

# COMBINING MULTIPLE BPM MEASUREMENTS FOR PRECESSION AC DIPOLE BUMP CLOSURE\*

P. Oddo, M. Bai, C. Dawson, J. Kewisch, Y. Makdisi, C. Pai, P. Pile, T. Roser  
BNL, Upton, NY 11973, USA

## Abstract

For the RHIC spin flipper to achieve a rotating field, it requires operating five AC dipoles as a pair of closed orbit bumps. One key requirement is to minimize the remnant AC dipole driven betatron oscillation outside of the spin flipper by 50 dB [1]. In the past, due to its inherent sensitivity, a single pickup with a direct-diode detector (3D) [2] and dynamic signal analyzer (DSA) were used to measure bump closure by measuring the remnant oscillations. This however proved to be inadequate, as the betatron phase advance between the AC dipoles is non-zero. A method of combining multiple BPMs into a sensitive measure of bump closure has been developed and was tested during RHIC polarized proton operation in 2013. This technique as well as the experimental results will be presented.

## INTRODUCTION

A spin flipper for RHIC (Relativistic Heavy Ion Collider) has been developed for RHIC spin-physics experiments. It is needed to cancel systematic errors by reversing the spin direction of the two colliding beams multiple times during a store [3].

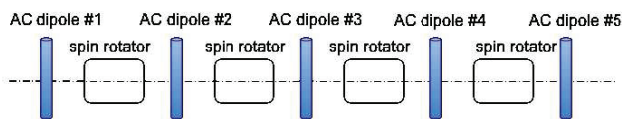


Figure 1: Spin flipper configuration.

The spin flipper system consists of four DC dipole magnets (spin rotators) and five AC dipole magnets (see fig. 1). The aim of this configuration is to produce a rotating field. Multiple AC dipoles are needed to localize the driven coherent betatron oscillation inside the spin flipper [1, 4]. While results from the 2012 run did suggest the presence of a rotating field, the polarization lifetime was degraded with the AC dipoles on. This suggested incomplete bump closure and/or incorrect phase between bumps [1] which lead to reinvestigating the method used to close the AC dipole bumps.

Operationally the AC dipoles form two bumps that minimize the effect of the AC dipoles outside of the spin flipper. The central AC dipole, #3 in figure 1, is common to both bumps. Both AC-dipole bumps operate at the same frequency, but are phase shifted from each other. The convention used when expressing closure in dB is to make the 0 dB reference the strongest AC dipole. In case of the dual bump, AC dipole #4 is used.

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## BBQ 3D AFE & DSA

Up until the 2013 run the closure was only trimmed using the pickup and direct-diode detector (3D) analog front end (AFE) of the RHIC baseband tune meter (BBQ) processed via a DSA.

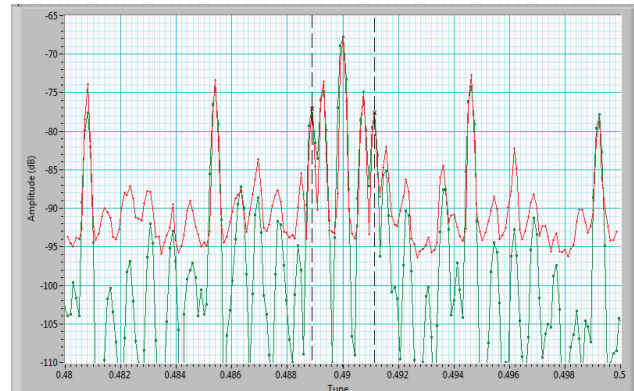


Figure 2: Closed bump DSA beam spectrum (green plot). The red plot is the fitted AC dipole magnet currents.

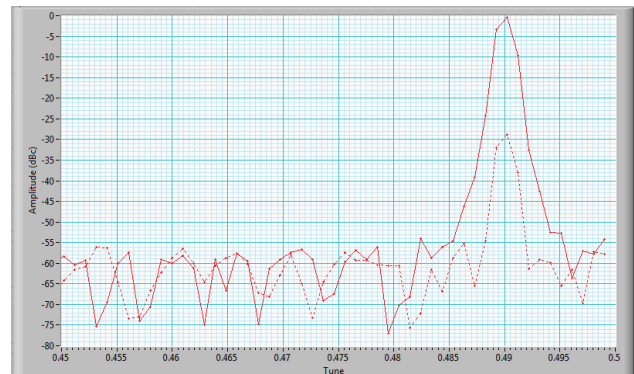


Figure 3: AC dipole #4 alone (solid) and closed bump BPM beam spectrum of the most sensitive BPM.

The DSA spectrum in figure 2 (green plot) shows that the closure for the AC dipole bumps was 67 dB. However, the spectrum of the most sensitive BPM (fig. 3, dotted plot) shows a closure of only 28 dB. This nearly two order of magnitude difference clearly shows that it's not possible to determine closure using a single pickup (at a single frequency). The possibility of using a single pickup at multiple frequencies has not yet been fully explored.

## COMBINING BPM MEASUREMENTS

Even though discrete Fourier transform (DFT) spectrums, which typically are calculated using the fast Fourier transform (FFT) algorithm, are used here, these

methods are not strictly DFT/FFT methods. As a matter of fact the BPM magnitude and phase used by software calculations used a sine/cosine fit, which can be thought of as the evaluation of the discrete time Fourier transform (DTFT) or z-transform at a single frequency.

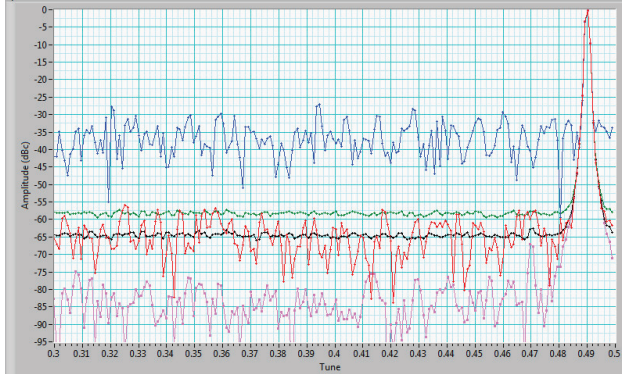


Figure 4: BPM spectrums of weakest (blue), strongest (red), average (green), weighted average (black) and vector average (purple) for AC dipole #4 at 90  $A_{pk}$  (76 G·m) for PP at injection (23.8 GeV).

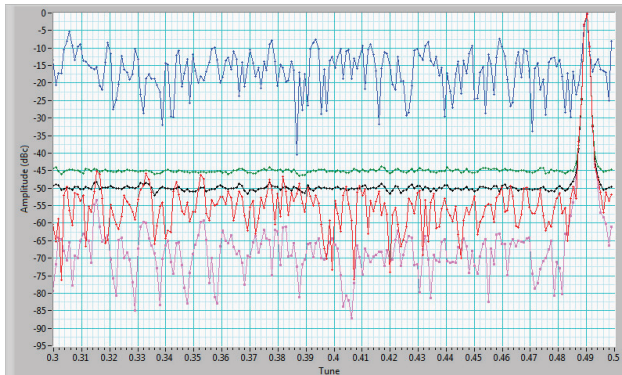


Figure 5: BPM spectrums of weakest (blue), strongest (red), average (green), weighted average (black) and vector average (purple) for AC dipole #4 at 117.9  $A_{pk}$  (100 G·m) for PP at store (255 GeV).

Figures 4 and 5 show the weakest and strongest BPM spectrums and the spectrums for different methods of combining BPMs for polarized proton beam at injection and store respectively when excited by a single AC dipole (#4). In all cases the response is normalized to place the AC dipole peak at the driven frequency (0.49) at 0 dB. This is done as convenient way to visualize the signal to noise ratio. BPM data was taken with 1024 turn data records. For the 2013 run, 4096 turn records were available and these longer records would improve the signal to noise ratio by 6dB. Also note that the AC dipole excitation is 2 dB stronger for the data taken at store. The weakest BPM responses (blue traces) do change proportionally with the change in energy or magnetic rigidity ( $\sim 20$  dB). The strongest response (red traces) changes less ( $\sim 12$ dB), which is just a direct result of the optics also being different. The weakest and strongest responses were also produced by different BPMs.

The average response (green trace) is just a simple magnitude average:

$$k_s \sum_{n=1}^N |Y_n| \quad (1)$$

$Y_n$  is the frequency response for BPM  $n$  and  $k_s$  is a scale factor which normalizes the average to 1 (0 dB) when excited by a single AC. Since this is a magnitude response of all BPMs, all need to be zero for this to be zero and this would only happen for a closed bump. The noise floor for 1024 turn data at store was  $\sim 45$  dB.

The weighted average (black trace) is a magnitude average weighted by each BPM's normalized signal to noise ratio squared:

$$\sum_{n=1}^N a_n |Y_n| \quad (2)$$

Software calculations for  $a_n$  use the mean magnitude of the DFT/FFT bins from 0.025 to 0.48 as the estimated noise value. The RMS error from a fit could also be used. The noise floor for 1024 turn data at store was  $\sim 50$  dB.

The vector average (purple trace) scales frequency response of each BPM by the normalized signal to noise ratio squared, just as the weighted average, but also counter rotates the phase by measured phase:

$$\sum_{n=1}^N a_n e^{-i\phi_n} Y_n \quad (3)$$

Phase  $\phi_n$  is the measured phase of BPM  $n$  when it was excited by a single AC dipole. The noise floor for 1024 turn data at store was  $\sim 70$  dB. While this might look like a good candidate for determining bump closure, because this is a linear combination of BPMs, it is possible for it to be zero for combinations of only two AC dipoles and therefore not useful for definitely trimming bump closure (see eqn. 6 of next section).

### Frequency Response of Multiple AC Dipoles

From previous treatments of transverse beam motion due to a single AC dipole [5] the basic equation of motion can be thought of as a discrete sampled time system, but the actual sampling is done by a particle or bunch.

Extending the model for an arbitrary number of AC dipoles in the time domain is:

$$\begin{pmatrix} y_0[n] \\ y'_0[n] \end{pmatrix} = \mathbf{M} \begin{pmatrix} y[n-1] \\ y'[n-1] \end{pmatrix} + \begin{pmatrix} e[n] \\ e'[n] \end{pmatrix} \quad (4)$$

$$\begin{pmatrix} e[n] \\ e'[n] \end{pmatrix} = g_{acd} \sum_{k=1}^N \mathbf{M}_{kN} \begin{pmatrix} 0 \\ i_1[n] \end{pmatrix} \quad (5)$$

Functions  $y_0[n]$  and  $y'_0[n]$  are the beam position and slope at center of the last AC dipole,  $e[n]$  and  $e'[n]$  are the effective stimulus of all AC dipoles, matrix  $\mathbf{M}$  is the transport matrix for a full turn,  $g_{acd}$  is a constant which converts magnet current into deflection (units  $A^{-1}$ ) and matrix  $\mathbf{M}_{kN}$  is the transport matrix from AC dipole  $k$  to the last AC dipole ( $N$ ).

These equations illustrate that superposition can be used and that each AC dipole stimulus includes the path or optics to the reference point (center of last AC dipole).

Although not presented here, eqns. 4 and 5 can be transformed into the frequency domain. However, since this is a linear time invariant (LTI) system, certain assumptions can be made. The first is that the BPM position is a superposition of AC dipole currents:

$$Y_n(z) = \sum_{m=1}^M H_{nm}(z) I_m(z) \quad (6)$$

$H_{nm}(z)$  is the transfer function from AC dipole  $m$  to BPM  $n$ , with  $M$  the number of AC dipoles.

Similarly, based on eqn. 5, BPM position is also a superposition of the error signals:

$$Y_n(z) = G_n(z)E(z) + G'_n(z)E'(z) \quad (7)$$

$G_n(z)$  and  $G'_n(z)$  are the transfer functions from AC dipole stimulus (or bump error) signal to BPM position  $n$ .

While both eqns. 6 & 7 were shown as continuous functions in  $z$ -transform form, actual calibrations are done at a fixed frequency ( $z=e^{i2\pi Q_{acd}}$ ). The calibration process then just becomes a matter of multiplying complex constants. The transfer functions  $H_{nm}$  are also not calculated from a model, but a result of BPM position and AC dipole current measurements. For a single AC dipole on one at a time (superposition) eqn. 6 becomes:

$$H_{nm}(z) = \frac{Y_n(z)}{I_m(z)} \quad (8)$$

Not shown, but it's also possible to derive these transfer functions from stepped AC dipole data.

### *Closing AC Dipole Bumps Using Calculated Correction Factors*

Once the transfer functions have been determined, eqn. 6 can be used to solve for the precise currents needed to close a bump by setting  $Y_n=0$  and solving for currents (or correction factors). Since the spin flipper contains two bumps, both need to be calculated separately using:

$$H_{n3} = 2k_2 H_{n2} - k_1 H_{n1} \quad (9)$$

$$H_{n3} = 2k_4 H_{n4} - k_5 H_{n5} \quad (10)$$

These equations assume a value for the shared AC dipole (#3) and calculate correction factors ( $k_1$ ,  $k_2$ ,  $k_4$ , and  $k_5$ ) for the other four magnets assuming ideal settings.

Two methods have been used to calculate these correction factors. One involves a matrix operation using all BPMs at once for eqn. 9 and 10. The other method is a cutting method that involves iteratively calculating average correction factors for all combinations of BPM pairs and removing BPM pairs that produce correction factors that deviates more than four standard deviations from the average.

### *Measuring Bump Closure by Estimating AC Dipole Stimulus Components*

A direct consequence of eqn. 7 is that the total AC dipole stimulus or bump error components ( $E$ ,  $E'$ ) can be calculated using pairs of BPMs using:

$$E = p_n Y_n + p_m Y_m \quad (11)$$

$$E' = p'_n Y_n + p'_m Y_m \quad (12)$$

The  $E$  and  $E'$  used are the ideal values calculated from the magnet current (based on eqn. 5). The scaling convention used is to make both  $E$  and  $E'$  equal 1 when excited by AC dipole #4 alone. Constants  $p_n$ ,  $p_m$ ,  $p'_n$ , and  $p'_m$  are then calculated using matrix operations while iterating over all BPM pairs (each of BPM  $n$  and  $m$ ). These constants are summed and scaled to produce coefficients for each BPM so that producing the  $E$  and  $E'$  response only requires a single pass over the BPM data. The scaling used depends on which BPM pairs were used. When using all BPM pairs, the scaling should use the normalized signal to noise ratio squared to improve the resultant signal to noise ratio. When only using the final pairs used to calculate the bump correction factors, then the coefficients only need to be normalized by the number of pairs.

## CONCLUSION

It is possible to combine multiple BPM measurements to close the AC dipole bumps. Using the calculated correction factors produced good results during the 2013 run. There are also numerous ways to verify closure, and this still includes the 3D pickup and DSA.

## REFERENCES

- [1] M. Bai et al, "RHIC Spin Flipper Commissioning Results," Proceedings of IPAC'12, 2012.
- [2] M. Gasior et al, "The Principle and First Results of Betatron Tune Measurement by Direct Diode Detection," LHC-Project-Report 853, 2005.
- [3] M. Bai et al, "RHIC Spin Flipper," Proc. 2007 IEEE U.S. Part. Accel. Conf., 2007.
- [4] M. Bai et al, "Commissioning of RHIC Spin Flipper," Proceedings of IPAC'10, 2010.
- [5] S. Peggs et al, "Nonlinear diagnostics using an AC dipole," RHIC/AP/159, 1998.