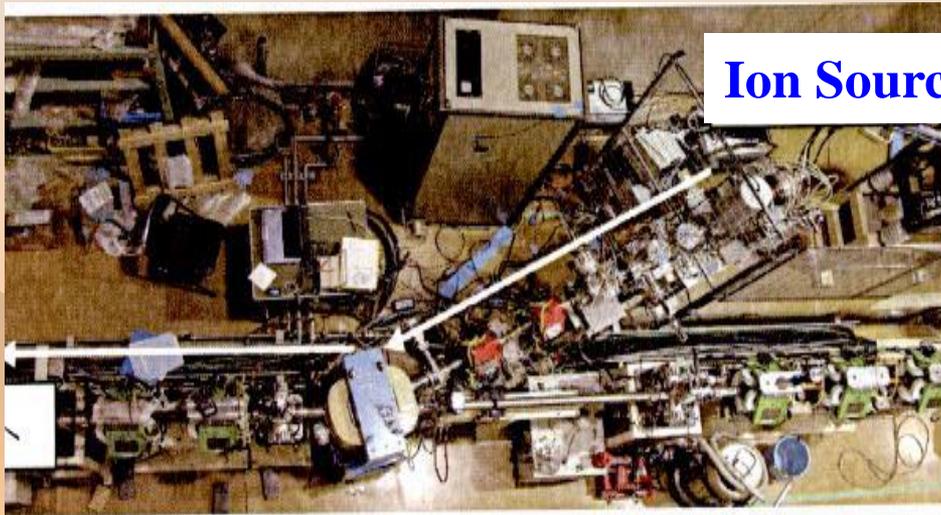
Principle of Laser Cooling (Longitudinal)



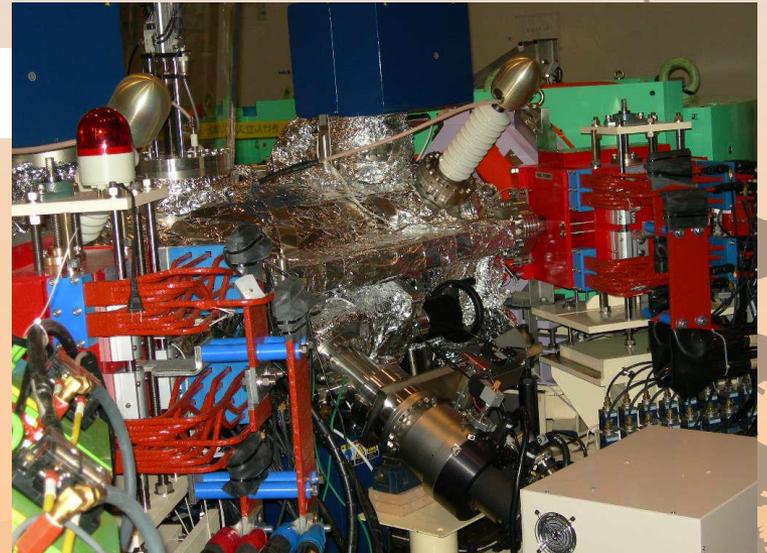
Block Diagram of Laser Cooling at S-LSR



$^{24}\text{Mg}^+$ Ion Source (40 keV)

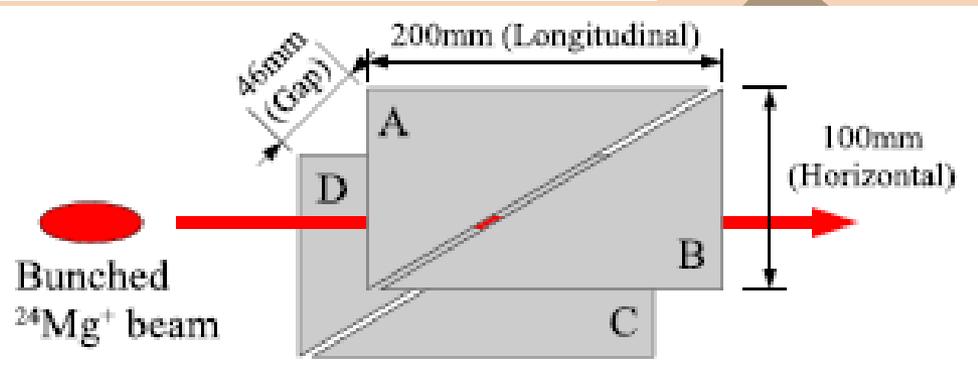
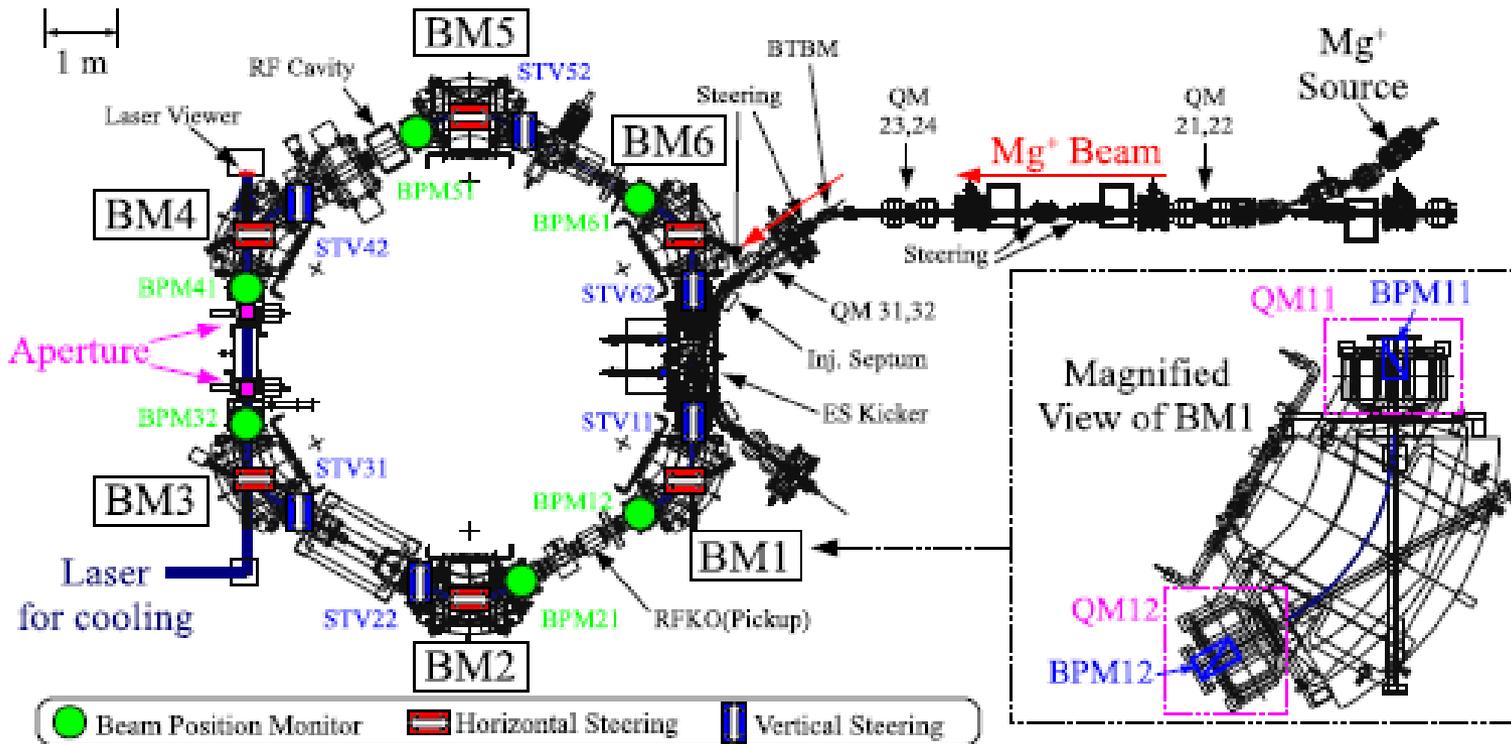


Ion Source



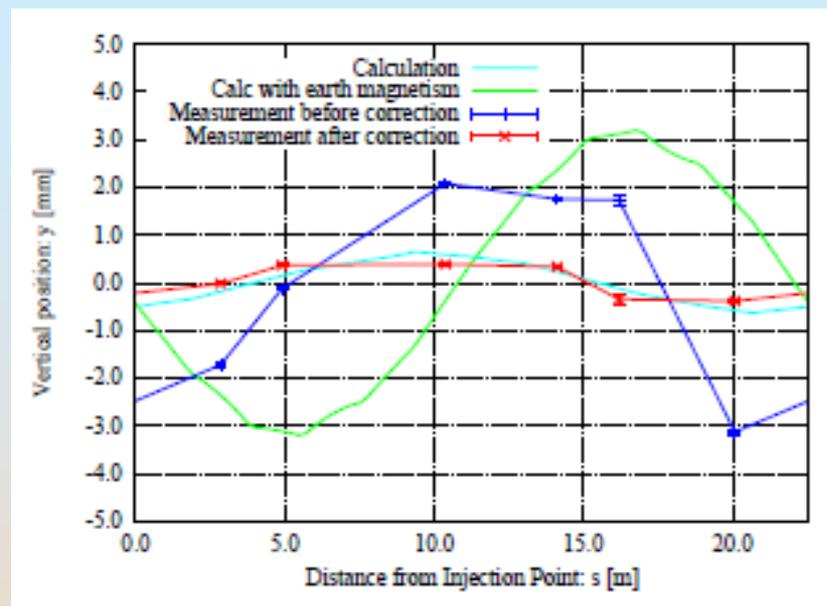
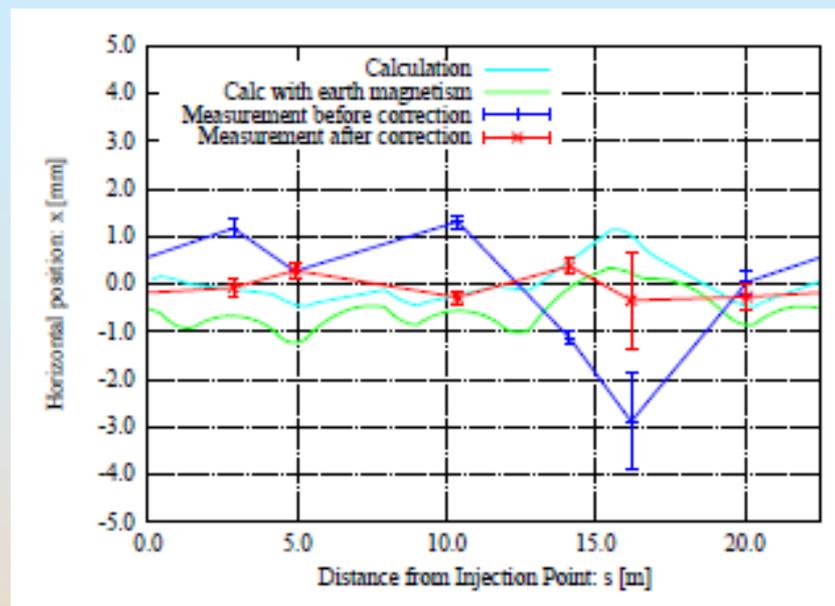
COD Correction System of S-LSR

H. Souda et al., N.I.M. A597 (2008), pp160-165



COD Correction and Beam Life of Mg Ion

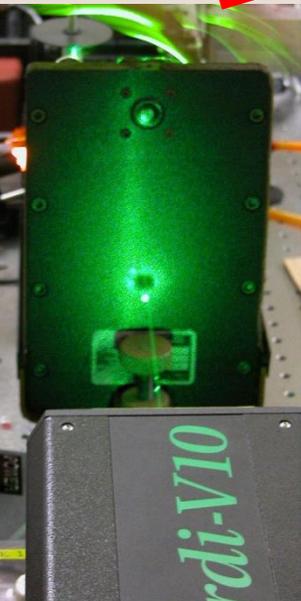
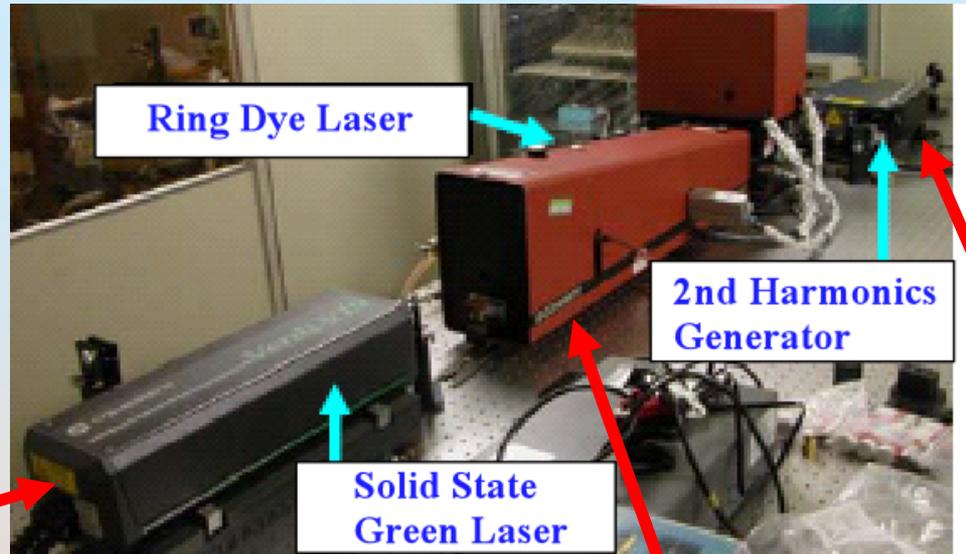
H. Souda et al., N.I.M. A597 (2008), pp160-165



Beam Life of 40 keV $^{24}\text{Mg}^+$ Ion for Various Operation Points

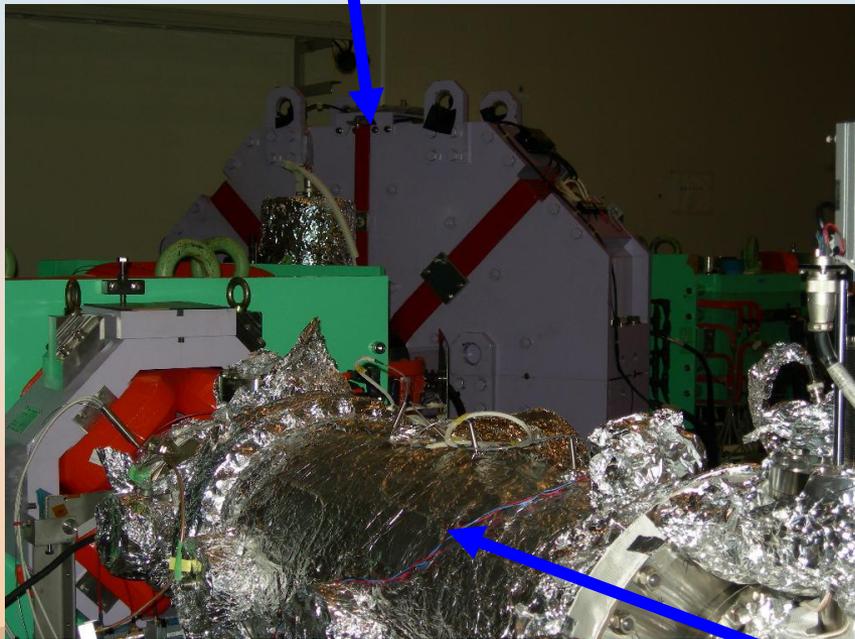
v_x	v_y	Beam Life
2.068	1.069	7.5 s (10.3s)
2.115	0.724	14.2 s
1.53	1.34	14.1 s
1.642	1.198	13.5 s

Laser System for Cooling

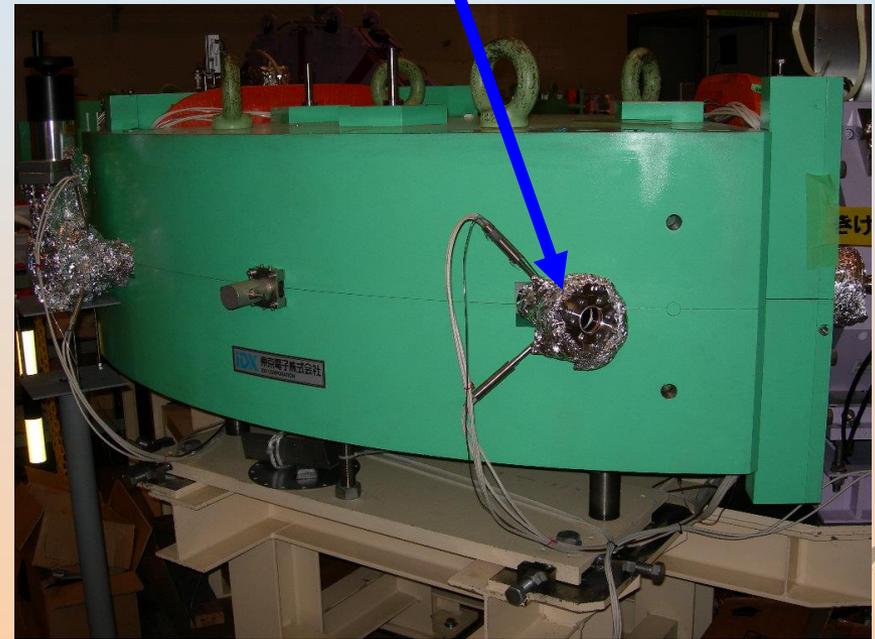


Laser Cooling Section of S-LSR

Induction Accelerator

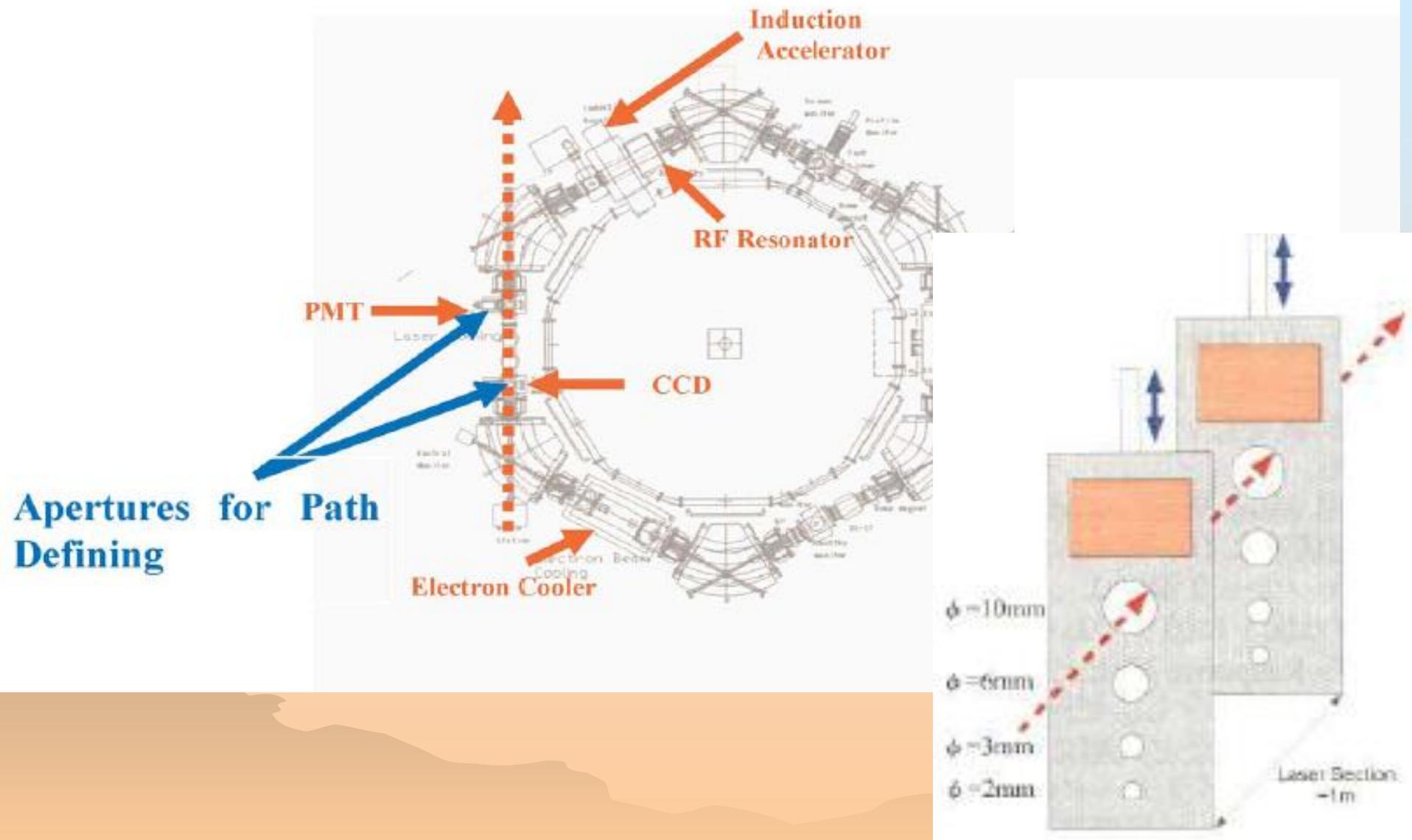


Window for Laser port



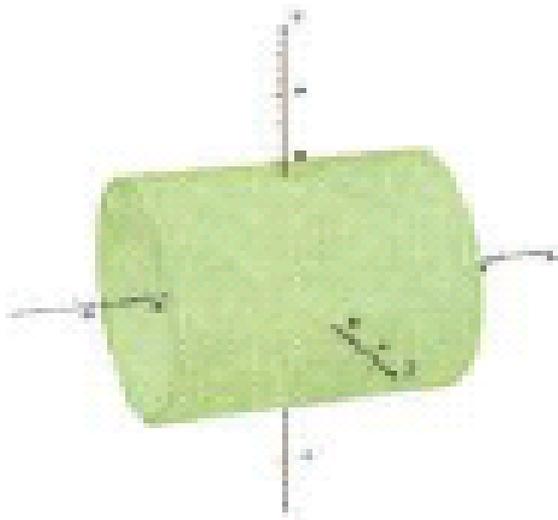
Helical Schottky Pick-up for 7 MeV proton is installed here.

Overlapping of Ion and Laser Beams



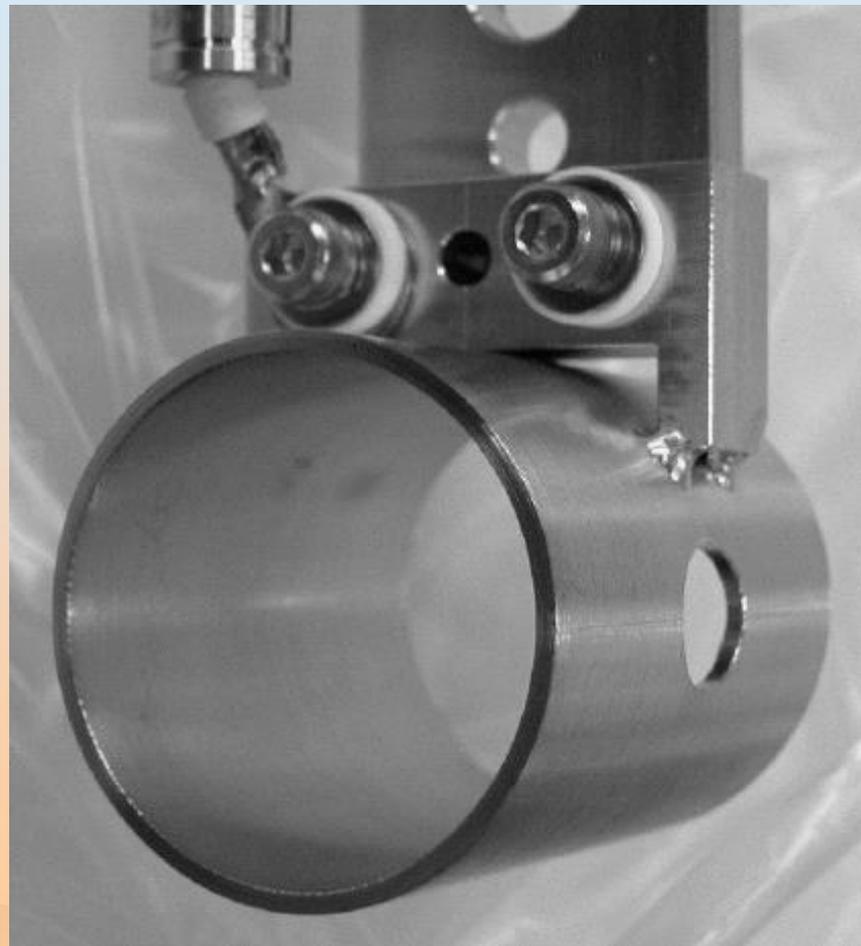
Post Acceleration Tube (PAT)

-Energy Sweep is applied for Distribution Measurement-

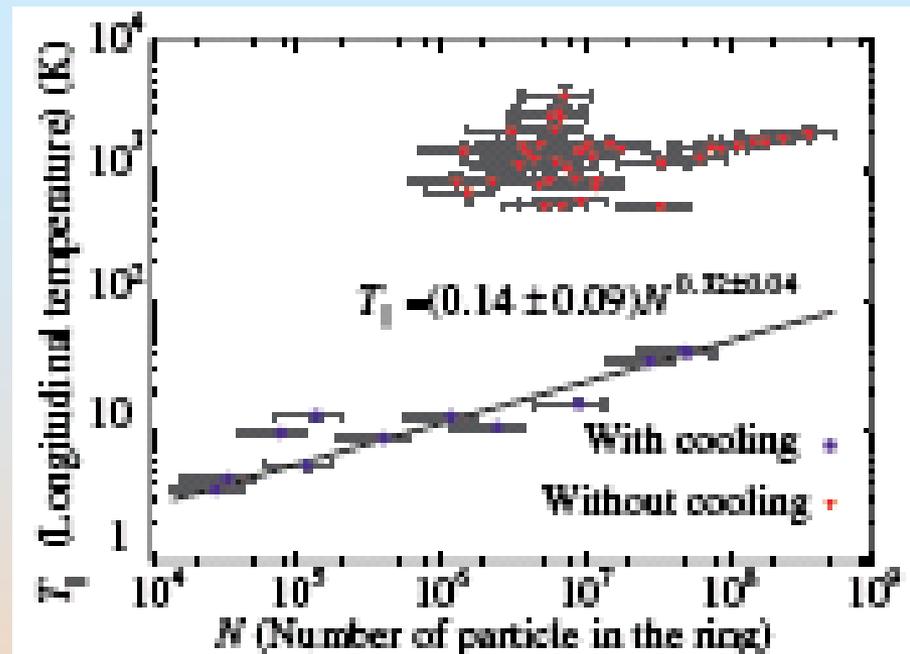
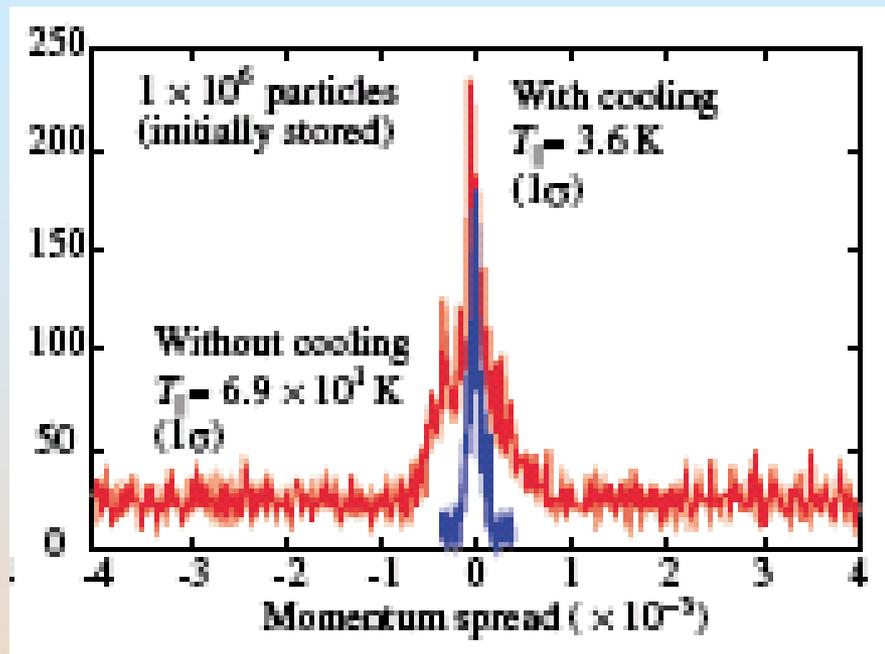


Specification of PAT

Inner Diameter	$\phi 35$ mm
Outer Diameter	$\phi 38$ mm
Length	44 mm
Observation Hole	$\phi 10$ mm



Laser Cooling of Coasting Beam at S-LSR



$$k_B T_L = m v_0^2 \left(\frac{\Delta p}{p} \right)^2$$

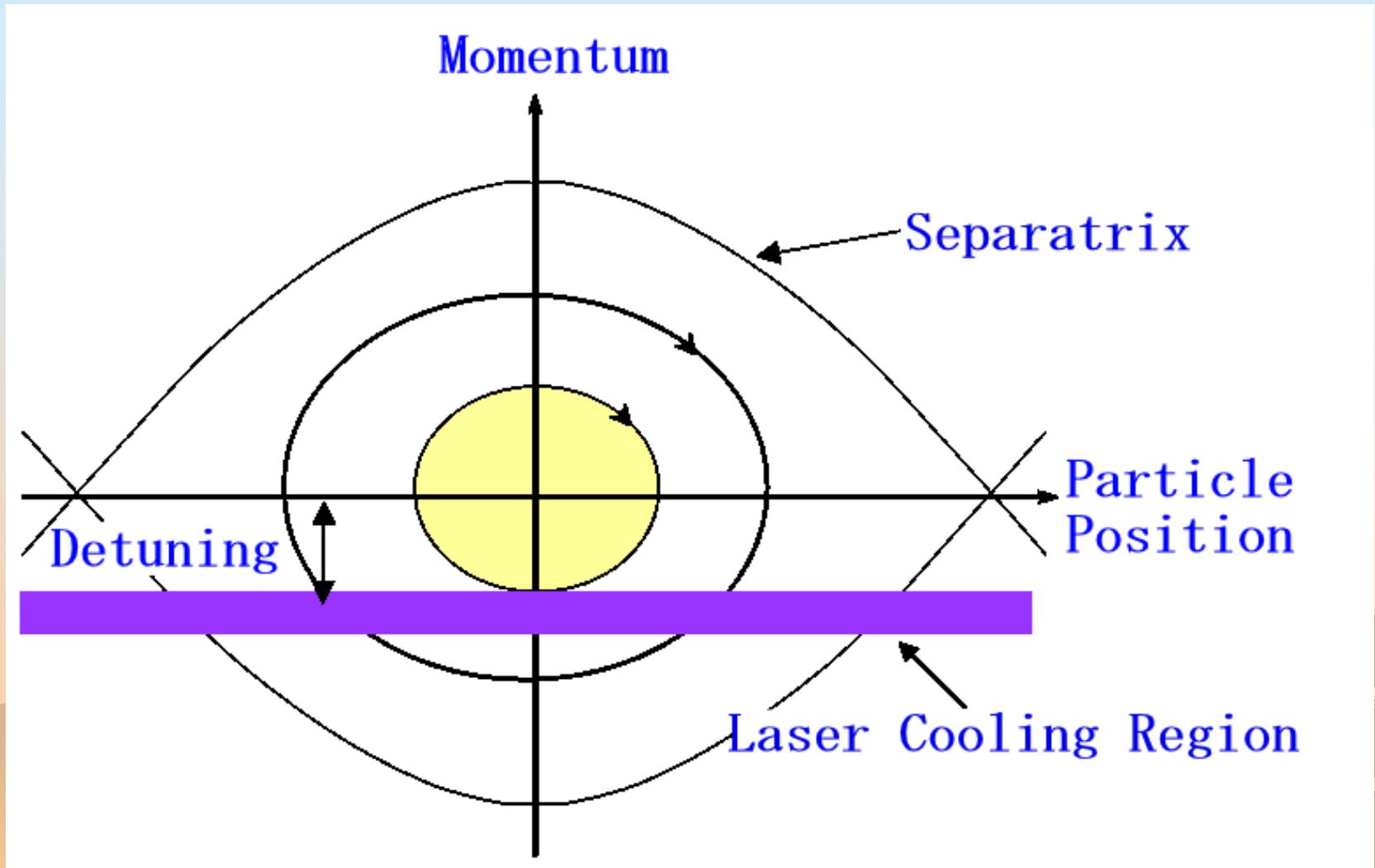
$$\Lambda_{IBS} \propto \frac{N}{T_H T_V \sqrt{T_L}}$$

$$T_L \propto N^{0.32 \pm 0.04}$$

$$T_L = 0.02 T_{\perp}$$

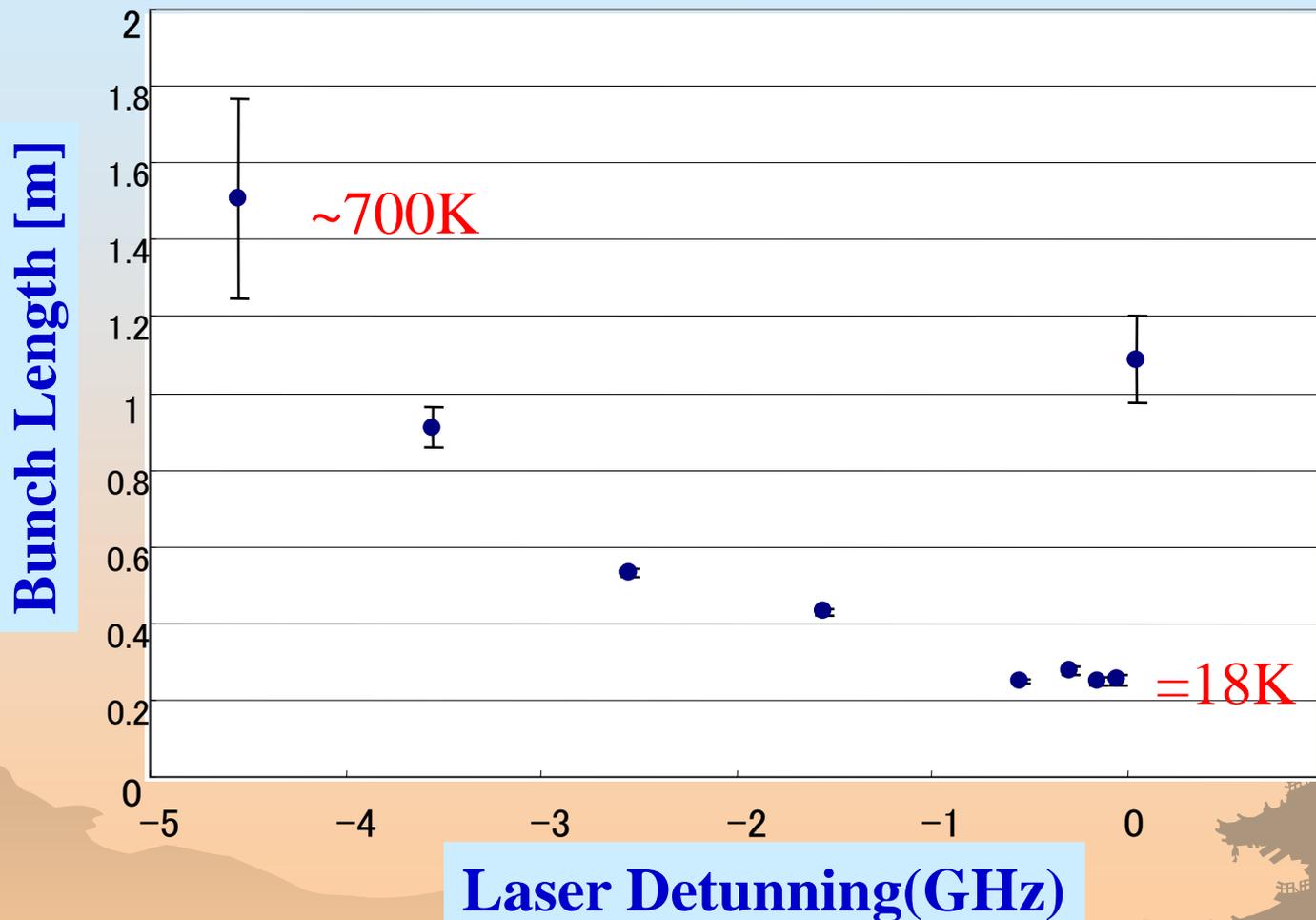
$$T_L \propto N^{0.4}$$

Bunched Beam Cooling



Result of Bunched Beam Cooling

$N=6 \times 10^6$, RF Freq=125.96kHz($h=5$), Voltage=3.06V



Resonant Coupling Method

— Hiromi, Andy and Dieter, Phys. Rev. Lett. 72
(1944), 3977 —

$$H = \underbrace{\frac{1}{2}(p_x^2 + \kappa_x^2 x^2)}_{\text{Betatron oscillation}} + \underbrace{\frac{1}{2}(p_y^2 + \kappa_y^2 y^2)}_{\text{Synchrotron oscillation (laser cooled)}} + \frac{1}{2}(p_z^2 + \kappa_z^2 z^2) + \psi_c$$

Betatron oscillation

Synchrotron oscillation
(laser cooled)Controllable
coupling potential

- When three degrees of freedom are independent of each other ($\psi_c = 0$), nothing takes place in x and y directions even if we strongly cool the z direction.
- Switch on the coupling potential to correlate the harmonic motions in the three directions. Linear coupling potentials should be employed for this purpose:

$$\psi_c = g_1 xy \cdot \delta_p(s - s_1) + g_2 xz \cdot \delta_p(s - s_2)$$

- Move the operating point onto coupling resonance:

$$\nu_x - \nu_y = \text{integer}, \quad \nu_x - \nu_z = \text{integer}$$

Coupling Sources

❁ Betatron-betatron coupling

Skew quadrupole magnets; **Solenoid magnets, etc.**

❁ Synchro-betatron coupling

Regular RF cavities placed at dispersive positions;
Coupling RF cavities; Wien filters, etc.

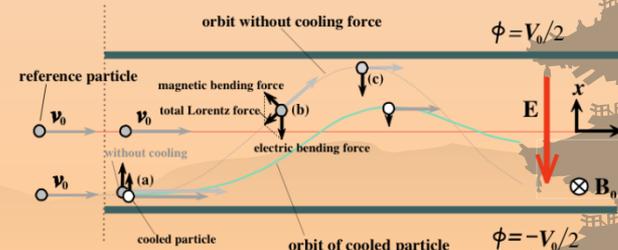
Rectangular cavity operating
in a deflective mode (TM_{210}).

$$\mathbf{A} = (0, 0, g_c \cdot x \cdot \sin \omega t)$$

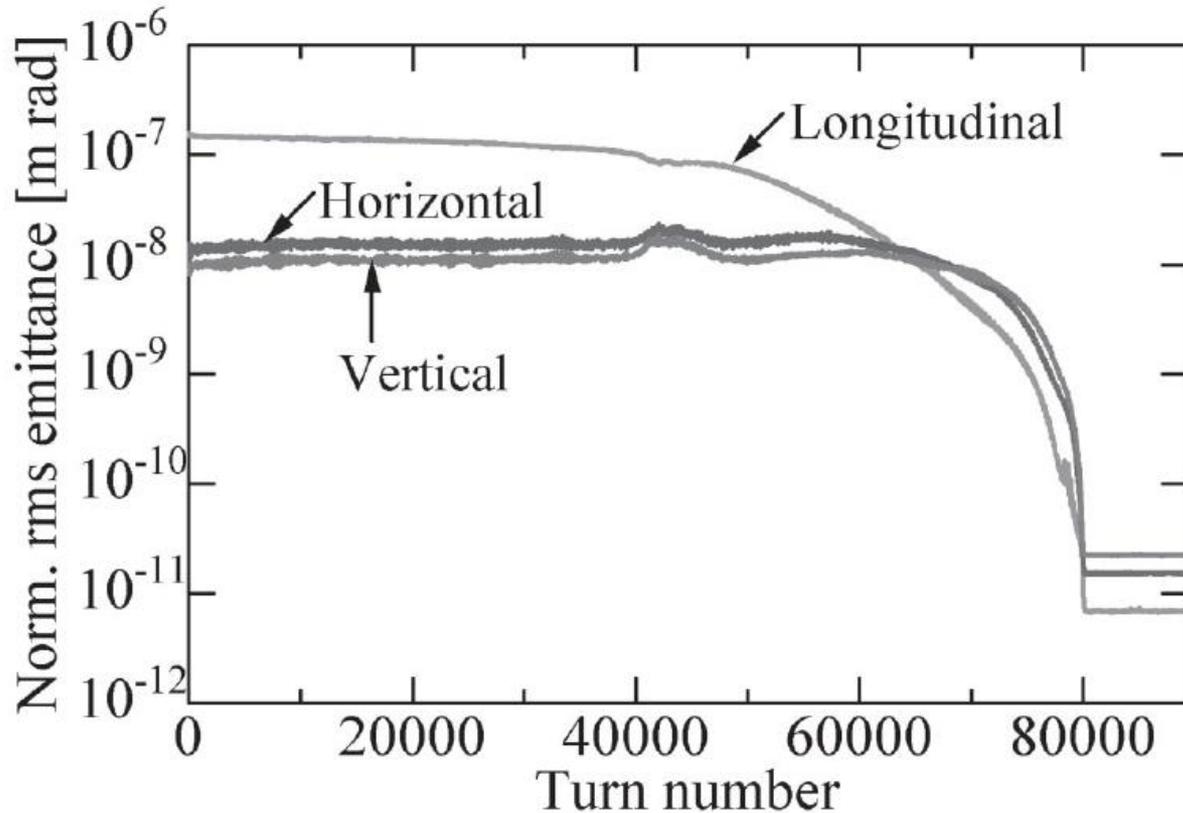
Direct vertical-longitudinal coupling
can readily be generated by rotating
this cavity around the axis by 90 deg.

$$H_{\text{Wien}} = \frac{p_x^2 + p_y^2 + p_z^2}{2} + \frac{1}{2} \mu_x^2 x^2 - \mu_x x p_z$$

The longitudinal linear friction can naturally be
tapered by a Wien filter if momentum dispersion
is finite in the cooling section.



3 D Laser Cooling expected by Simulation

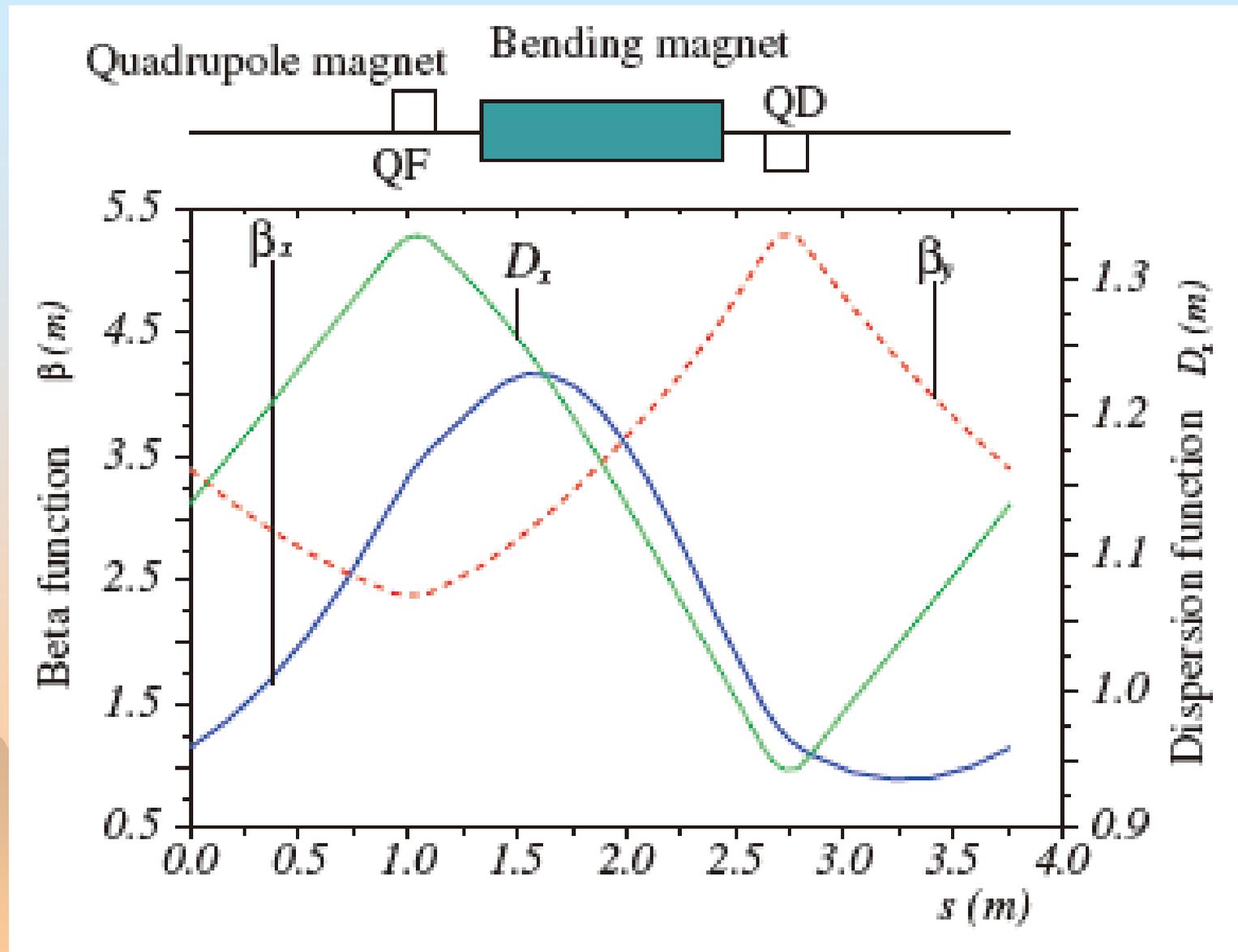


$$\nu_H - \nu_s = \text{integer},$$

$$\nu_H - \nu_V = \text{integer}$$

Y. Yuri and H. Okamoto,
Phys. Rev. ST-AB, 8,114201 (2005)

Beta- and Dispersion Functions of S-LSR



L-H Coupling

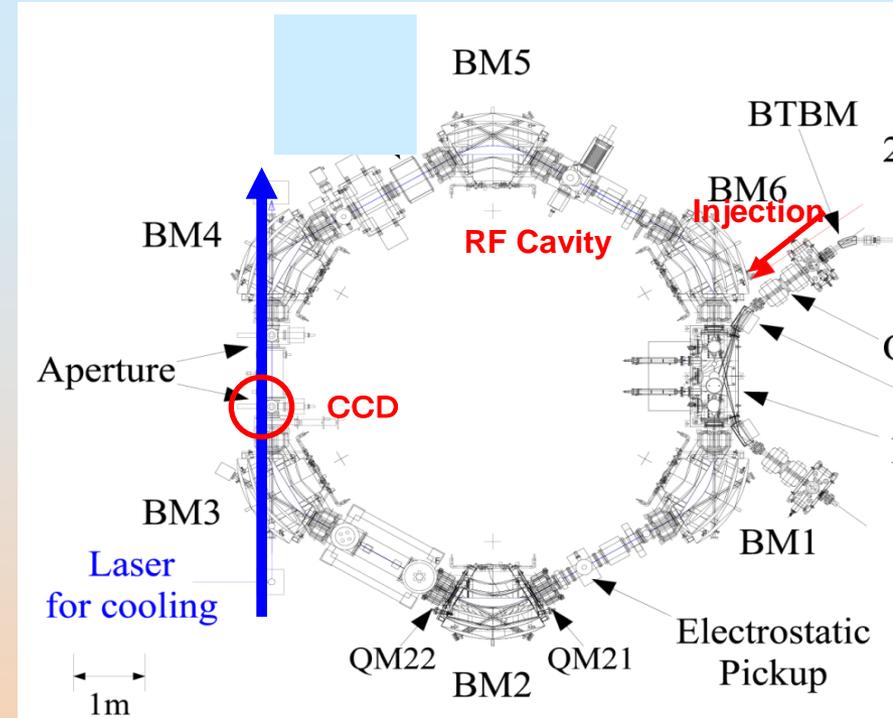
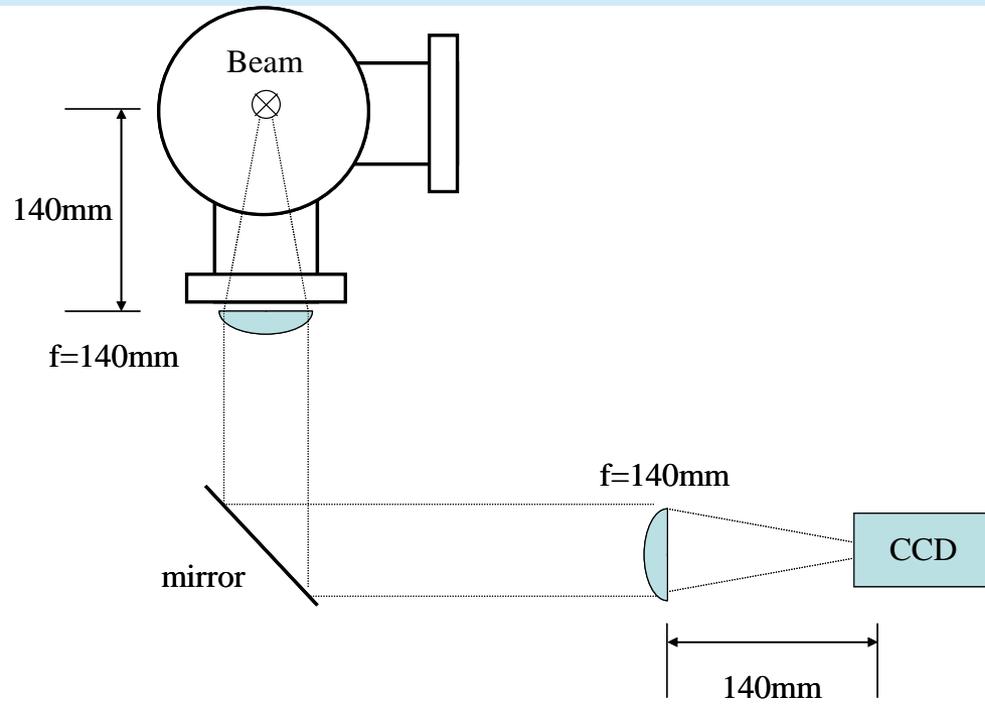
Only the relation:

$$\nu_H - \nu_s = \text{integer}$$

is satisfied!



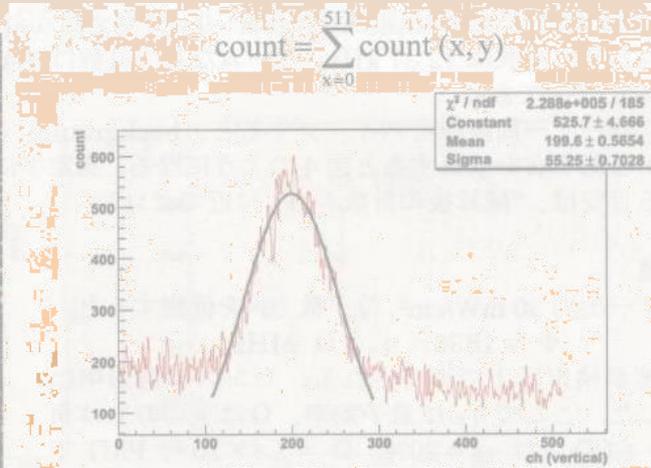
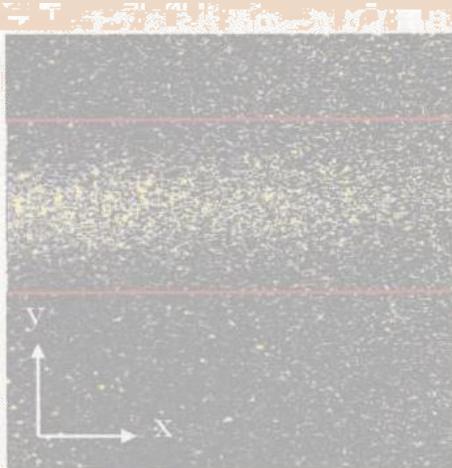
Observation of Transverse Beam Size by CCD Camera



Cooled CCD Camera
(Hamamatsu Photonics C7190-11W)

Ion Observation with Emitted Light

Laser Cottage



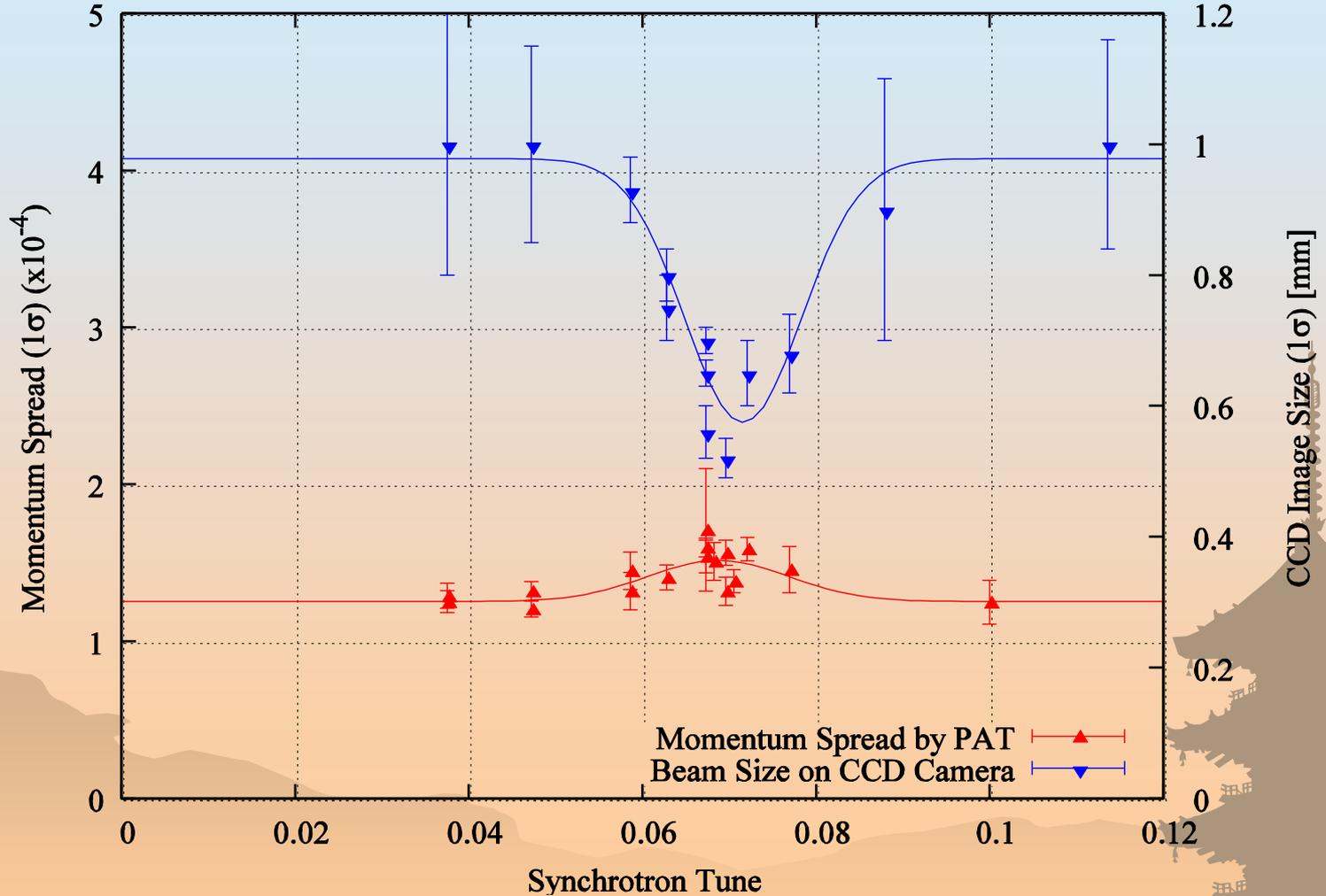
Laser Profile



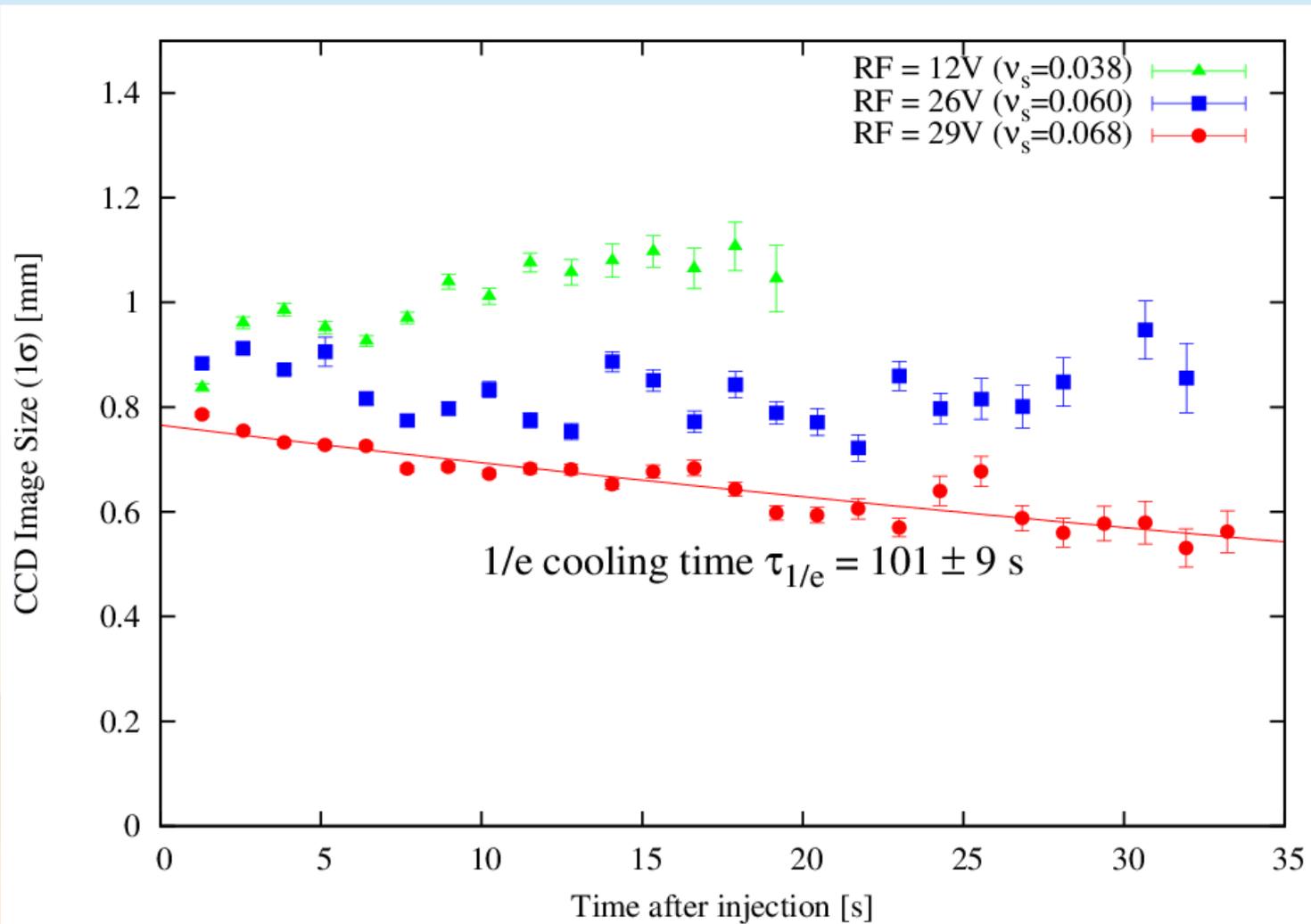
Fluorescent light from the ion beam

Transverse Laser Cooling by Synchro-Betatron Coupling

$(\nu_H, \nu_V) = (2.068, 1.105)$



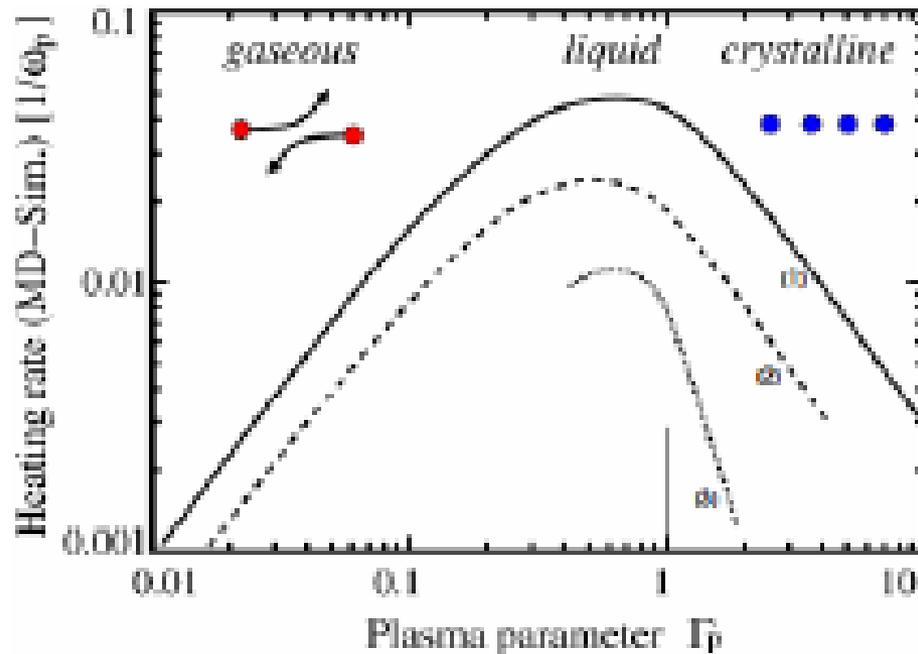
Time Variation of Transverse Beam Size for Various Synchrotron Tune

(Beam Intensity 1×10^7) $(\nu_H, \nu_V) = (2.068, 1.105)$ 

Controlled Scraping to Suppress IBS Effects

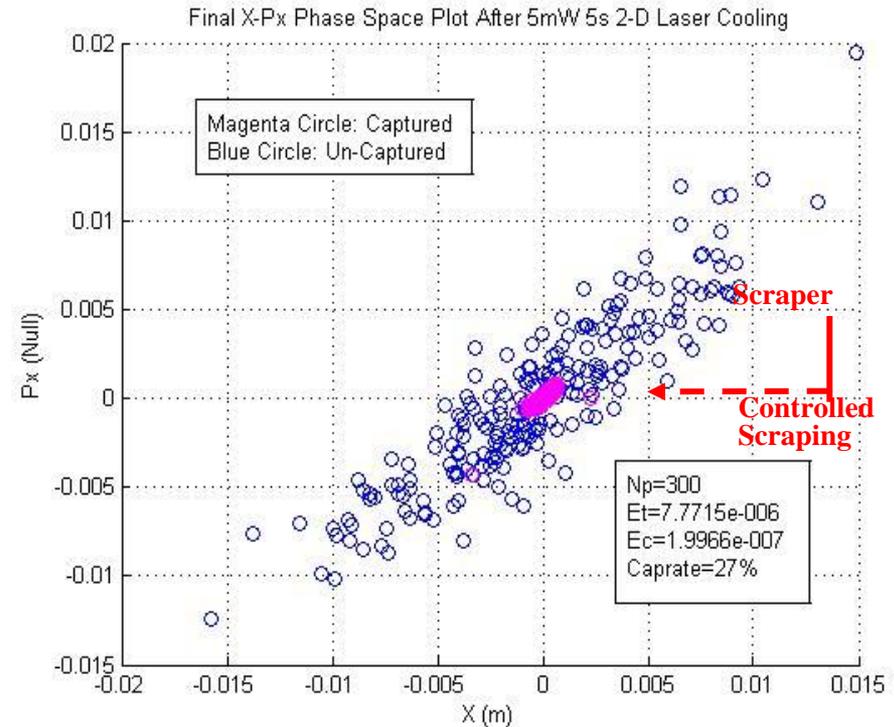
By M. Bussmann U. Schramm
and D. Habs et al., SPARC07

He Zhengqi et al., to be published

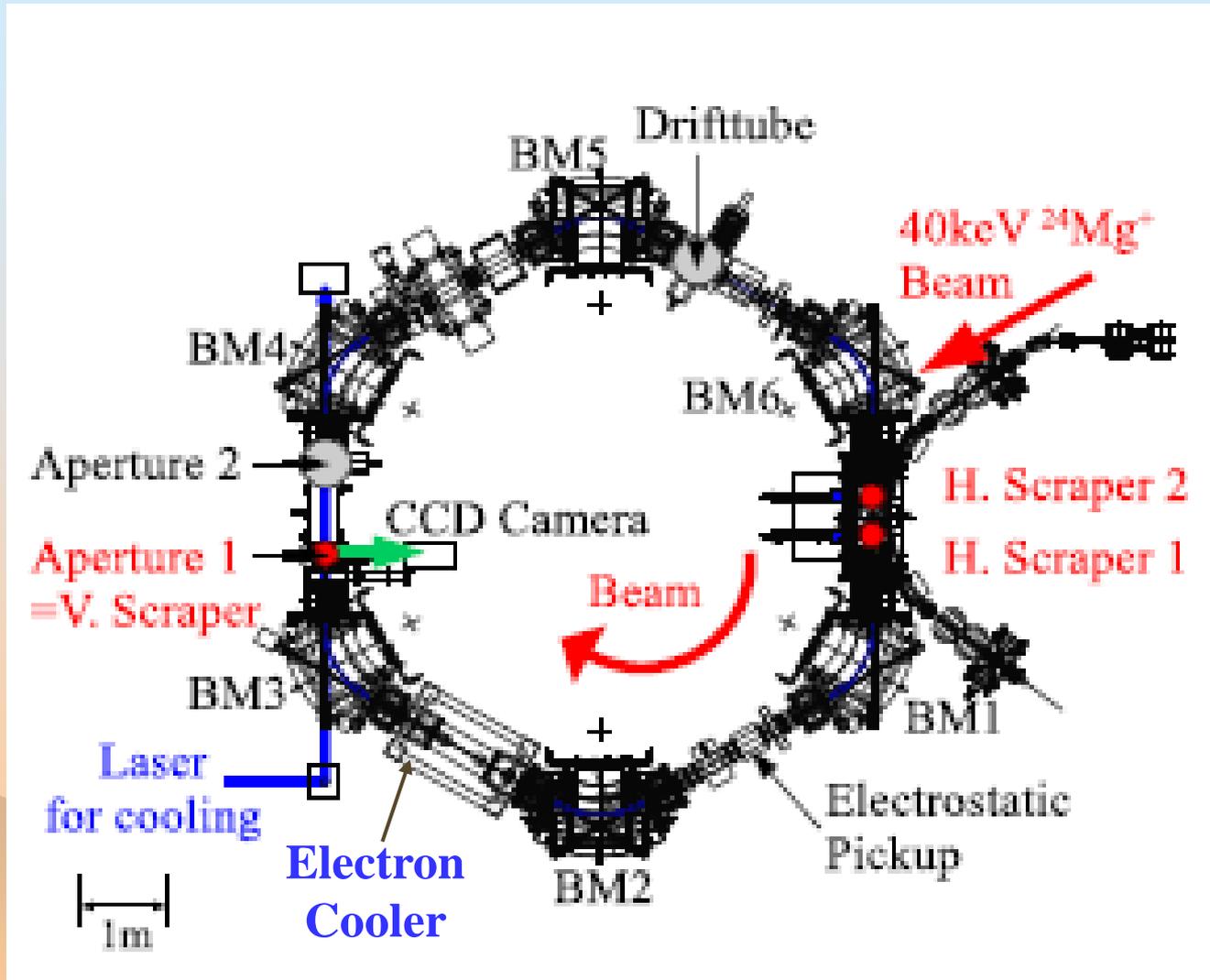


$$\Gamma_p = \frac{E_{\text{Coulomb}}}{E_{\text{thermal}}} = \frac{Z_{\text{ion}}^2 e^2}{4\pi\epsilon_0 \alpha_{\text{WS}} \cdot k_B T_{\text{ion}}}, \quad \alpha_{\text{WS}} = \left(\frac{4}{3}\pi n_{\text{ion}}\right)^{\frac{1}{3}}$$

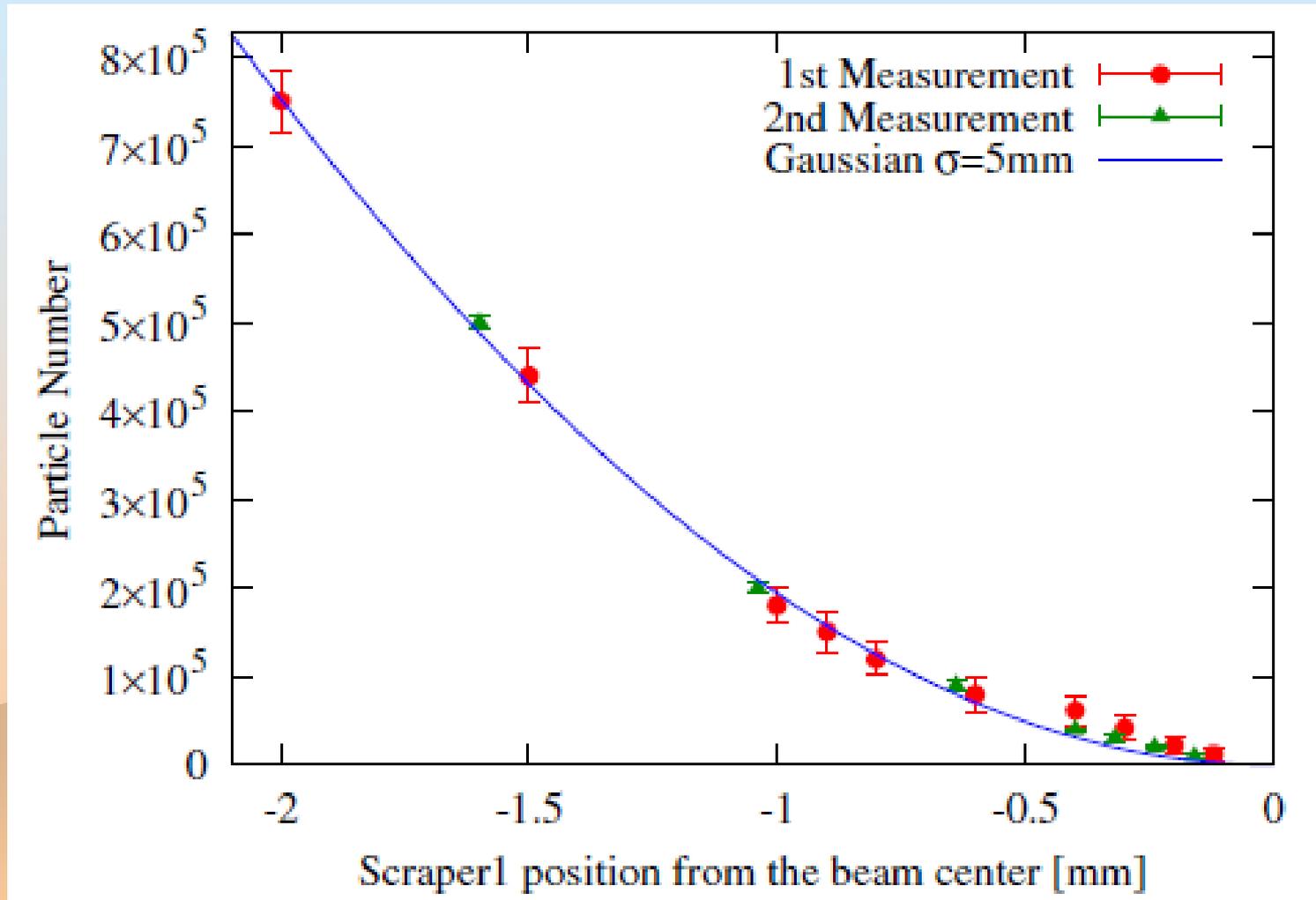
- (1): Q. Spreiter et al., NIM A 364 (1995), 239
- (2): linear ion density reduced by a factor of 10
- (3): string, J. Wei et al., PRL 80 (1998), 2606



Scraping System for Intensity Reduction and Beam Size Measurement

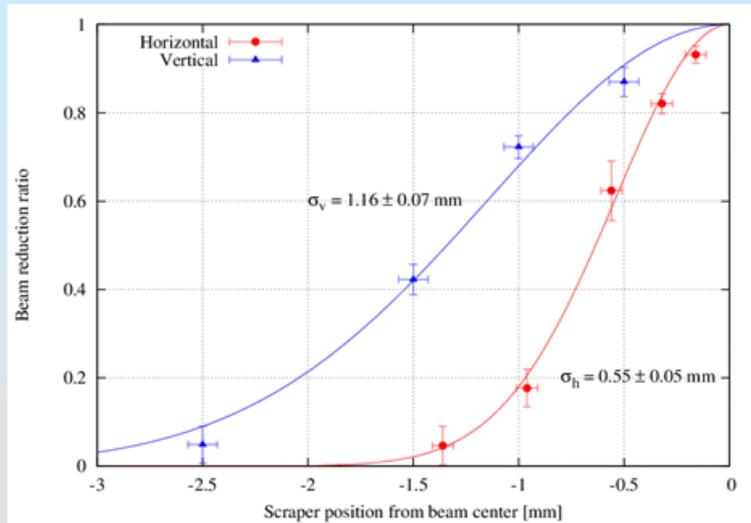


Relation between Scraper 1 Position and Surviving Beam Intensity

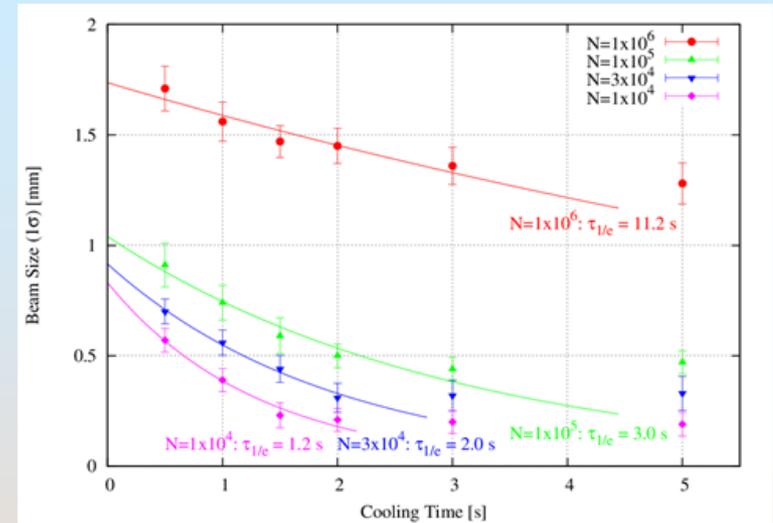


Efficiency Increase of Indirect Transverse Laser Cooling

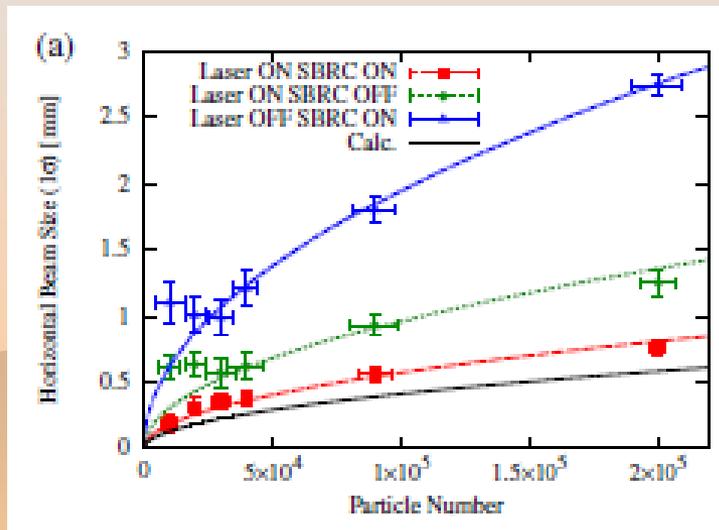
H. Souda et al., Jpn. J. Appl. Phys. 52 (2013) 030202



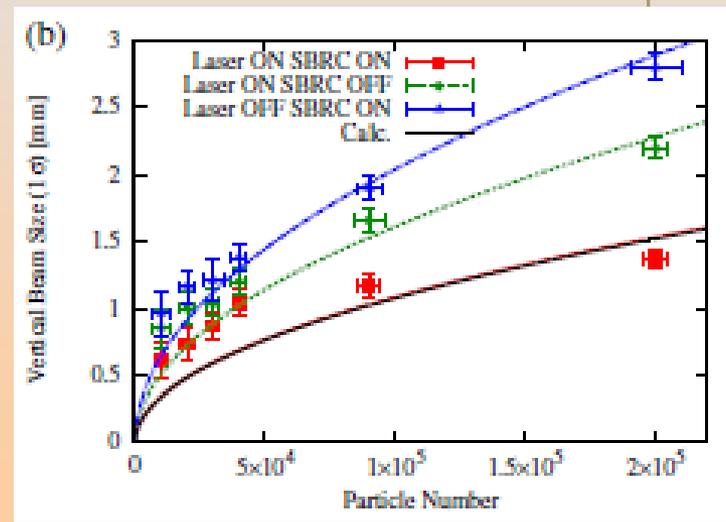
Beam size measurement by scraping



Time dependence of the cooled beam size



Horizontal beam size



Vertical beam size

Ion Number Dependence of the Indirectly laser-cooled Laser cooled Beam Size

H-V Coupling is added

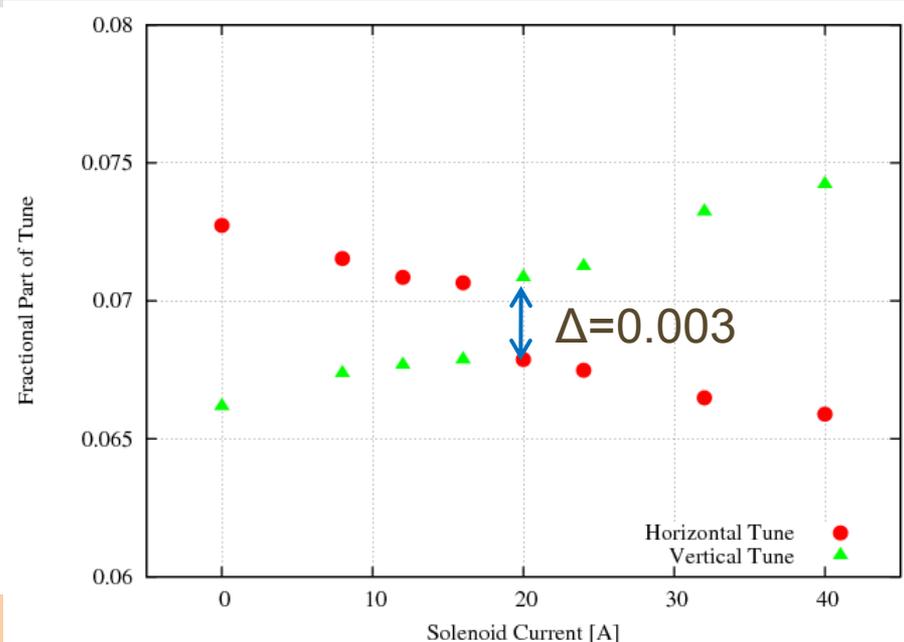
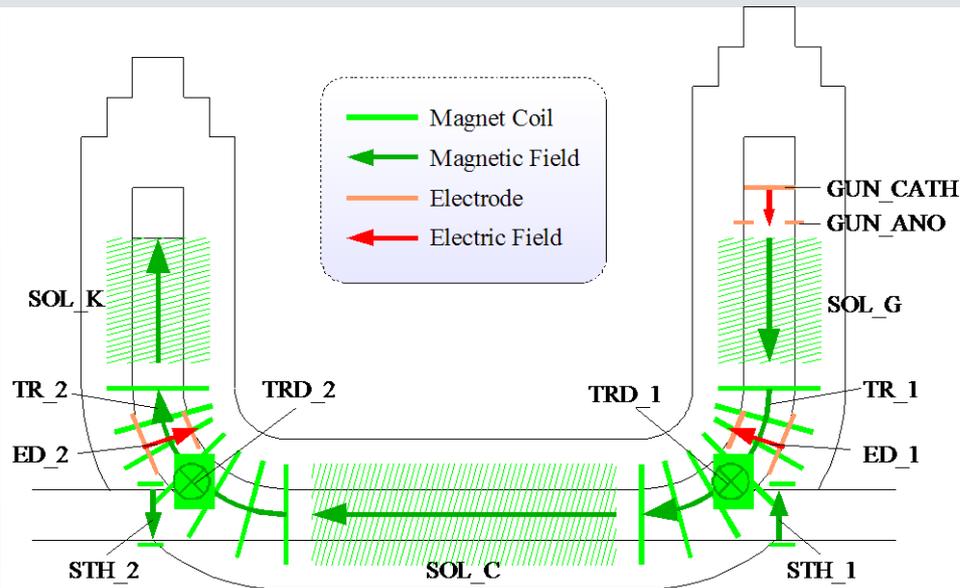
Relations:

$$\nu_H - \nu_s = \text{integer},$$

$$\nu_H - \nu_V = \text{integer}$$

**are satisfied together with
the use of a Solenoid**

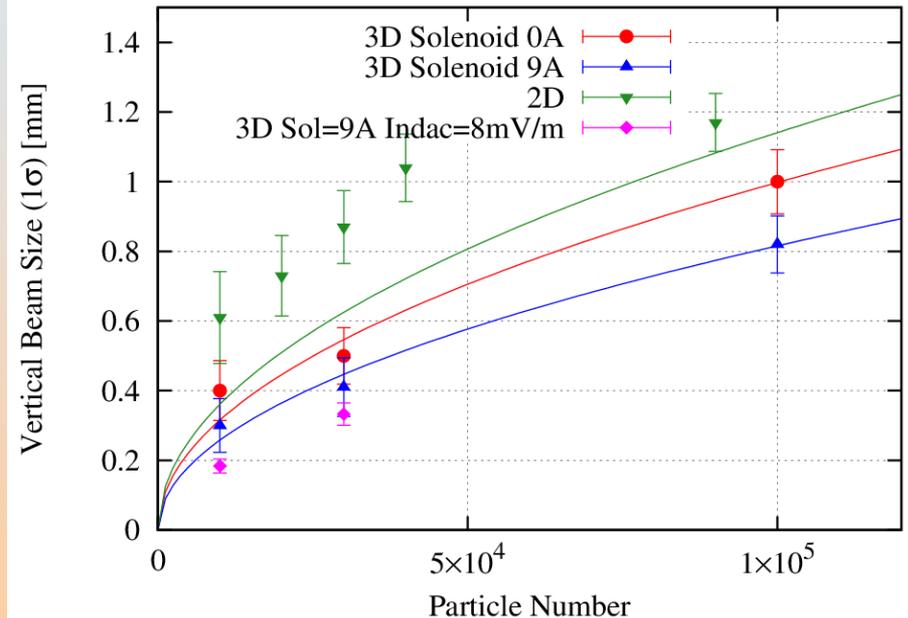
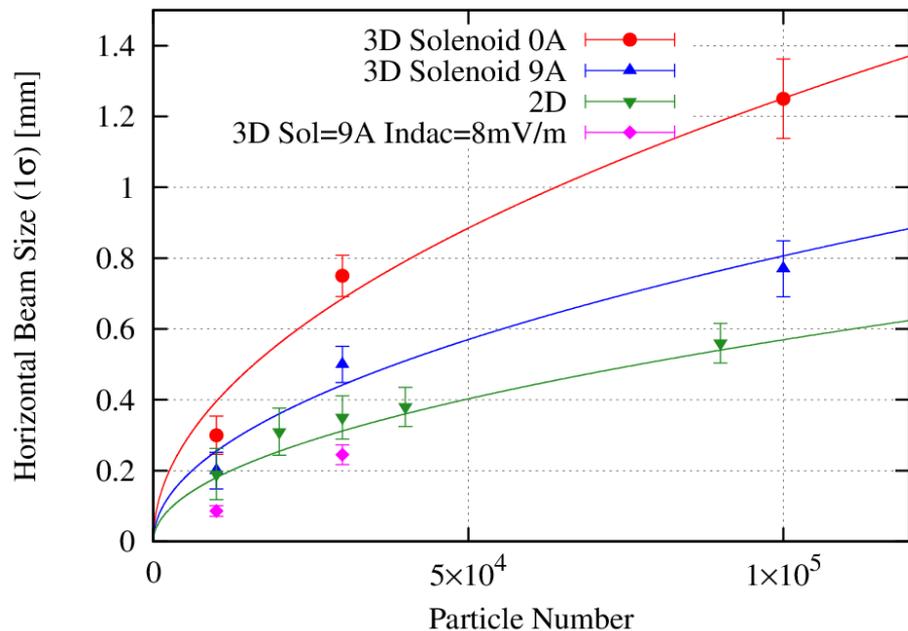
H-V Coupling with a Solenoid Field



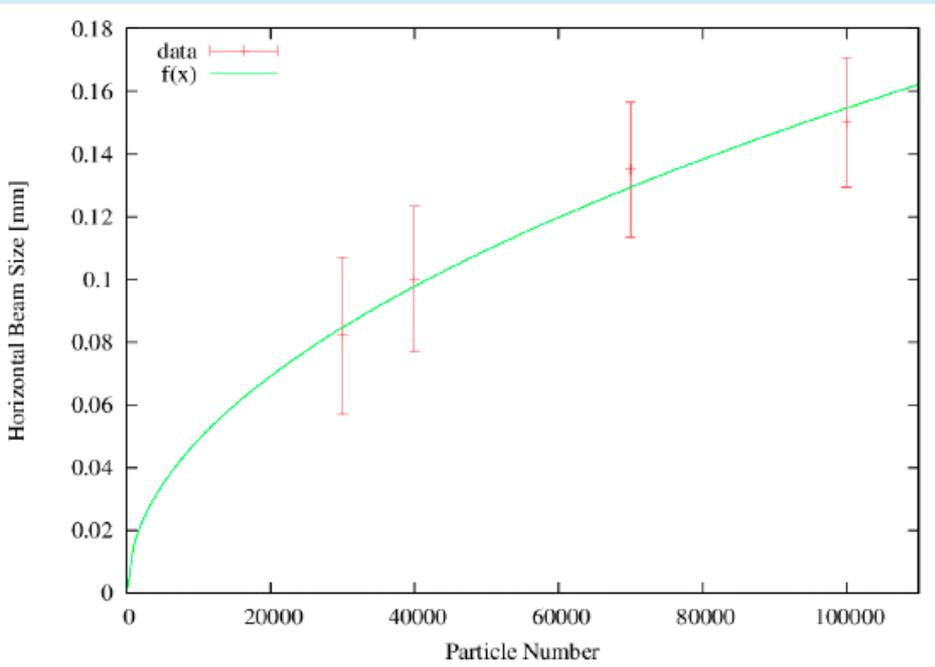
**Solenoid Field of Electron Cooler
(Effective Length=1.2 m)**

Operating Point $\sim (2.067, 1.070)$

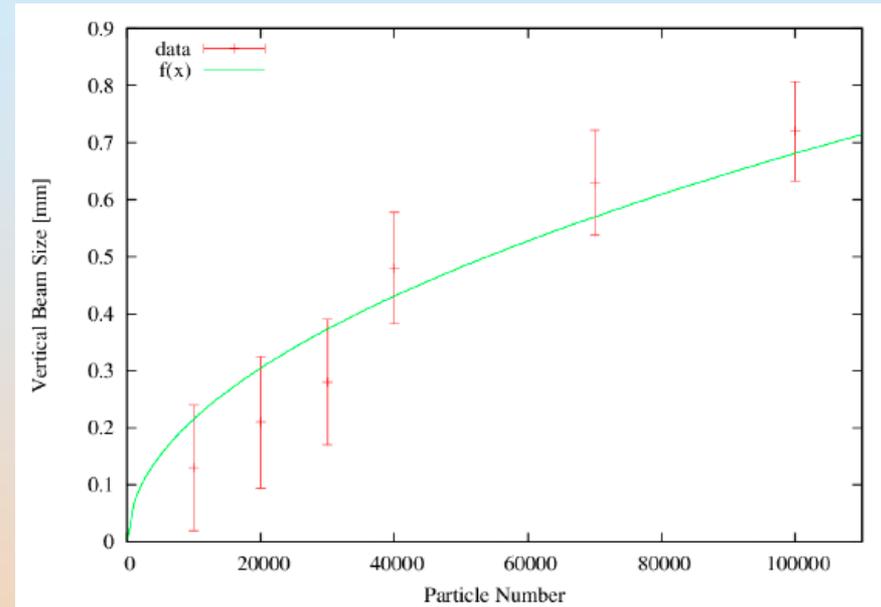
Comparison of Beam Sizes between 2D and 3D Indirect Laser Cooling



3D Laser Cooling + INDAC → Detuning Optimization



Horizontal Beam Size measured by CCD
0.08mm with the intensity of 3×10^4



Vertical Beam Size measured by a Scraper
0.13mm with the intensity of 1×10^4

$$T_y = \frac{1}{k_B} mc^2 \beta^2 \langle \gamma \rangle \frac{\sigma_y^2}{\beta_y}$$

$$\langle \gamma \rangle = \frac{1}{C_0} \oint \frac{1 + \alpha^2}{\beta} ds$$

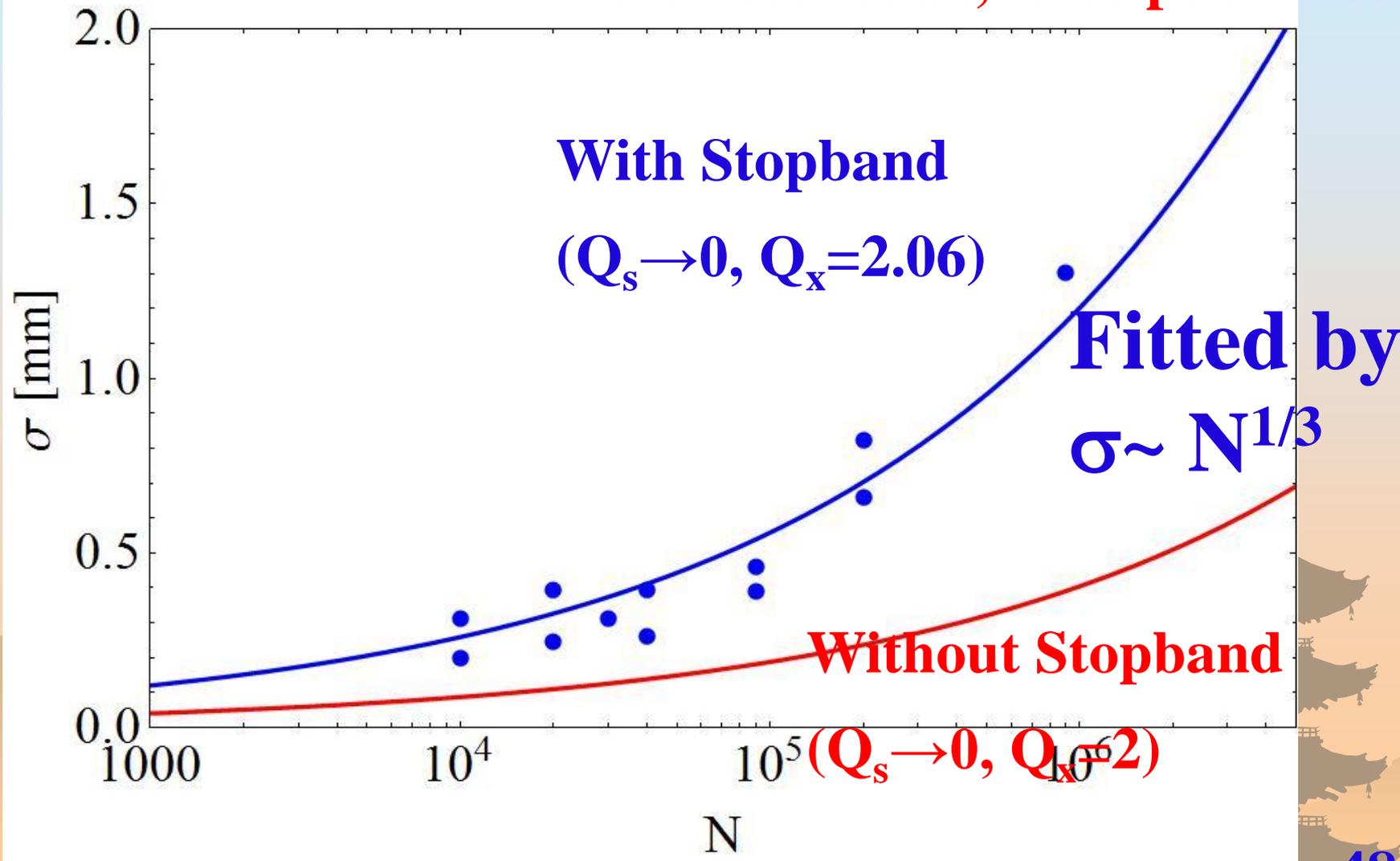
Horizontal Beam Temperature 7.0K with 3×10^4 Vertical Beam Temperature 2.1K with 1×10^4

Comparison with Former Data

Year Ring	Method	Ion	Kinetic Energy	Intensity	T_{\parallel}	T_{H}	T_{V}
1996 TSR	IBS	$^9\text{Be}^+$	7.3 MeV	2.0×10^7	15	4000	500
1998 TSR	Dispersive cooling	$^9\text{Be}^+$	7.3 MeV	1.0×10^7	few tens	$\sim 500^{\#}$	$\sim 150^{\#}$
1999 ASTRID	IBS	$^{24}\text{Mg}^+$	100 keV	7×10^6	2-5	17	21
2001 PALLAS	RFQ	$^{24}\text{Mg}^+$	1 eV	1.8×10^4	<3 m	$T_{\perp} < 0.4$	
2008 S-LSR	IBS	$^{24}\text{Mg}^+$	40 keV	1.0×10^7	11	-	500
2009 S-LSR	W SBRC (2D)	$^{24}\text{Mg}^+$	40 keV	1.0×10^7	27	220 ^{\$}	
2009 S-LSR	WO SBRC	$^{24}\text{Mg}^+$	40 keV	1.0×10^7	16		
2012 S-LSR	W SBRC (2D)	$^{24}\text{Mg}^+$	40 keV	1×10^4	(0.4)	20	29
2013.2.1 S-LSR	W SBRC (3D)	$^{24}\text{Mg}^+$	40 keV	1×10^4	-	40	11
2013.3.7 S-LSR ($\Delta f = -190$ MHz)	W SBRC (3D) (INDAC ON)	$^{24}\text{Mg}^+$	40 keV	1×10^4	-	8.1	4.1
2013.3.22 S-LSR ($\Delta f = -26$ MHz)	W SBRC (3D) (INDAC ON)	$^{24}\text{Mg}^+$	40 keV	1×10^4	-	7.0 (3×10^4)	2.1

Comparison between Experimental Data and Calculation

M. Grieser et al., to be published



Consideration

- **Experimental Data can be well fitted by the formula $\sigma \sim N^{1/3}$ with assumption of the horizontal tune shift due to space charge stops at 2.06 due to stopband → agrees with Yuri's simulation [THAM1HA03]**
- **Trial with higher synchrotron tune to reduce the effect of stopband might realize the further reduction of the beam size.**

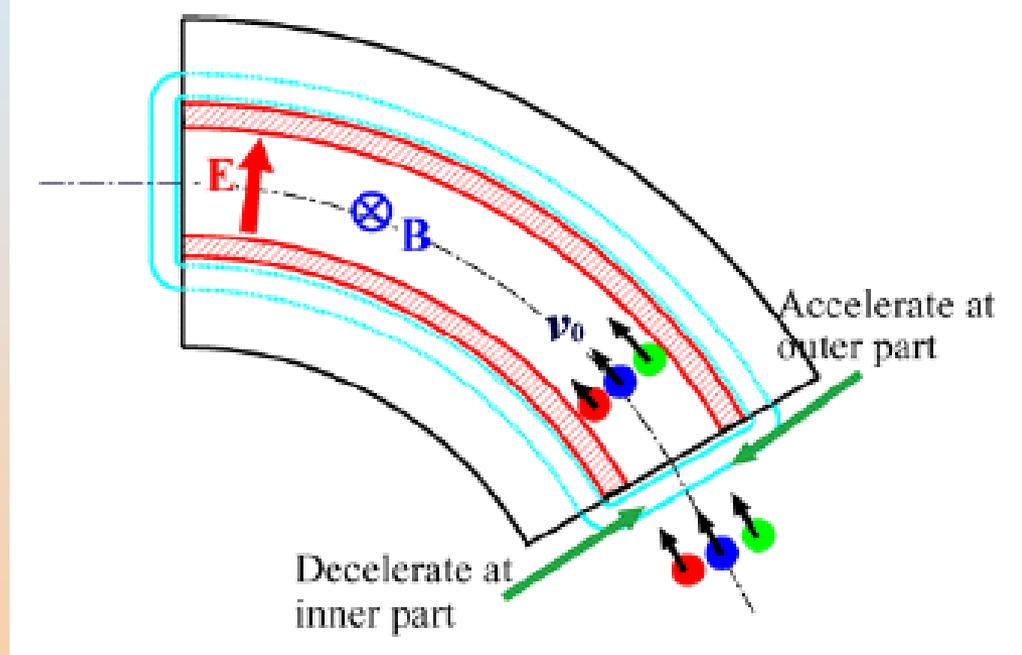
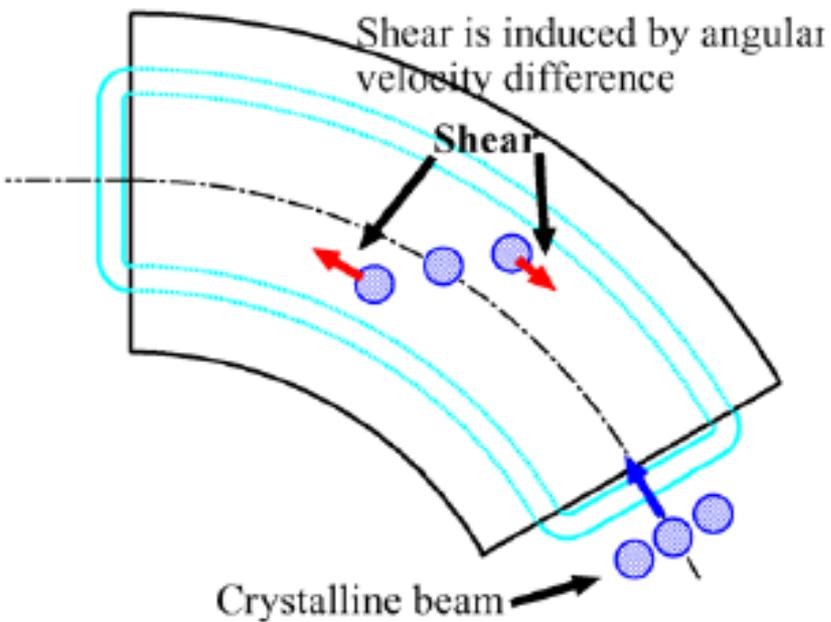
Present Mile Stone Attained

- **Simultaneous** observation of reduction of **both horizontal and vertical** beam sizes has been attained by laser cooling.
- IBS has been reduced by Scraping → Cooling Efficiency has been largely improved!!
 - **Observable down to 1×10^4** beam intensity
 - Computer Simulation tells us that Crystal String will be expected at **10^3** beam intensity
- **1 Order Improvement of Beam Observation Scheme will realize crystalline String!!**

Future Perspective

Application of dispersion free lattice → **3D Crystalline Beam**

Shear Heating and Dispersion Suppressor



Dispersion Suppressor

$$\frac{d^2 x}{ds^2} + \frac{3-n}{\rho^2} x = \frac{1}{\rho} \frac{\Delta W}{W}$$

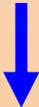
Electric Field

$$\frac{d^2 x}{ds^2} + \frac{1-n}{\rho^2} x = \frac{1}{\rho} \frac{\Delta p}{p}$$

Magnetic Field

$$\frac{\Delta W}{W} = 2 \frac{\Delta P}{P}$$

Non-relativistic Case


$$2\vec{E} = -(\vec{v} \times \vec{B})$$

Acknowledgements

Heartful Thanks to all collaborators
both in and outside of Japan



妻と今は亡き両親にも！



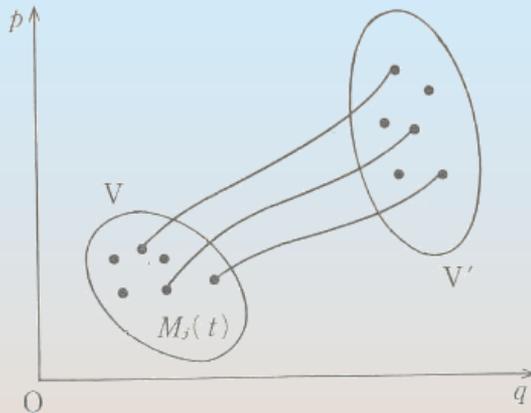
Thank you for your kind attention !



Back Up Slides



Liouville's Theorem



Trajectories in the 6 dimensional phase space does not cross

Laminar Flow-velocity distribution at a point which is single valued.

Phase Space Density $f(x,p)$ does not change

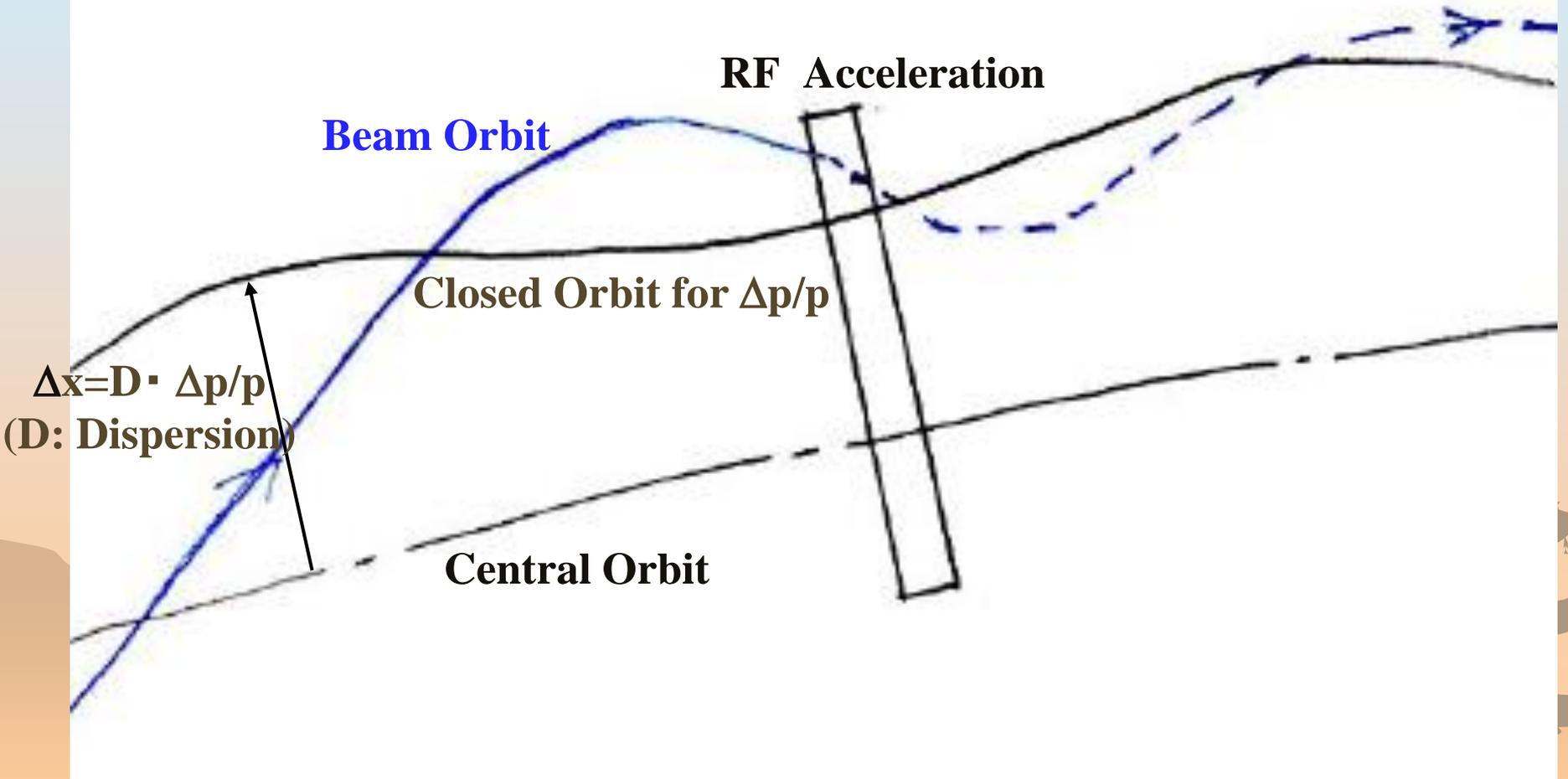
$$\frac{df}{dt} = 0$$

Phase Space Volume occupied by the beam does not change

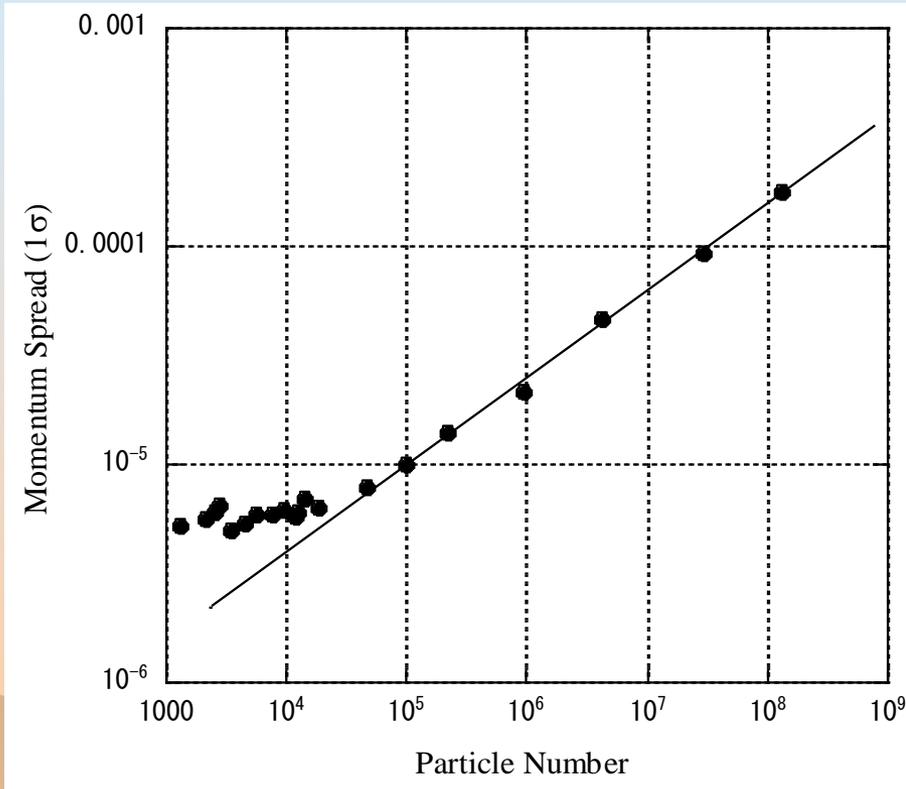
Beams in the accelerators basically follows Liouville's Theorem
(without inter-particle interaction)

Transverse Laser Cooling by SBRC

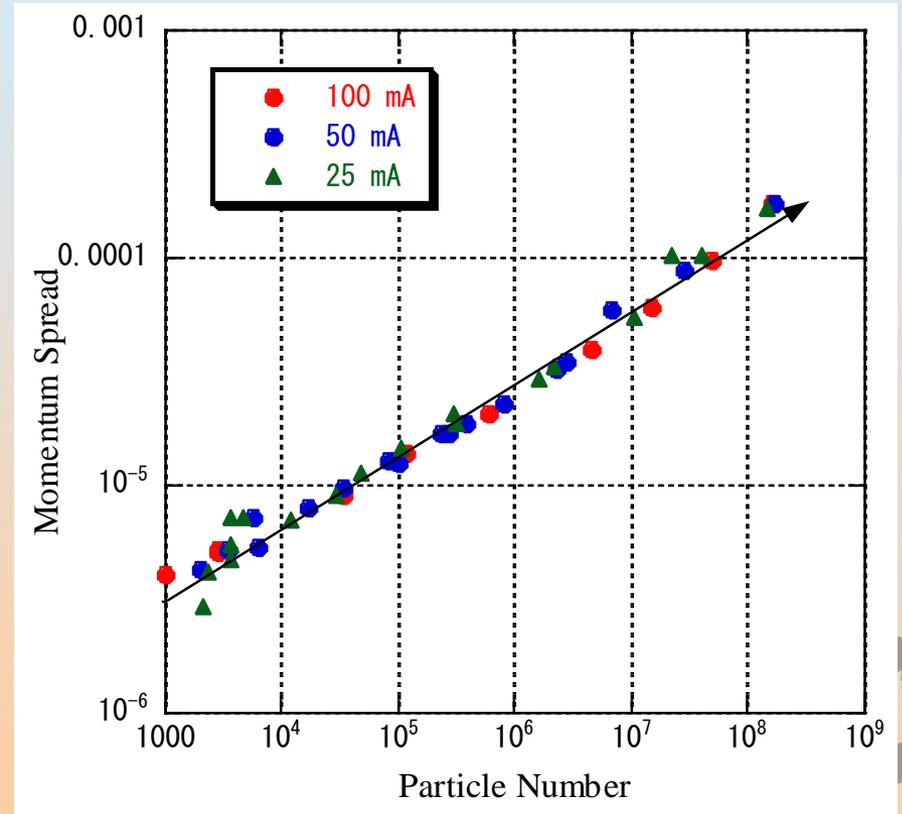
Heat is Transferred from Horizontal to Longitudinal Direction
for this example



Fractional Momentum Spread vs Particle Number

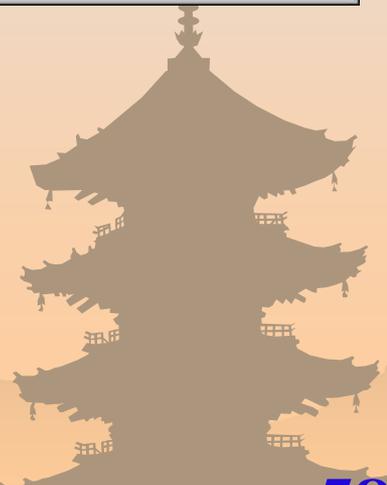
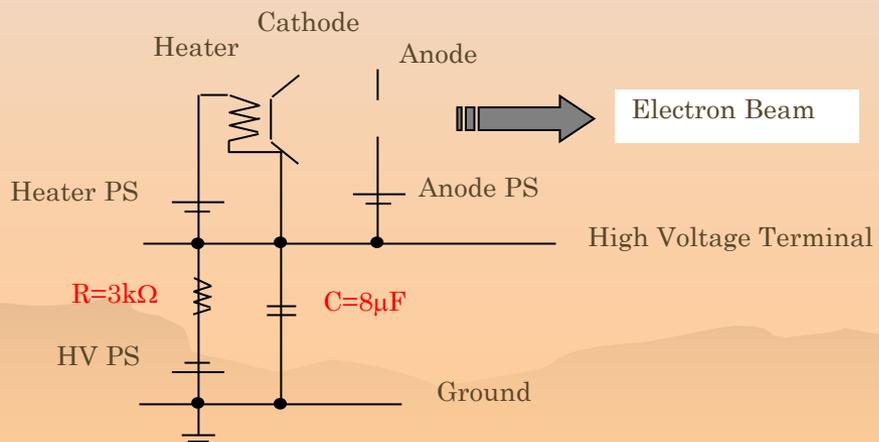
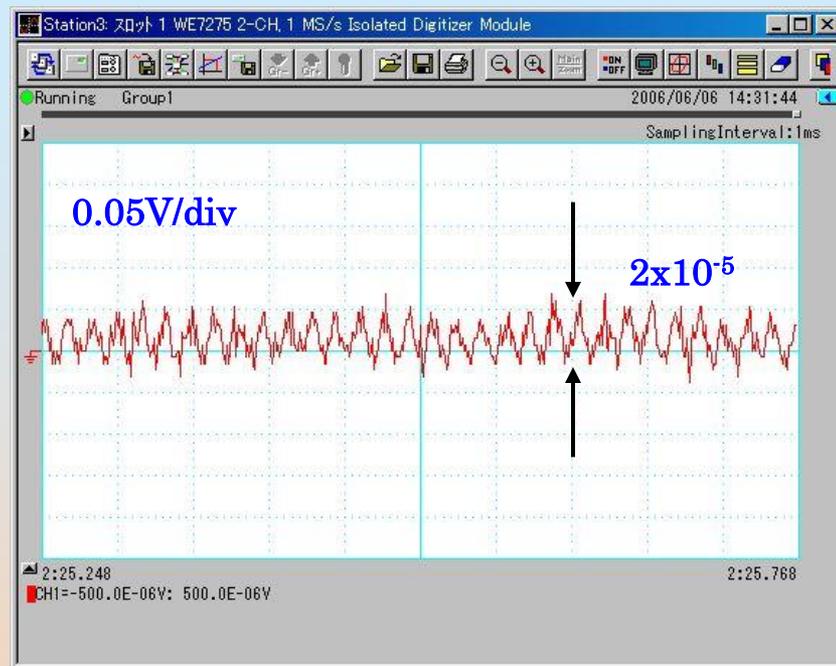
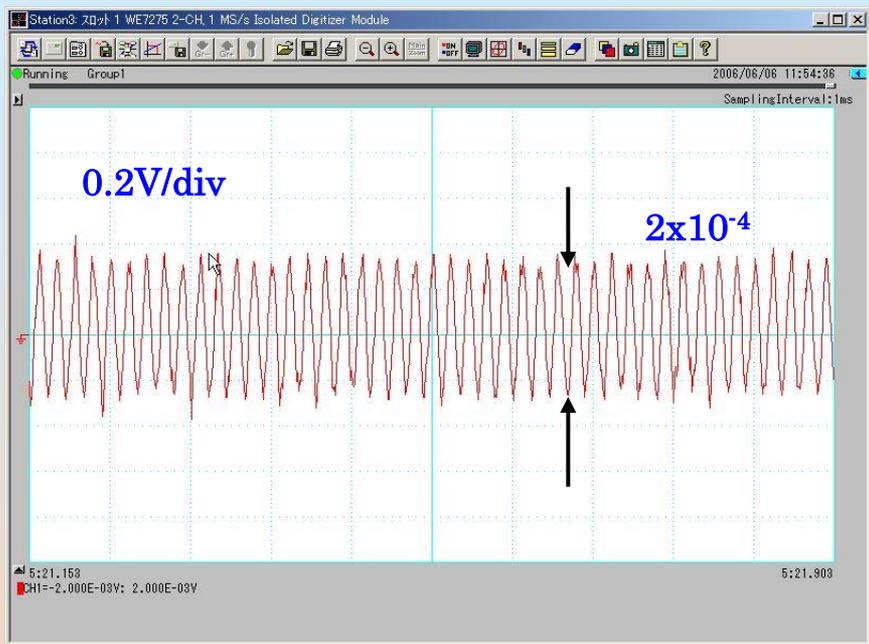


Data in Feb., 2006

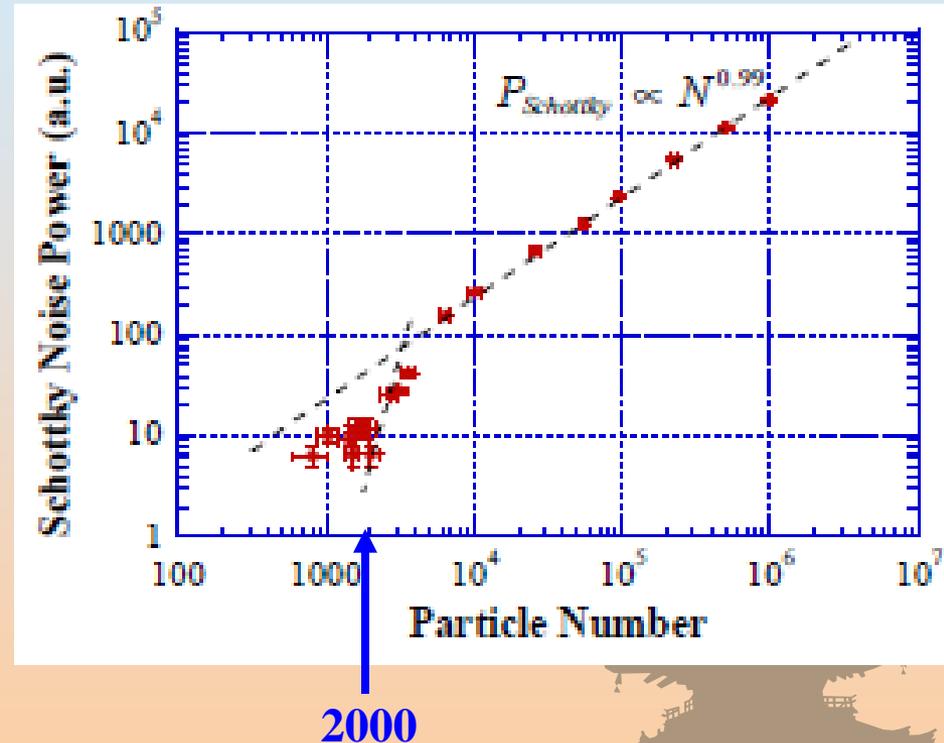
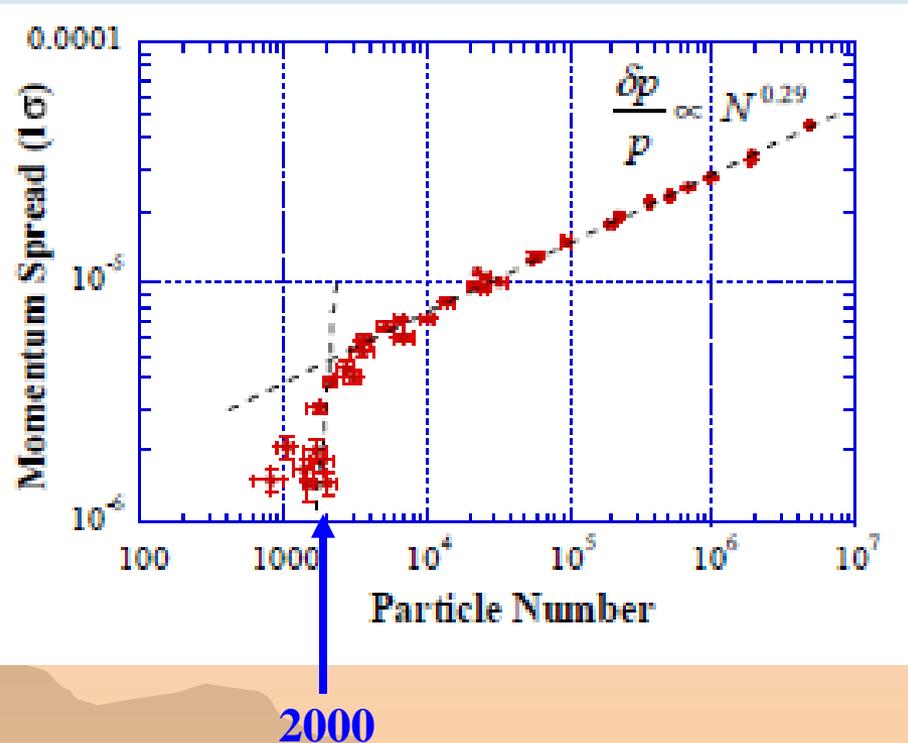


Data on the 8th, June, 2006

Reduction of Ripple in Electron Gun



Abrupt Jump of Momentum Spread and Schottky Power



T. Shirai et al., PRL, 98 (2007) 204801

DNA Double Strand Break by Laser-produced Proton beam

A. Yogo et al., APL, 94, 181502 (2009)

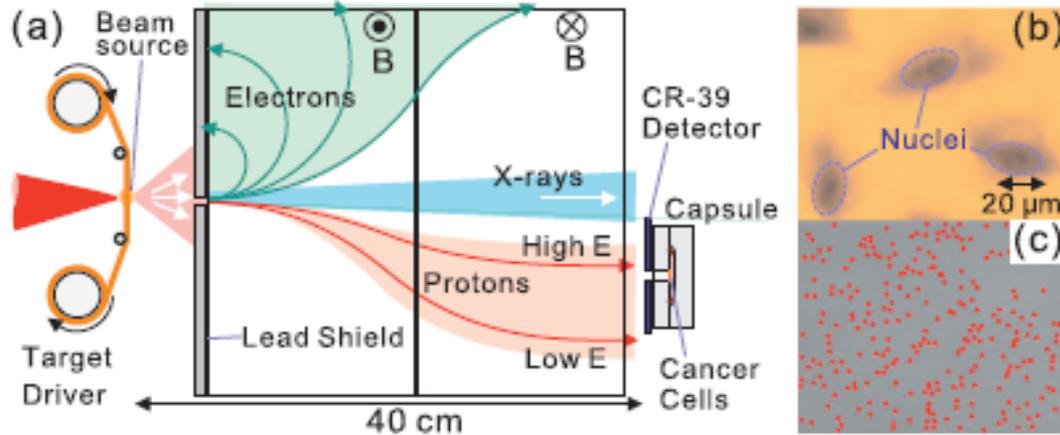


FIG. 1. (Color) (a) A schematic drawing of experimental setup. (b) An image of cancer cells taken by a microscope. (c) A spatial distribution of protons detected by CR-39 in a single laser shot. Each red point represents a single proton bombardment. The screen size is set to be same as that in the frame (b).

Pulse Width 15ns, 20 Gy

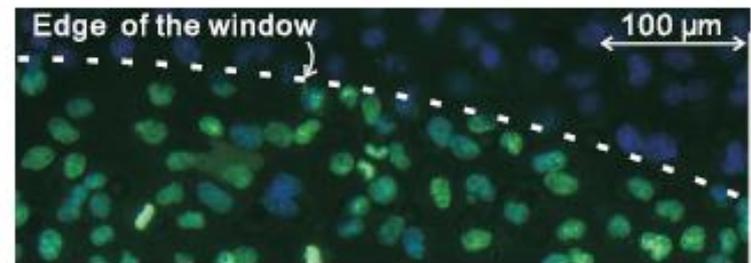
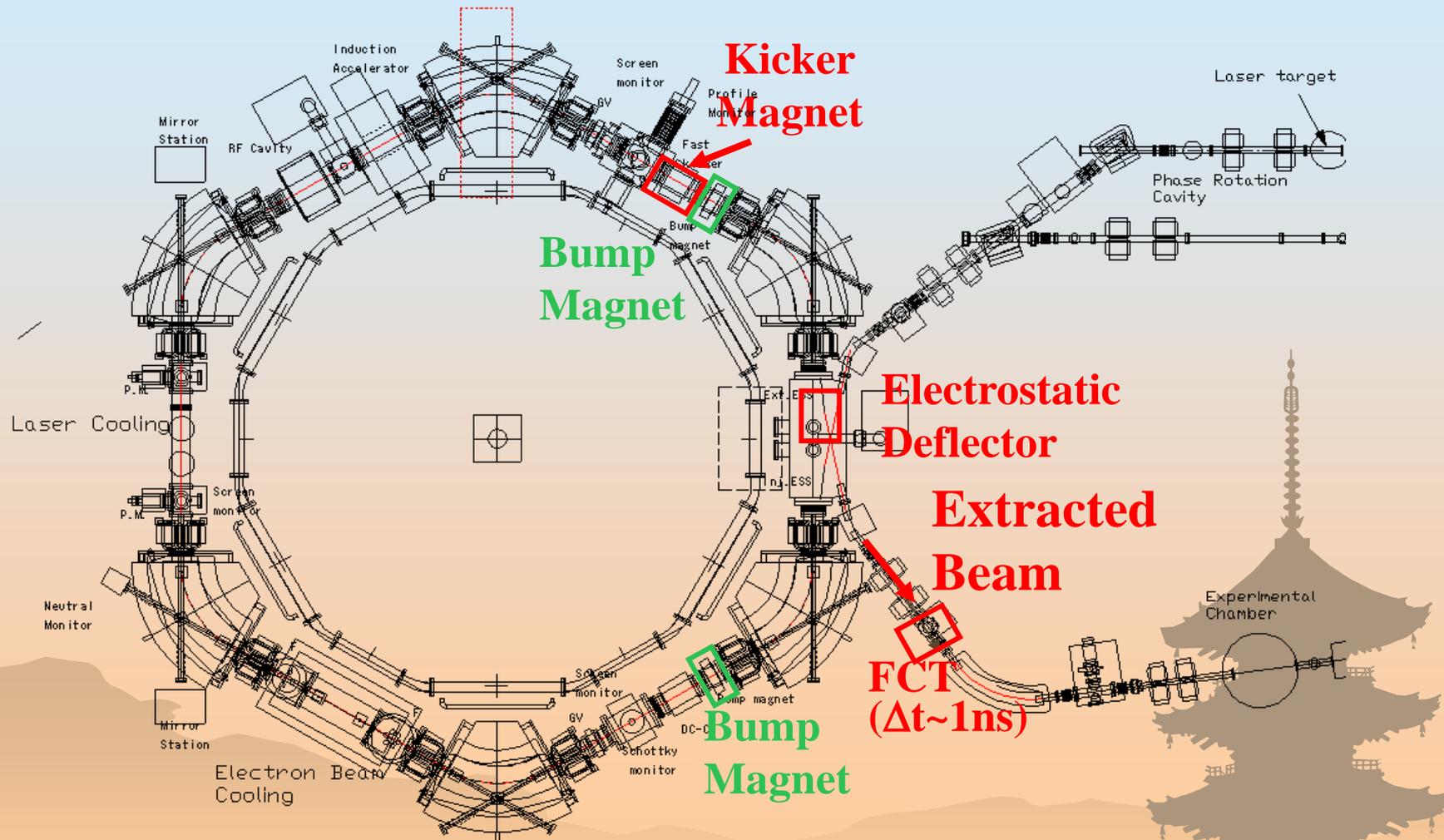
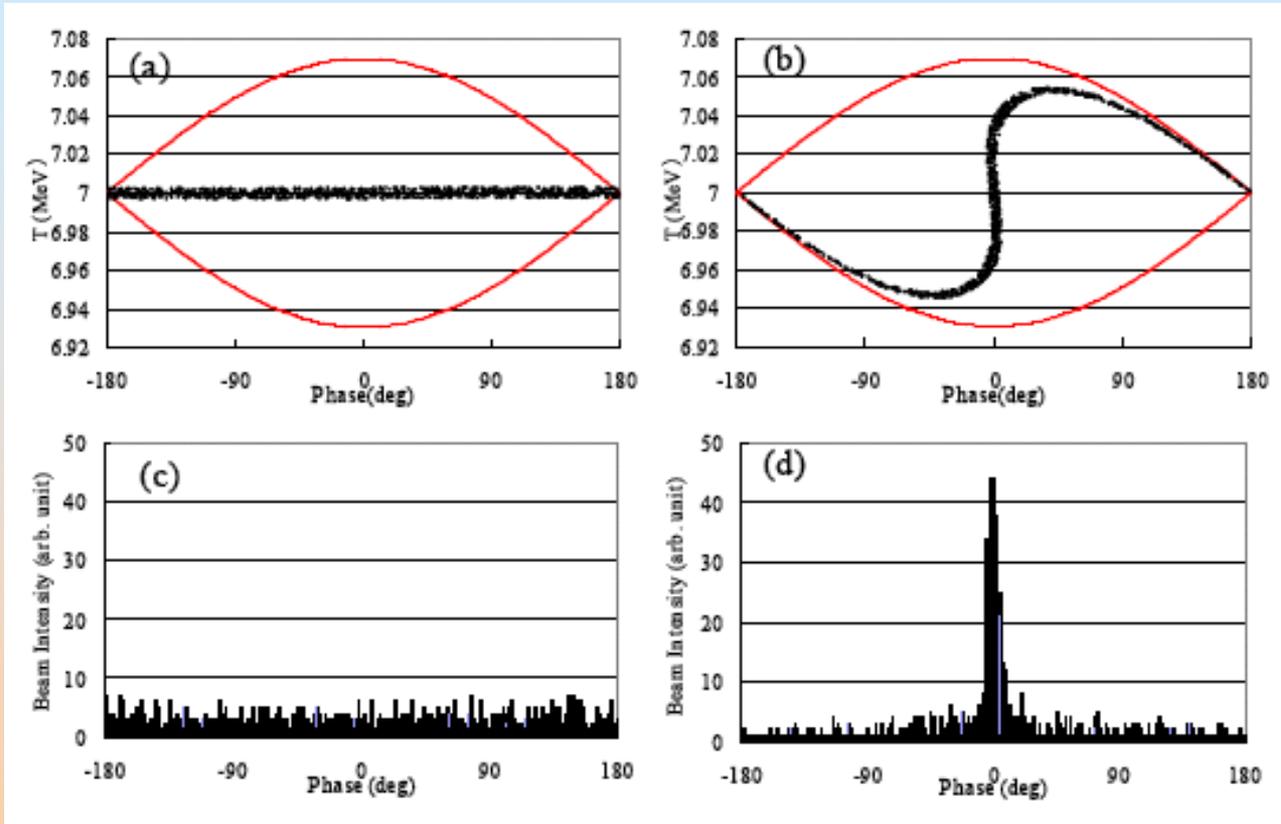


FIG. 3. (Color) γ -H2AX focus formation induced by irradiation of laser-accelerated protons with 20 Gy. γ -H2AX and nucleus are stained with anti- γ -H2AX antibody (green) and DAPI (blue).

Fast Extraction System at S-LSR

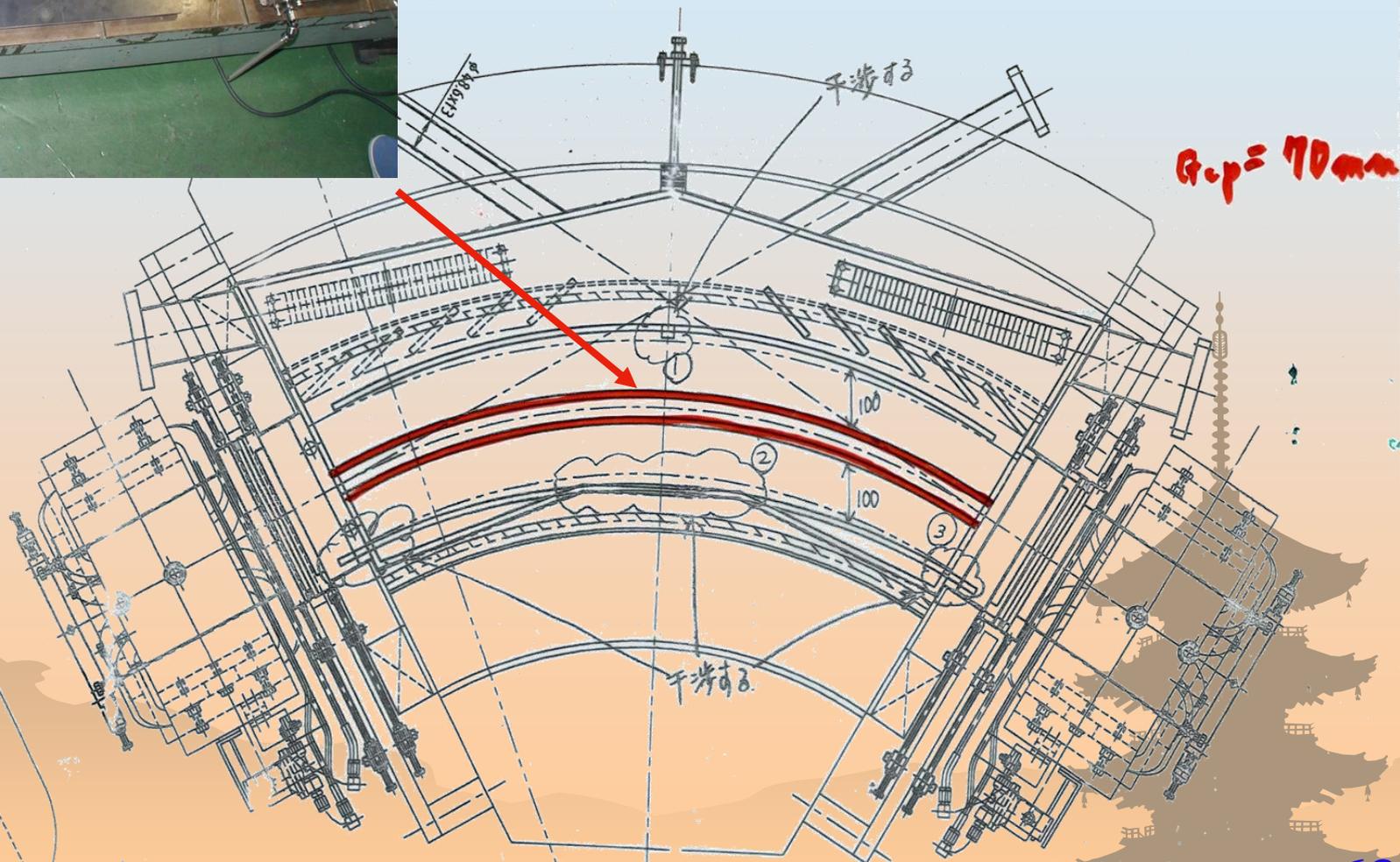


Bunch Rotation of 7 MeV Proton

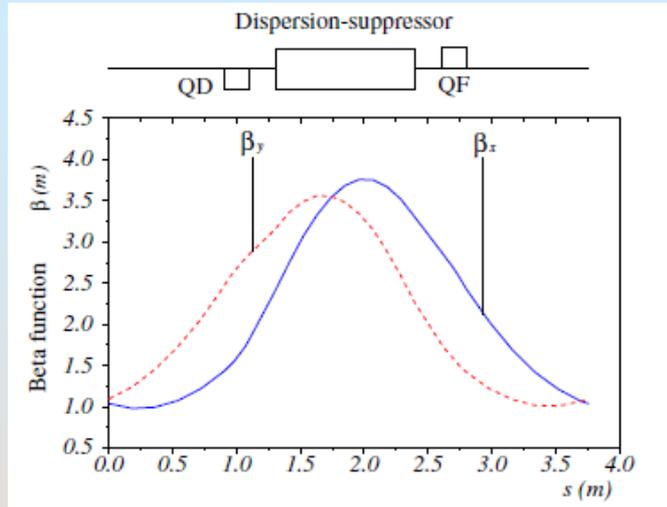


RF field (800 V) is applied to coasting beam after electron cooling and is extracted when the beam is rotated $\sim 90^\circ$.

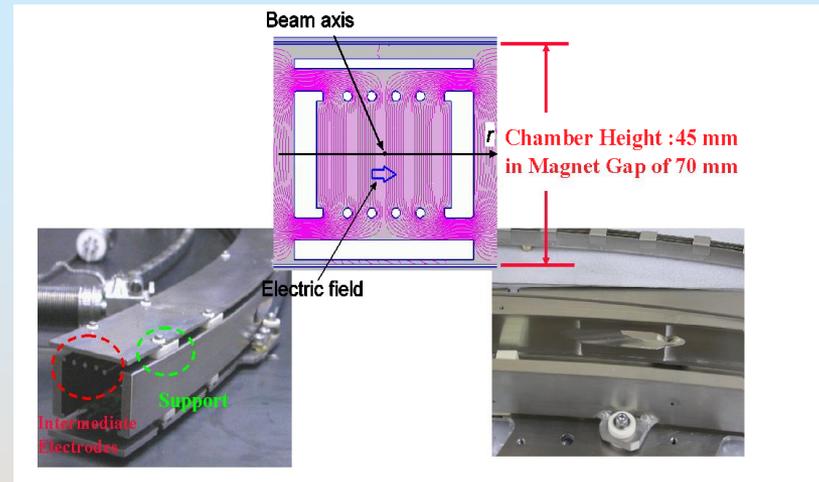
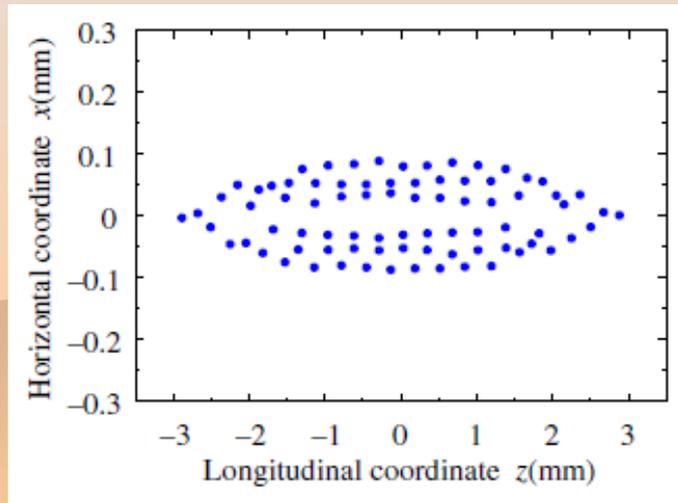
Vacuum Chamber in the Magnet Section (includes the Electrodes)



3D Laser Cooling with Dispersion Free Lattice



$$(v_x, v_y) = (2.07, 2.07)$$



$$2\vec{E} = -(\vec{v} \times \vec{B})$$

A coupling cavity is needed
To couple the longitudinal
and transverse degrees of
Freedom.

A few layers 3D crystalline
beam is expected.

3 D Laser Cooling + INDAC

Operation Point = (2.068, 1.07)

