

SPACE CHARGE EFFECTS AND FOCUSING METHODS FOR LASER ACCELERATED ION BEAMS



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Laser Ion Generation, Handling and Transport

Contents



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Introduction:

- The LIGHT-Project
- Simulation setup, major tasks and objectives

Part 1: Space charge and beam/bunch model

- Space charge criteria and beam model
- Deneutralization with thin metal foil
- Sample calculation

Part 2: Focusing methods

- Focusing with pulsed solenoid
- Combination of space charge criteria and focusing
- Inductive coupling and ohmic losses

Conclusions

Outlook

LIGHT – Laser Ion Generation, Handling and Transport

(see e.g. A. Almomani et al: *LIGHT Project Report*)

Experimental sequence:

- GSI *PHELIX* Laser hits a thin metal foil target
- Proton plasma is accelerated by TNSA mechanism (e.g.)
- Proton beam is focused and carried to re-buncher cavity

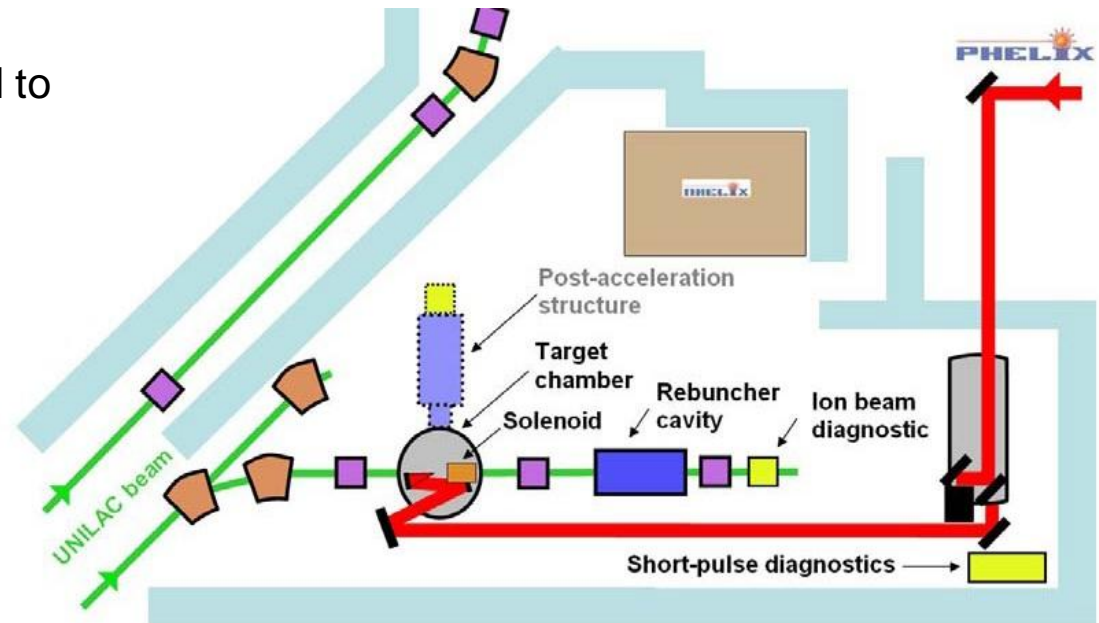


Fig from: A. Almomani, S. Busold et. al. : *LIGHT Project report*

Z6 target chamber

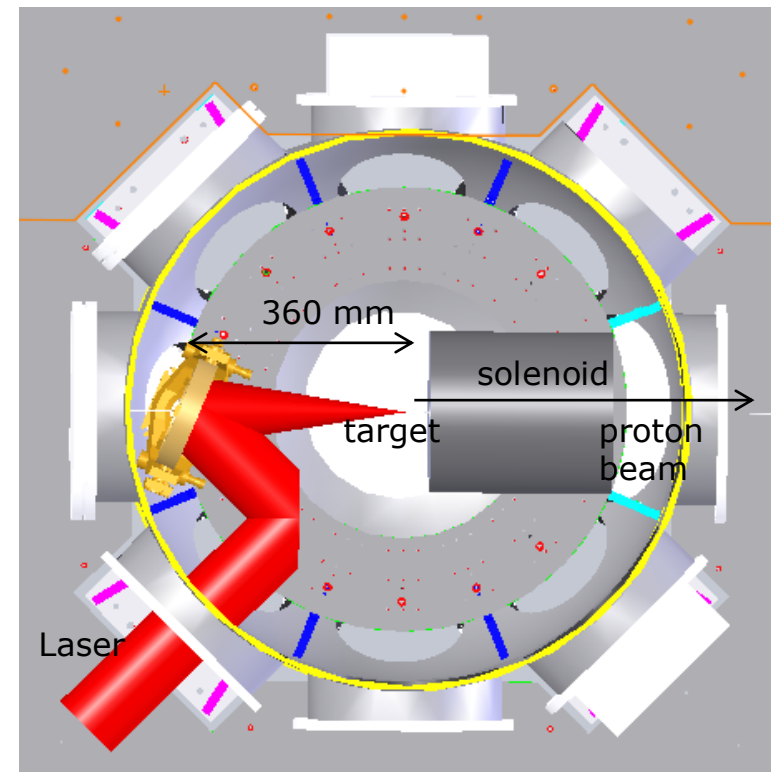


Fig from: S. Busold et. al. : *DPG 2012 Stuttgart talk*



From TNSA mechanism we know:

- High intense proton beam
- Beam shows high energy spread
- After acceleration beam can be treated as quasi neutral: Protons and co-moving electrons
- Beam shows high initial divergence

Z6 target chamber

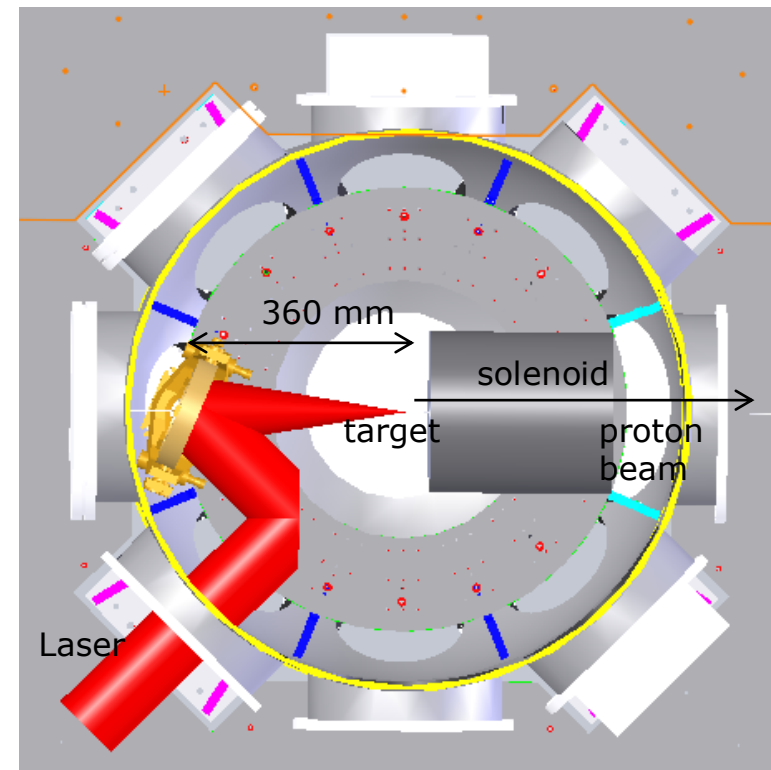


Fig from: S. Busold et. al. : DPG 2012 Stuttgart talk

Considered area:

- Beam properties and models after acceleration
- Beam focusing and collimation methods
- Optical and technical properties of the focusing elements

Z6 target chamber

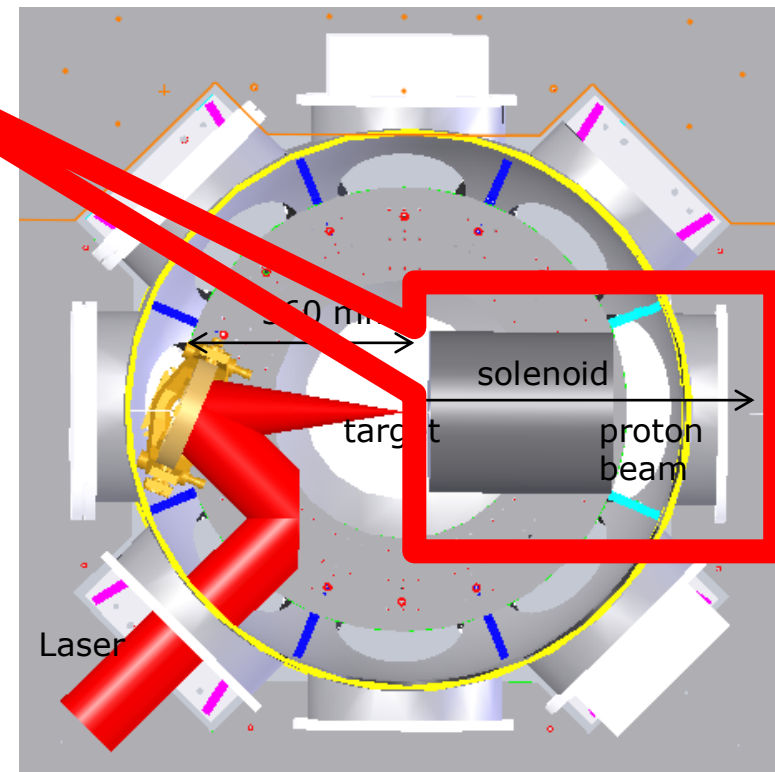
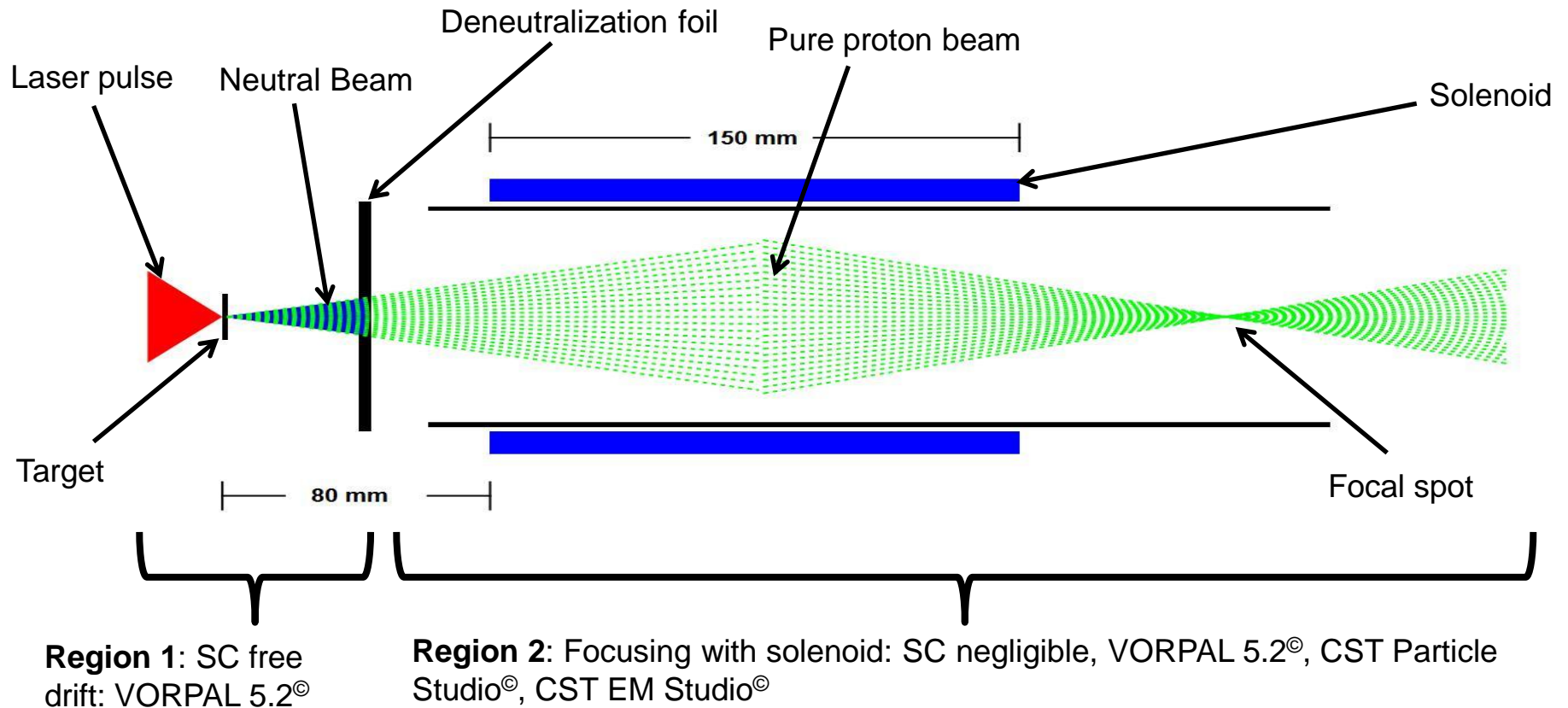


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Sketch of simulation setup



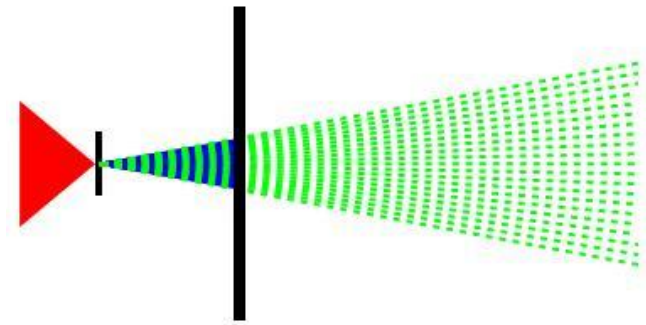
Major Objectives, Tasks and Tools

Region 1:

- Neutral beam of protons and co-moving electrons drifts into space
- A thin metal foil removes all electrons of the beam

Tasks: Where to place the foil, so that after the foil space charge can be neglected?

Tools: VORPAL 5.2[©]



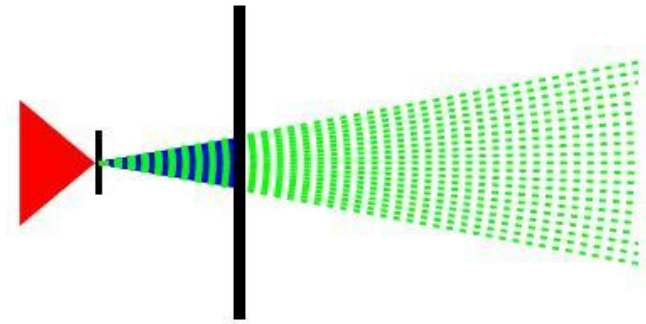
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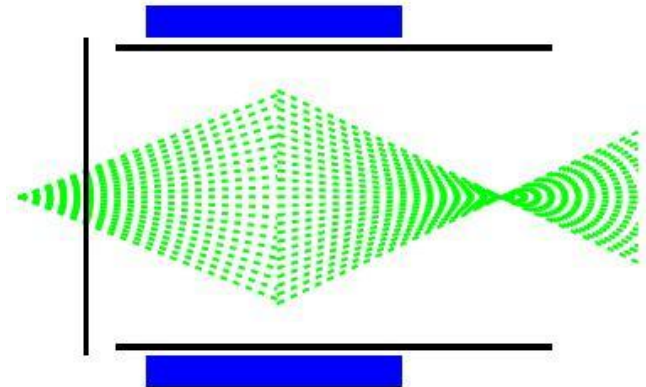
Region 2:

- Pure proton beam focused by a pulsed power solenoid
- Space charge negligible

Tasks:

- Verify the Space charge criterion
- Get optical and technical properties of the solenoid

Tools: VORPAL 5.2[©], CST Studio[©]



Space charge and beam model



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Simple bunched beam model:

- Homogeneous cylindrical bunch
- Has Initial divergence
- Longitudinal energy spread
- Consists of protons and co-moving electrons

Space charge and beam model



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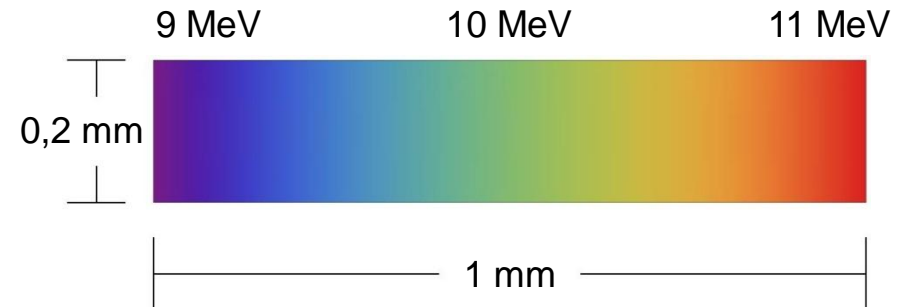
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Reference Parameters:

N_0	$1 \cdot 10^{11}$
r_0	0,1 mm
l_0	1 mm
E_{kin}	10 MeV
ΔE_{kin}	± 1 MeV

Bunch model:



Space charge and beam model



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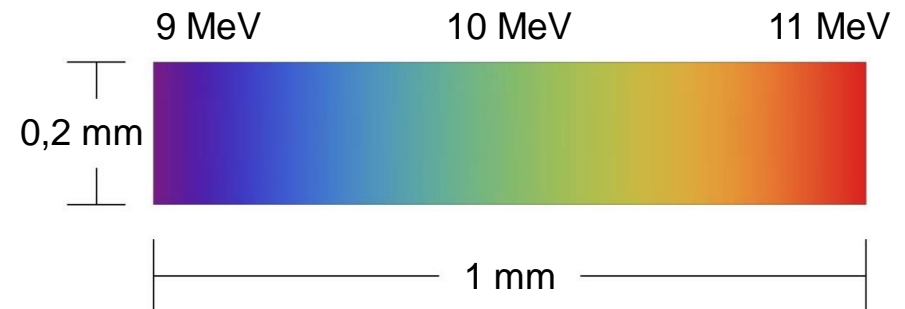
Approximations:

- Longitudinal expansion only due to velocity spread:
- Edge effects neglected \leftrightarrow infinite long beam

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N_0	$1 \cdot 10^{11}$
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Bunch model:



Transversal envelope equation



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One finds the **transversal envelope equation** for the expansion of the beam radius r :

$$\frac{d^2 \sigma}{dz^2} = \frac{K(z)}{\sigma}, \quad \sigma = \frac{r}{r_0}$$

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With the **perveance**:

$$K(z) = \frac{Z^2 \rho(z)(1-\kappa)}{\beta_{\parallel}^2 c^2 \gamma^3 m_p} \frac{e^2}{2\epsilon_0}, \quad \kappa = \frac{N_e}{N_p}$$

With: Z charge number of the ions (e.g. $Z=1$ for protons), ρ particle density, m_p particle mass, r_0 initial radius, e elemental charge, c lightspeed, γ Lorentzian factor and κ the ratio of protons and electrons (neutralization factor)

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Perveance is a measure for space charge effects and depends on beam parameters! It is the leading quantity in rating the importance of space charge !

Verification by VORPAL[©] simulation



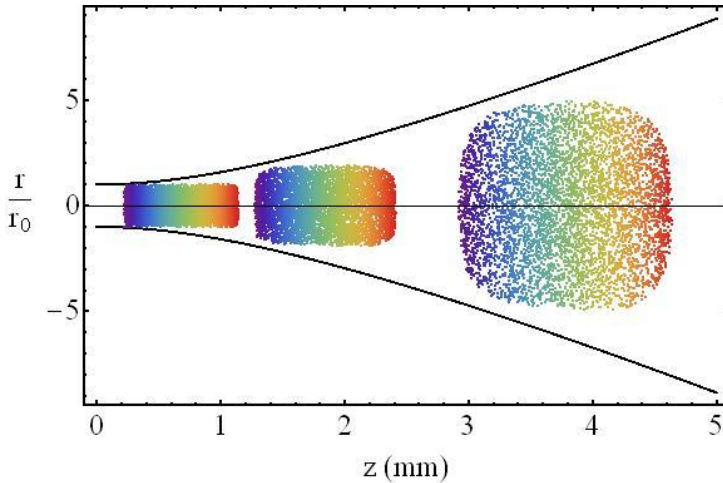
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Worst case: Bunch only consists of protons, $\vartheta_0 = 0^\circ$.
 $K_0 = 1,32 \cdot 10^6 \text{ m}^{-2}$

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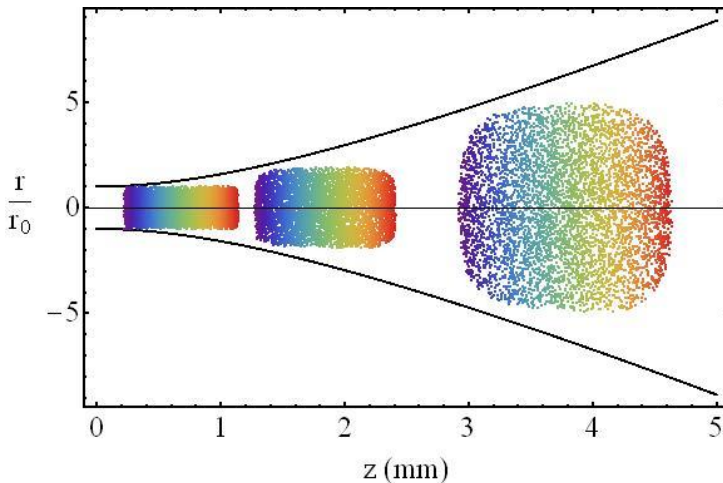
Transversal expansion:

Analytical calculation from envelope equation (black line) and VORPAL[©] simulation (stroboscopic pictures)

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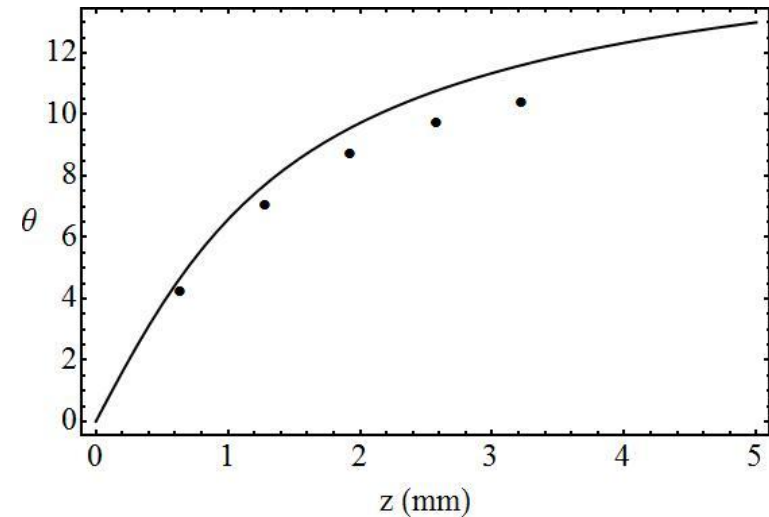
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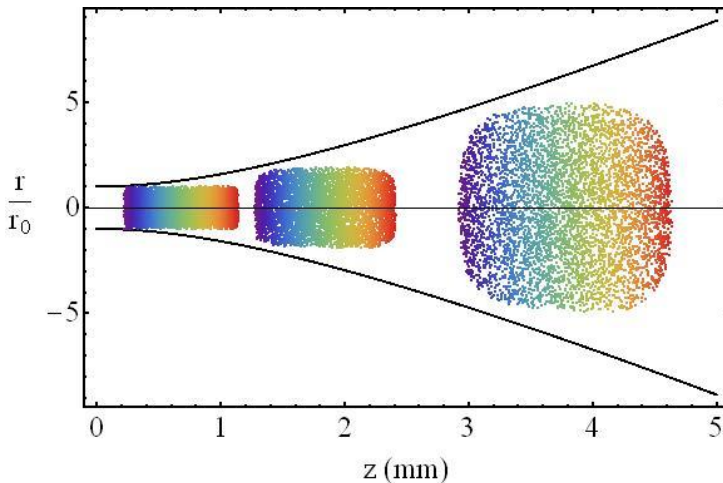
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Bunch divergence angle:

Comparison of analytical calculation from envelope equation (black line) and VORPAL[©] simulation (dots).



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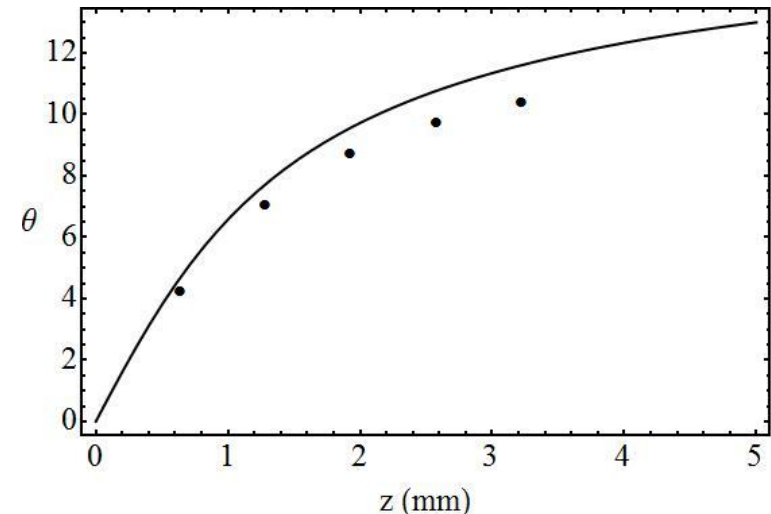
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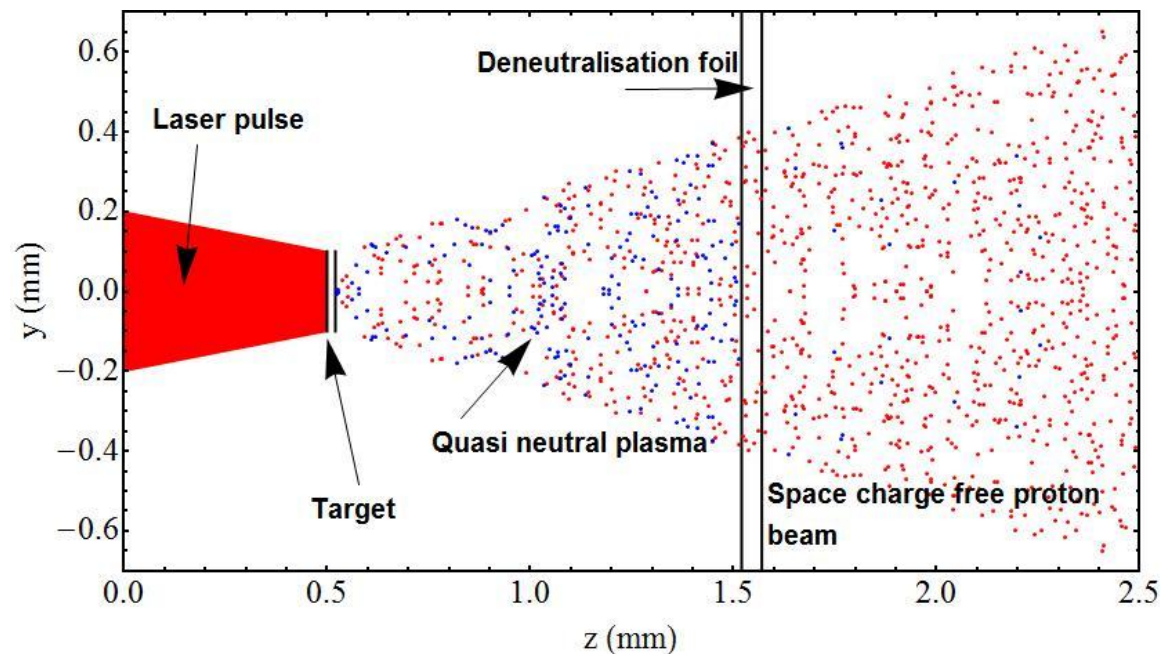


Due to finite bunch length, simulation results are below analytical → analytical calculations are upper limit!

Deneutralization with a foil

Deneutralization with thin metal foil:

- Bunch is initially quasi neutral and drifts into space
- At some position z_{foil} place a thin foil to absorb electrons
- Determine z_{foil} such that space charge can be neglected behind foil
- Place focusing elements behind the foil



Sample calculation



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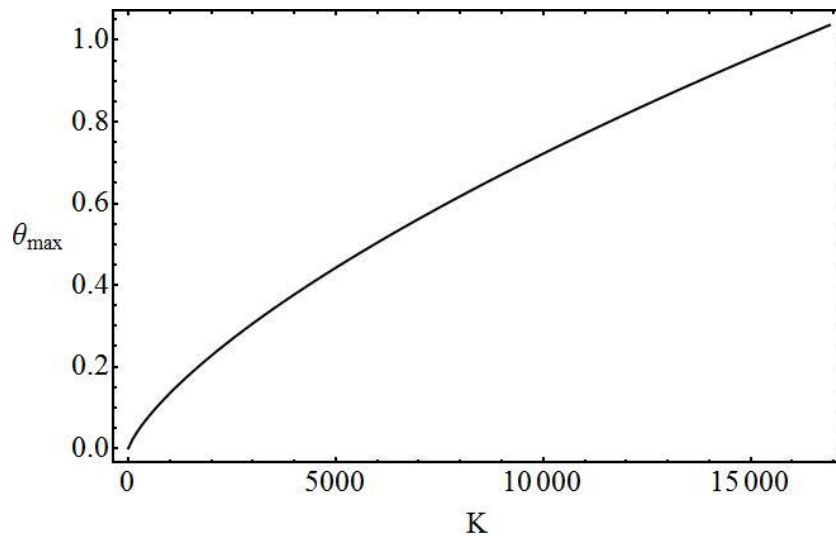
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- Bunch is neutral with $\vartheta_0 = 0^\circ$ and $K_0 = 1,32 \cdot 10^6 \text{ m}^{-2}$

Sample calculation

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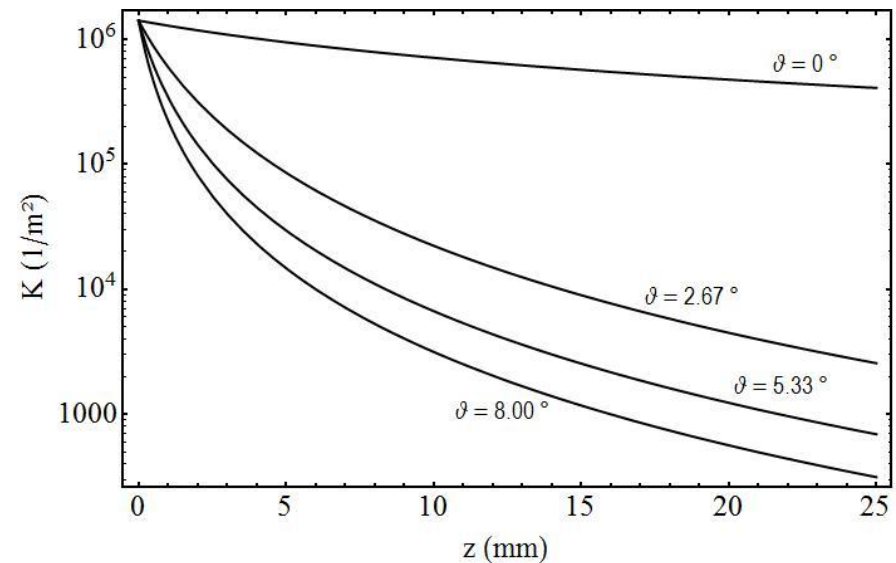
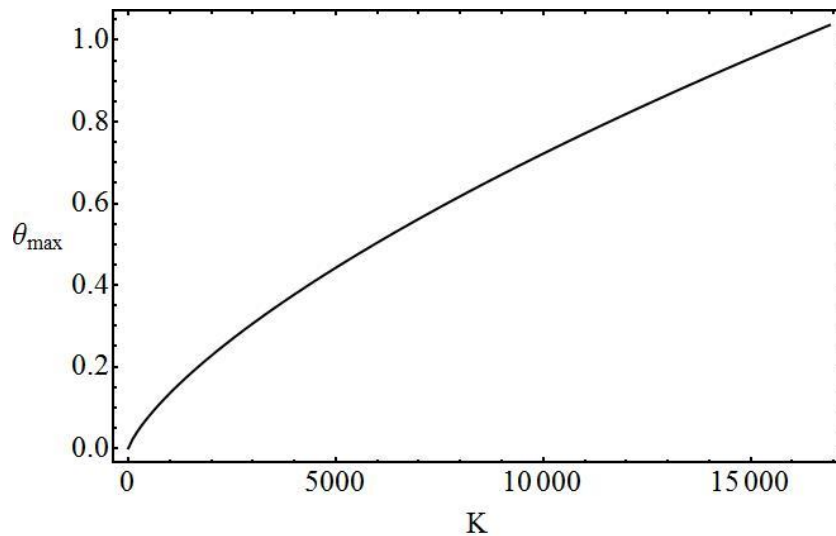
- Bunch is neutral with $\vartheta_0 = 0^\circ$ and $K_0 = 1,32 \cdot 10^6 \text{ m}^{-2}$
- Tolerable max. angle after deneutralization: $\vartheta_{\text{max}} \leq 1^\circ \rightarrow K \leq 15.000 \text{ m}^{-2}$ after foil!



Sample calculation

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Foil position from Space charge criterion:
 $z_{\text{foil}} \approx 1 \text{ m}$ behind the target!

Focusing with pulsed power solenoid



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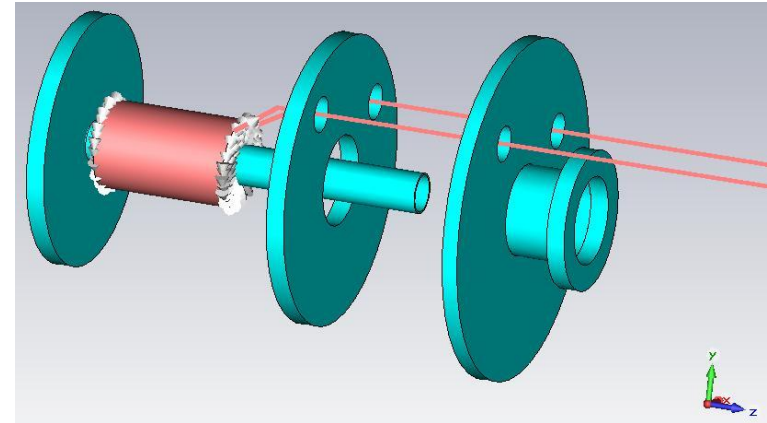
Pulsed power solenoid:

- Model designed in CST EM Studio[©]
- CST[©] tracking simulation (space charge free)
- VORPAL[©] simulation (with space charge)
- Comparison of both validates space charge criterion

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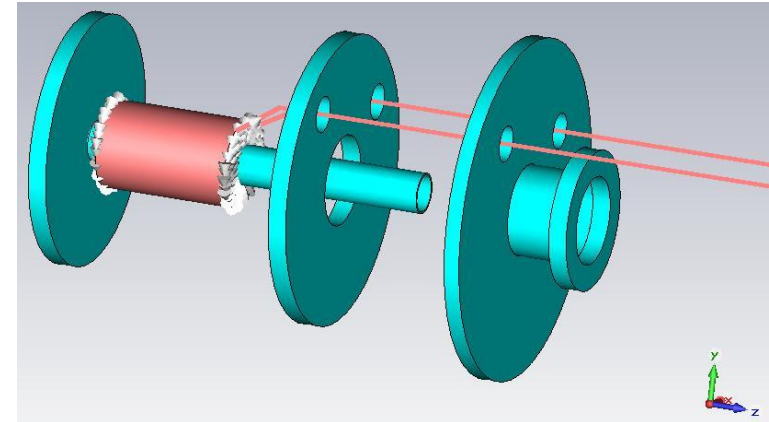
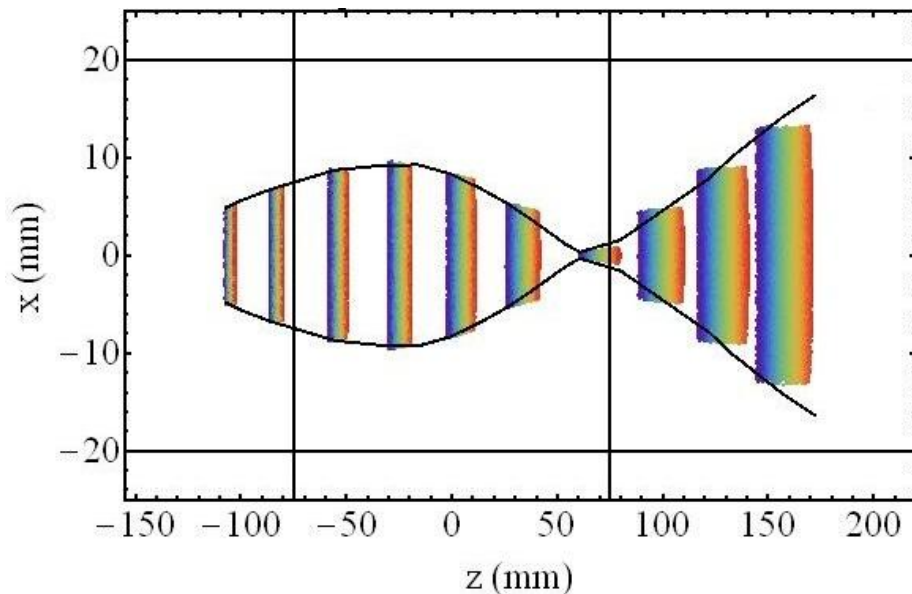


CST[®] model of the solenoid. Some parts are hidden for better overview

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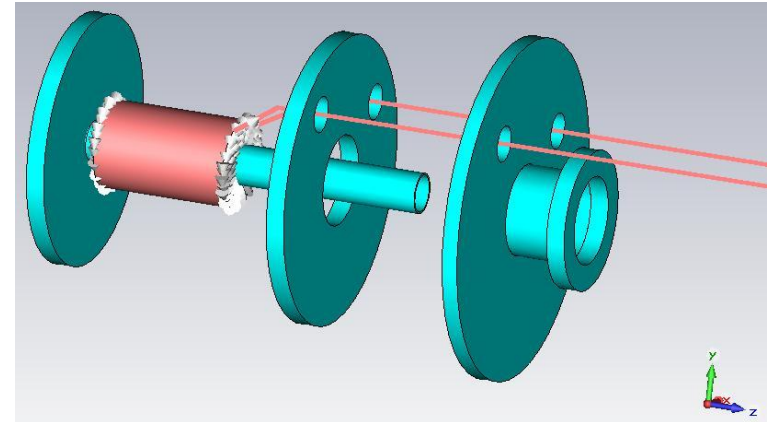
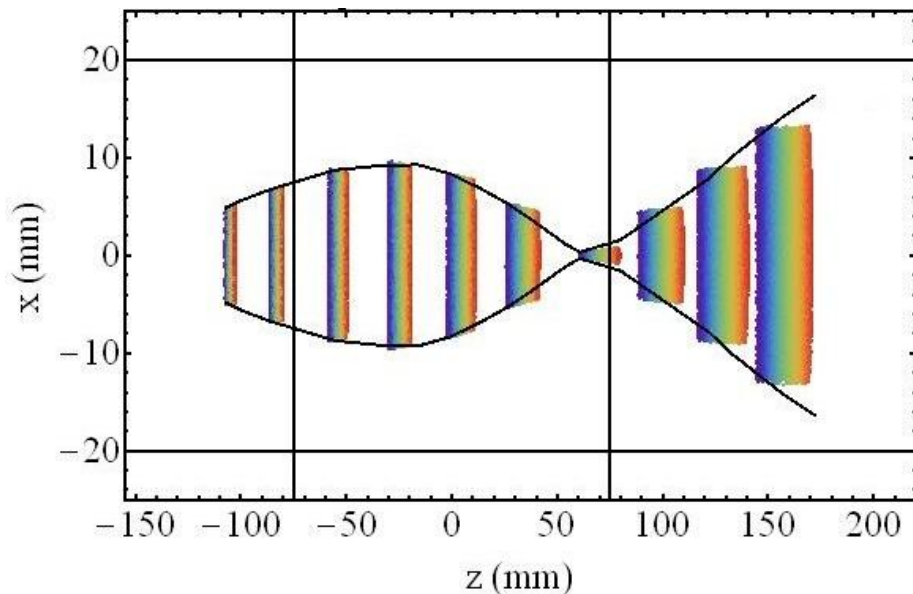


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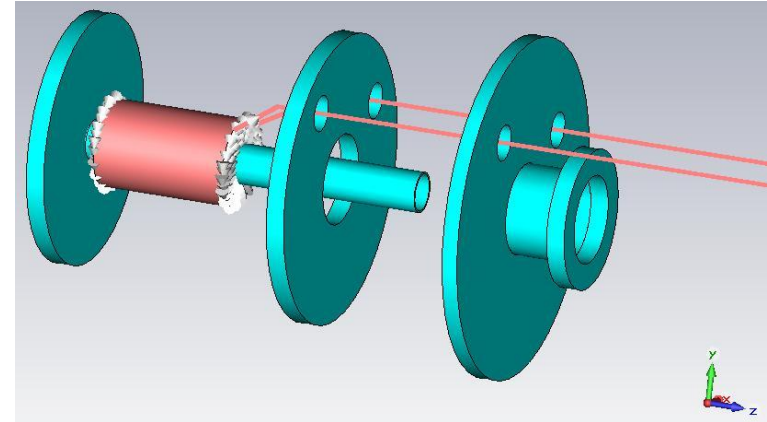
CST[®] model of the solenoid. Some parts are hidden for better overview

Results are in good agreement → Space charge criterion yields good results!

Supply wires field

Supply wires:

- Former solenoid power supply by two wires parallel to the beam pipe
- Dipol field of the wires lead to deflection of the beam
- Results simulated with CST Particle Studio[®]

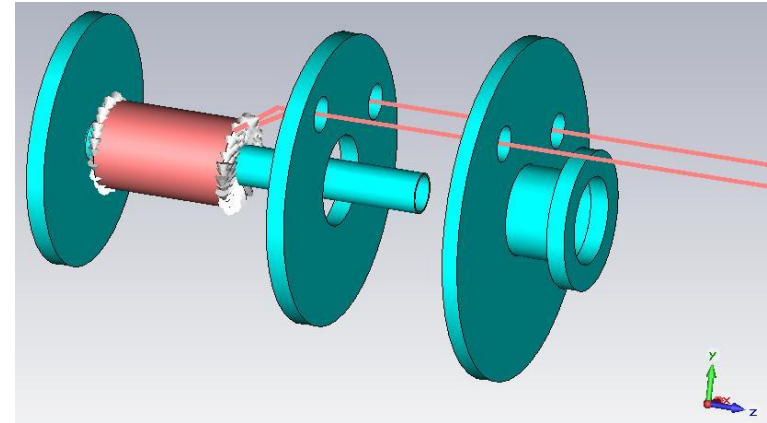
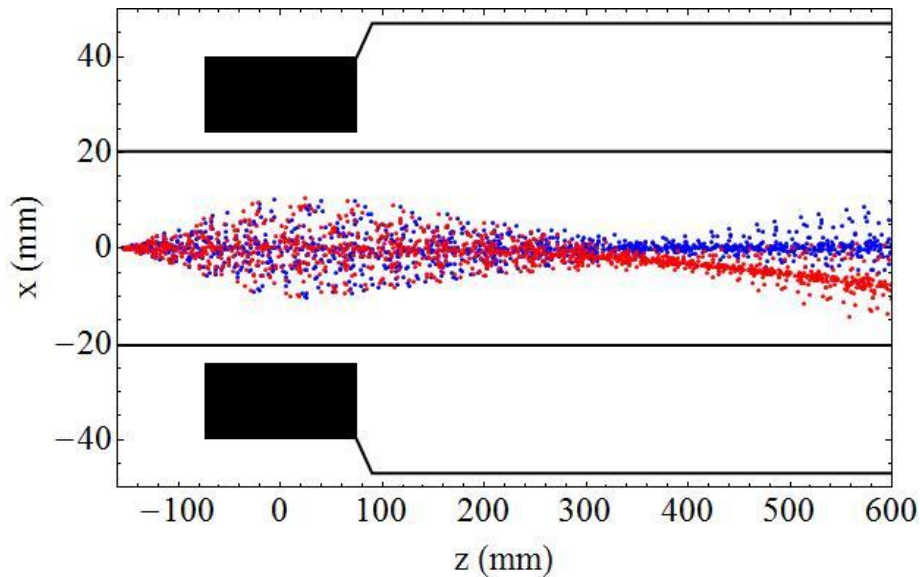


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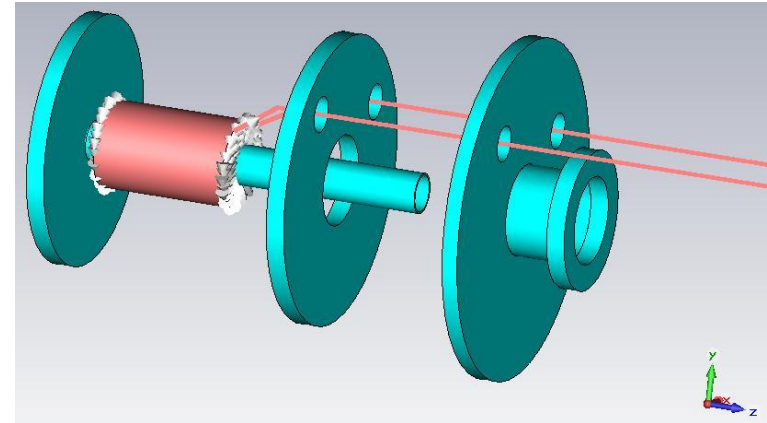
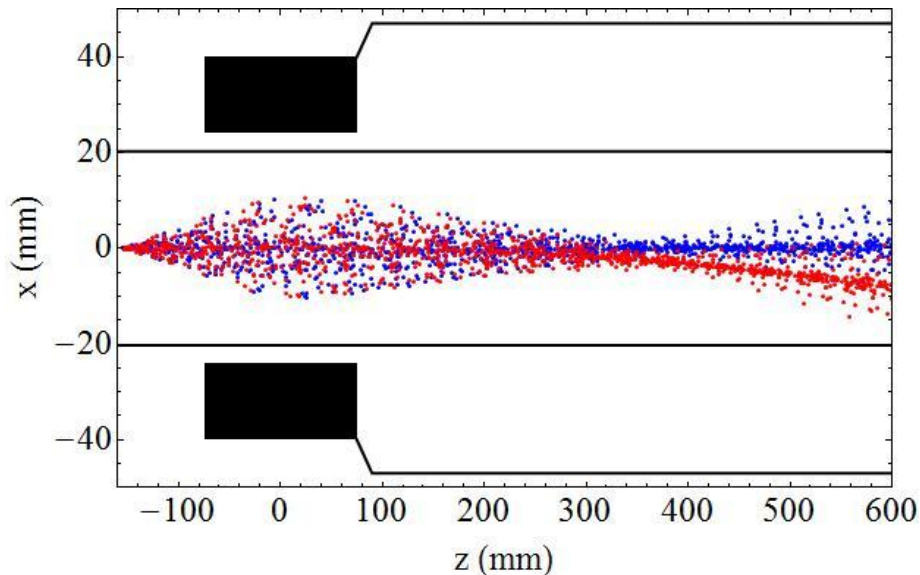


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Based on this simulation, the experimental setup was improved!

Ohmic losses and inductive coupling



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Ohmic losses and coupling:

- Solenoid operated in pulsed mode
- Shows inductive coupling to surrounding metal parts → time shift between current –and field maximum

Ohmic losses and inductive coupling



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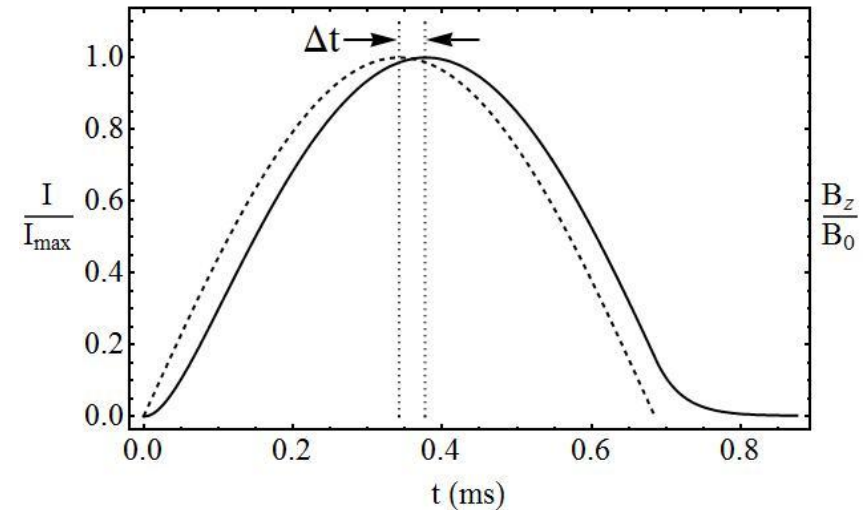
- Induced eddy currents lead to power losses

→ use CST EM Studio[®] to calculate both!

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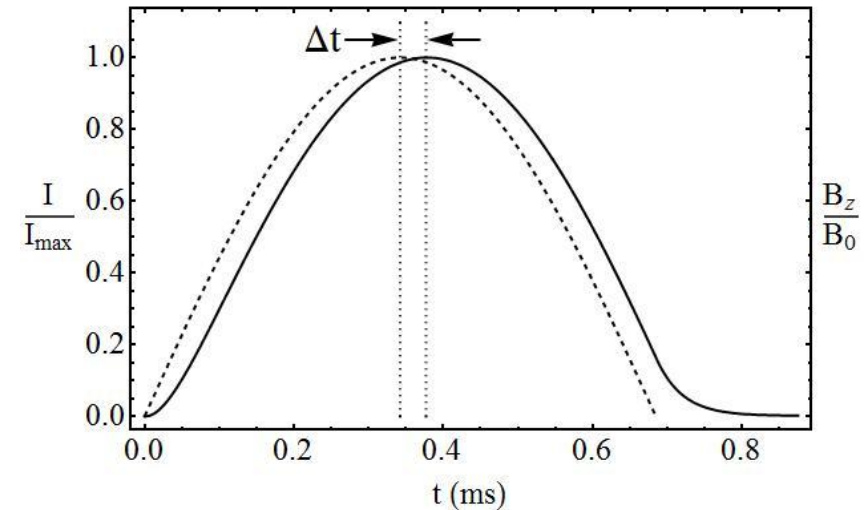
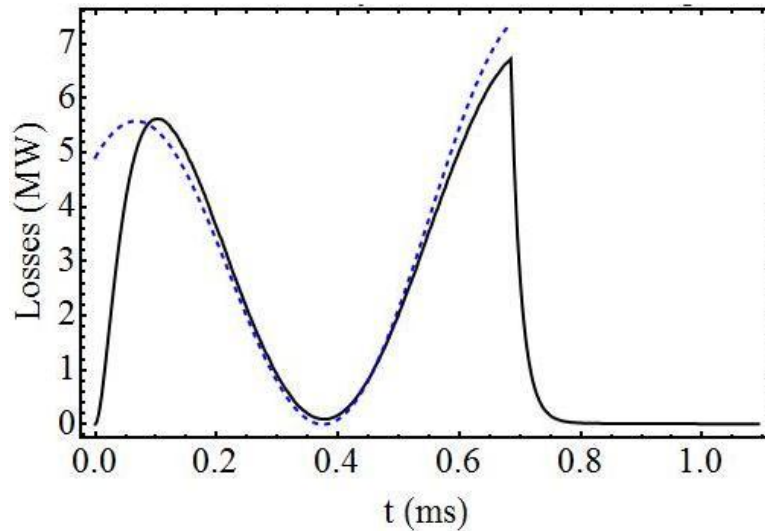
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Conclusions and Outlook



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Conclusion:

- Simple bunch model could be verified by VORPAL[®] simulations
- Comparison of VORPAL[®] and CST[®] simulations show the validity of the worked out space charge criteria
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Outlook:

- Compare different focusing methods, e.g. solenoid and quadrupol triplets
- Work out a quality criterion for focusing methods
- Answer question: For given task, which method is best?

The End



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Thanks for your attention!