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Real-Time Feedback on Beam Parameters

... the essentials

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- Stability Requirements
- Medium and Long Term Stability
- 3rd Generation Beam-Based Feedback Design:
 - Space & Time Domain
 - Optimal Controller Design and Non-Linear Control
 - Cross-Dependability and Cross-Constraints between Feedback loops
- Disclaimer: cannot go into/bore you with
 - tedious details
 - details on instrumentation
- Goal: provide roadmap to avoid less obvious pot holes





- Accelerators can be grouped into three groups
 - Light Sources: (list not exhaustive¹⁻³)
 ALBA, ANKA, ALS, APS, BSRF, BESSY, CLS, DELTA, ELETTRA, ESRF, INDUS2, LNSLS, SLS, DIAMOND, SOLEIL, SPEAR3, Spring-8, Super-ACO...
 - mostly orbit and energy feedback (radial steering) only
 - Lepton Collider: LEP⁴, PEP-II⁵, KEK-B
 - orbit and tune feedback (mostly during ramp)
 - Hadron Collider: Hera, LHC, RHIC, Tevatron
 - mostly slow orbit feedback, except:
 - Hera: Orbit, Tune
 - RHIC: Tune⁶/Coupling, Chromaticity⁷
 - LHC: Orbit/Energy, Tune/Coupling, Chromaticity, ...



Beam Parameter Stability in Lepton Machines (e⁺e⁻ Collider, Light Sources, ...)



- Main requirements for orbit stability⁸:
 - Effective emittance preservation
 - (τ_{d} sampling/integration time, $\tau_{fluctuation}$ time)

$$\tau_{d} \gg \tau_{f}: \quad \epsilon_{eff} = \epsilon_{0} + \epsilon_{cm}$$

$$\tau_{d} \ll \tau_{f}: \quad \epsilon_{eff} \approx \epsilon_{0} + 2\sqrt{\epsilon_{0}\epsilon_{cm}} + \epsilon_{cm}$$

- Minimisation of coupling (vertical orbit in sextupoles)
- Minimisation of spurious dispersion (vertical orbit in quadrupoles)
- Collider Luminosity and collision point stability (in case of two separated rings)

$$L = L_0 \cdot \exp\left\{\frac{(\overline{x} - x)^2}{2\sigma_x^2} + \frac{(\overline{y} - y)^2}{2\sigma_y^2}\right\} \cdot 1/\sqrt{1 + \left(\frac{\theta_c \sigma_z}{2\sigma_{x/y}}\right)^2} \quad \dots$$

\rightarrow Nearly all 3rd generation light-sources deploy at least orbit/energy feedbacks¹⁻³







- Traditional requirements on beam stability...
 - ... to keep the beam in the pipe!
- Increased stored intensity and energy:
 - → sufficient to quenches all magnets and/or to cause serious damage⁹
- Requirements depend on:
 - 1. Capability to control particle losses in the machine
 - Machine protection & Collimation
 - Quench prevention
 - 2. Commissioning and operational efficiency



Beam 3 σ envel.

~ 1.8 mm @ 7 TeV



Hadron Collider Requirements LHC Collimation System and Closed Orbit





- LHC Collimation System, N_{max}≈ 5·10¹⁴ protons/beam (nominal)
 - required collimation inefficiency^{10,11}:

 $\eta = \frac{number \ of \ particles escaping \ collimation}{number \ of \ particles \ impacting \ collimation}$

 \rightarrow LHC: η < 0.001

- Orbit stability requirement better than $\sigma/6 < \sim 25 \mu m$ at collimator jaws Several other similar and distributed requirements:
 - local ≈ global requirements¹³



Hadron Collider Requirements on Tune and Chromaticity

- Lepton machines: δQ ~ 10⁻² ... 10⁻³
 - avoid up to ~3rd order resonance
- Hadron machines:
 - negligible synch. radiation damping
 - large tune footprints
 - avoid up to 12th order resonances
- Example LHC:
 - Tune spread (LHC) ΔQ|_{av}≈1.15·10⁻²
 (fixed by available space in Q-diagram)
 - $\rightarrow \delta Q \leq 0.003...0.001$ (nominal)
 - Chromaticity (SPS: Δp/p ≈ 2.8·10⁻⁴)
 - allowed max lin. chromaticity^{14,15} (5-6 σ , first order):

$$Q'_{max} \propto \frac{\Delta Q_{av}}{\Delta p / p} \longrightarrow Q'_{max} \approx 2 \pm 1 \& Q' > 0$$
(expected drifts¹: $\Delta Q' \approx 140$)

Ø^{>,59.35}





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Parameters

Beam

Feedback

APAC'07. Real-Time



- ...can be grouped into:
 - Environmental sources:

(mostly propagated through quadrupoles/girders)

- temperature and pressure changes,
- ground motion, tides,
- cultural noise
- Machine inherent sources:
 - decay and snap-back of multipoles,
 - cooling liquid flow, pumps/ventilation vibrations
 - eddy currents
 - changes of machine optics (final focus)
- Machine element failures:
 - corrector circuits (LHC: 1300++ circuits)







- Feedbacks perform well on short to medium term time scales
- Corrector circuit noise and systematics
 - Hysteresis, eddy-currents, ADC quantisation noise, element failure
 - trend: 10/12 ADC bits \rightarrow 16 ADC bits²⁶ \rightarrow 18/20 ADC bits^{27,28,29}
- Beam instrumentation noise and its systematic
 - Dependence on bunch length and intensity (charge)
 - Thermal expansion of girders, drift of electronics
 - mechanically decoupling/stiffening of BPM girders (Invar, Carbon Fibre)
 - extensive temperature stabilisation:
 - tunnel and cooling water
 - discrete photon absorbers
 - water cooled vacuum chambers
 - 'top-up' operation^{1,2}

e.g. SLS²⁵: electronics: ± 0.1 °C experimental hall: ± 1.0 °C

thermal exp. of steel: 1m of steel, 1°C: Δx≈ 10.. 17 μm





space domain

time

domain

- Feedback controller usually decomposed into three stages:
 - 1 Compute steady-state corrector settings $\vec{\delta}_{ss} = (\delta_{1,...,\delta_{n}})$ based on measured parameter shift $\Delta x = (x_{1,...,x_{n}})$ that will move the beam to its reference position for t $\rightarrow \infty$.
 - 2 Compute a $\vec{\delta}(t)$ that will enhance the transition $\vec{\delta}(t=0) \rightarrow \vec{\delta}_{ss}$
 - 3 Feed-forward: anticipate and add deflections $\vec{\delta}_{ff}$ to compensate changes of well known and properly described¹ sources:



¹ properly described = accurate & fast real-time model of the source





Effects on orbit, Energy, Tune, Q' and C⁻ can essentially be cast into matrices:

$$\Delta \vec{x}(t) = \underline{R} \cdot \vec{\delta}(t) \quad \text{with} \quad R_{ij} = \frac{\sqrt{\beta_i \beta_j}}{2 \sin(\pi Q)} \cdot \cos(\Delta \mu_{ij} - \pi Q) + \frac{D_i D_j}{C(\alpha_c - 1/\gamma^2)}$$

matrix multiplication orbit response matrix
similar for other parameters:
• Tune, Coupling,
• Chromaticity,
• Energy, ...
$$\begin{pmatrix} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{pmatrix} = \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_m \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_1 \\ \cdots \\ \Delta x_1 \\ \cdots \\ \Delta x_1 \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_1 \\ \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_1 \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \Delta x_2 \\ \cdots \\ \Delta x_1 \\ \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \cdots \\ \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \cdots \\ \end{array} \right) \left(\begin{array}{c} \Delta x_1 \\ \end{array} \right) \left(\begin{array}{c} \Delta x_1$$

COD phase $[2\pi]$

- Control consists essentially in inverting above matrices
 - Potential complications: singularities = over/under-constraint matrices, noise, element failures, spurious BPM offsets, calibrations errors, ...
 - Common Workhorse: Singular-Value-Decomposition (SVD¹⁶)
 - all light sources (& LHC) go in this direction!!





- Number of for the inversion used eigenvalues #λ_{svd} steers accuracy versus robustness of correction algorithm
 - Orbit attenuation



Sensitivity to BPM noise





• Machine imperfections (beta-beat, hysteresis....), calibration errors and offsets can be translated into a steady-state ε_{ss} and scale error ε_{scale} :

 $\Delta x(s) = R_i(s) \cdot \delta_i \rightarrow \Delta x(s) = R_i(s) \cdot (\epsilon_{ss} + (1 + \epsilon_{scale}) \cdot \delta_i)$

Integral feedback: Feed-Forward: Reference = 1 Reference = 1parameter parameter actual parameter 1-ε actual parameter error signal $\Delta =$ norm. norm. integral feedback signal 1^{rst} time 2nd nth time

Uncertainties and scale error of beam response function affects convergence speed (= feedback bandwidth) rather than achievable stability





SVD algorithm part of the class of gradient based minima searches



- Implication on optimal feedback sampling frequency:
 - digital approx. of analogue system: $f_s > 10...20 \cdot f_{bw} \xrightarrow{\text{imperf.}} f_s > 20...40++ \cdot f_{bw}$
 - Example f_s/f_{bw} ratios: SLS: 40, ALS: 45, LHC: 25/50 (budget limited)
 14/22





- PID/Controller design often regarded as specialists' topic only wrong!
- Youla^{17,18} showed that all stable closed loop controllers D(s) can be written as:

$$D(s) = \frac{Q(s)}{1 - Q(s)G(s)} \tag{1}$$

Example: first order system

$$G(s) = \frac{K_0}{\tau s + 1}$$
 with τ being the circuit time constant (2)

Using for example the following ansatz:

$$Q(s) = F_Q(s)G^i(s) = \frac{1}{\alpha s+1} \cdot \frac{\tau s+1}{K_0}$$
(3)
E (s) models the desired closed loop response $\rightarrow T_i(s) = \frac{1}{1}$

- F_Q(s) models the desired closed-loop response
- Gⁱ(s) being the pseudo-inverse of the nominal plant G(s)
- (1)+(2)+(3) yields PI controller:

$$D(s) = K_p + K_i \frac{1}{s}$$
 with $K_p = K_0 \frac{\tau}{\alpha} \wedge K_i = K_0 \frac{1}{\alpha}$

 $\alpha s+1$





- $\alpha > \tau... \infty$ facilitates the trade-off between speed and robustness
 - quantitative verification of loop stability w.r.t. noise, model errors ...
 - operator has to deal with one parameter $\rightarrow\,$ enables simple adaptive gain-scheduling based on the operational scenario!







If G(s) contains non-stable zeros e.g. delay λ & non-linearities G_M(s)

$$G(s) = \frac{e^{-\Lambda s}}{\tau s + 1} \cdot G_{NL}(s)$$

- with τ the power converter time constant, then:
- $G^{i}(s) = \frac{\tau s + 1}{1}$ Using (1) and (3) yields $T_0(s) = F_0(s) \cdot e^{-\lambda s} G_{NL}(s)$
- Inserting in (1) yields Smith-Predictor and Anti-Windup schemes:





Motivation for Smith-Predictor and Anti-Windup Example: LHC orbit feedback control



amping rate ΔI/Δt [A/s]









- orbit micrometer constraint
 - Improves machine performance
 - Significantly minimises feed-down effects of higher multipoles (esp. coupling)
 - No (large) kicks/momentum modulation: Q/Q' measurements have to measure within the stability requirements
 - Development of new tune measurement techniques²³
 - CERN SPS/LHC tune PLL operates within < 1 μ m excitation level^{21,22}
- Robust tune feedback requires measurement/control of Coupling²⁴
 - Additional decoupling between PLL phase and amplitude²²









Beam response: open loop gain $K_0 \sim$ phase response slope

- Common^{4-6,19} (classic) PLL loop design: $K_0 = \text{const.}$ & filter bandwidth = 1/T
 - \rightarrow PLL low-pass:

$$G(s) = \frac{K_0}{\tau \, s + 1}$$

Note: K_0 const. for $|\Delta \phi| \le 60^\circ$ (linear. regime) K_0 depends on Q' (non-linear. regime)

- Optimal tune PLL gain parameters depend on chromaticity^{20,21}
 - Optimal PI for high Q' \leftrightarrow sensitivity to noise (unstable loop) for low Q'
 - Optimal PI for small $Q' \leftrightarrow$ slow tracking speed for large Q'





- Traditionally loop designs are often addressed one-by-one
 - neglects cross-dependence and cross-constraints w.r.t. other nested FB loops



Additional cross-dependence with orbit and energy feedback (dispersion orbit)
 ^{21/22}



Conclusion



- Beam-based FBs are remedies for perturbations on slow/medium time scales
 - Limited by thermal drifts, noise and systematics of involved devices
 - Systematic and thorough analysis of involved beam instrumentation and corrector circuits is essential!
 - Use of imperfect (design) beam response for SVD based FB Systems:
 - does not affect the precision of the correction but reduces rather the effective bandwidth \rightarrow favours higher feedback sampling frequencies
- Youla's affine parameterisation facilitates optimal adaptive non-linear control
 - enables gain-scheduling based on operational scenario
 - (Ziegler-Nichols/Coohen-Coon PID tuning are outdated!)
- Beware of cross-constraints/coupling of simultaneous nested loops:
 - Feedbacks should be designed as an ensemble

The author gratefully acknowledges contributions from many colleagues!





Reserve Slides



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IWBS'04: "LHC is a pretty dangerous machine" Livingston Style plot















- Stabilisation "record" in the SPS
 - 270 GeV coasting (proton) beam,
 72 nom. bunches, $β_ν ≈ 100$ m
 - rivals most modern light sources
 - magnitudes better than required
 - Target: maintain same long term stability









Full LHC orbit simulation @1KHz sampling, (BPM sampling: 25Hz)







Full LHC orbit simulation @1KHz sampling, (BPM sampling: 25Hz)







• ... sample the position (Q, ...) at 10Hz to achieve a closed loop 1Hz bandwidth



- ... a theoretic limit assuming a perfect system!
- common: sampling frequency > 25 ...40 desired closed-loop bandwidth





Automated Orbit Correction using Singular Value Decomposition







The superimposed beam position shift at the ith monitor due to single dipole kicks is described through the orbit response matrix \underline{R} . It can be written as

$$\Delta x_i = \sum_{j=0}^{n} R_{ij} \cdot \delta_j \quad \text{with} \quad R_{ij} = \frac{\sqrt{\beta_i \beta_j}}{2\sin(\pi Q)} \cdot \cos(\Delta \mu_{ij} - \pi Q)$$

$$\Leftrightarrow \quad \Delta \vec{x} = \sum_{j=0}^{n} \delta_j \vec{u}_j \quad \text{with} \quad \vec{u}_j = (R_{1j}, \dots, R_{mj})^T \Leftrightarrow \quad \Delta \vec{x}(t) = \underline{R} \cdot \vec{\delta}_{ss}$$

where (β,μ,Q) depends on the machine optic (example: Q=4.31).





Theorem from linear algebra*:



eigen-vector relation:

$$\lambda_i \vec{u}_i = \underline{R} \cdot \vec{v}_i$$
$$\lambda_i \vec{v}_i = \underline{R}^T \cdot \vec{u}_i$$

final correction is a simple matrix multiplication

large eigenvalues ↔ bumps with small COD strengths but large effect on orbit

$$\vec{\delta}_{ss} = \tilde{R}^{-1} \cdot \Delta \vec{x} \quad with \quad \tilde{R}^{-1} = \underline{V} \cdot \underline{\lambda}^{-1} \cdot \underline{U}^T \quad \Leftrightarrow \quad \vec{\delta}_{ss} = \sum_{i=0}^n \frac{a_i}{\lambda_i} \vec{v}_i \quad with \quad a_i = \vec{u}_i^T \Delta \vec{x}$$

Easy removal of singular (=undesired, large corrector strengths) eigen-values/solutions:

- near singular eigen-solutions have $\lambda_i \sim 0$ or $\lambda_i = 0$
- to remove those solution: $\lim \lambda_i \rightarrow \infty 1/\lambda_i = 0$

discarded eigenvalues corresponds to bumps that won't be corrected by the fb

*G. Golub and C. Reinsch, "Handbook for automatic computation II, Linear Algebra", Springer, NY, 1971





Eigenvalue spectra for vertical LHC response matrix using all BPMs and CODs:





































- CERN's Technical Network as backbone
 - Switched network
 - no data collisions
 - no data loss
 - double (triple) redundancy
- Core: "Enterasys X-Pedition 8600 Routers"
 - 32 Gbits/s non-blocking, 3·10⁷ packets/s
 - 400 000 h MTBF
 - hardware QoS
 - One queue dedicated to real-time feedback
 - ~ private network for the orbit feedback
- Routing delay
- Iongest transmission delay (exp. verified)

(500 bytes, IP5 -> Control room ~5 km)

- 20% due to infrastructure (router/switches)
- 80% due to traveling speed of light inside the optic fibre





- ~ 13 µs
- ~ 320 µs





- The maximum latency between CCC and IR5
 - tail of distribution is given by front-end computer and its operating system







Two main strategies:

- actual delay measurement and dynamic compensation in SP-branch:
 - high numerical complexity, due to continuously changing branch transfer function
 - only feasible for small systems
- Jitter compensation using a periodic external signal:
 - CERN wide synchronisation of events on sub ms scale that triggers:
 - Acquisition of BPM system, reading of receive buffers, processing and sending of data, time to apply in the power converter front-ends
 - The total jitter, the sum of all worst case delays, must stay within "budget".
 - Measured and anticipated delays and their jitter are well below 20 ms.
 - feedback loop frequency of 50 Hz feasible for LHC, if required...







- The front-end network interfaces are presently the bottleneck. e.g. feedback controller @ 50 Hz:
- lots of in-/outbound connections:
 - Two types of loads:
 - Real-Time: BPM and COD control data
 - Avg. bandwidth: ~13 Mbit/s
 - short bursts: full I/O load within few ms (100 MBit/s resp. 1GBit/s, burst duration desired to be short in order to minimise the total loop delay)
 - Non-Real-Time:
 - transfer of new settings to OFC (matrix ~30 MB)
 - PID configuration etc.
 - relay of BPM and feedback data (monitoring/logging)
 - ..

- non RT-traffic
- (Peak) load similar to high-end network servers
 - Nearly constant full load during certain operational phases
- network interface should be scheduled on the device level to provide a Quality of Service (QoS) for real-time data
 - One reserved FIFO queue for feedback data
 - General purpose queue for other data







Hardware:

- both rings covered by 1056 BPMs
- Measure both planes (2112 readings)
 - Organised in front-end crates (PowerPC/VME) in surface buildings
 - 18 BPMs (hor & vert) ⇔ 36 positions / VME crate
 - 68 crates in total, 6-8 crates /IR

Data streams:

- Average data rates per IR:
 - 18 BPMs x 20 bytes+overhead
 - 1056 BPMs x 20 byte
 - @ 10 Hz:
 - @ 50 Hz:

- ~1500 bytes / sample / crate
 - 94 kbytes / sample
- ~ 7.7 Mbit/s
- ~ 38.4 Mbit/s
- Peak data rates (bursts): 100Mbit/s resp. 1Gbit/s (depending on Ethernet interface)







- Two main dynamic contributions
 - Delays: computation, data transmission, etc.
 - Slew rate of the corrector circuits (voltage limitation): $\Delta I/\Delta t|_{max} < 0.5 \text{ A/s}$
 - ±60A converter:
 - ±600A converter:



 $\Delta I/\Delta t|_{max} < 10 \text{ A/s}$





- The open-loop corrector circuit bandwidth depends on the excitation current:
 - non-linear phase once rate limiter is in action

