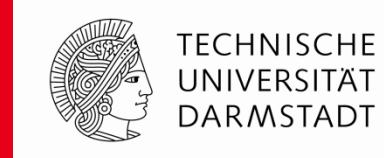


# Numerical Modeling of RF Electron Sources for FEL-Accelerators



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Technische Universität Darmstadt, Germany**

11th International Computational Accelerator  
Physics Conference (ICAP)  
August 19 – 24, 2012, Rostock-Warnemünde  
(Germany)



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- Self-consistent simulations with PBCI
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  - CDS booster
  - Diagnosis cross
- Summary and conclusions

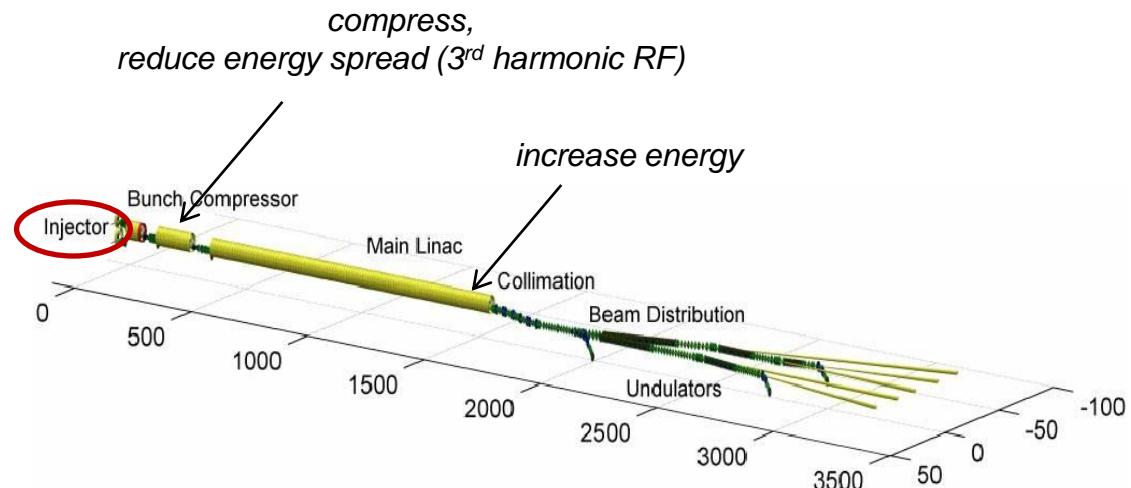
# Low emittance electron sources



## The European X-Ray Laser Project (XFEL)

- Electron beam specifications:

- Peak current (1-10 kA)
- **Emittance (< 1 mm mrad)**
- Energy (10-20 GeV)
- Energy spread (~0.01 %)
- Bunch length (10  $\mu\text{m}$  - 1 mm)
- ...



Cannot control transverse beam emittance except for at injection time

⇒ Low emittance source necessary

European XFEL design layout

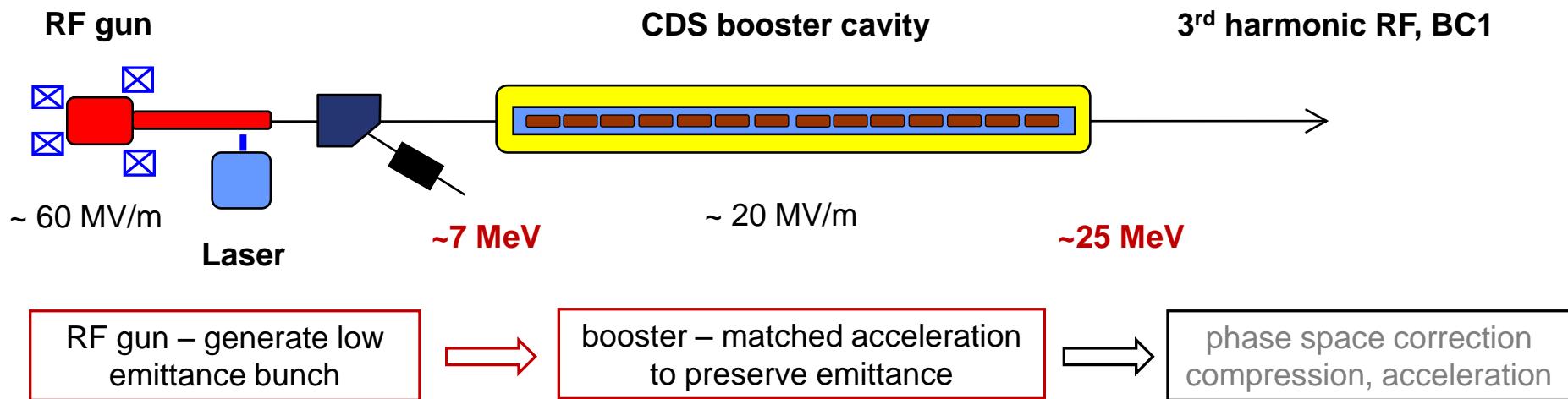
→ RF photoinjector

# Low emittance electron sources



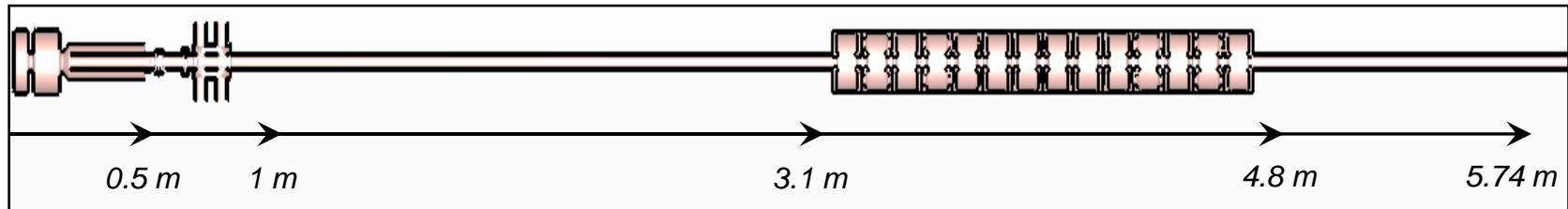
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## DESY PITZ-1.8 photoinjector setup

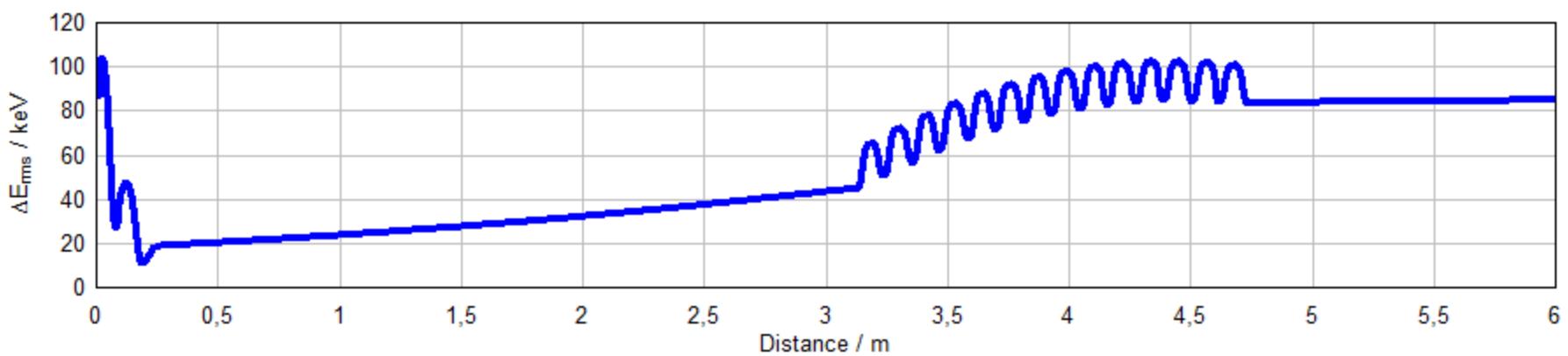
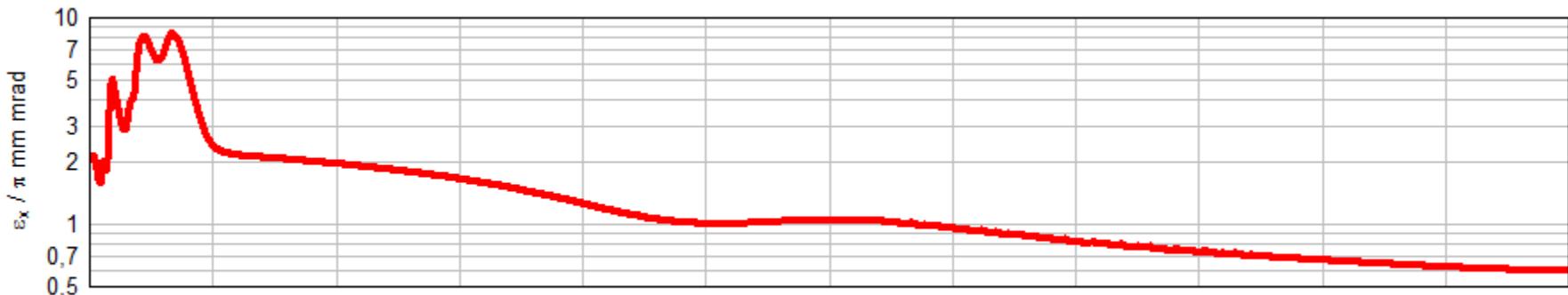
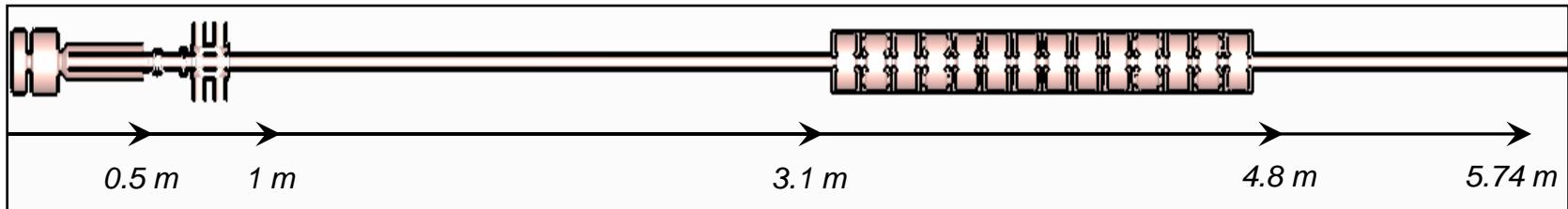


- 1999: project begin at PITZ facility in Zeuthen, Berlin
- 2003: first operating device – 1.7 mm mrad for 1nC bunch
- 2010: PITZ-1.6 – 1.2 mm mrad
- 2011: PITZ-1.8 meets E-XFEL specification – 0.9 mm mrad

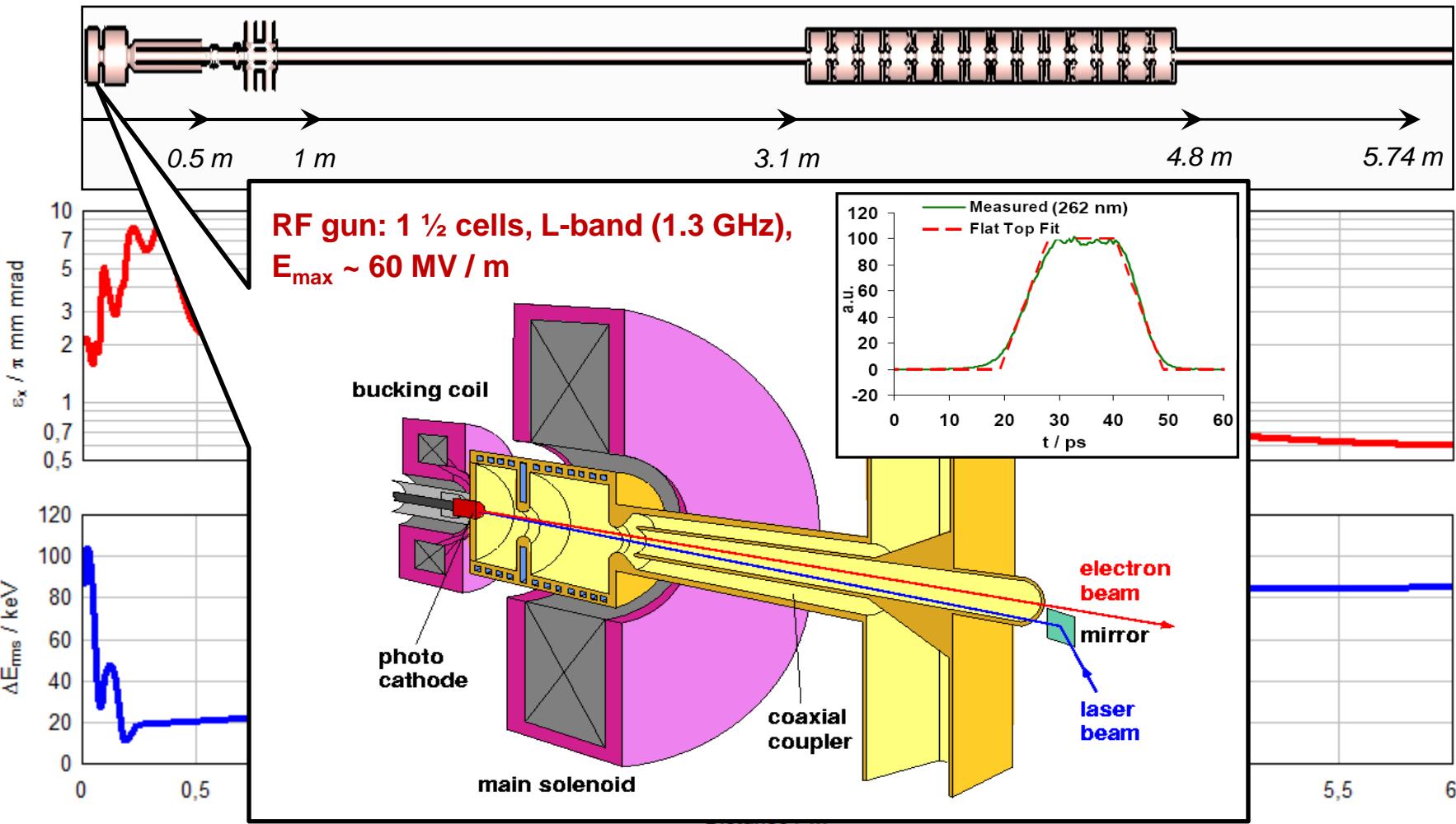
# Low emittance electron sources



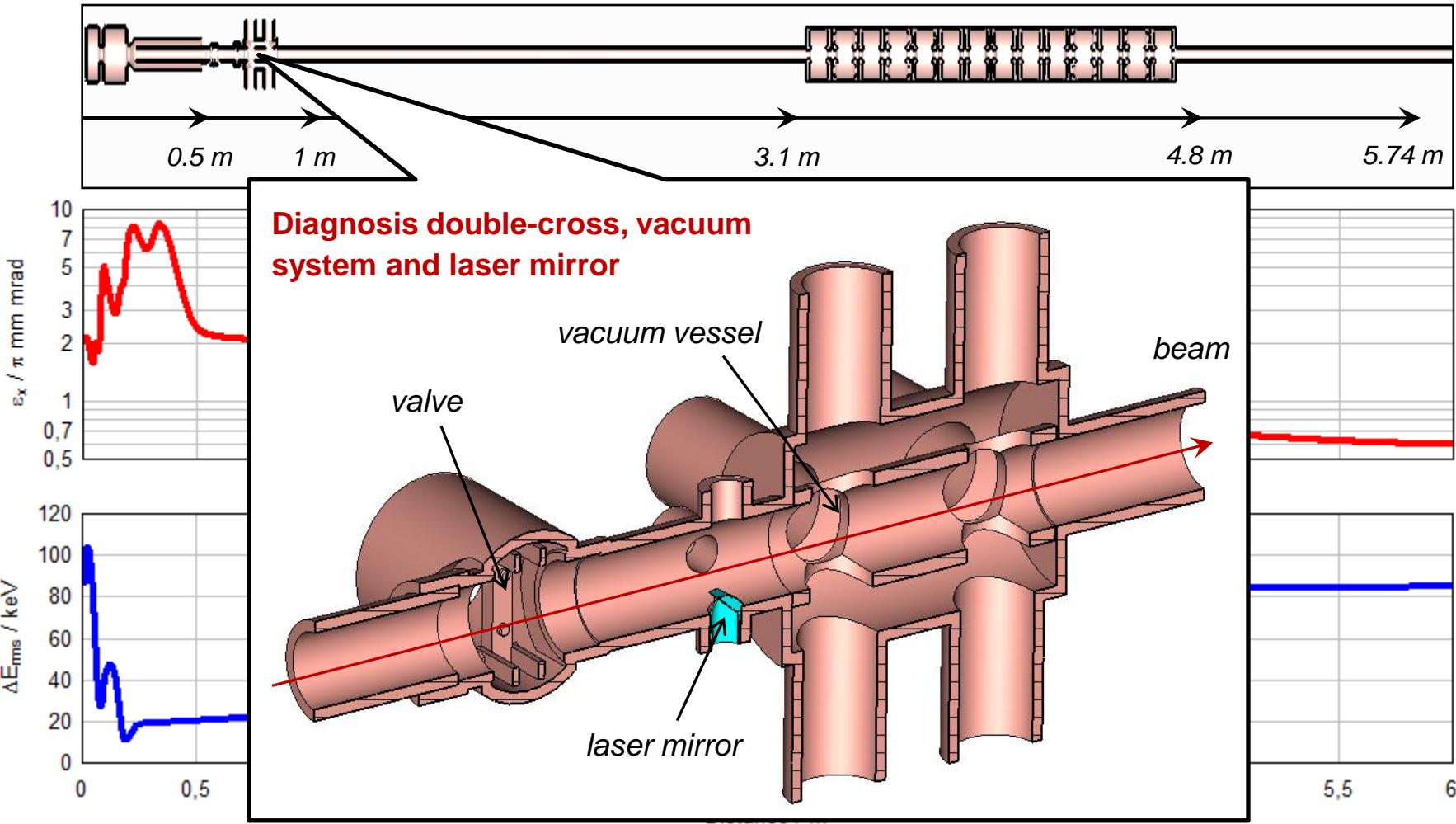
# Low emittance electron sources



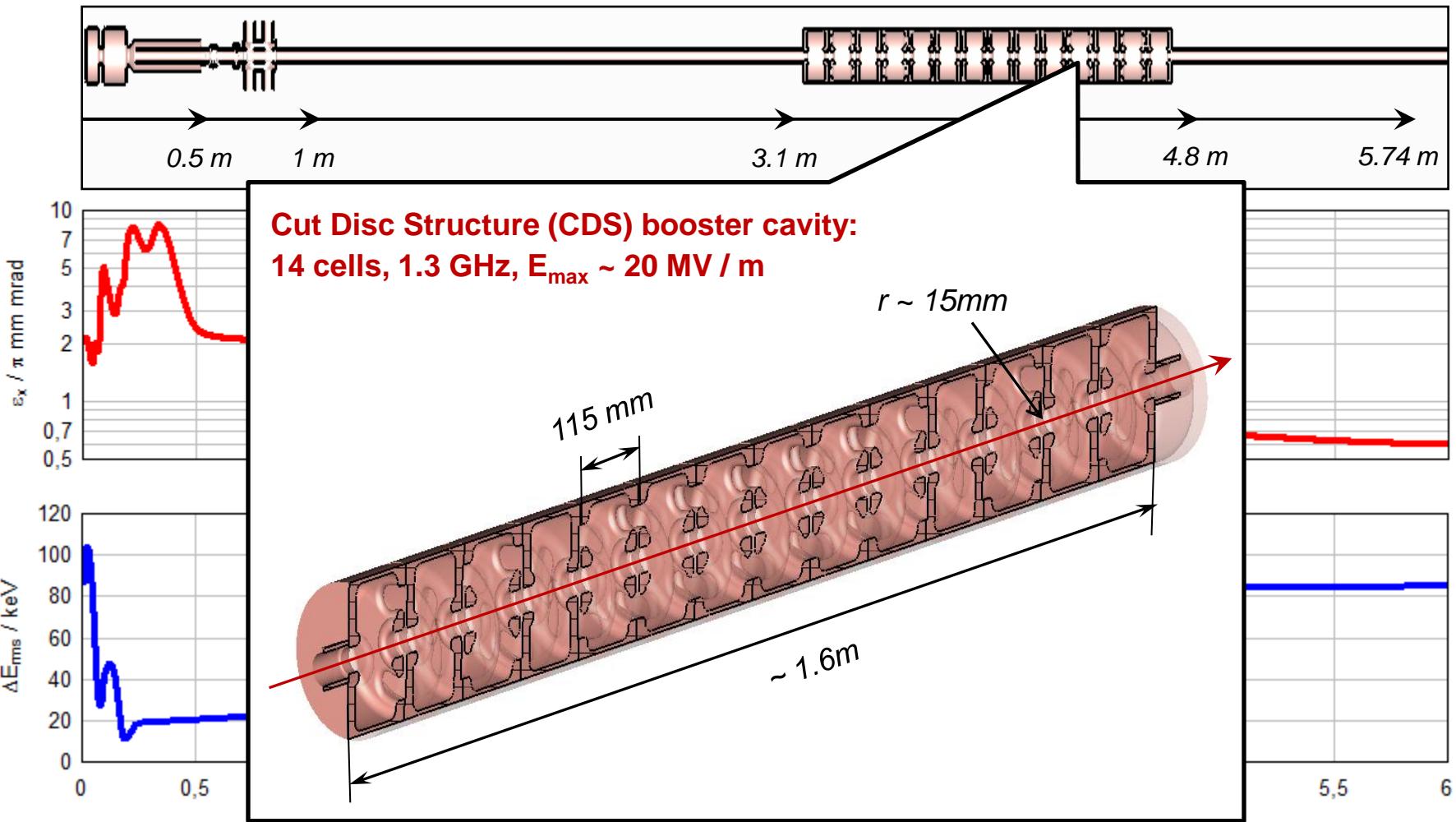
# Low emittance electron sources



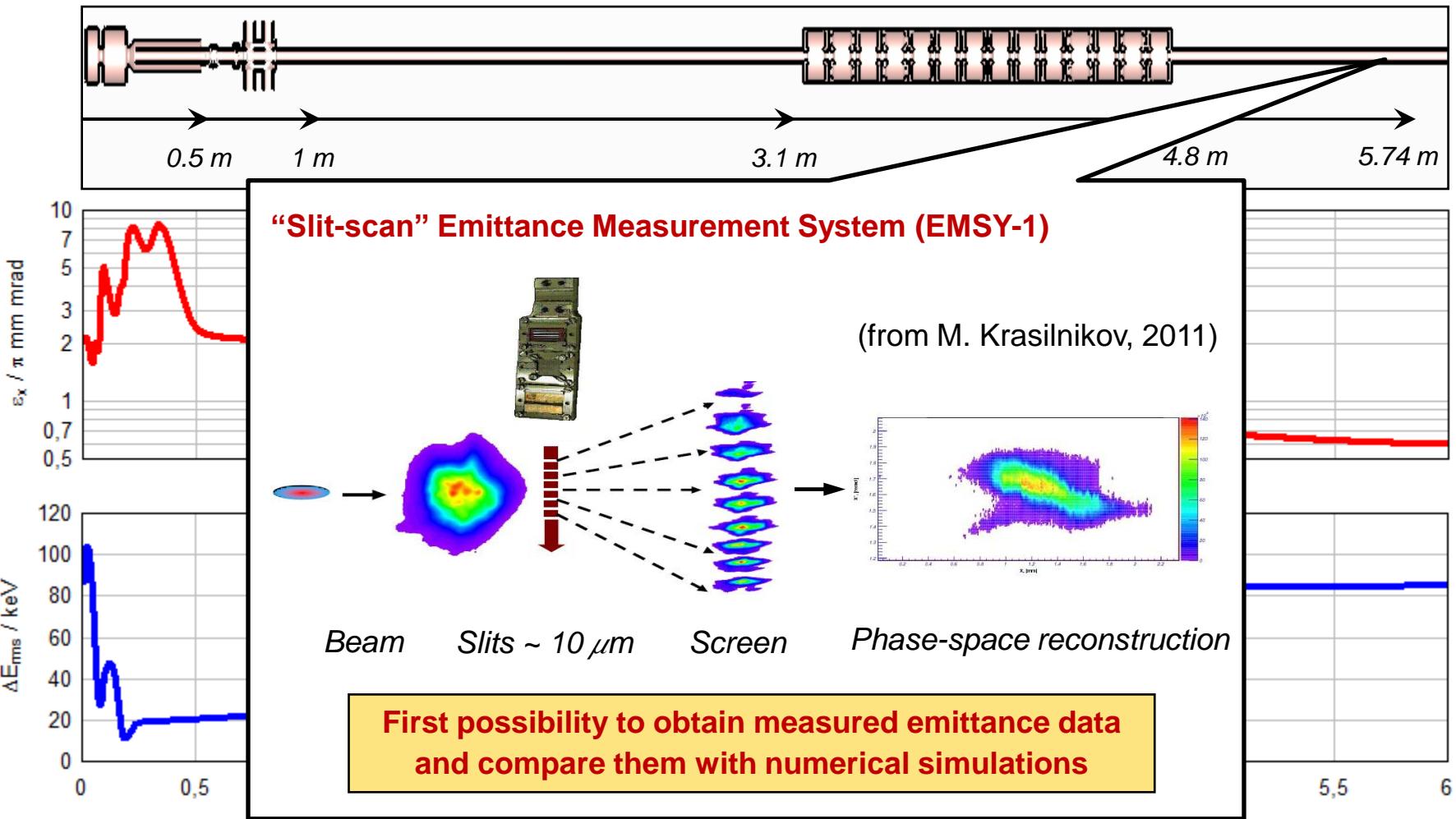
# Low emittance electron sources



# Low emittance electron sources



# Low emittance electron sources





## (Some) particle tracking codes

- Rest frame space-charge field codes (Parmela, Astra, IMPACT-T, GPT, ...)
- Vlasov moment equation solvers (V-code, ...)
- Envelope equation solvers (Homdyn, ...)
- ...

- Use of various physical approximations
- Space-charge fields do not „see“ cavity geometry (except for cathode)
- Wakefields only as fixed external maps or Green functions
- Numerically efficient (mostly axis-symmetric)



## (Some) particle tracking codes

- Rest frame space-charge field codes (Parmela, Astra, IMPACT-T, GPT, ...)
- Vlasov moment equation solvers (V-code, ...)
- Envelope equation solvers (Homdyn, ...)
- ...
- Wakefield codes (Echo, Pbc, Gdfidl, CST PS, ...)

- Ultra-relativistic beams with fixed beam current only
- No space-charge
- Full-wave in 3D using moving window and dispersion free algorithms



## (Some) particle tracking codes

- Rest frame space-charge field codes (Parmela, Astra, IMPACT-T, GPT, ...)
- Vlasov moment equation solvers (V-code, ...)
  - First principle
  - No geometry (except for cathode)
  - Computationally extremely inefficient
- Lienard-Wiechert solvers (Tredi, Quindi, ...)



## (Some) particle tracking codes

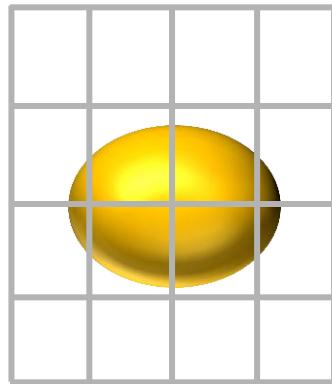
- Rest frame space-charge field codes (Parmela, Astra, IMPACT-T, GPT, ...)
- Vlasov moment equation solvers (V-code, ...)
- Envelope equation solvers (Homdyn, ...)
  - First principle
  - Full geometry and arbitrary transient beam distributions
  - Computationally less efficient in 3D: not applicable for short bunches and long accelerator structures (> 1m)
- Full-wave PIC codes (Mafia, CST PS, Vorpal, ...)

# Low emittance electron sources

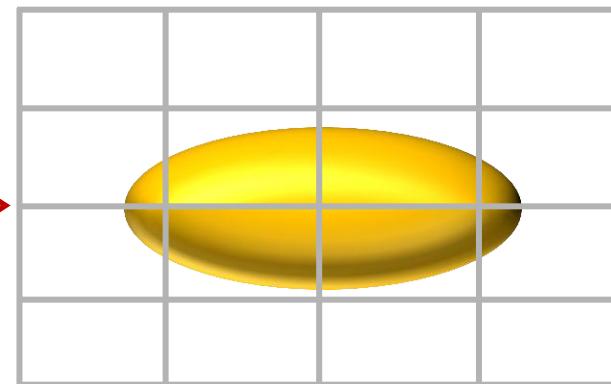


## Rest frame SC field codes

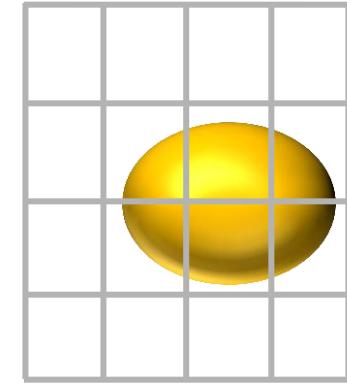
*Bring particles  
to computational grid*



*Solve for electrostatic field in  
the grid*



*Push particle positions  
and momenta*

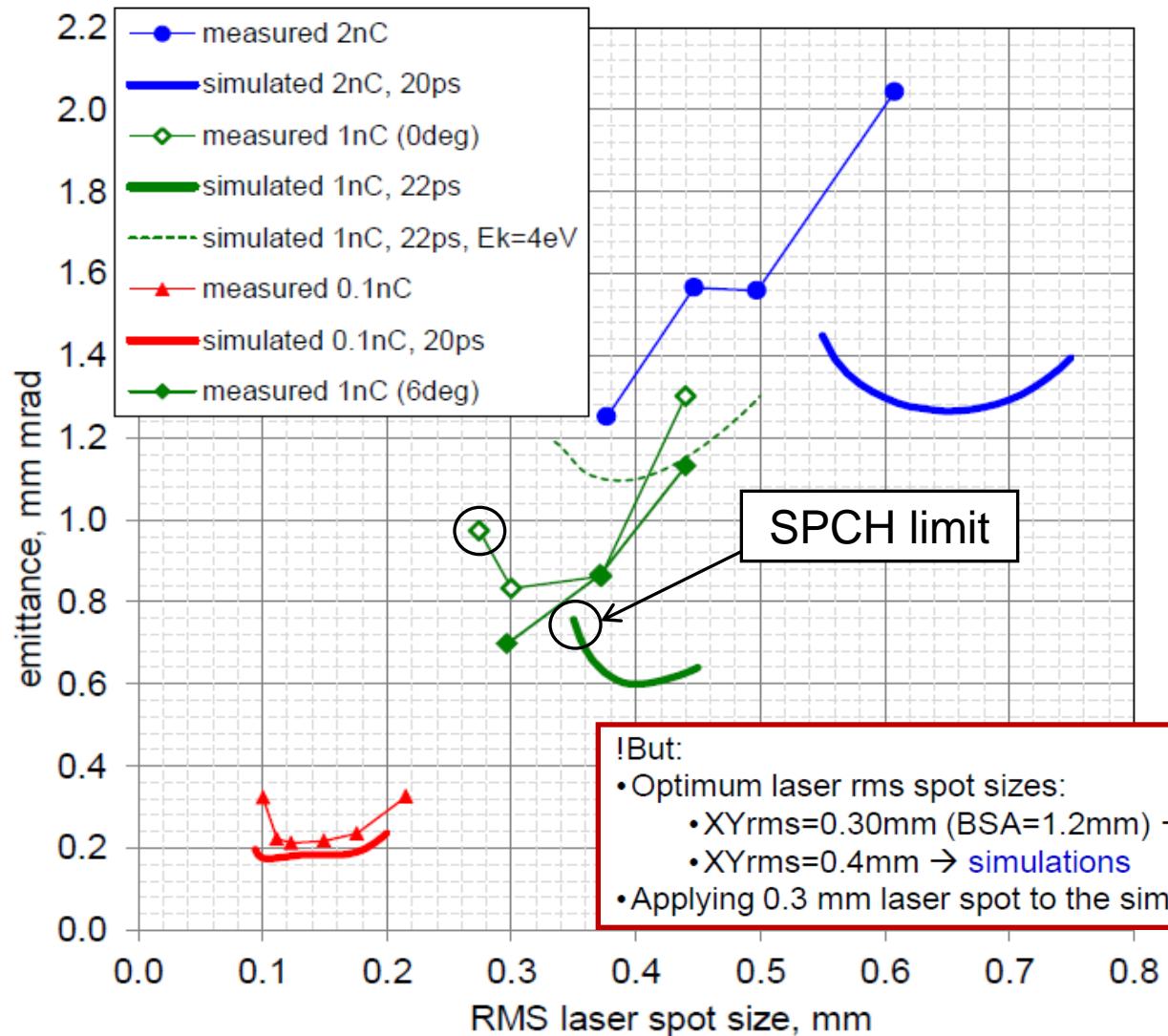


*Transform  
(charge) to average rest frame*

*Transform  
(fields) back to lab frame*

- Influence of rest frame approximation (neglect retardation and acceleration radiation) on simulation accuracy?
- Impact of geometrical wakefields on transverse emittance?

# Low emittance electron sources



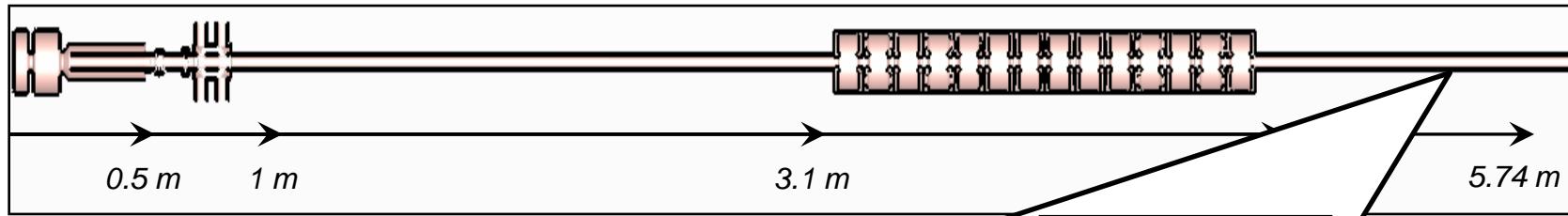
- Optimum machine parameters (laser spot size, gun phase):  
experiment ≠ simulations
- Difference in the optimum laser spot size is bigger for higher charges (good agreement for 100pC)
- Artificial increase of the thermal kinetic energy at the cathode (from 0.55eV to 4eV) did not improve the situation

(talk from M. Krasilnikov,  
Zeuthen, 2011)

# Self-consistent simulations with PBCI



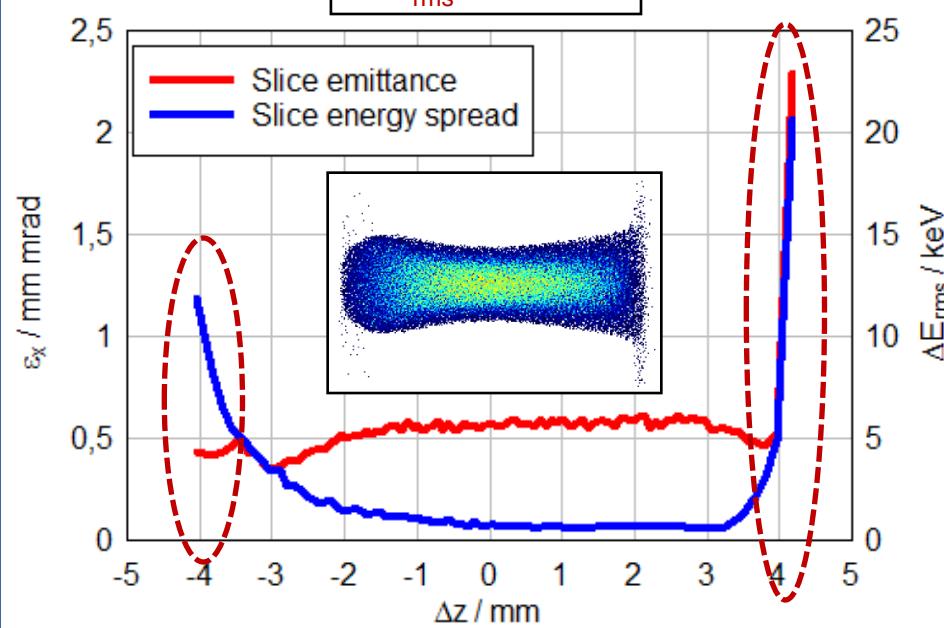
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Beam scraper for PITZ

$v/c$   
0.9998  
0.99976546

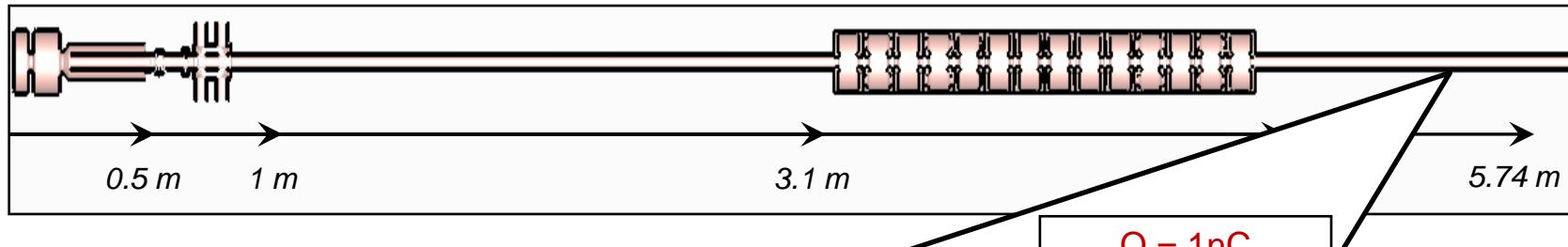
$v/c$   
0.9998  
0.99977382



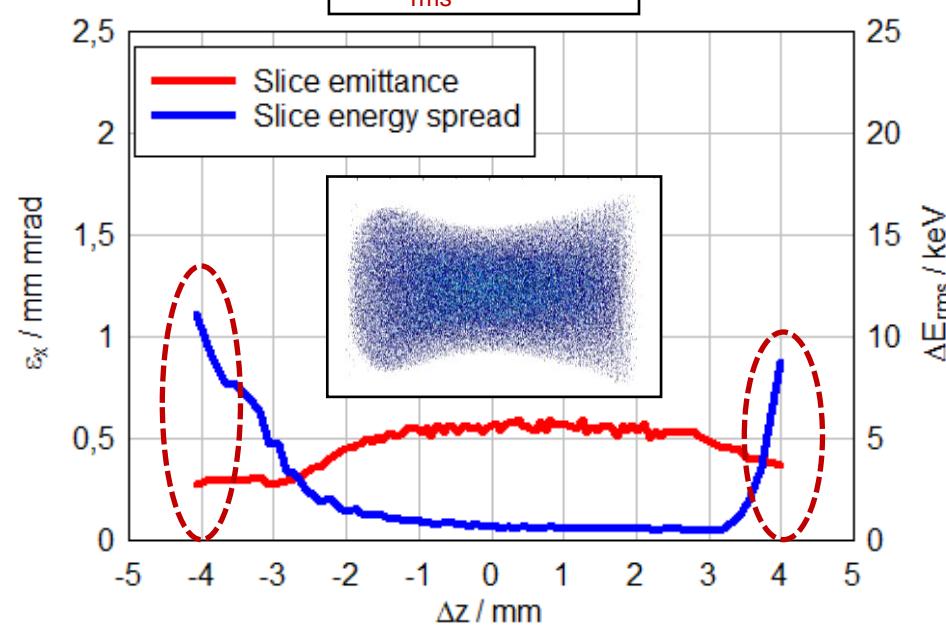
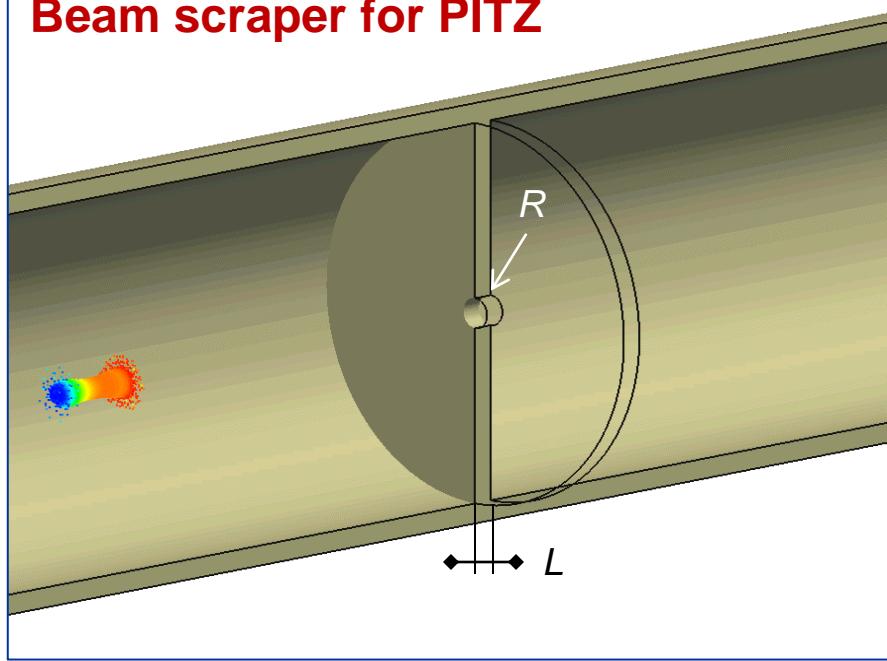
# Self-consistent simulations with PBCI



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## Beam scraper for PITZ

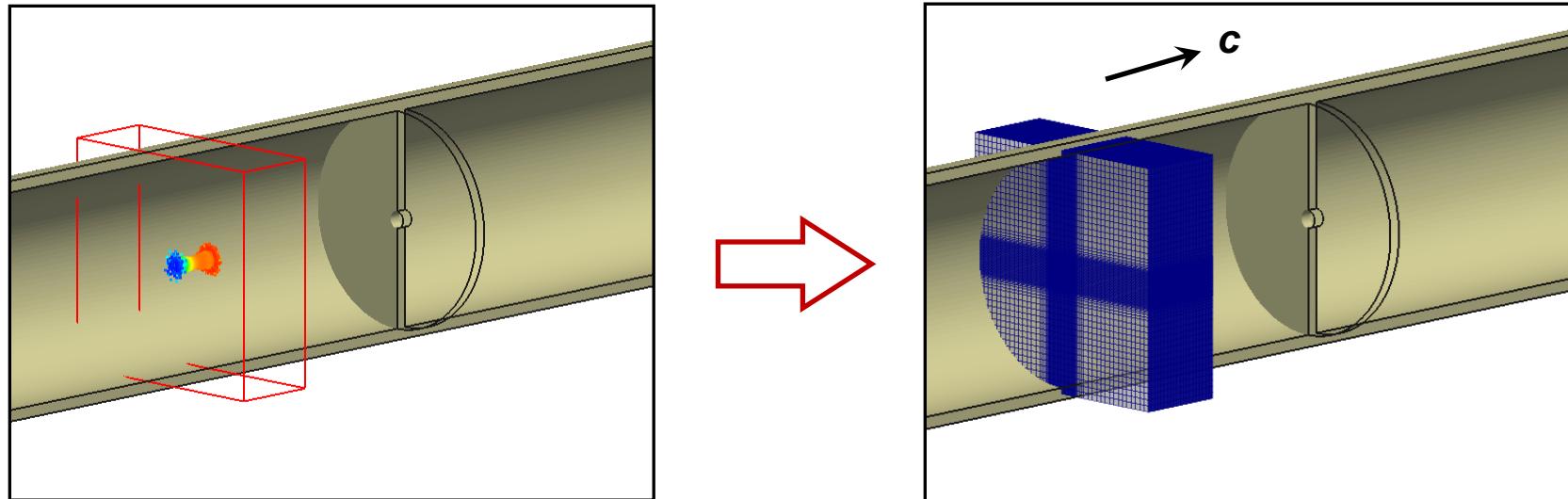


# Self-consistent simulations with PBCI



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## Particle-In-Cell in the moving window

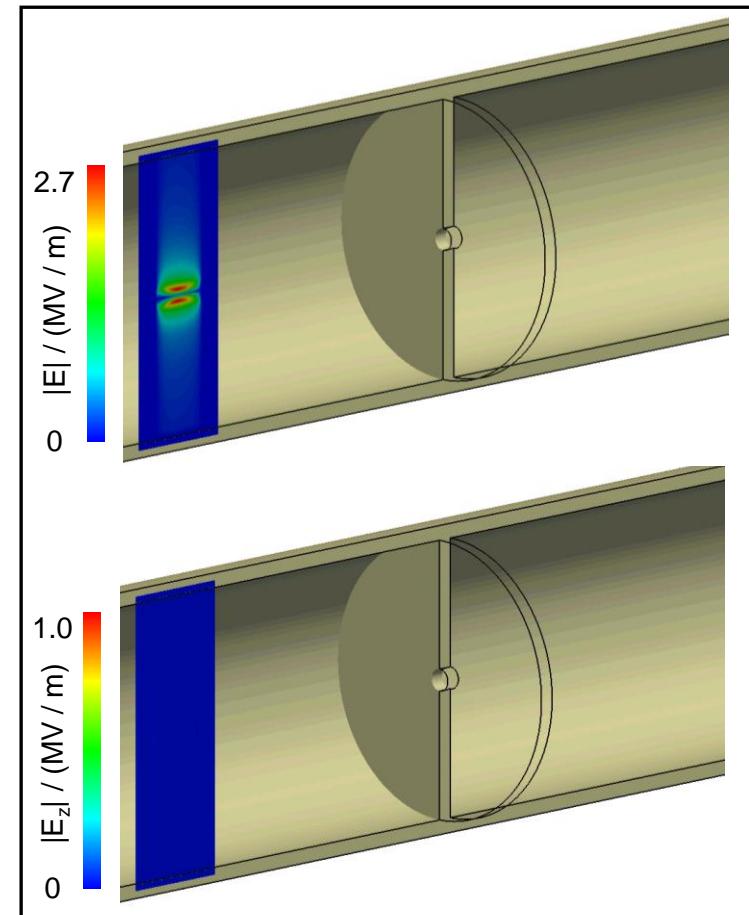


- Nearly ultra-relativistic but:
  - transverse dynamics over long distances not negligible
  - non-constant current due to scraping
- **Combine moving frame wakefield simulation approach (PBCI) with PIC**



## Particle-In-Cell in the moving window

- Dispersion-free EM field solution:
  - Optimum stable time step
  - Computational window moving with  $c$
  - Boundary conditions not needed
- Small discretization domain:
  - **Necessary transverse resolution for bunch and geometry  $< 50 \mu\text{m}$**
- Simple field initialization:
  - TEM field of ultra-relativistic bunch in pipe of arbitrary cross-section



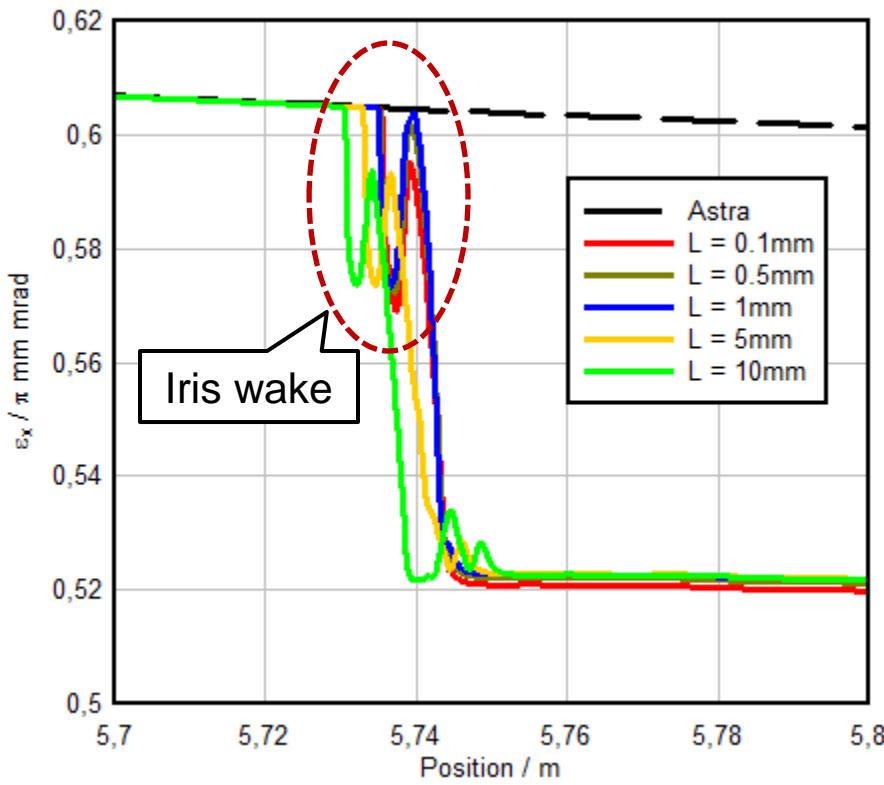
# Self-consistent simulations with PBCI



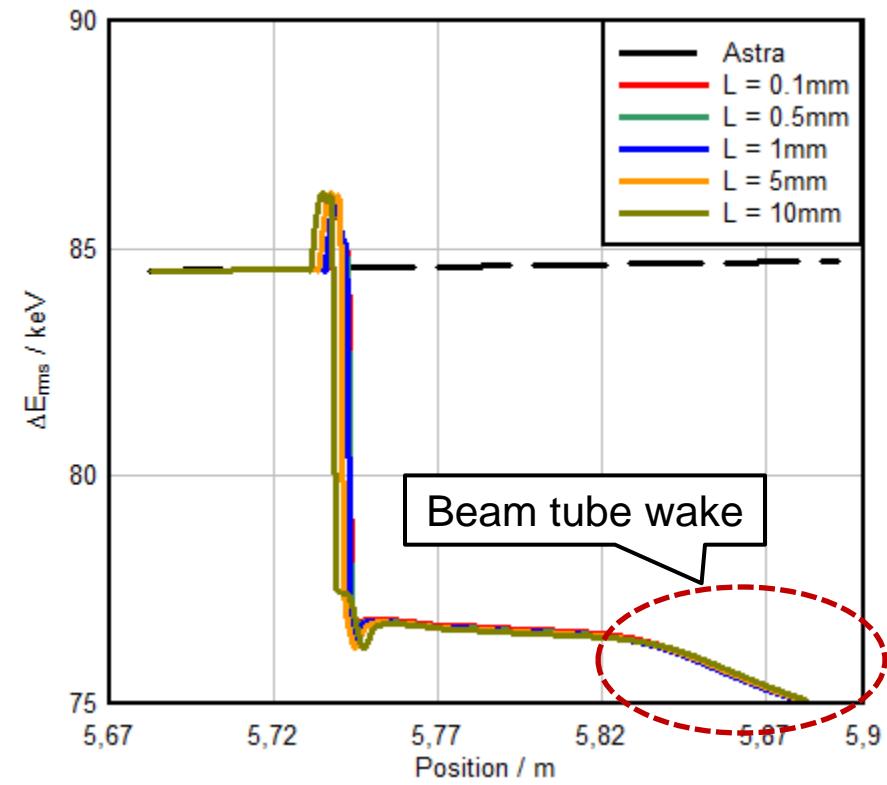
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## Beam scraper results

Emittance ( $1nC$ ,  $0.4mm$ ,  $R = 1mm$ )



Energy spread ( $1nC$ ,  $0.4mm$ ,  $R = 1mm$ )

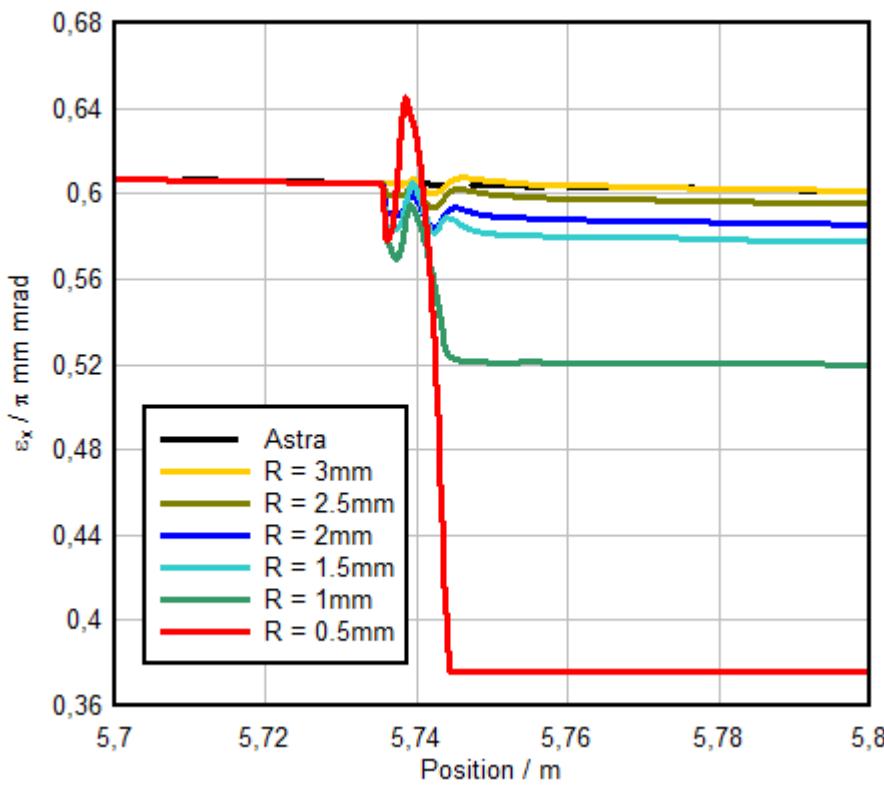


# Self-consistent simulations with PBCI

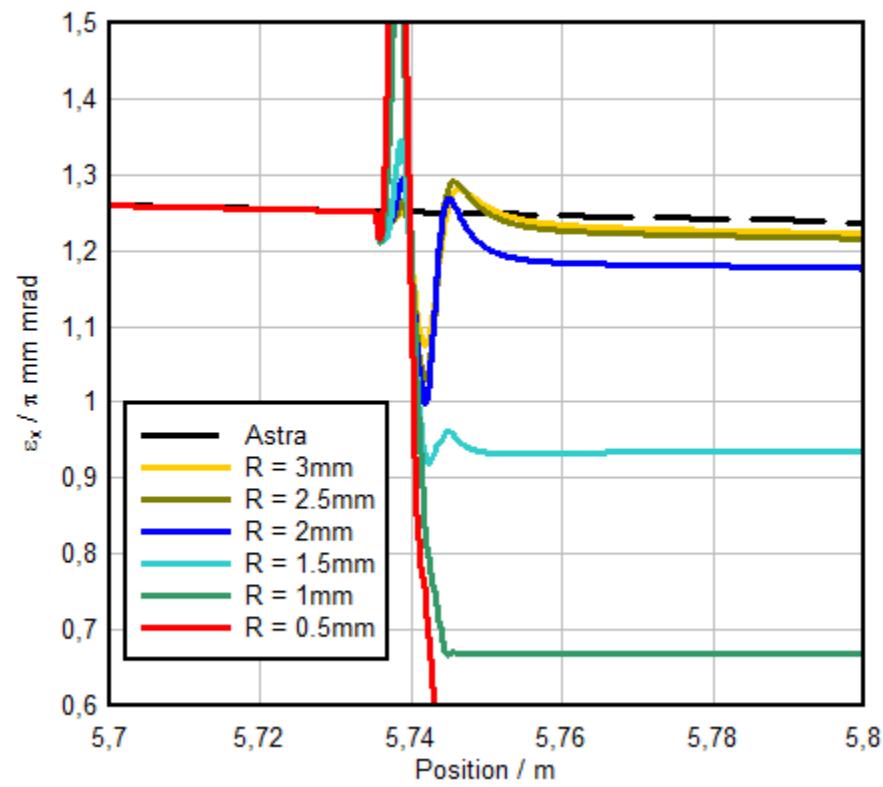


## Beam scraper results

Emittance ( $1nC$ ,  $0.4mm$ ,  $L = 0.1mm$ )



Emittance ( $2nC$ ,  $0.6mm$ ,  $L = 0.1mm$ )

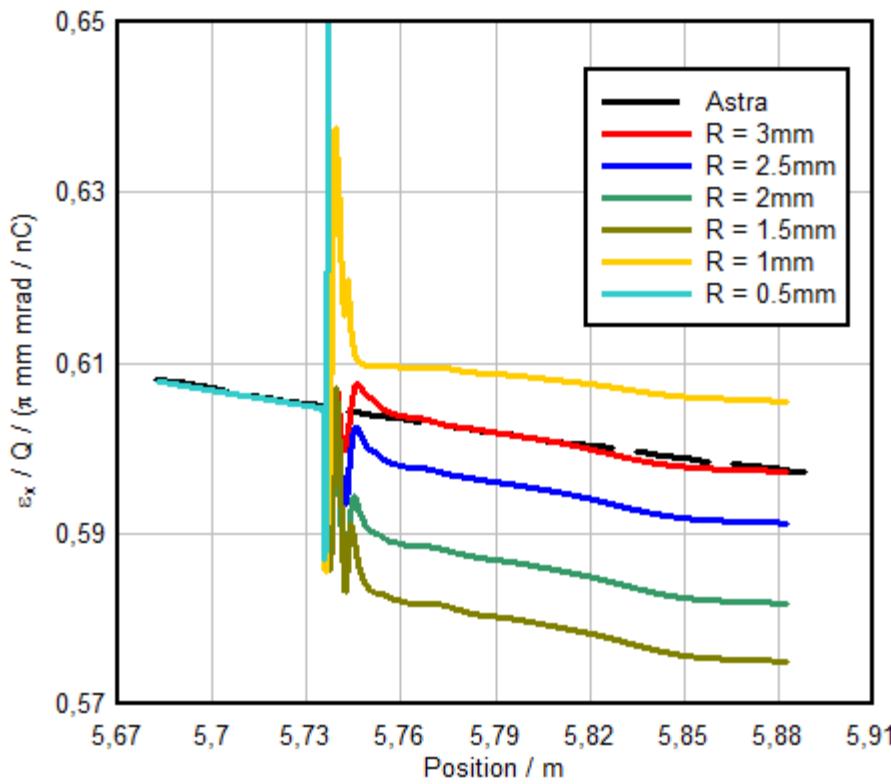


# Self-consistent simulations with PBCI

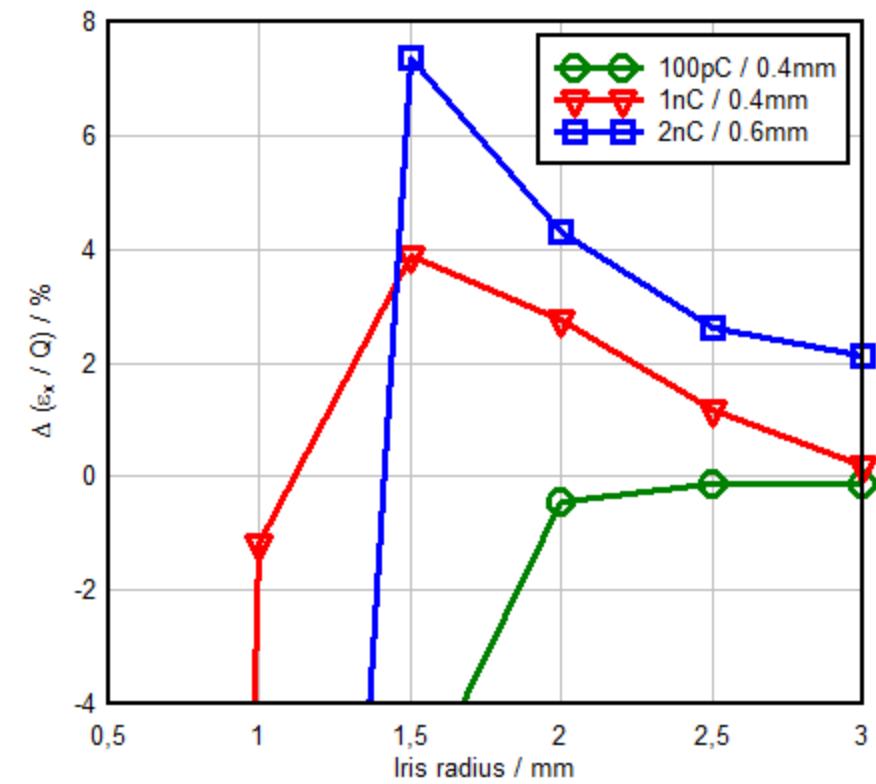


## Beam scraper results

Emittance per Q (1nC, 0.4mm, L = 0.1mm)



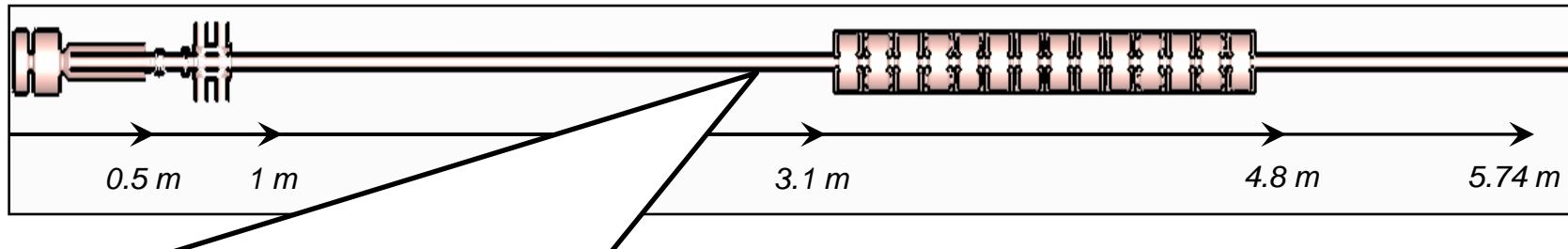
Expected gain in FEL-brilliance



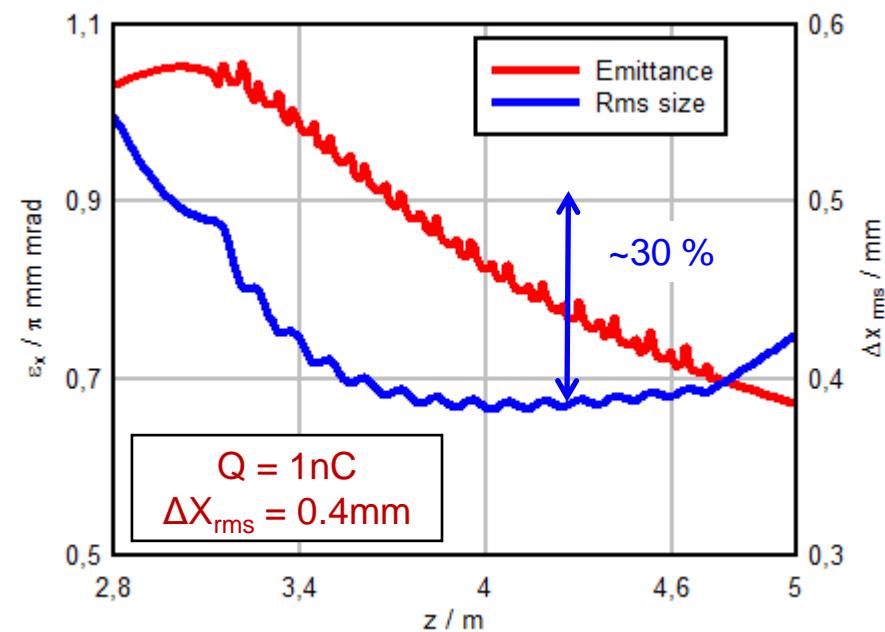
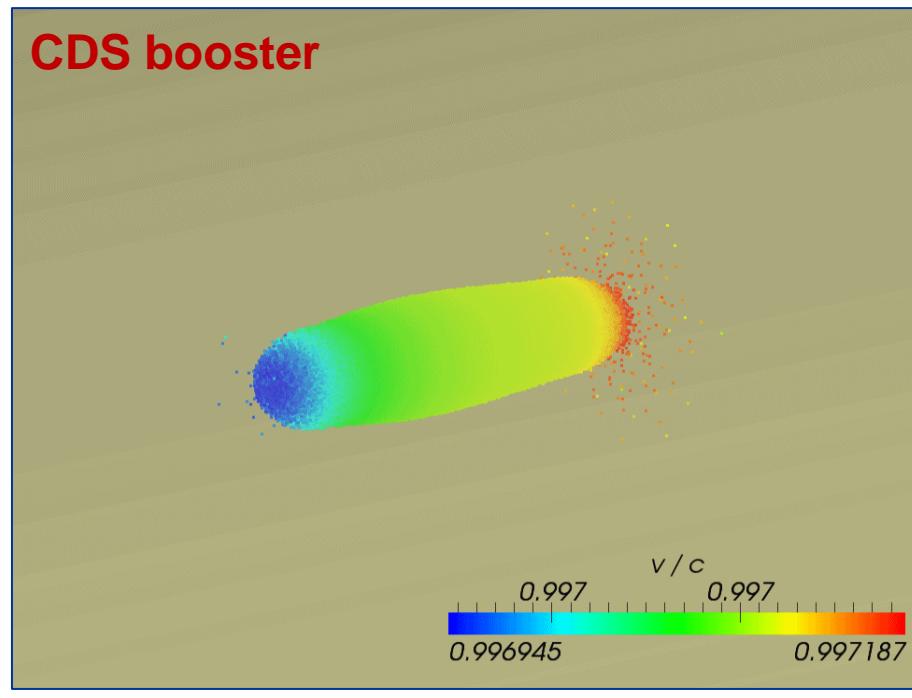
# Self-consistent simulations with PBCI



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CDS booster

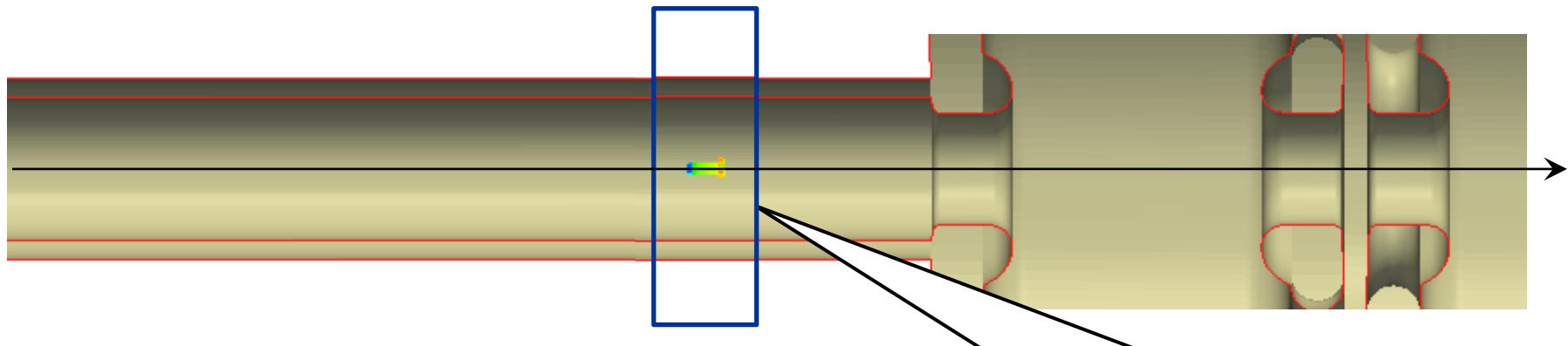


# Self-consistent simulations with PBCI



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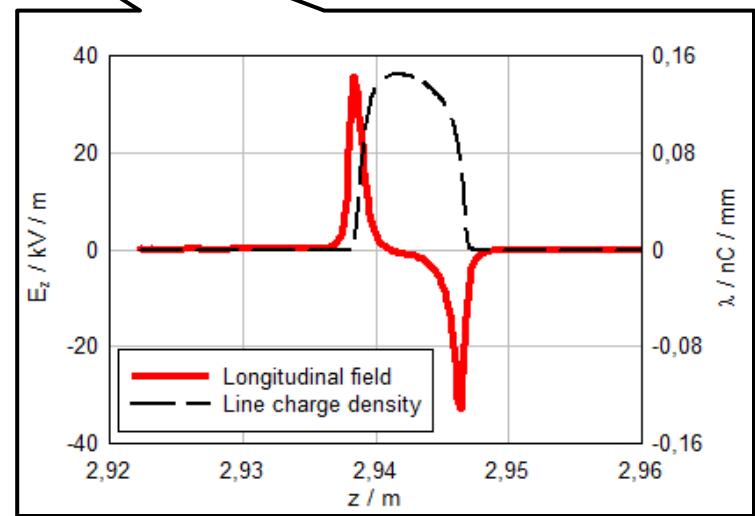
## Field initialization procedure



- Transform to (average) rest frame:

$$\left. \begin{aligned} \rho' &= \gamma \left( \rho - \frac{\beta}{c} j_z \right) := \frac{\rho}{\gamma} \\ j_z' &= \gamma(j_z - v\rho) := 0 \end{aligned} \right\} \Leftrightarrow j_z = \rho v$$

⇒ E-static rest frame solution violates charge conservation in PIC

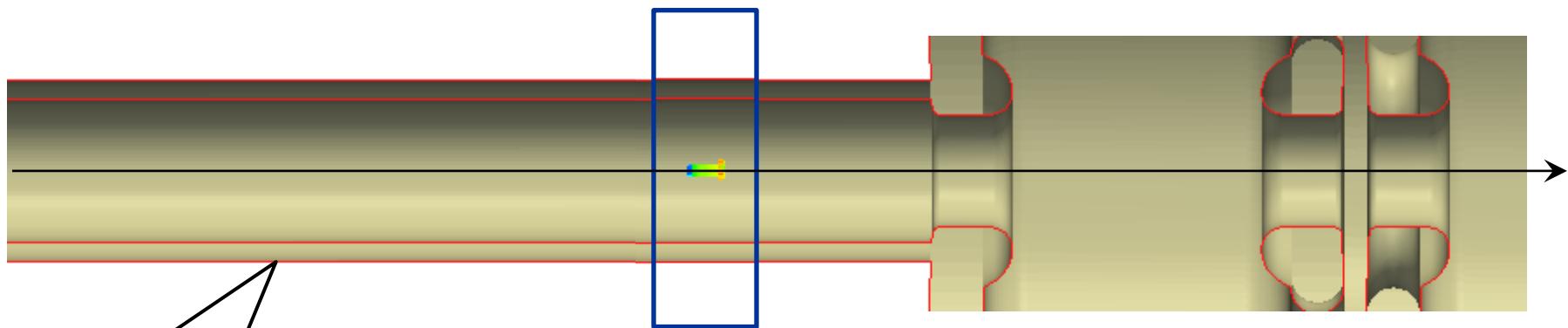


# Self-consistent simulations with PBCI



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## Field initialization procedure

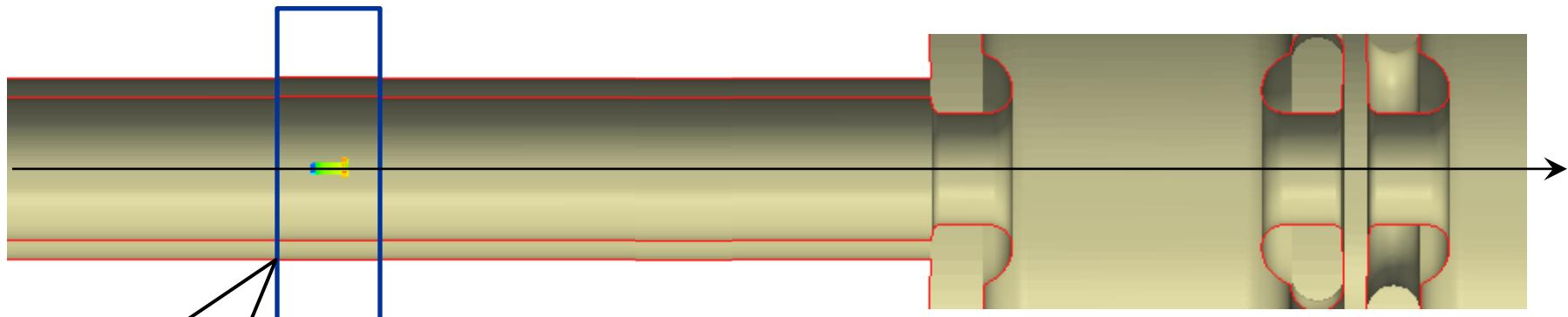


Track backwards  
with initial velocities

# Self-consistent simulations with PBCI

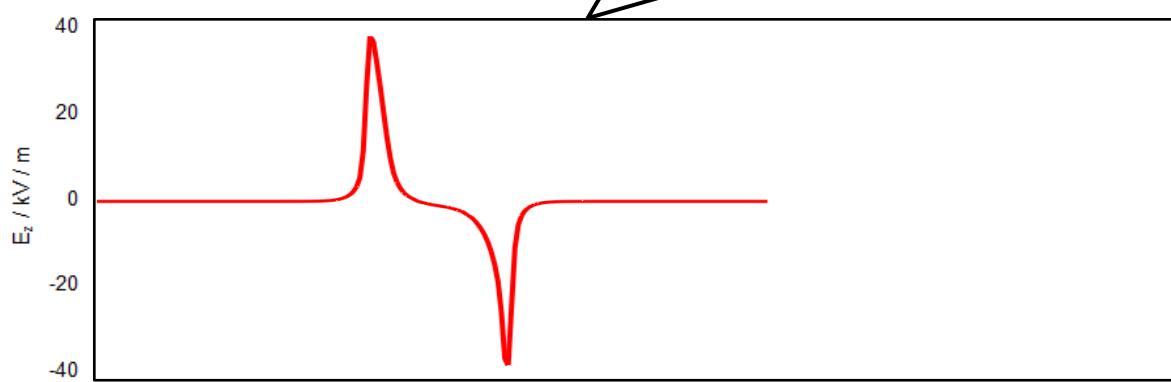


## Field initialization procedure



Track backwards  
with initial velocities

Initialize by rest  
frame transformation

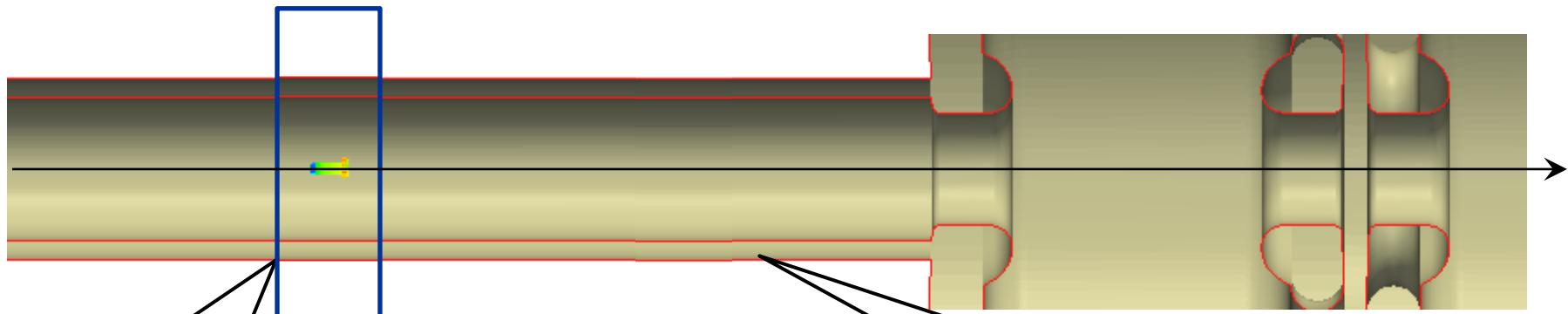


# Self-consistent simulations with PBCI



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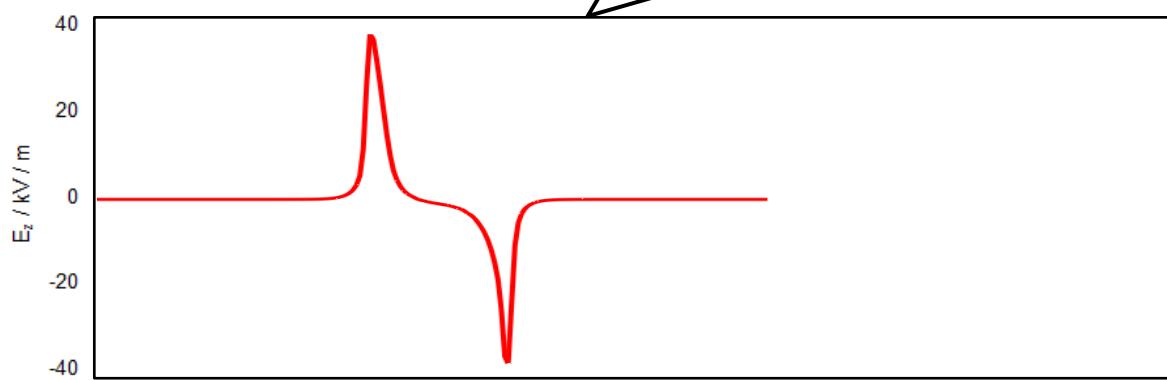
## Field initialization procedure



Track backwards  
with initial velocities

Initialize by rest  
frame transformation

Track forwards to initial  
positions / velocities

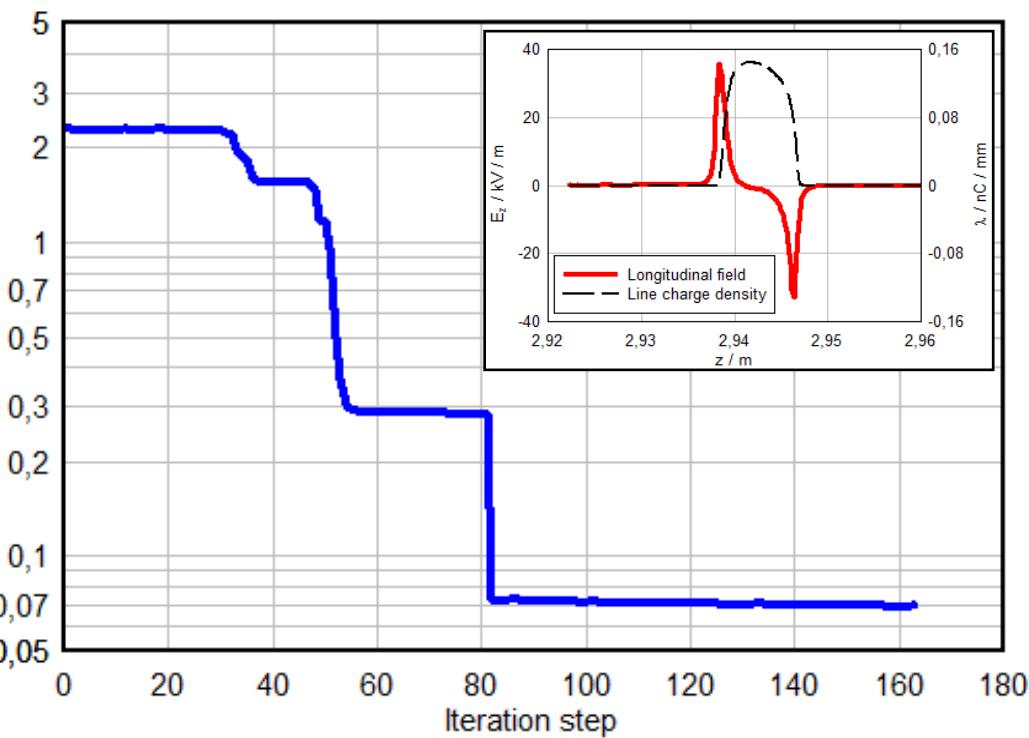


- Build-up consistent initial space-charge fields for PIC
- Include effects of relative motion within bunch

# Self-consistent simulations with PBCI

## Field initialization procedure

Relative error of  $\|E_z\|$  vs. iteration step



(Typical) data for CDS simulation

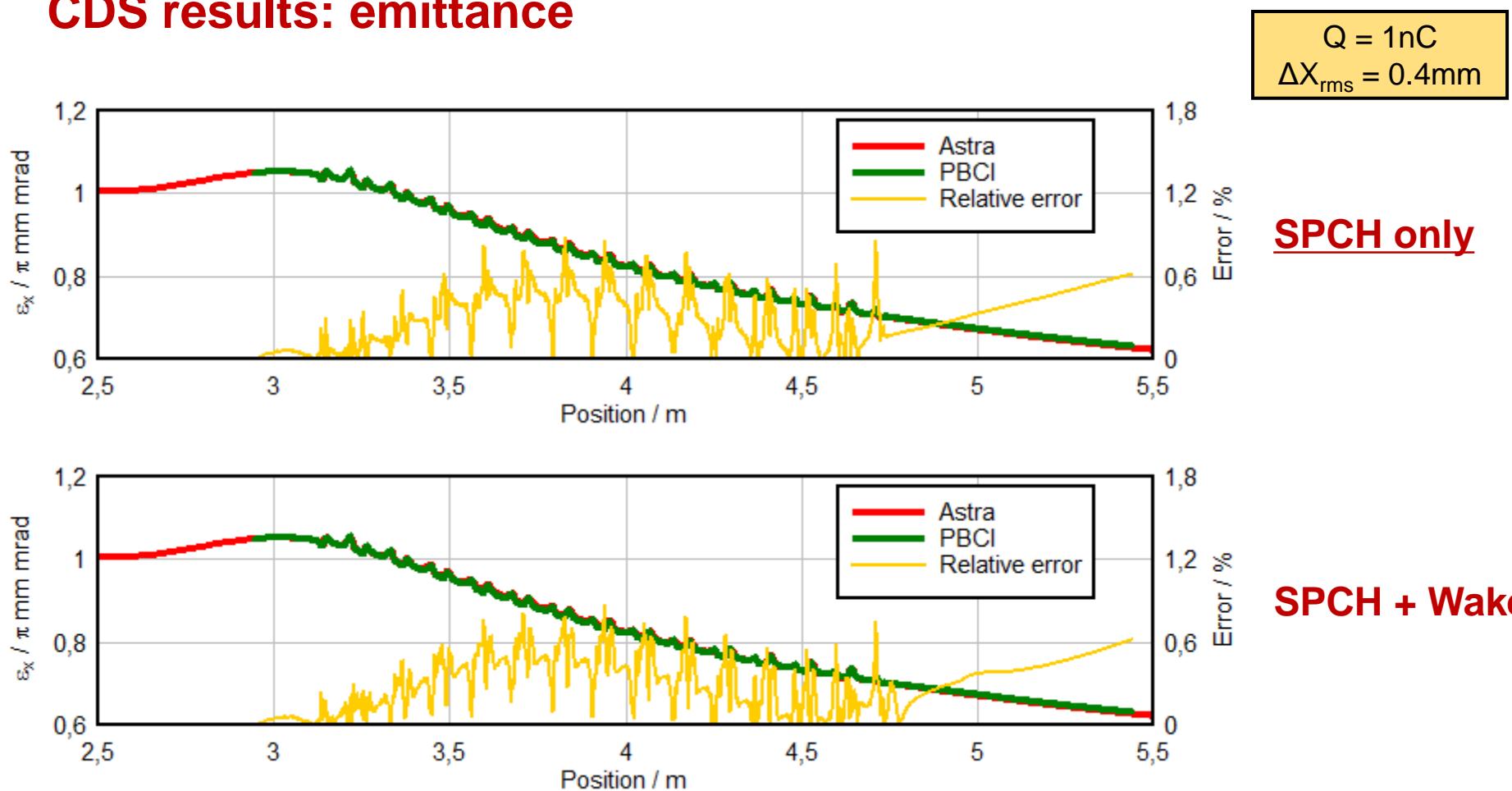
|                 |                                   |
|-----------------|-----------------------------------|
| Length          | 2.5m                              |
| Grid            | $\Delta x = \Delta z = 50 \mu m$  |
| No. DoFs        | $300 \times 10^6$                 |
| No. particles   | $0.5 \times 10^5 - 5 \times 10^5$ |
| No. steps       | $\sim 100,000$                    |
| Simulation time | $\sim 12 - 36 hrs.$               |

- Fast convergence (1-2 window lengths sufficient)
- Low cost compared to total simulation time

# Self-consistent simulations with PBCI



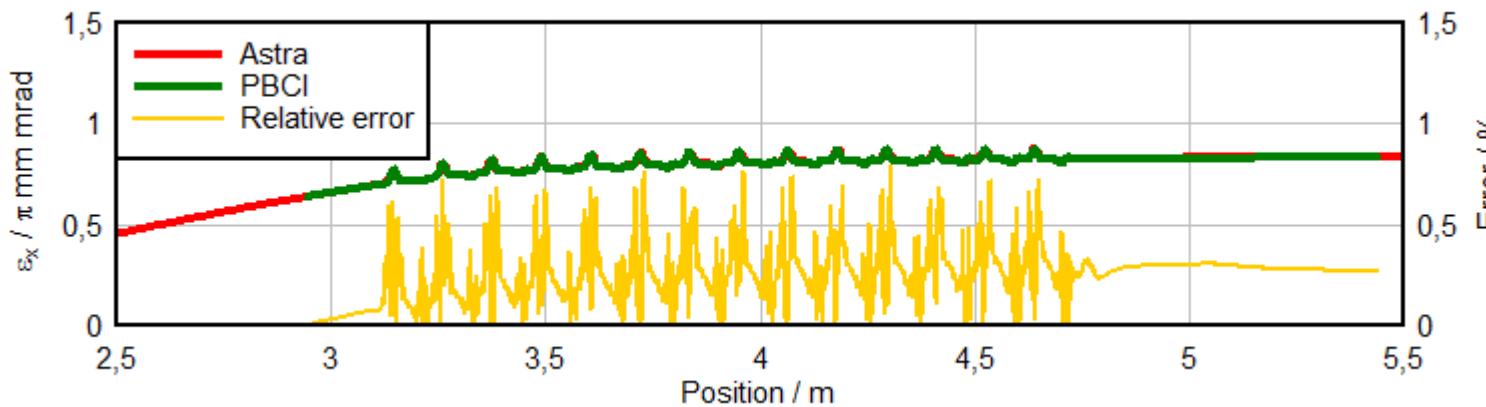
## CDS results: emittance



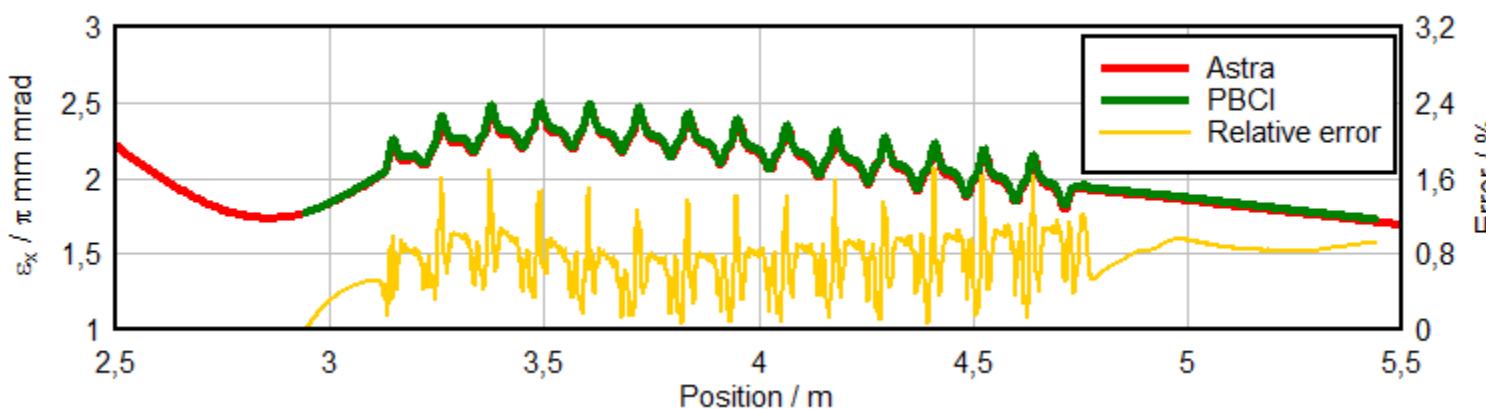
# Self-consistent simulations with PBCI



## CDS results: emittance



**SPCH + Wake**

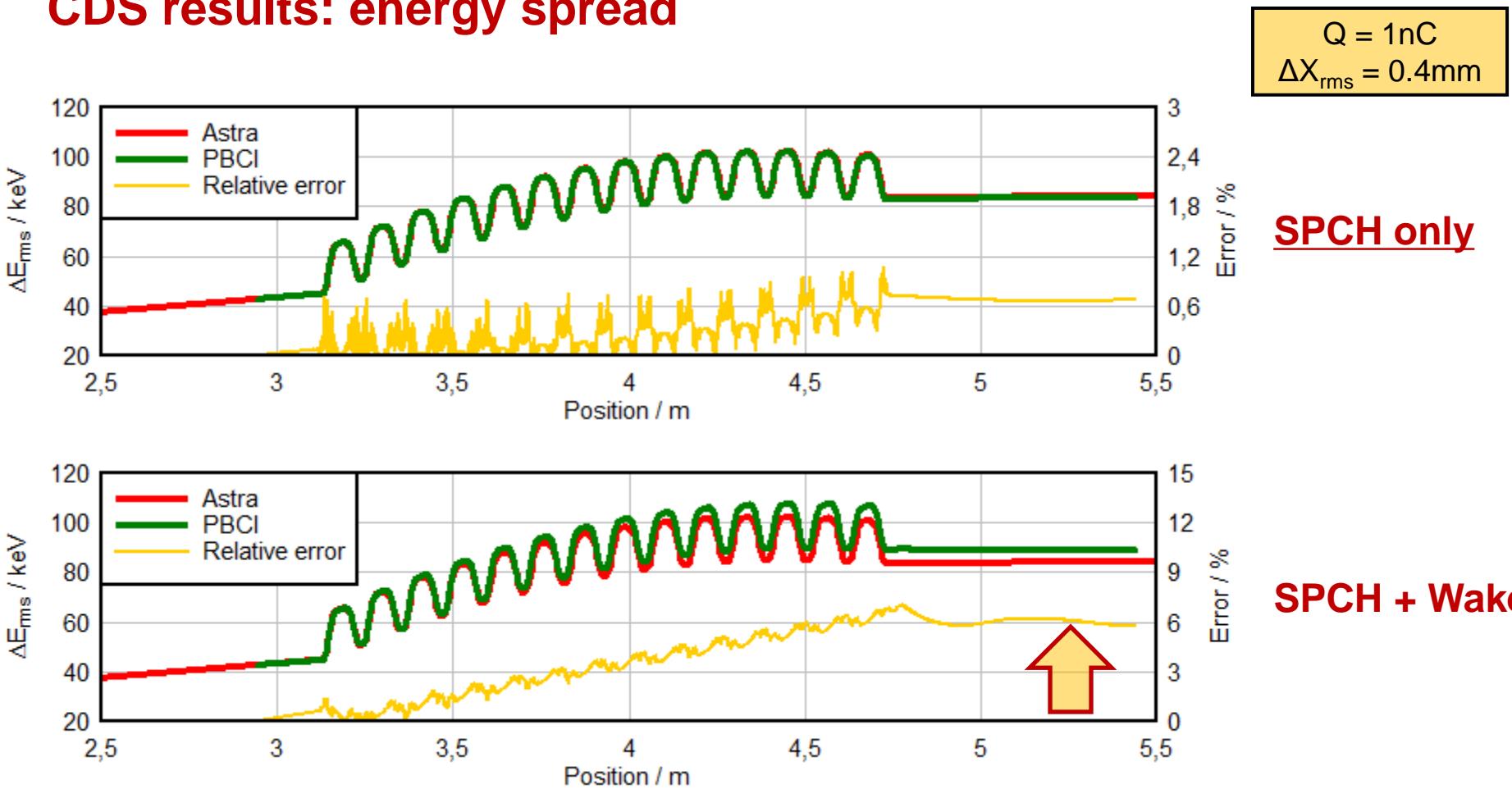


**SPCH + Wake**

# Self-consistent simulations with PBCI



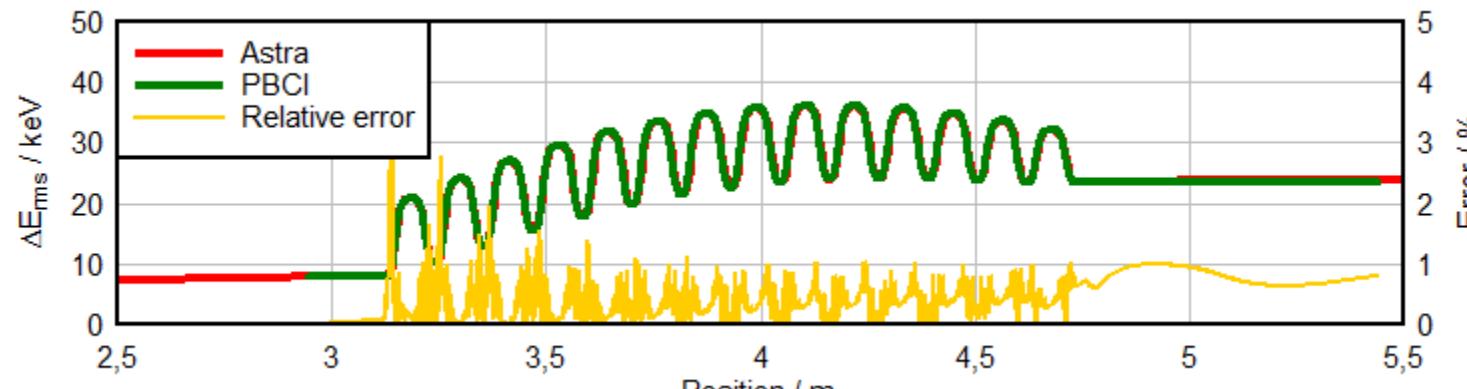
## CDS results: energy spread



# Self-consistent simulations with PBCI



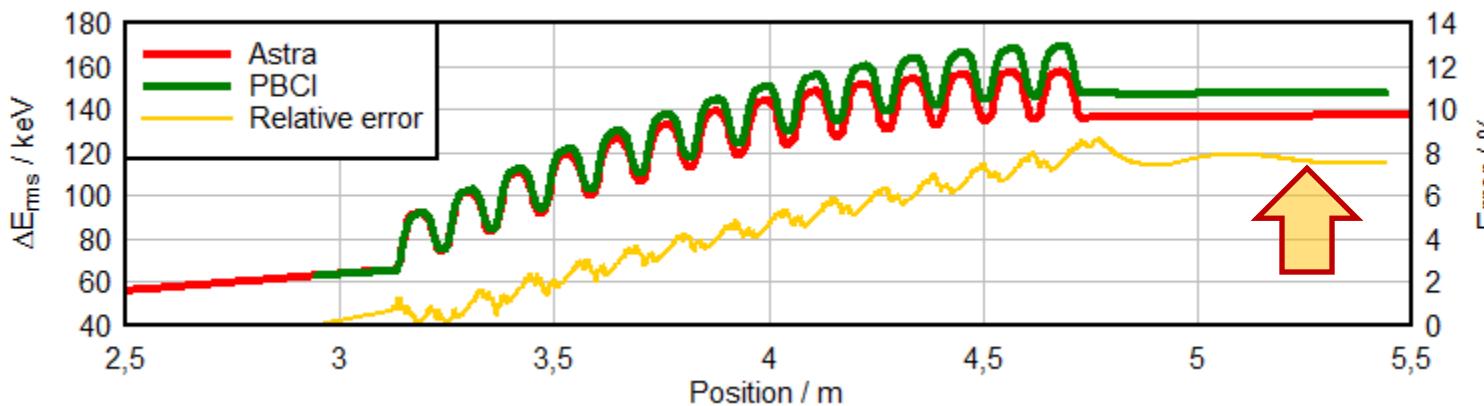
## CDS results: energy spread



$Q = 100 \text{ pC}$   
 $\Delta X_{\text{rms}} = 0.3 \text{ mm}$

SPCH + Wake

$Q = 2 \text{ nC}$   
 $\Delta X_{\text{rms}} = 0.5 \text{ mm}$

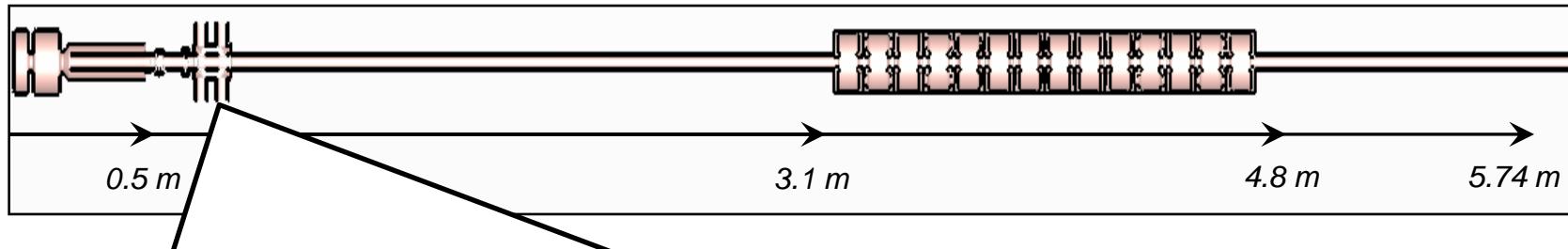


SPCH + Wake

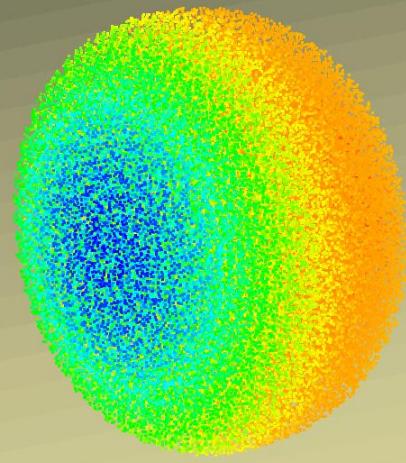
# Self-consistent simulations with PBCI



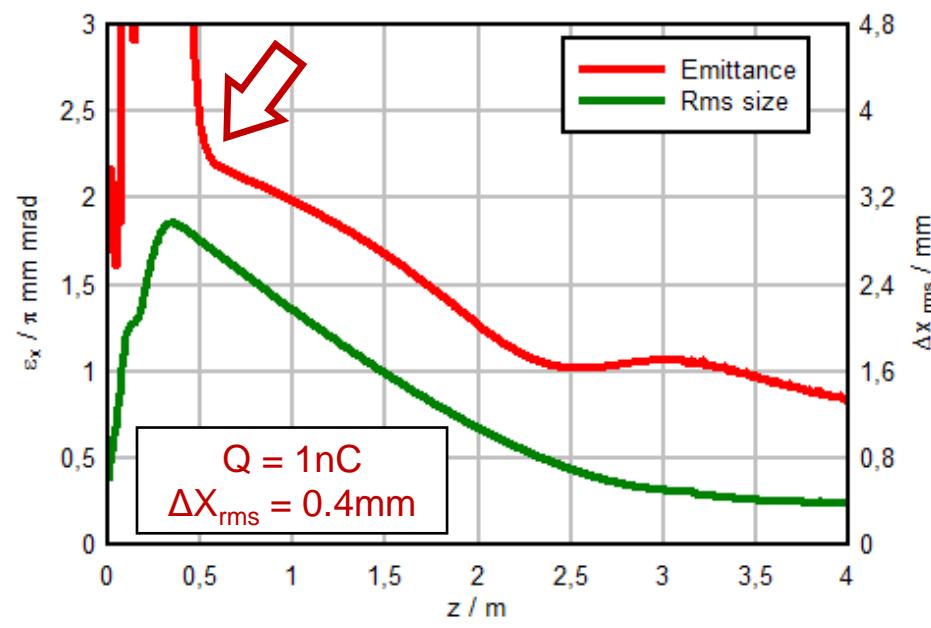
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Diagnosis / laser mirror



$v/c$   
0.99704 0.99706 0.99708 0.9971  
0.99702446 0.99711528

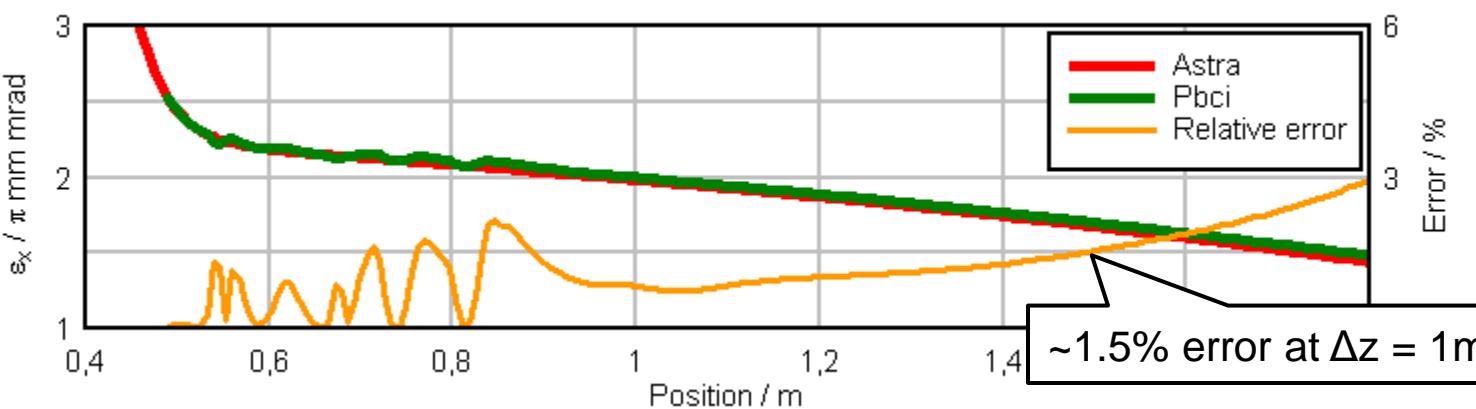
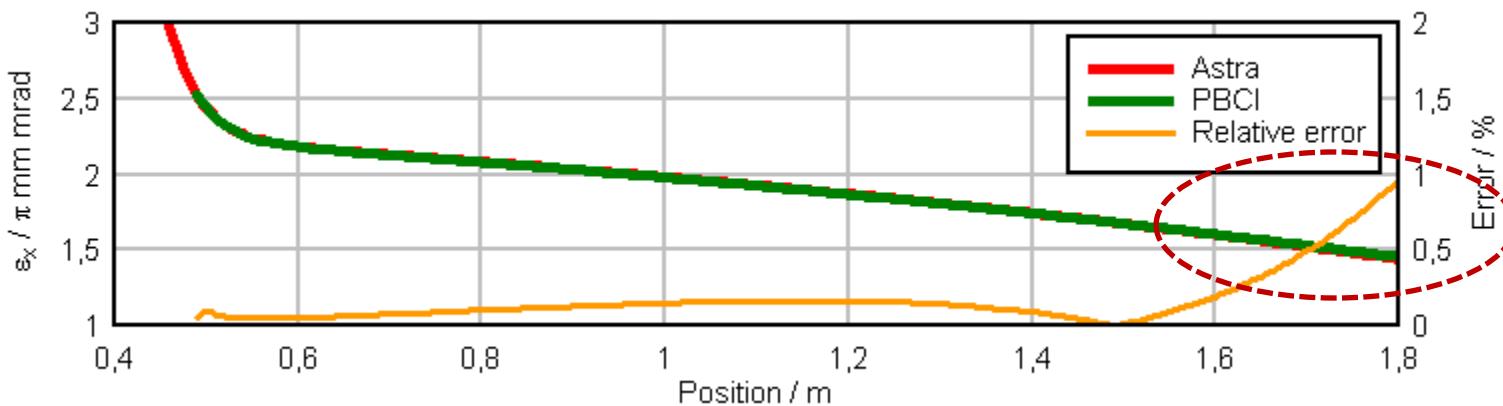


# Self-consistent simulations with PBCI



## Diagnosis cross results

$Q = 1\text{nC}$   
 $\Delta X_{\text{rms}} = 0.4\text{mm}$



# Summary and conclusions



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## Summary

- Beam dynamics simulations for photoinjector including SC and wakefields
  - Impact of geometry on soft beams?
  - Validity of rest frame transformation based computations?
- Introducing SC in PBCI
  - Moving window approach: allows for necessary grid resolution in the simulation of long structures
  - Consistent field initialization at any position within the injector by rest frame transformation + additional iterative procedure

# Summary and conclusions



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## Conclusions

- Long distance self-consistent simulations by combination of moving window / dispersions-free method and PIC
- Beam scraping at injector exit useful for (narrow range of) appropriate parameters
- Retardation field effects not important: gun and cathode region still need to be investigated
- Small impact of geometry on beam emittance: only beams on-axis considered
- Important deviations in energy spread due to wakefields (CDS) observed: should be taken into account by FEL designers
- Differences between measured and simulated emittances at PITZ most probably due to improper emission modeling

Thank You for your attention