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# Simulating radiation from Laser-wakefield accelerators

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# Acknowledgements

## PICongPU

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Wolfgang Hönig<sup>2</sup>, Guido Juckeland<sup>2</sup>, Wolfgang Nagel<sup>2</sup>, Felix Schmitt<sup>2</sup>

## Laser wakefield experiments

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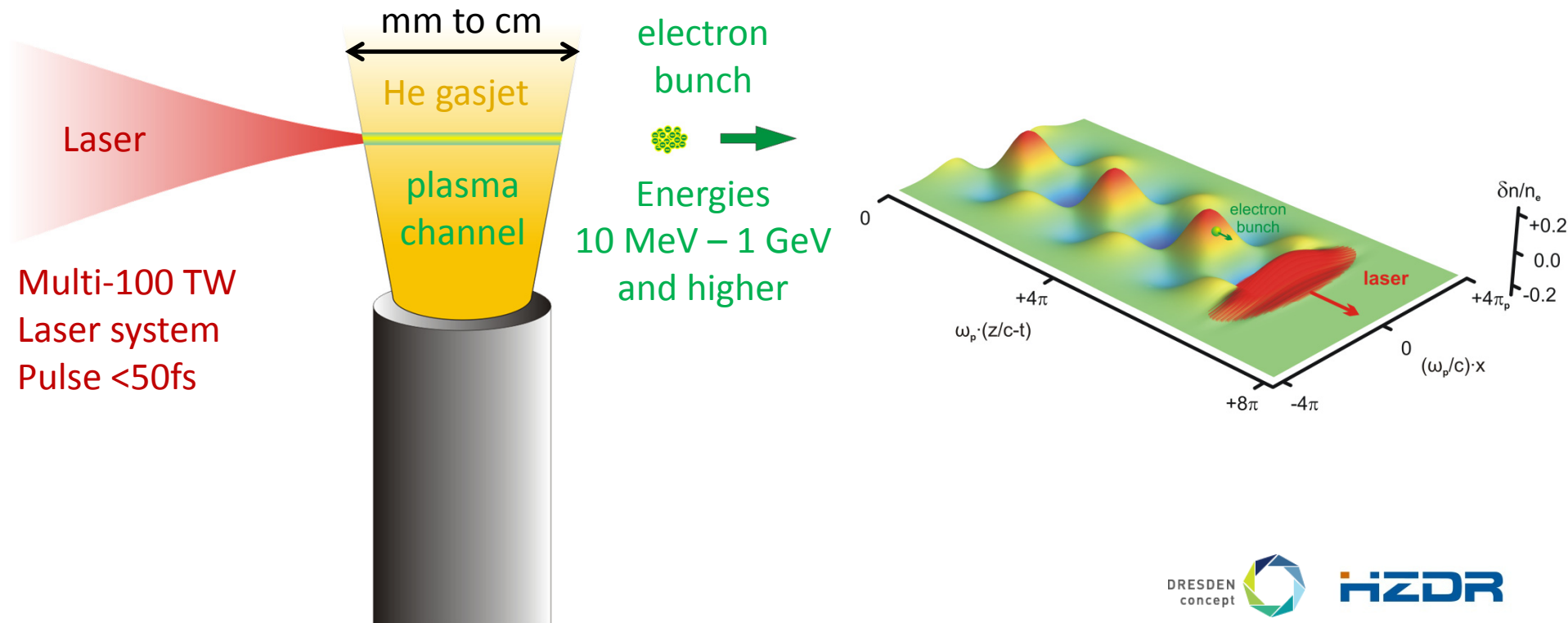
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# Laser-wakefield accelerators can accelerate electrons to the GeV level and are promising for compact x-ray sources of high brilliance.

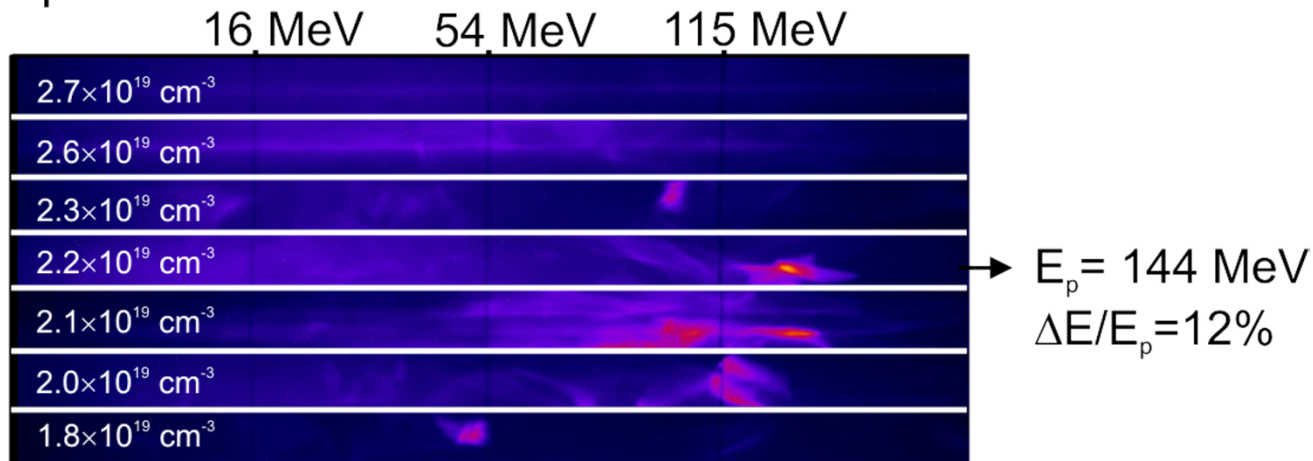
- High-power lasers generate plasma waves in underdense plasmas.
- Into these plasma waves electrons can be (self-) injected and over mm- distances accelerated to MeV to GeV energies.



# Plasma radiation has the potential of being a quantitative comparison between theory and experiment.

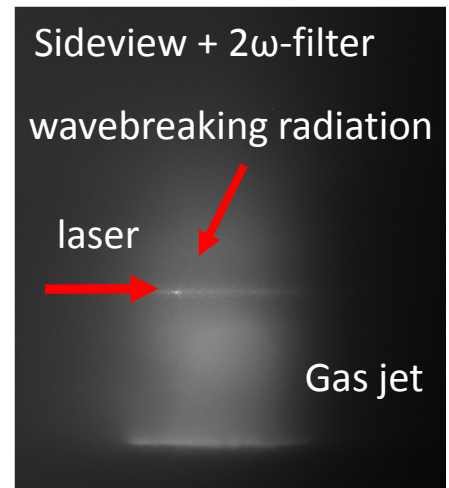
- Highly nonlinear processes make laser-accelerated electrons challenging to control.
- Especially diagnostics and control of the electron (self-)injection process is necessary.
- Electron spectra are measurements after the fact.  
(Currently best source for Theory vs. Experiment comparisons.)
- Radiation spectra tell us more on the processes during laser-plasma interaction.

## Spectra



2.3 J, 25 fs,  $I_{\text{peak}} : 2.4 \times 10^{19} \text{ W cm}^{-2}$  ( $a_0 = 3.4$ )

## plasma self-emission

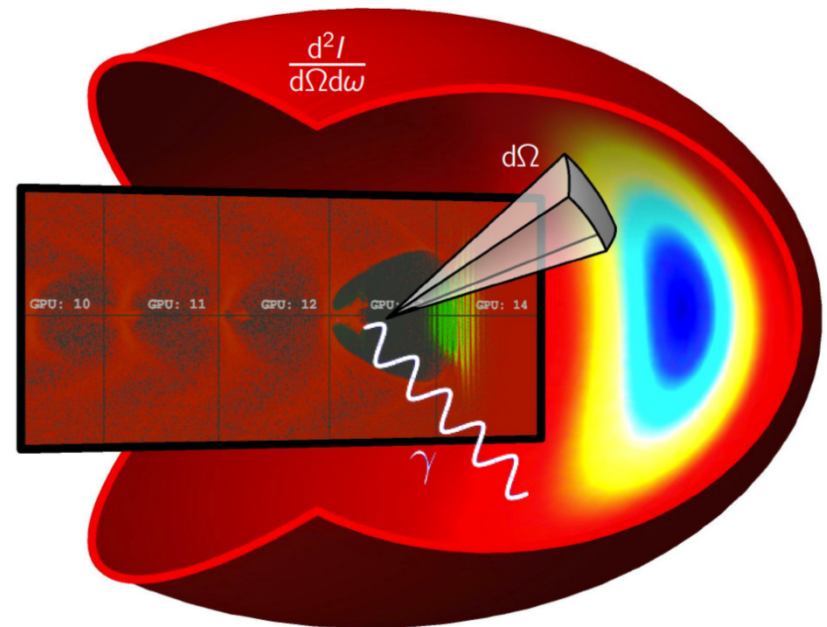


## Detecting radiation is straightforward in experiment, but poses a challenge for computation.

- Physics: Calculate radiation and characterize signatures from electron injection and betatron oscillations.
- Goal: Calculate radiation from ALL electrons with full angular characteristics.

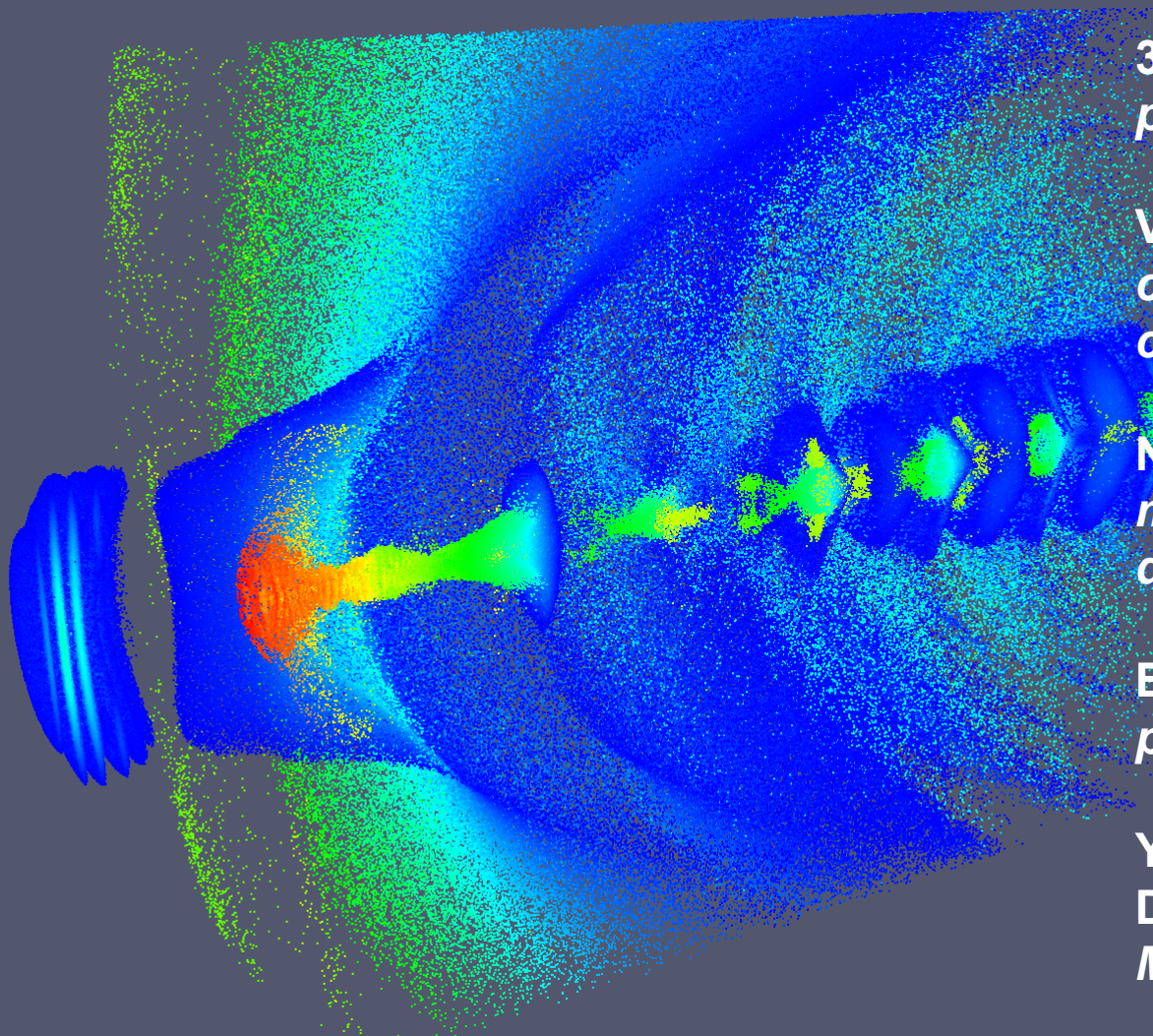
Radiation codes as post-processing after PIC quickly become impracticable.

CPU-PIC: 200 TB raw particle data within 3 weeks.



- EM fields from the PIC grid do not have enough spatial resolution for X-Ray radiation arising from large Doppler-shifts.
- Approach here: Liénard-Wiechert potentials → Calculate from trajectories.

# PIConGPU - a GPU driven 3D-PIC code provides the basis.



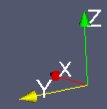
**3D3V relativistic  
*particle-in-cell code***

**Villasenor-Buneman  
*charge conserving  
current deposition***

**NGP / CIC / TSC  
*macro-particle  
distribution functions***

**Boris Push  
*particle pusher***

**Yee-scheme /  
*Directional splitting  
Maxwell-Solver***



# PIConGPU

GPU: 33 GPU: 35 GPU: 37 GPU: 39 GPU: 41 GPU: 43 GPU: 45 GPU: 47 GPU: 49 GPU: 51 GPU: 53 GPU: 55 GPU: 57 GPU: 59 GPU: 61

**64 NVIDIA  
Fermi GPUs**

**45 min**

**0.09 seconds per time step**

# FORTRAN LEGACY

**128 AMD cores**

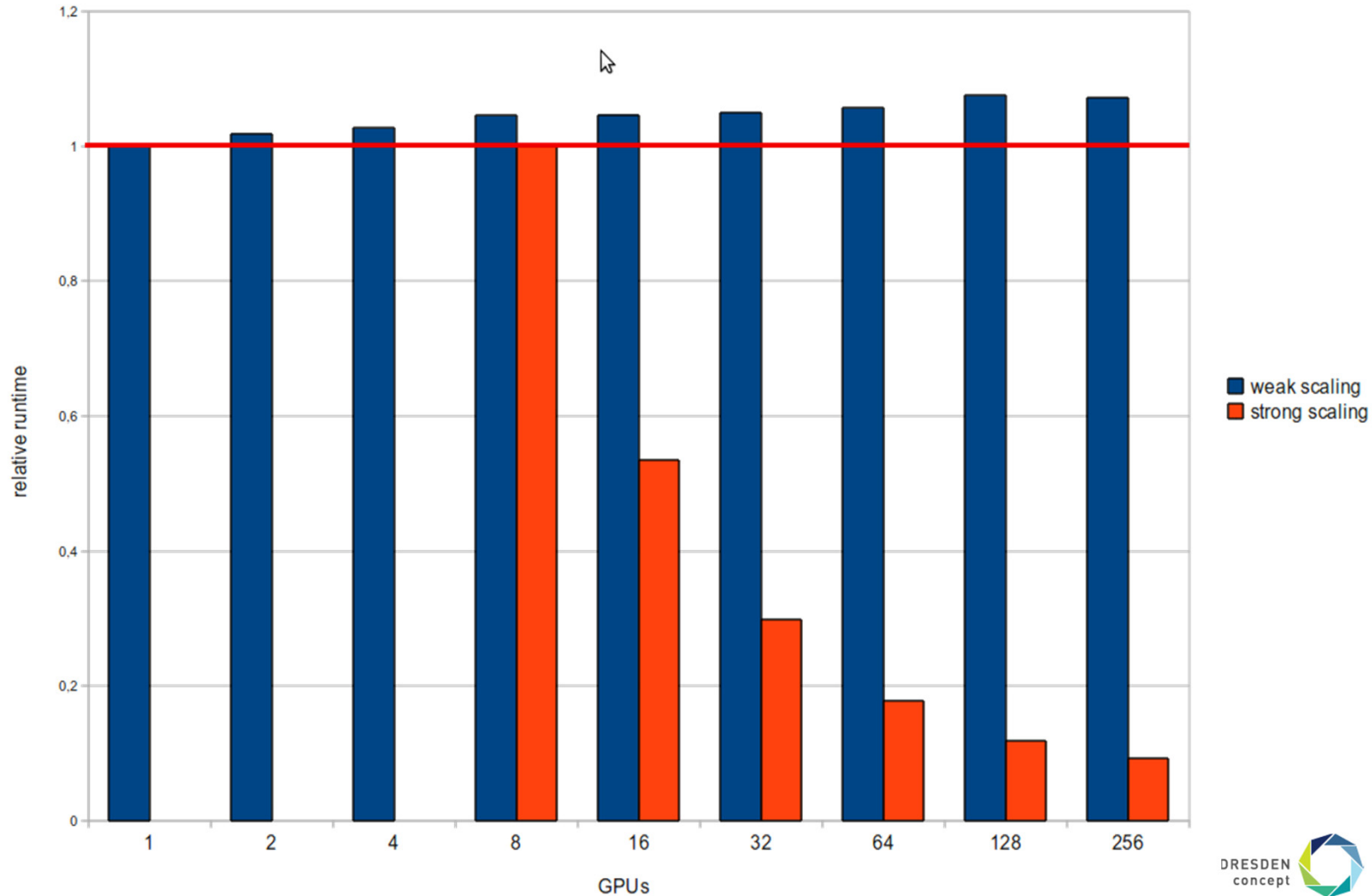
**8 days**

**480x480x3070 Cells,  $2.8 \times 10^9$  macro particles, 30,000 time steps**

# Strong and Weak Scaling on NVIDIA TESLA M2090

## Scaling PIconGPU 3D on TESLA M2090

weak scaling: 28 mill. partilces, 192x192x192 cells per GPU  
strong scaling: 535 mill. partilces 512x512x512 cells





# Radiation calculations are highly parallel!

Spectral energy density

Blows up in  
ultrarelativistic regime

retarded time requires interpolation  
In FFT algorithms because of  
equidistant time steps

$$\frac{d^2 I}{d\omega d\Omega} = \frac{e^2}{4\pi^2 c} \left| \mathbf{P} \cdot \sum_j \int_{-\infty}^{+\infty} \underbrace{\frac{\mathbf{n} \times [(\mathbf{n} - \boldsymbol{\beta}_j) \times \dot{\boldsymbol{\beta}}_j]}{(1 - \boldsymbol{\beta}_j \cdot \mathbf{n})^2}}_{\text{ultrarelativistic regime}} e^{i\omega(t - \mathbf{n} \cdot \mathbf{r}_j(t)/c)} dt \right|^2$$

Radiation amplitude for each **particle** at each **time** step, each observation **direction** and each **frequency**.

- $\mathbf{n}$  ... normalized observation vector (Yes, this is a far field solution!)
- $j$  ... particle number
- $\boldsymbol{\beta}_j$  ... normalized particle velocity
- $\mathbf{r}_j$  ... particle position
- $\mathbf{P}$  ... Polarisation filter vector ( (1,1,1) accepts all polarisations )

# Discrete Fourier transform (DFT) is a good choice for GPU implementations.

- For FFT the trajectories of the particles need to be kept in memory, but not for DFT.
- DFT does not require interpolation of velocities and accelerations to equidistant retarded times.

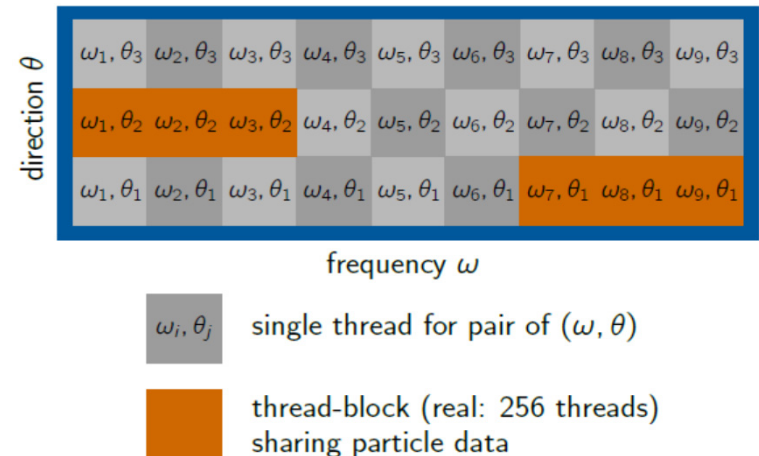
- From the physics side DFT is more flexible, because frequencies can be chosen arbitrarily.

→ Good for small-bandwidth „sky surveys“ for radiation localisation calculations or logarithmic spectra from X-ray to IR wavelengths.

- However: Since resulting spectra at different observation directions have to be stored in CPU memory anyway, FFT is still interesting in a GPU-CPU-hybrid implementation. ( GPU: Amplitudes, interpolation and superposition

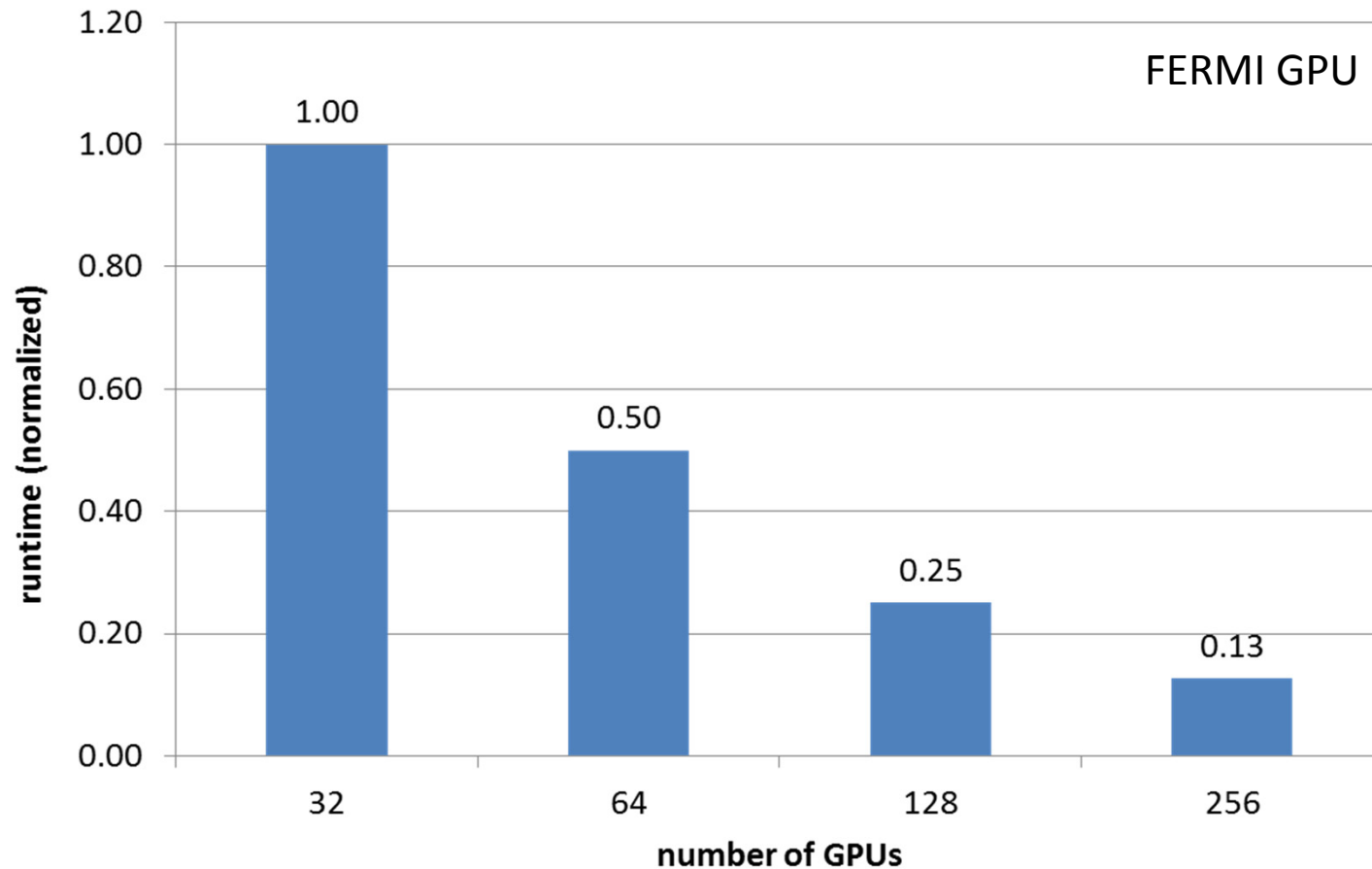
CPU: Calculating FFTs. )

## Parallelization strategy on GPUs



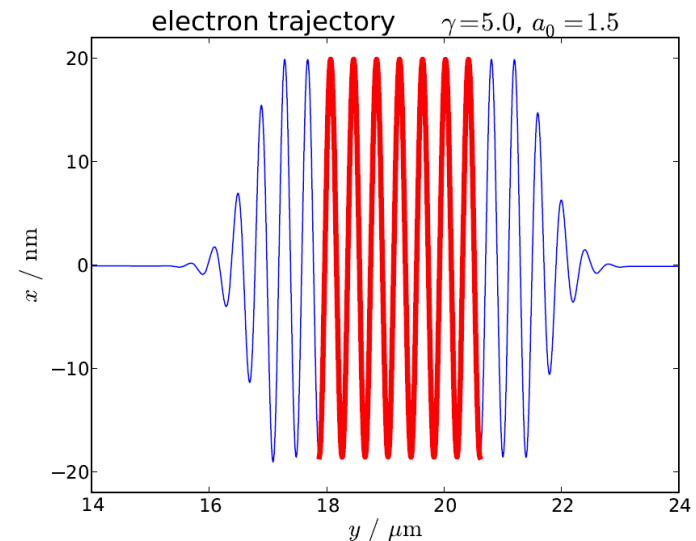
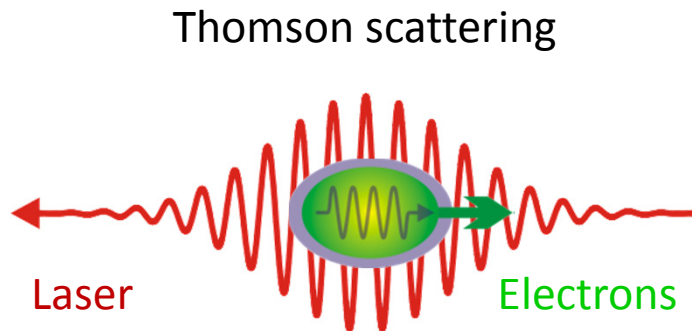
## Strong scaling: radiation code becomes the main activity.

- Strong scaling is near ideal (overhead < 1%)
- 128 spectra à 2048 frequencies ;  $1.1 \cdot 10^9$  particles in sim.; 70,000 part./s/GPU



# The code is validated using analytic results of Thomson scattering.

- (Nonlinear) Thomson scattering from is a test for relativistic particles in high-intensity laser fields against analytic results.
- The core implementation of radiation code with the numerics was validated independently from the PIC-Code using predefined trajectories.
- The following tests (single particles and plasma) target the integration into PIconGPU, correct laser initialisation and numeric issues of the PIC code rather than the radiation code.

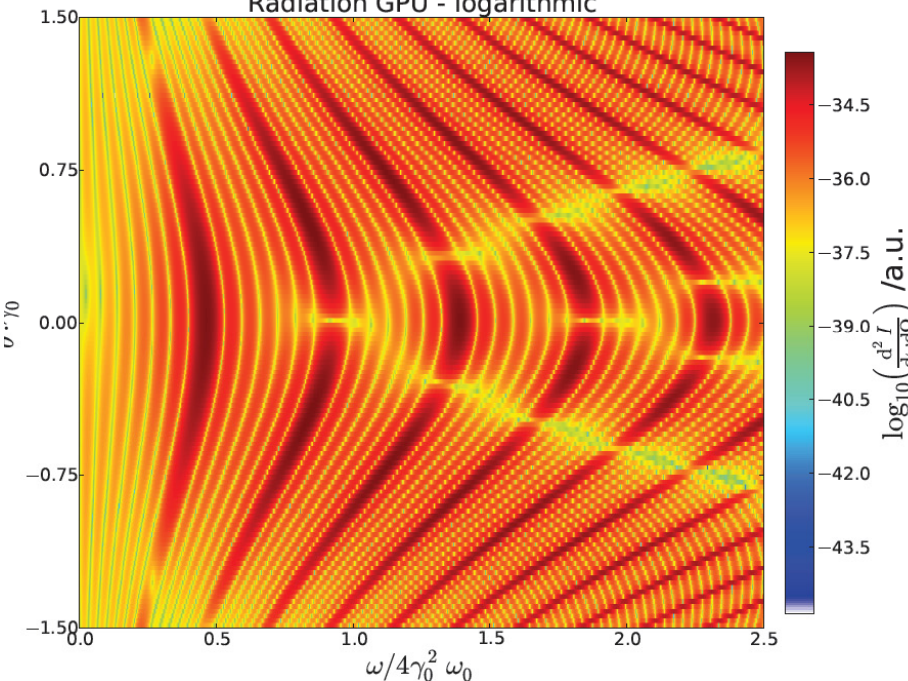


# Nonlinear Thomson scattering with relativistic single particles

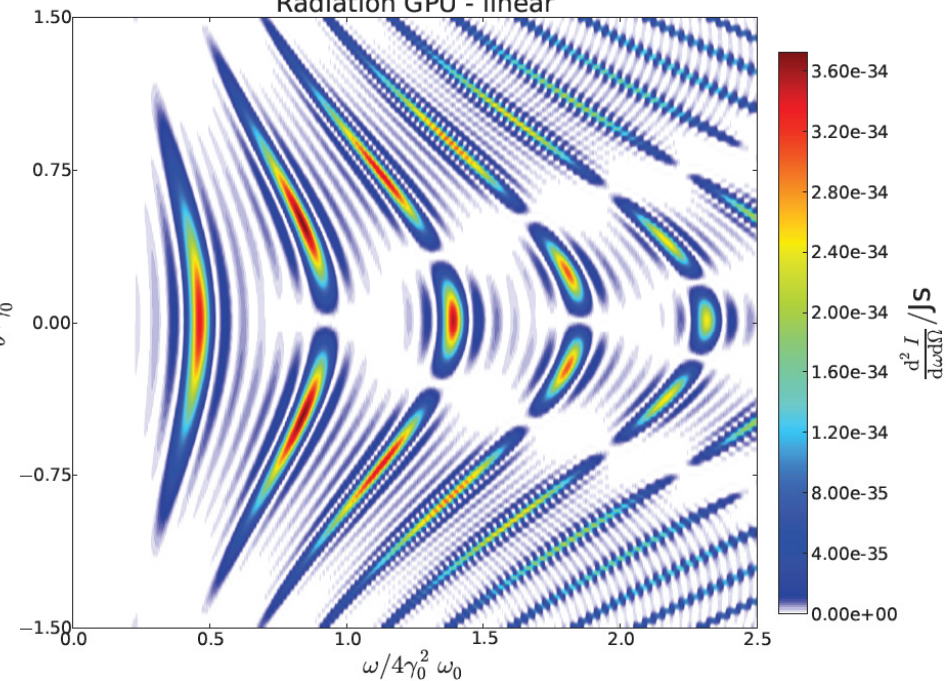
## Analytic solution

- Peak laser intensity  $I_0 = 4.9 \cdot 10^{18}$  W/cm<sup>2</sup> ( $a_0 = 1.5$ )

Radiation GPU - logarithmic



Radiation GPU - linear



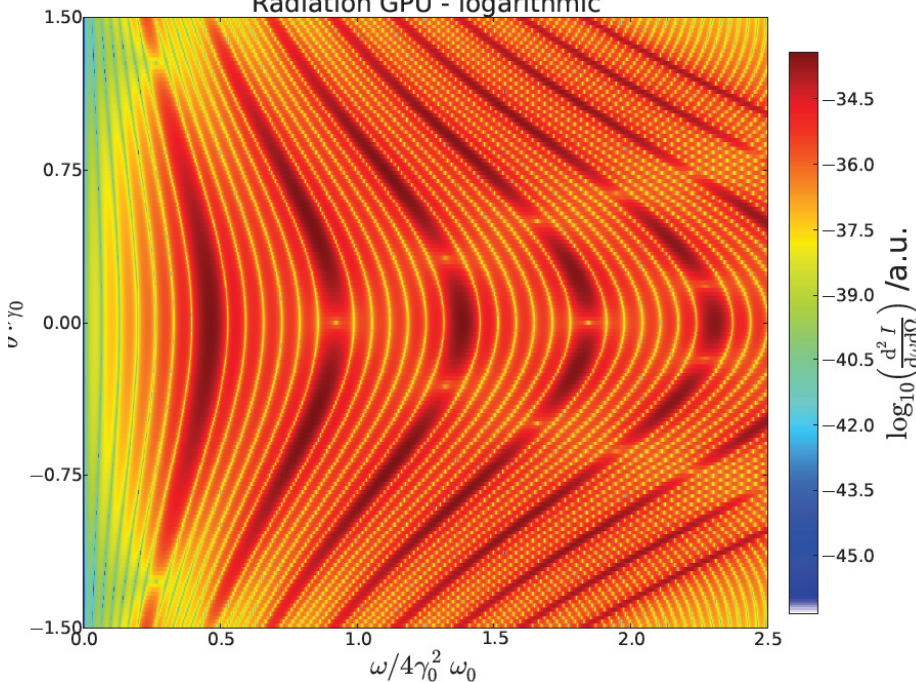
### Theory:

Esarey *et al.*, Nonlinear Thomson scattering of intense laser pulses from beams and plasmas  
Phys. Rev. E **48** (4), pp. 3003-3021, (1993).

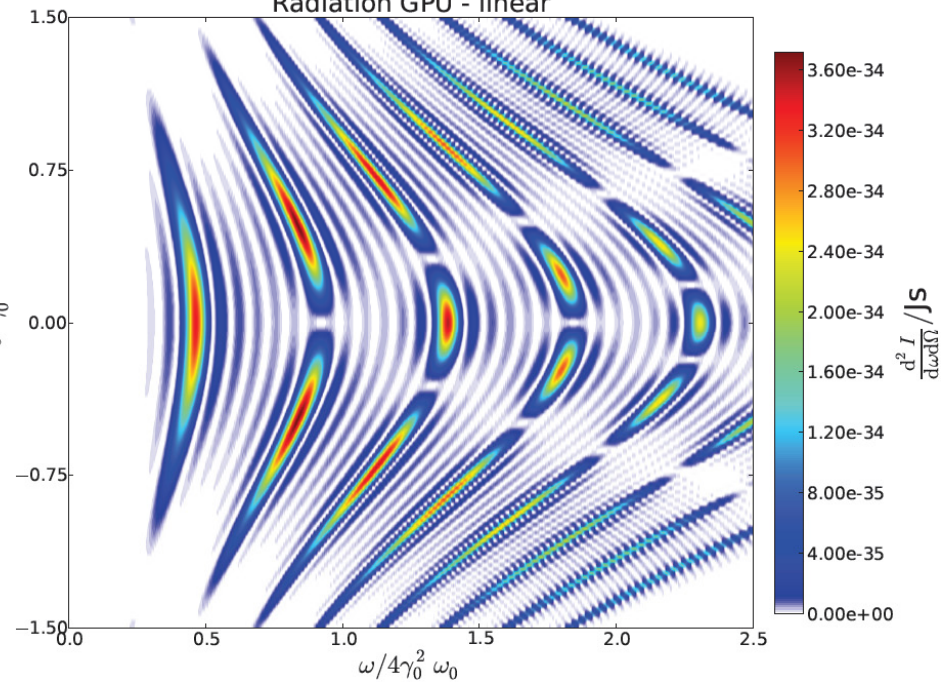
# Nonlinear Thomson scattering with relativistic single particles

## Numeric solution with PIconGPU

Radiation GPU - logarithmic



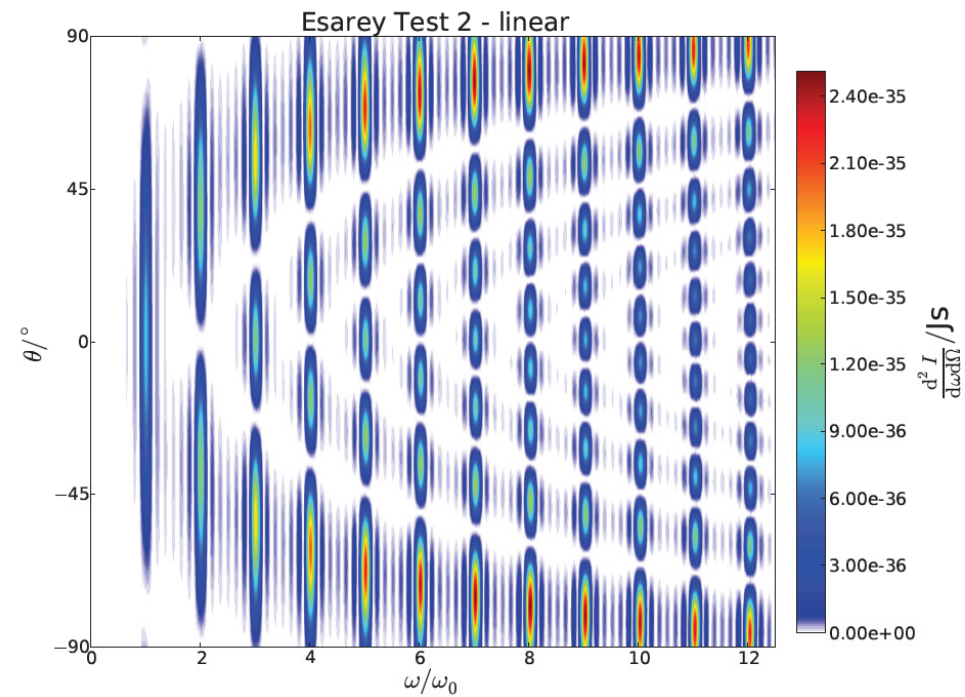
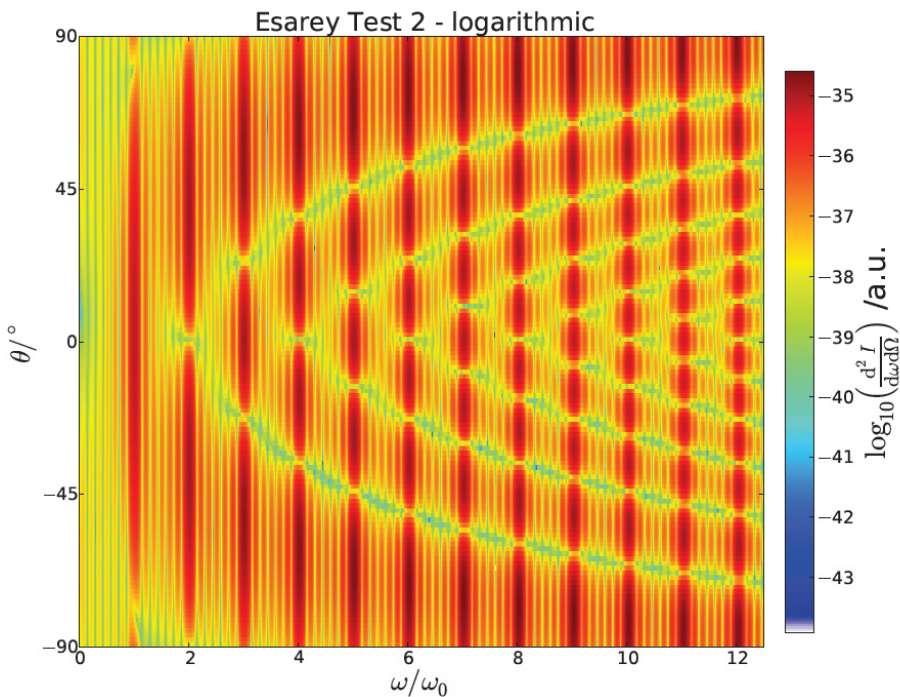
Radiation GPU - linear



# Nonlinear Thomson scattering in plasma

## Analytic solution

- Peak laser intensity  $I_0 = 8.7 \cdot 10^{18} \text{ W/cm}^2$  ( $a_0 = 2.0$ )

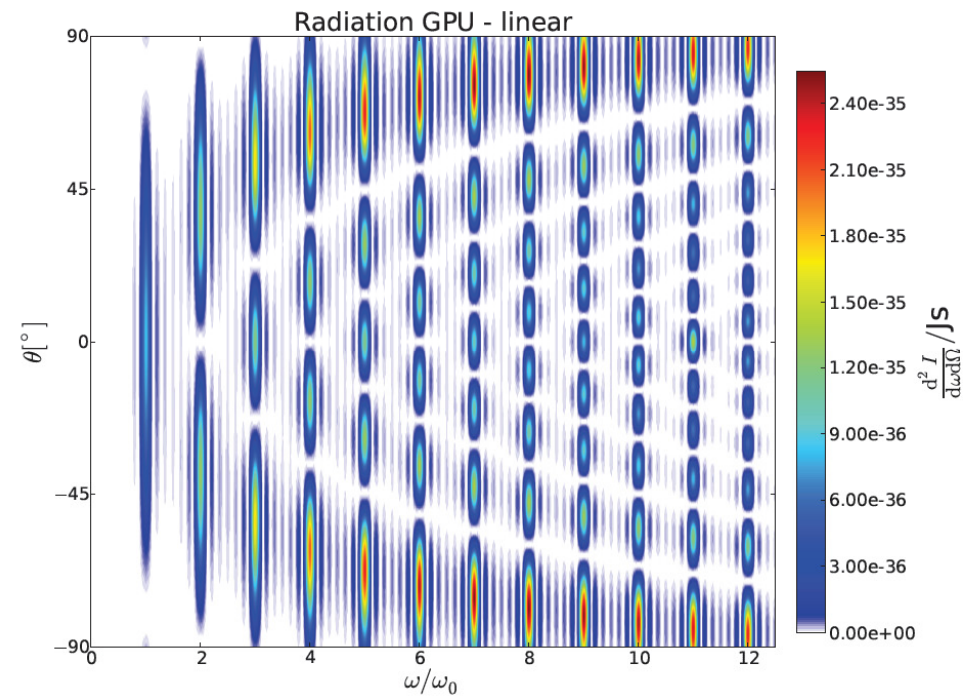
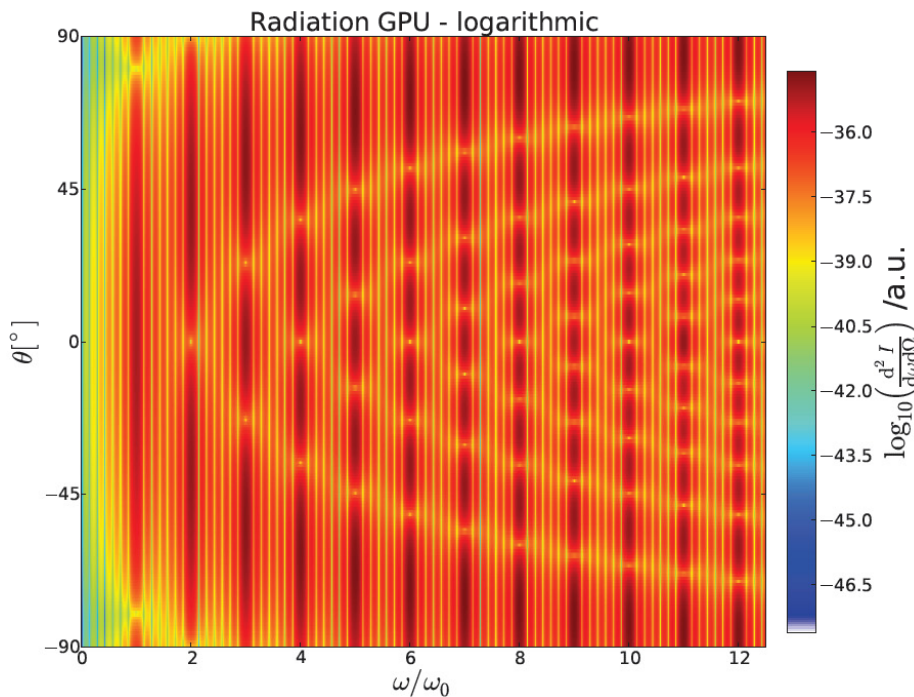


### Theory:

Esarey *et al.*, Nonlinear Thomson scattering of intense laser pulses from beams and plasmas  
Phys. Rev. E **48** (4), pp. 3003-3021, (1993).

# Nonlinear Thomson Scattering in plasma

## Numeric solution with PIconGPU

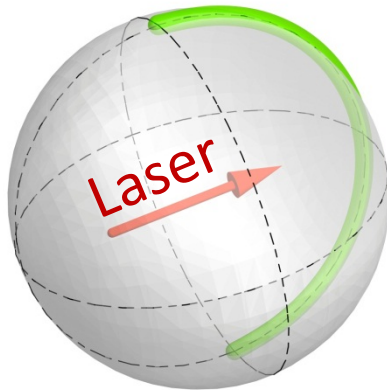




# Very preliminary results: Radiation from Laser-wakefield accelerators

- 30 min without radiation → 23h 15min with 128 spectra à 2048 frequencies
- 66 Mio particles on 8 GPU; 10% of all macro particles radiate

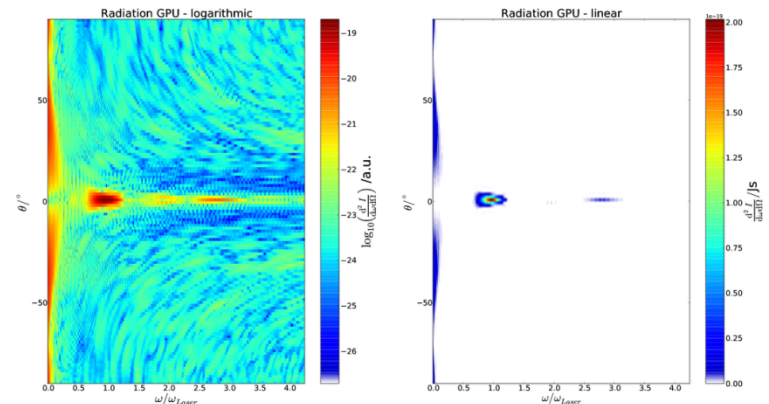
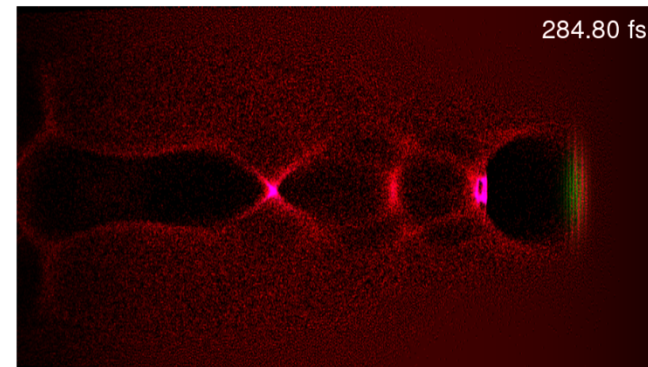
Observation directions  
around laser polarization



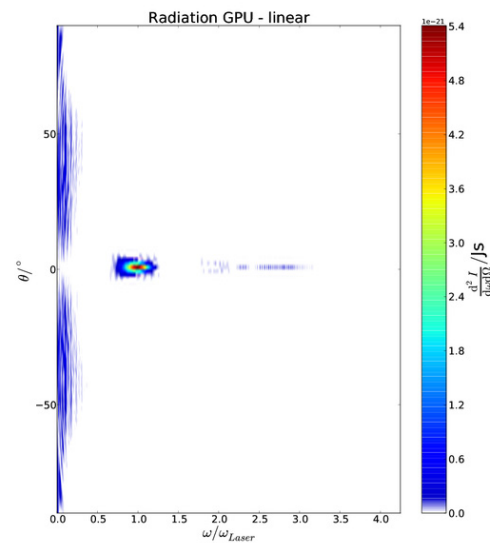
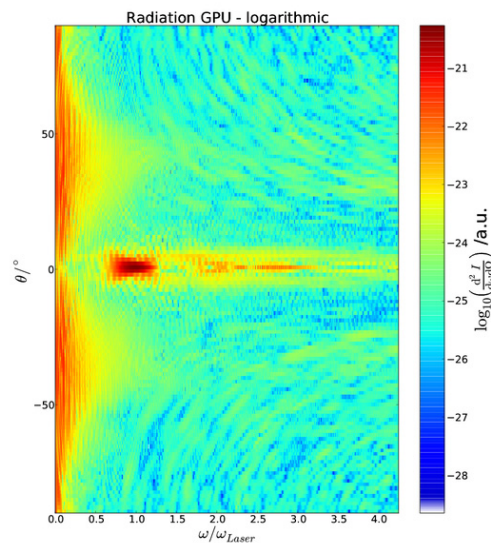
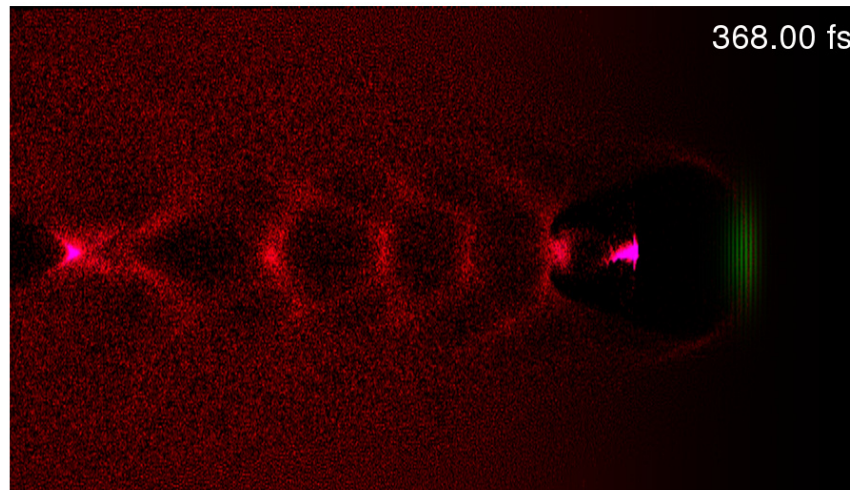
Disclaimer:

Wrong resolution due to lack of GPUs,  
This is a test, not physics!

For full resolution ~1000 GPUs are required.



# Very preliminary results: Laser-wakefield accelerator



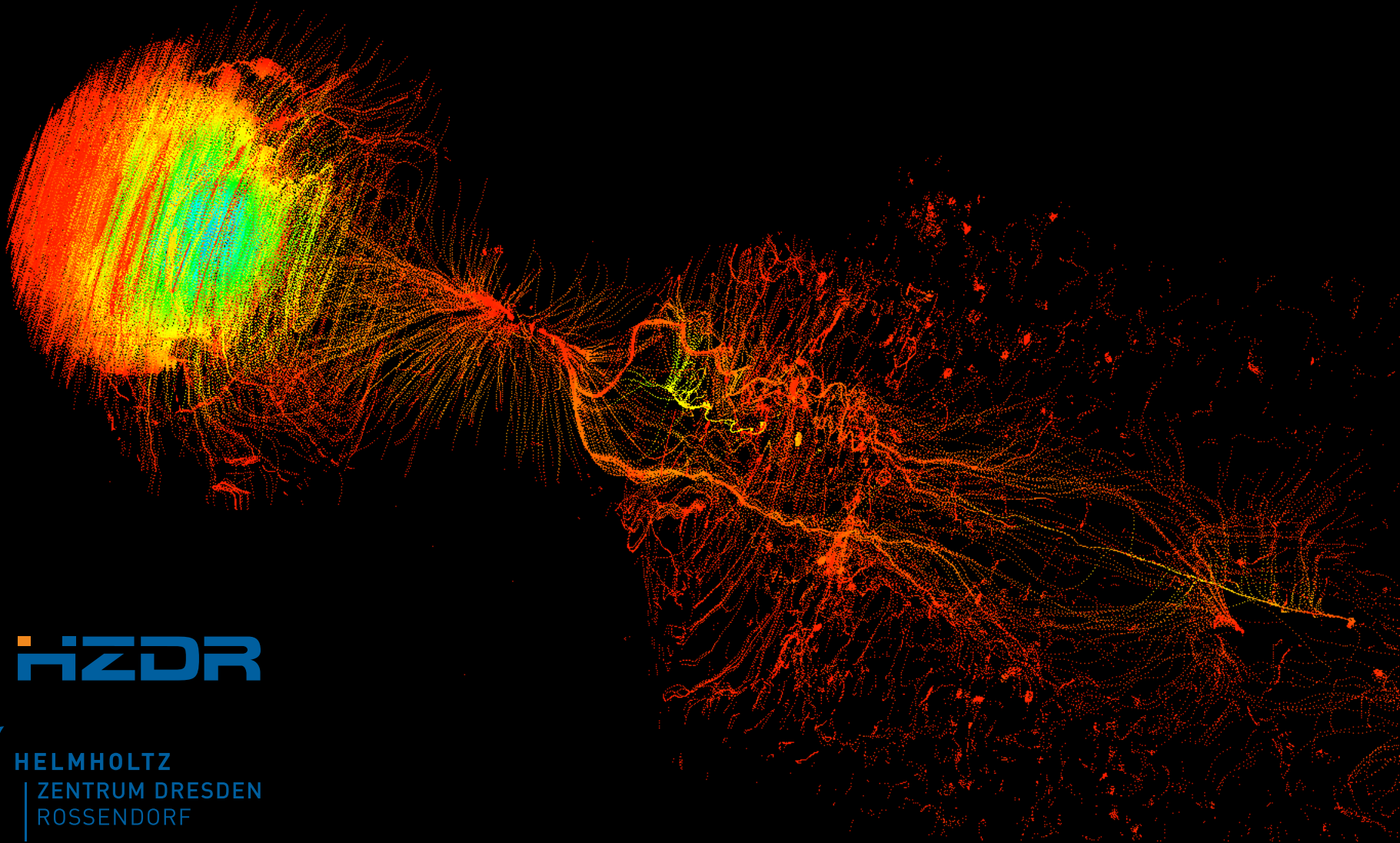
## Conclusions

- The GPU-based 3D-PIC code PIConGPU provides the basis for full-scale radiation calculations using all simulated particles.
- For computing the radiation on GPU minimal memory footprint a discrete Fourier approach has been implemented.
- Benchmarks for strong scaling and physics tests for the integration of the radiation code into PIConGPU have been shown.
- First Laser-wakefield radiation tests provide *proof-of-principle*.

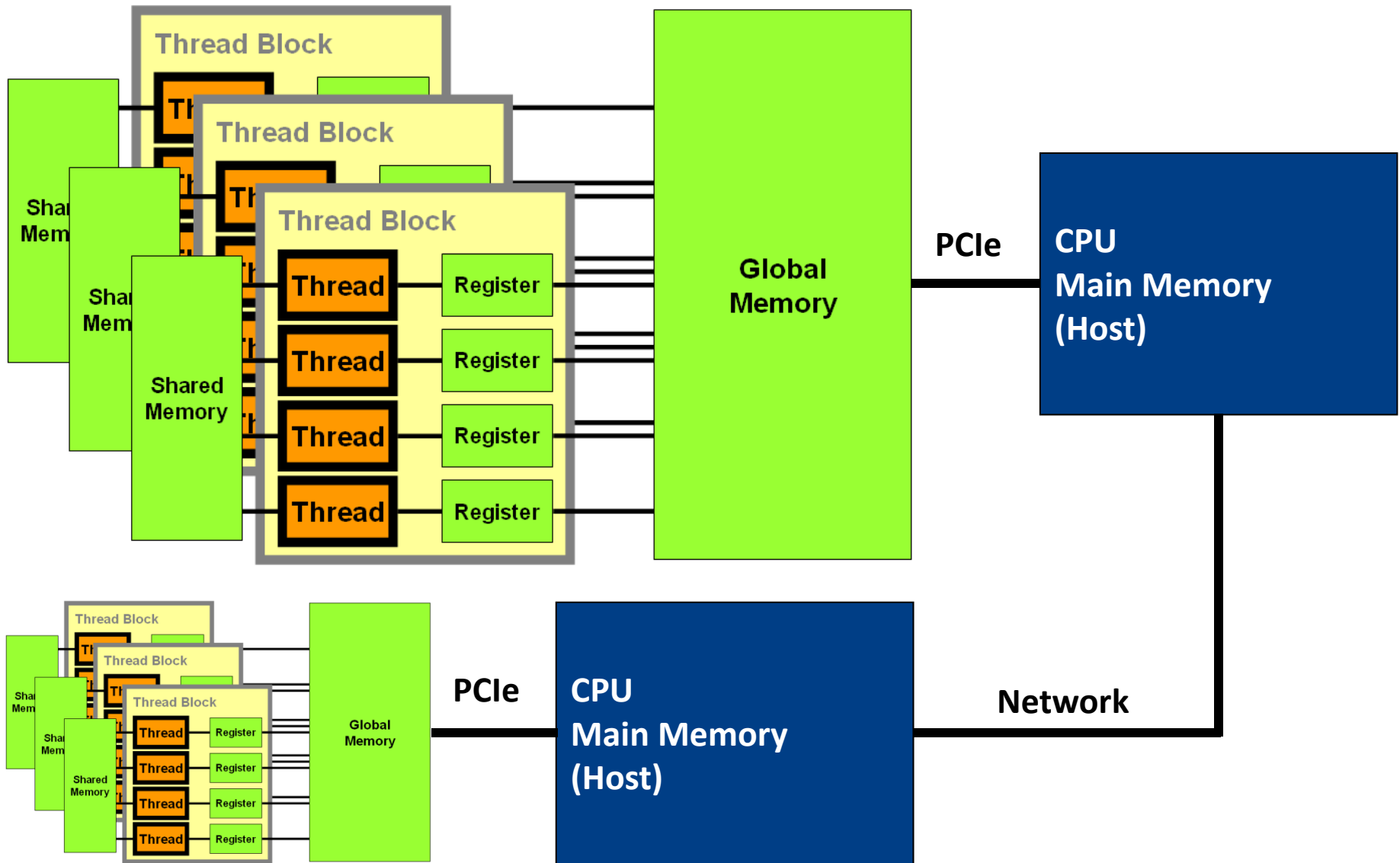
Near future:

- Full scale simulation LWFA PIC-simulation with more GPUs.
- FFT-based GPU-CPU Hybrid code (CPU provides memory and FFT) uniformly spaced spectral data in many directions over the full solid angle.

Thank you!

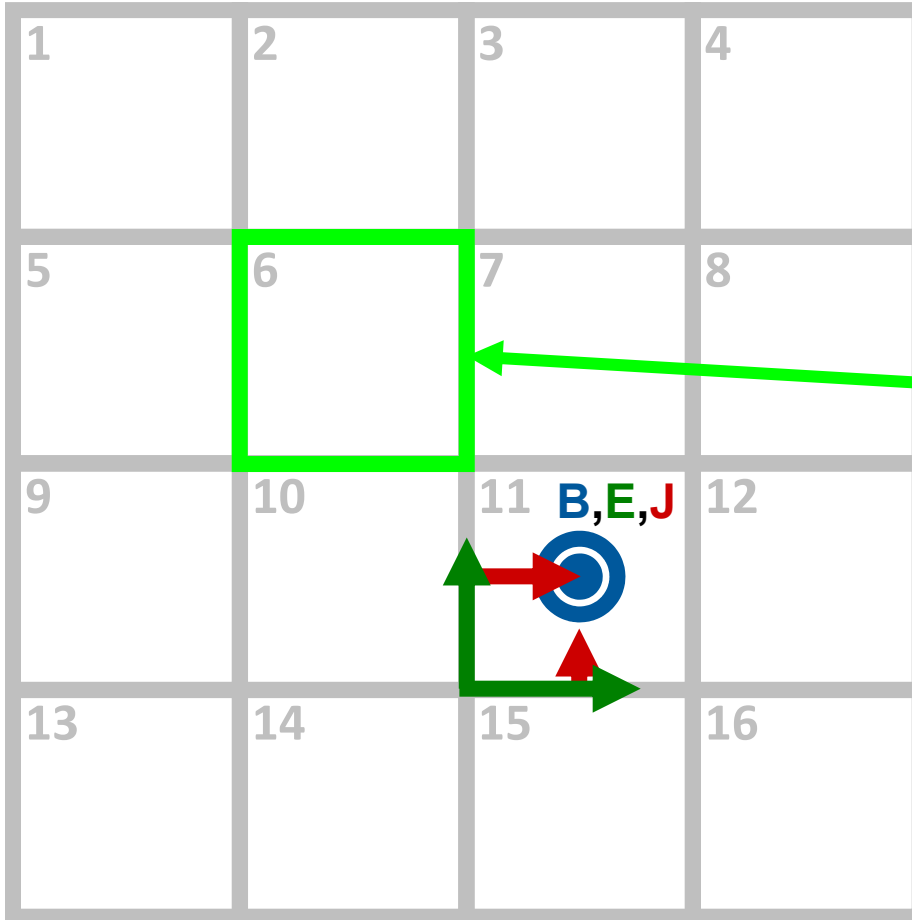


*“Almost all Programming can be viewed as an Exercise in Caching”*

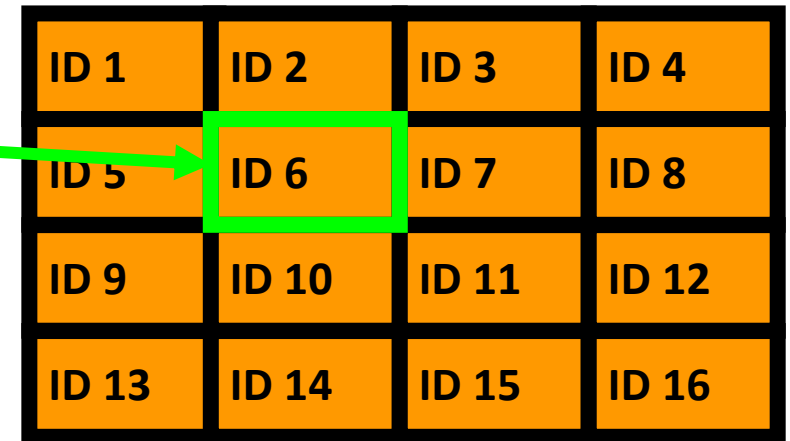


# Everything depends on Data Structures *PART 1* — Cell-based Data

## *Super Cell*

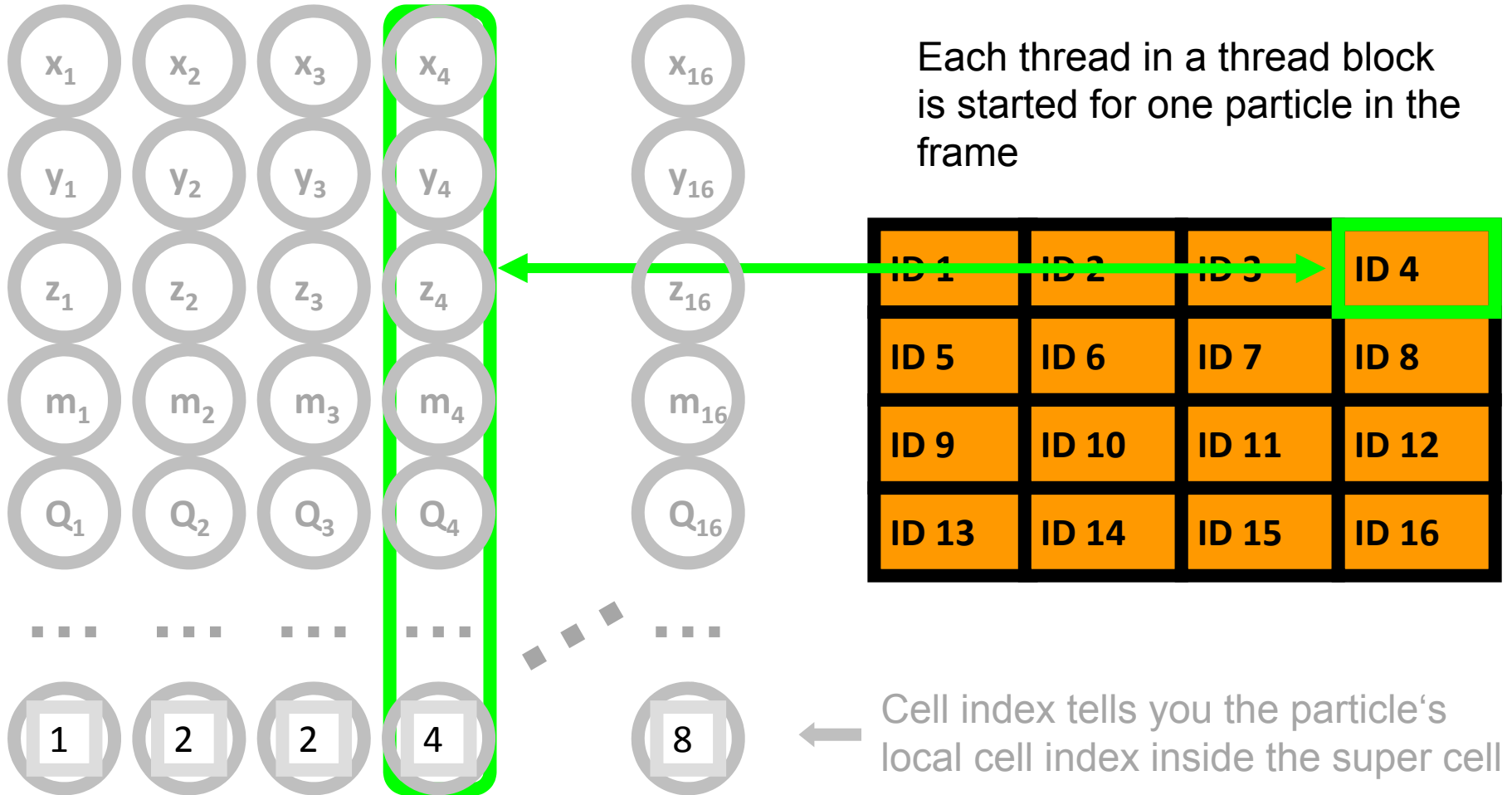


Each thread in a thread block corresponds to one cell in the super cell

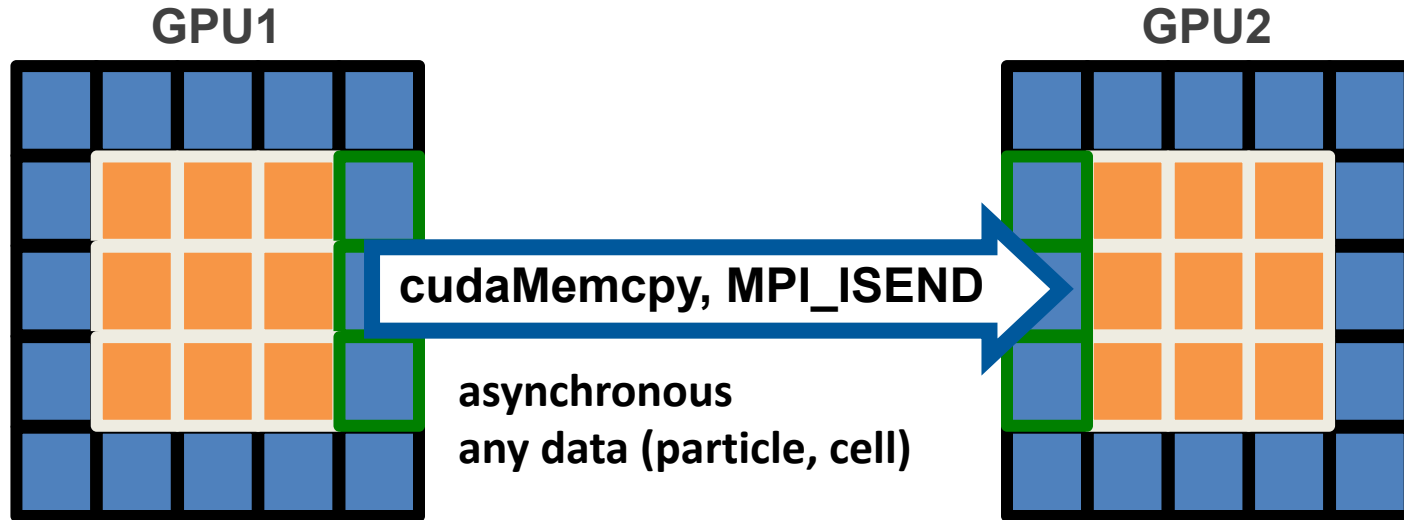


# Everything depends on Data Structures *PART 2* — Particle Data

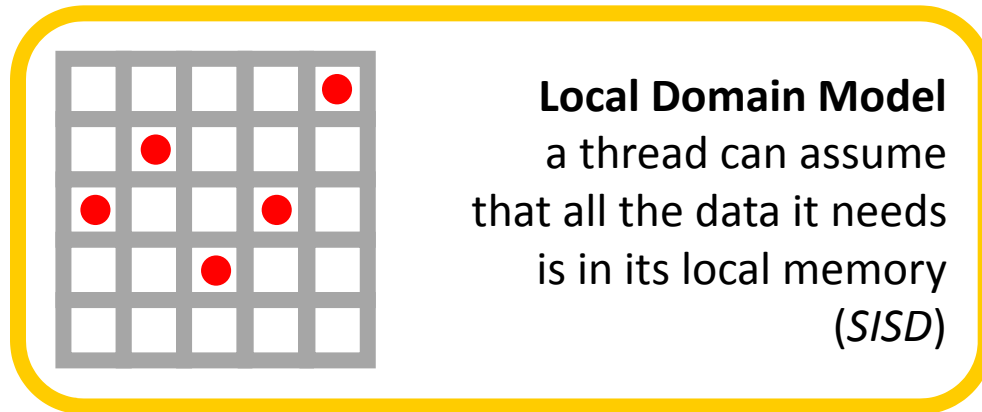
*Attribute Frame (the data structure formerly known as „tile“, „pool“, ....)*



# Encapsulation of all memory transfer functions



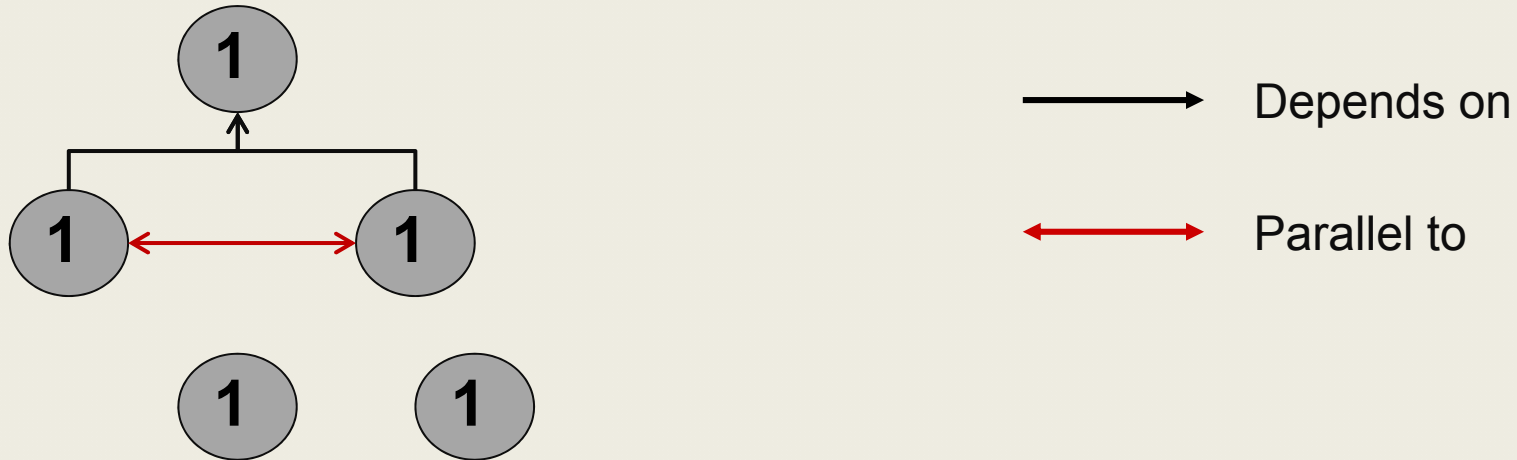
+





Events help to direct kernel execution, data exchange, etc.

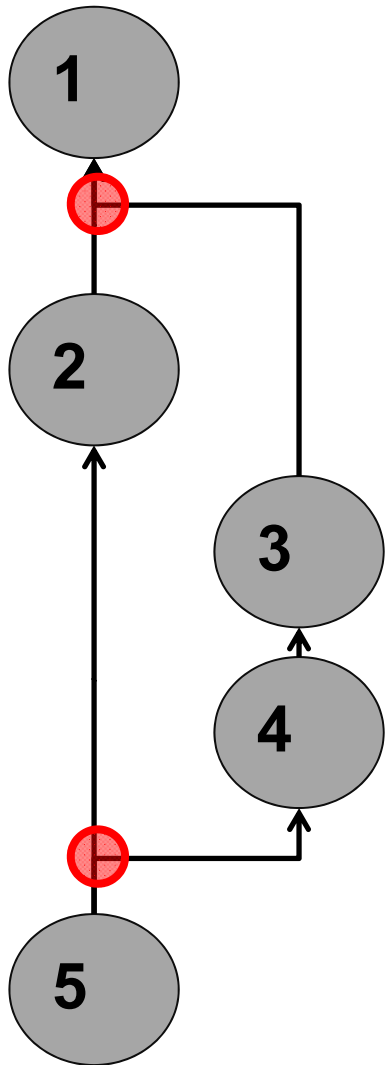
## EventTask tree



## Parallel hierarchy types

- TASK\_HOST (not parallel, limitation of cuda runtime)
- TASK\_CUDA (use streams for parallel work on gpu)
- TASK\_MPI

## Defining the algorithmic structure of a task graph



```
getSizeFromDevice(); // memcpy from device
```

```
EventTask e_split = __getTransactionEvent();
```

```
__startTransaction( e_split ); // depend from e_split
```

```
cudaKernel_X(); // create a kernel task
```

```
EventTask e1 = __endTransaction();
```

```
__startTransaction( e_split );
```

```
cudaKernel_Y();
```

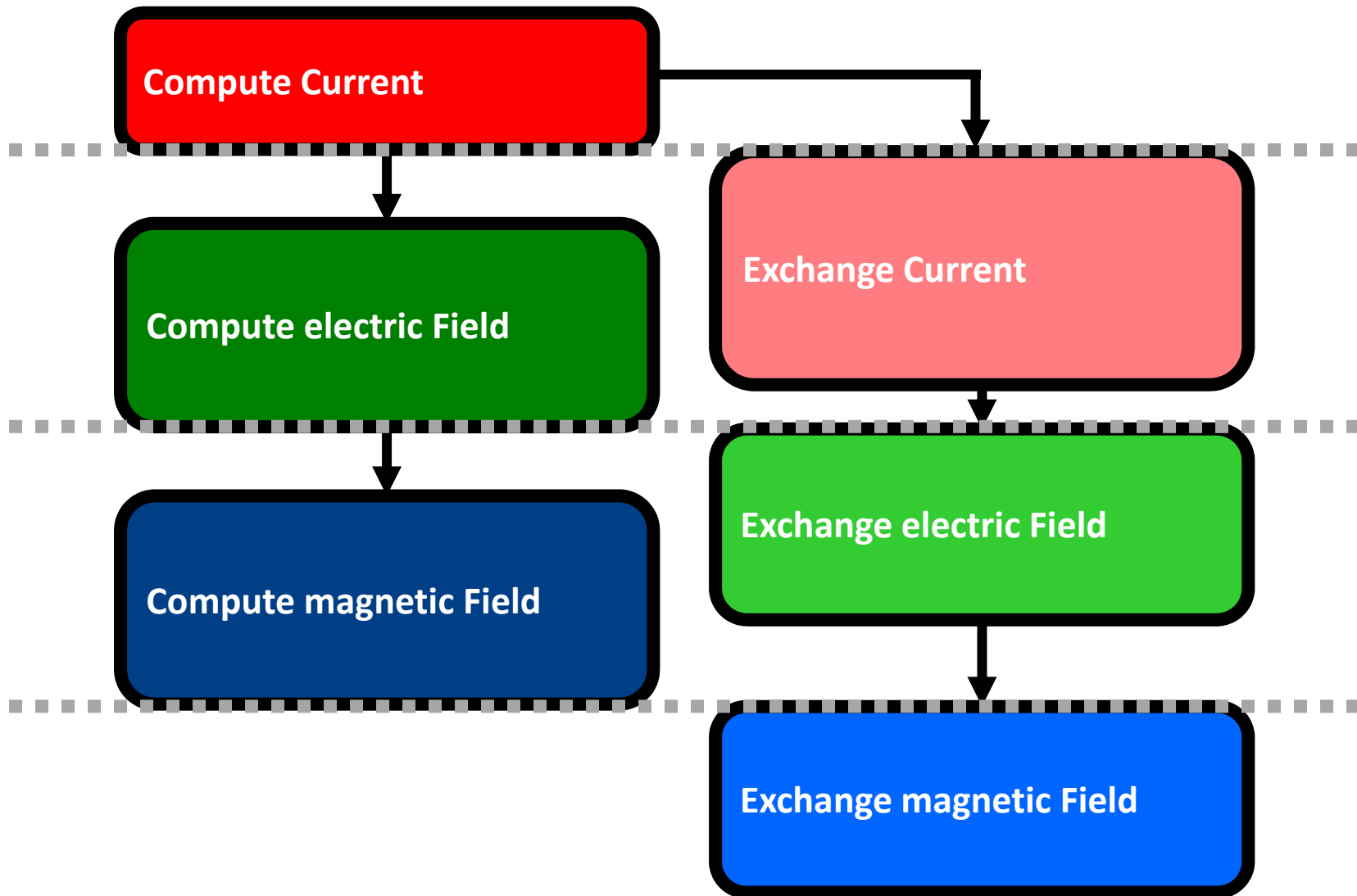
```
synchronizeWithNeighbor(); // memcpy+mpi task
```

```
EventTask e2 = __endTransaction();
```

```
__setTransactionEvent( e1+e2 ); // combine parallel work
```

```
cudaKernel_Z();
```

# Communicate and compute concurrently using Tasks



# Strong and Weak Scaling on NVIDIA FERMI

## Strong and Weak Scaling PConGPU 3D

Tesla S2050

