

# TRACKING OF A PETRA III POSITRON BUNCH WITH A PRE-COMPUTED WAKE MATRIX DUE TO ELECTRON CLOUDS

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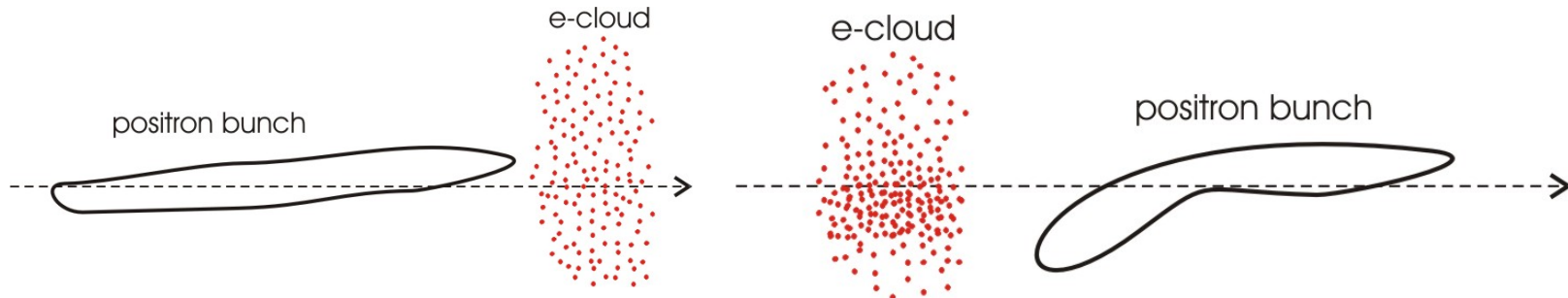
Work supported by DFG under contract number RI 814/20-2



## Overview

- Introduction, Challenges, Motivation, Idea
- Simulation of interaction beam – e-cloud
- Single bunch instability simulation
- Results for PETRA III
- Summary and conclusion

## Introduction - Head – Tail instability due to e-clouds



*Schematic of the single-bunch instability due to electron cloud after some time in the storage ring.*

## Challenges

Fact: Presently no computational resources for a full 3D strong-strong simulation of the beam- e-cloud interaction over the time of a synchrotron period!!!



Tracking with the optics matrices + the influence of the collective effects!



The transverse kick on the bunch due to the e-cloud :

Lumped, on one or more points in the lattice applying a kick on the bunch

## Motivation

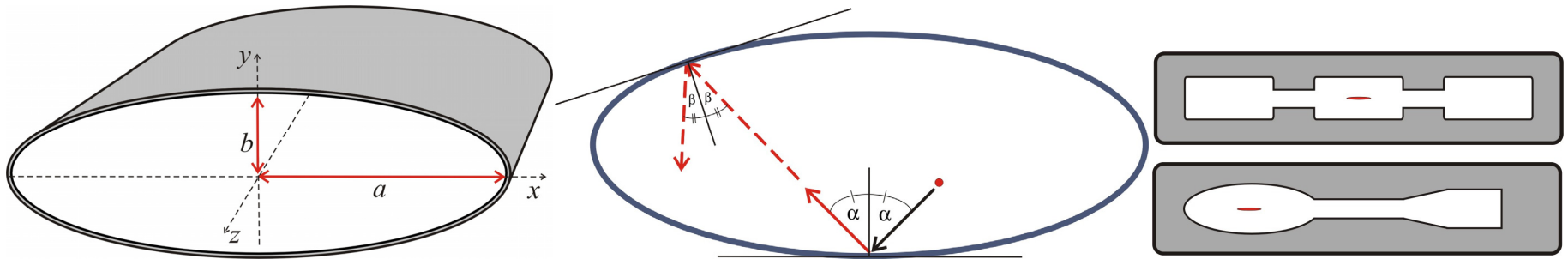
- To estimate the e-cloud effect on the beam by numerical simulation
- Simulation - fast and cheap but still to a certain extent reliable prediction of the effects

## Idea

- Pre-computed wake - idea of K. Ohmi
- Tracking with the pre-computed wake matrix

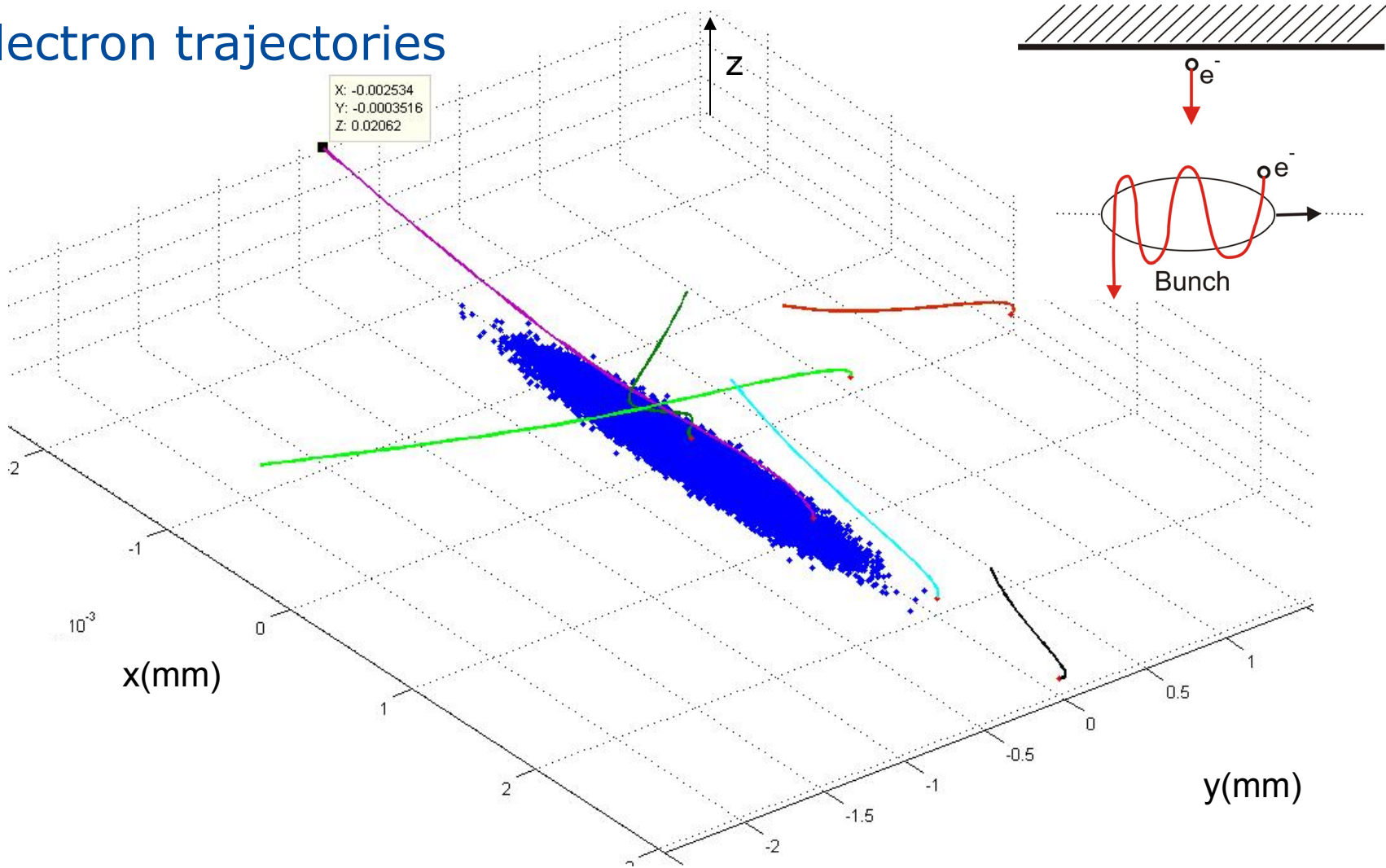


## Interaction: beam - e-cloud (MOEVE PIC Tracking)

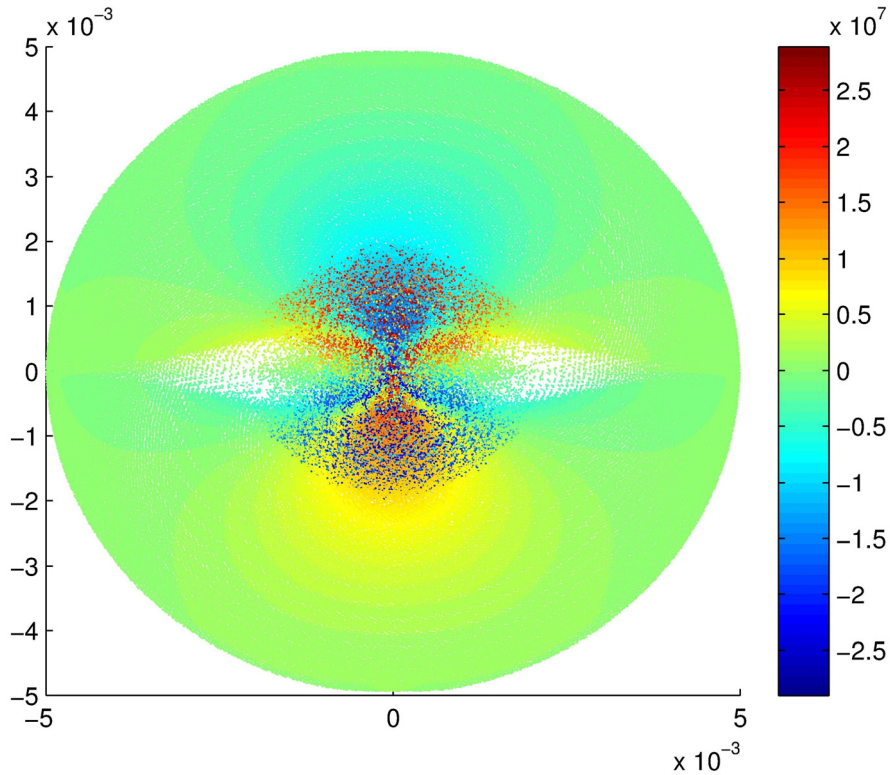


Momentum of the electrons along the bunch passage (symmetry)

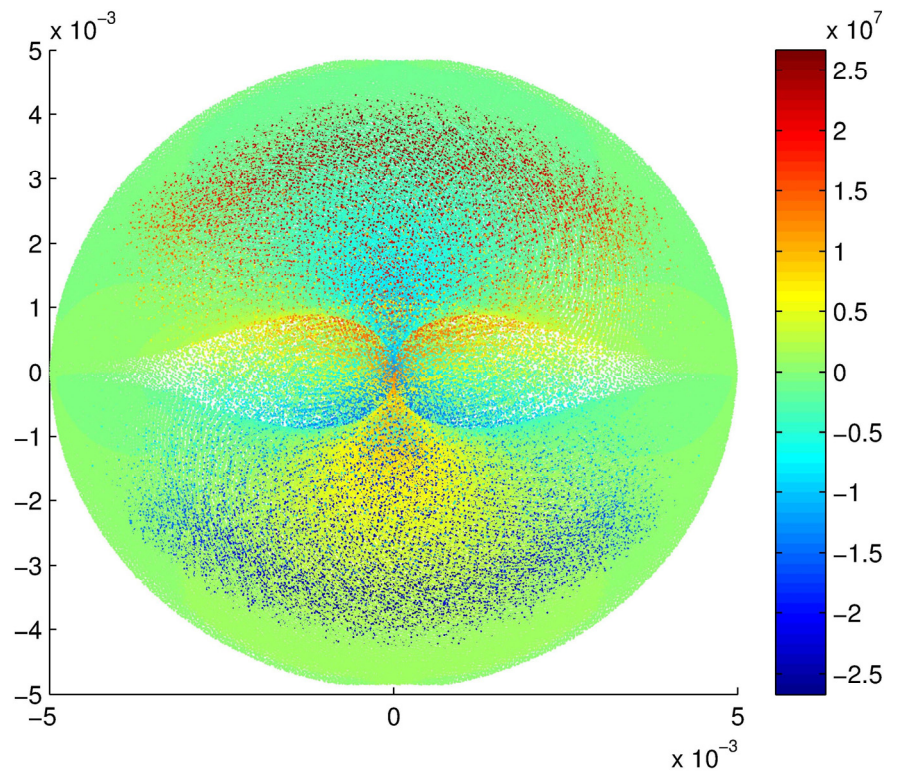
# Electron trajectories



## Electron velocity - vertical component (m/s)

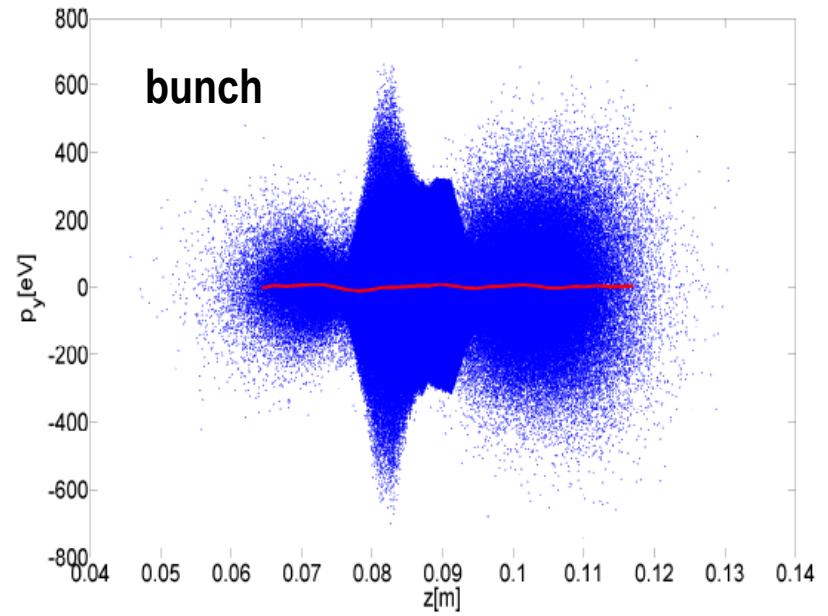
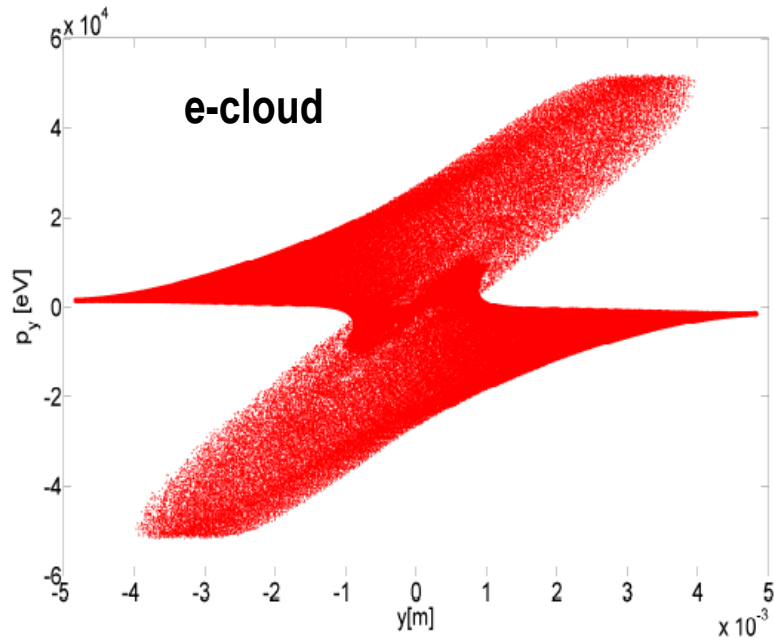


During the bunch passage



After the bunch passage

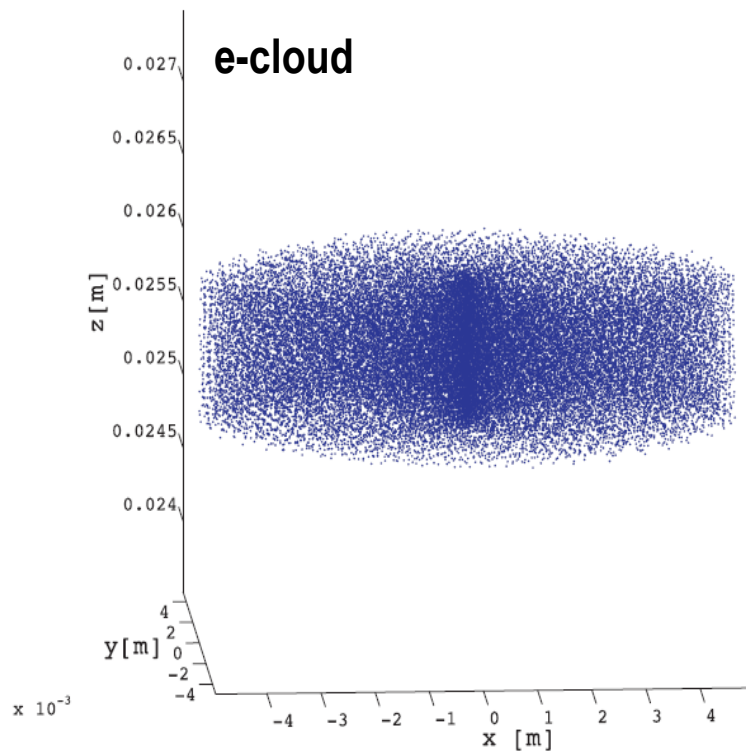
## After the interaction...



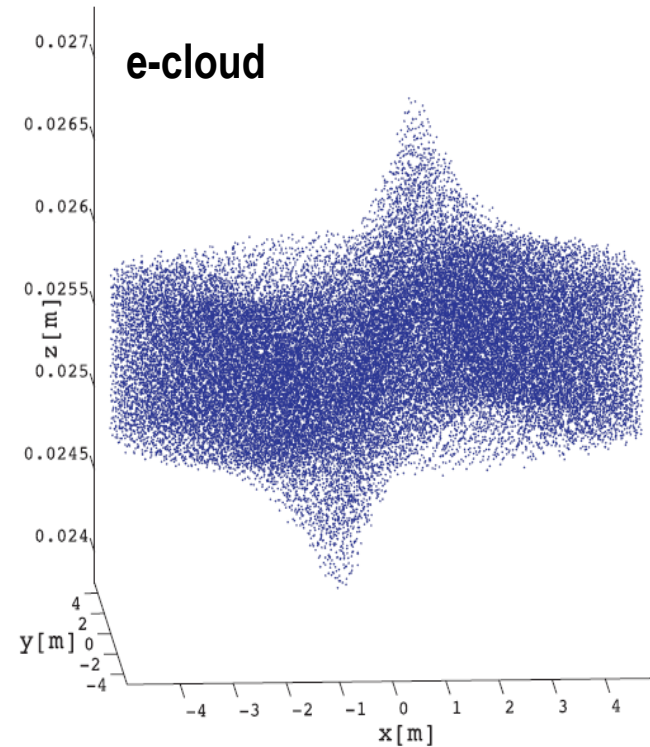
Vertical phase-space of the e-cloud after bunch passage (left), vertical momentum along the bunch length (right).



## Interaction: beam - e-cloud with and w/o dipole field



$\times 10^{-3}$



$\times 10^{-3}$

Electron distribution after the interaction with the bunch w/o dipole field (left) and with dipole field (right).

## Single bunch instability simulation

- Wake matrix by detailed beam – e-cloud interaction simulations with MOEVE PIC Tracking
- Tracking with “PEWKT” by K.Ohmi –Input: Wake Matrix with the transversal kick due to the e-cloud interaction

## Dipole kick from the e-cloud (head-tail)

A particle at a longitudinal position  $z_j$  in the tail of the bunch receives a dipole kick  $\Delta p_y(j, i)$  from the e-cloud perturbed by a preceding slice  $i$  ( $z_i > z_j$ ) with an off-set  $\Delta y_i$ .

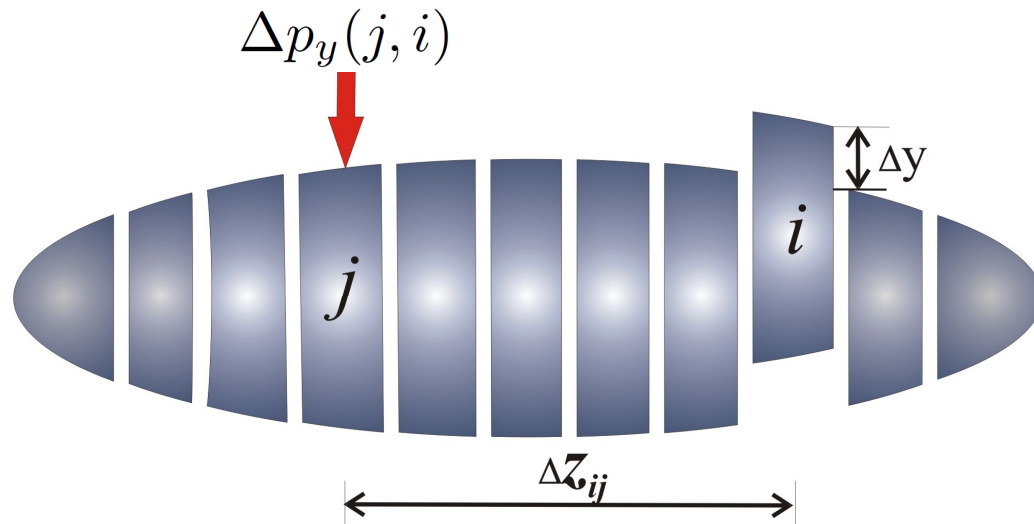
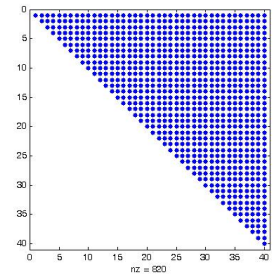


Fig.1: Slicing the 3D bunch in  $M$  longitudinal slices and introducing an offset  $\Delta y \leq \sigma_y$  in the transversal plane for each slice at the time.

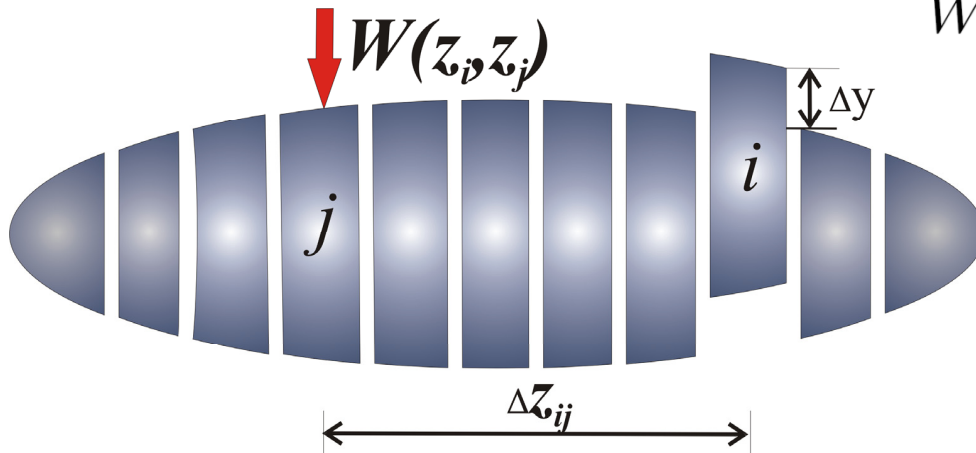


## Entries of the wake matrix $W_1$

Perform  $M$  MOEVE PIC Tracking simulations of the interaction where each of the slices  $i = 1, \dots, M$  has an off-set at a time which is responsible for inducing a dipole kick  $\Delta p_y(i, j)$  on the following  $j = i, \dots, M$  slices ( $z_i > z_j$ )

The entries of the wake matrix:

$$W_1(z_j, z_i) = \frac{\gamma \Delta p_y(j, i)}{p_b r_e \Delta y_i N_i} [1/\text{m}^2]$$



$\Delta y_i$  - The value of the offset of  $i$

$N_i$  - Particles in the off-set slice

$p_b$  - Longitudinal impulse  
of the bunch

$r_e$  - Classical radius of electron

$\gamma$  - Lorentz factor of the beam

$\Delta p_y(j, i)$  - Change of the transverse  
impulse of  $j$



## Tracking of a single bunch with a wake matrix

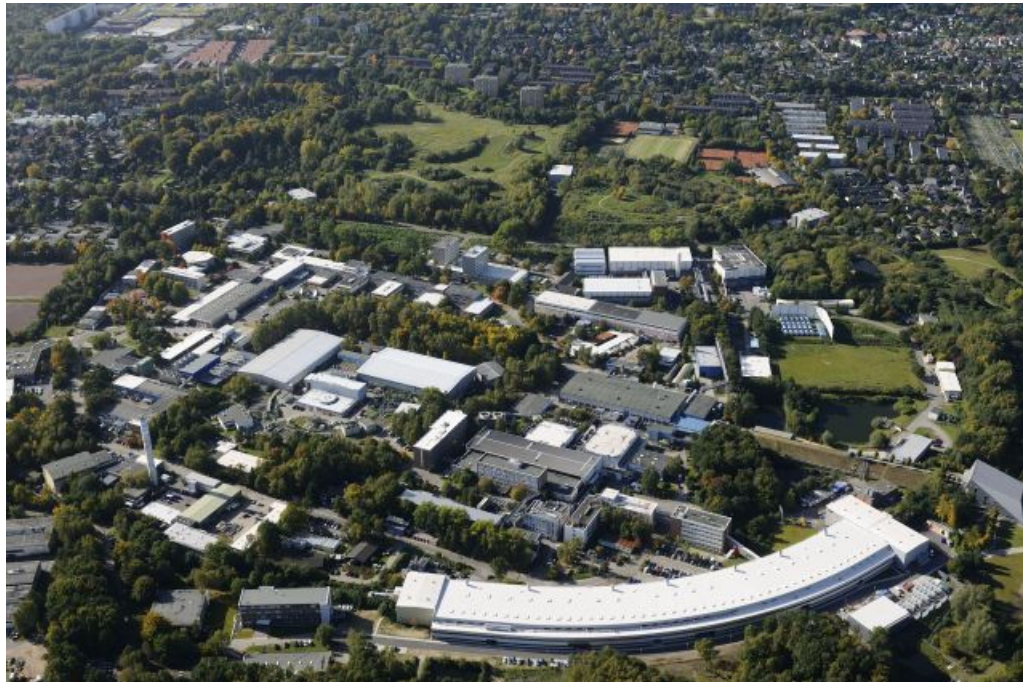
- With the tracking program PEWKT[1] of K. Ohmi we track the bunch through the linear optics of the storage ring while at each turn the  $M$  slices of the bunch receive a kick according to the pre-computed wake matrix.

### Main Assumptions:

- - The kick on the slice  $j$  is a superposition of the kicks induced by all the slices  $i = 1, \dots, j - 1$  ahead of the slice  $j$ .
- - The transverse kick scales linearly with the off-set  $\Delta y_i$  until  $\Delta y \leq \sigma_y$

[1] K. Ohmi. *Particle-in-cell simulation of beam-electron cloud interactions.*  
*In PAC, 2001, volume 3, pages 1895–1897, 2001.*

## Results for PETRA III



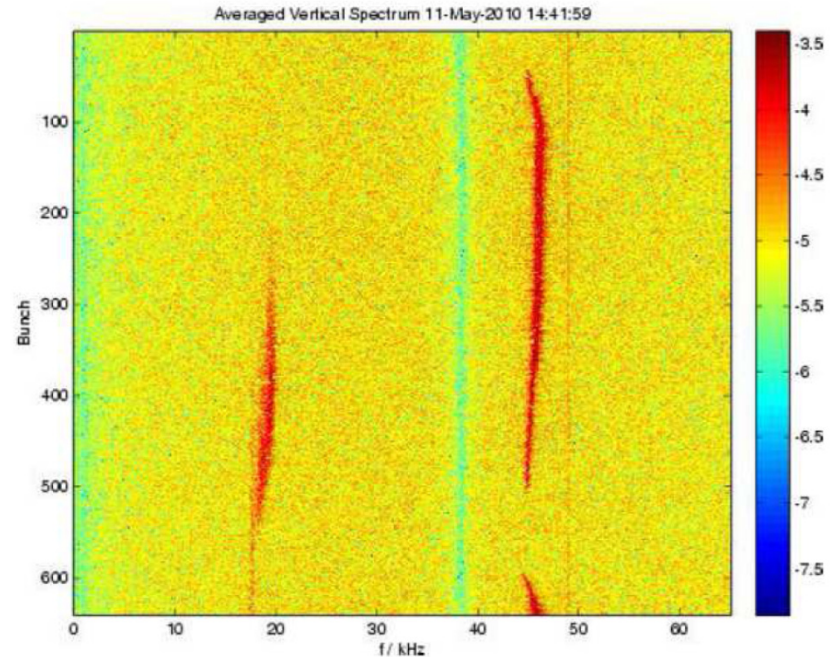
Aerial view of October 6, 2008

Photo: [http://petra3-project.desy.de/buildings/photos/october\\_2008/aerial\\_views/index\\_eng.html](http://petra3-project.desy.de/buildings/photos/october_2008/aerial_views/index_eng.html)

## PETRA III - synchrotron machine running with positrons in a top up operation with $I=100\text{mA}$

Parameter	Symbol	PETRA III
Circumference	$L$	2304 m
Beam energy	$E_b$	6 GeV
Length (rms)	$\sigma_z$	12 mm
Emittance	$\epsilon_x$	1nm
	$\epsilon_y$	0.01nm
Synchrotron tune	$\nu_s$	0.049
Betatron tune	$\nu_{x(y)}$	36.13/30.29
Radiation Damping	horizontal	19.75 ms
	vertical	19.75 ms
	longitudinal	9.84 ms
Momentum compaction factor	$\alpha$	$1.2010^{-4}$
RF Frequency	RF	499.564 MHz

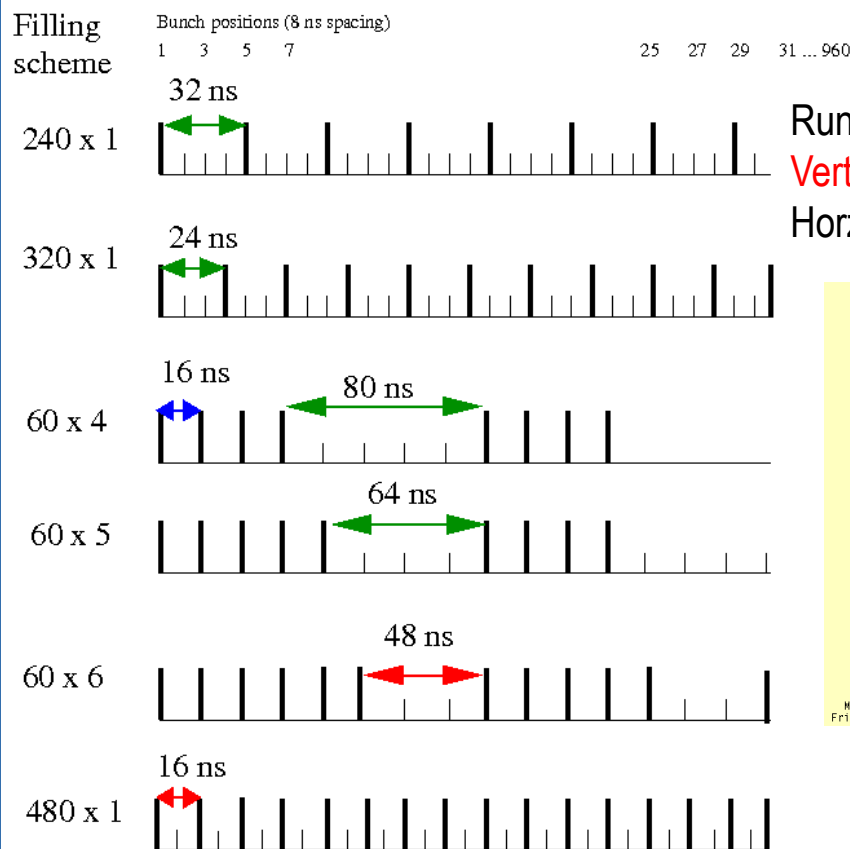
Table 1: PETRA III machine parameters. Designed for 960 and 40 bunches with equidistant spacing of 8 and 192 ns.



Vertical tune spectra of each of the 640 bunches with 8ns spacing, measured on May 11, 2010[1]. The total beam current was 62mA.

Courtesy of R.Wanzenberg.

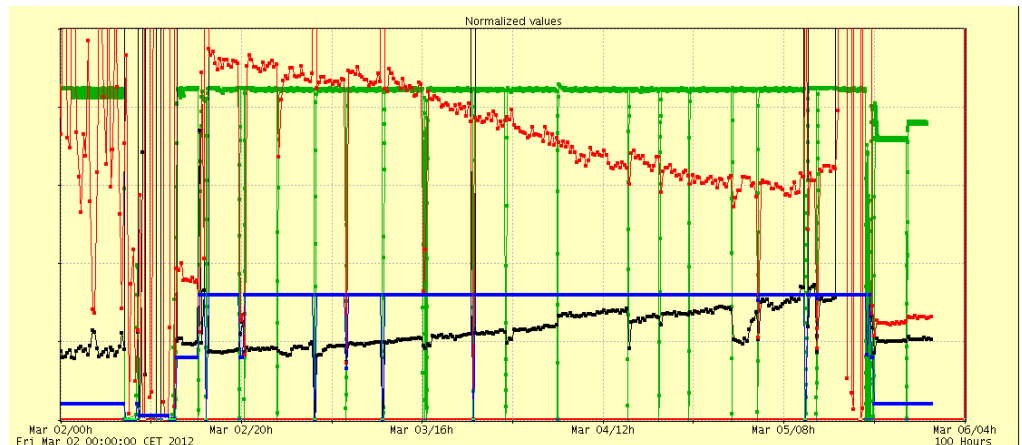
## Different filling schemes of the machine:



Courtesy of R.Wanzenberg.

Run: 480 x 1 Beam Scrubbing, March 3 / 4, 2012

Vert. Emittance  $\sim 140$  pm rad ( for 20 h), then dropping to 97 pm rad  
Horz. Emittance Starting at 1.0 nm rad Increasing to 1.8 nm rad



Green: total current (100 mA)

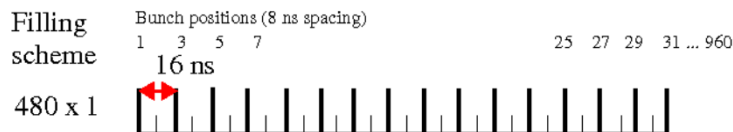
Red: vertical emittance (scale 0 ... 150 pm rad)

Blue: Number of bunches (480)

Black: horizontal emittance (scale 0 ... 6 nm rad)



## Simulation of a single bunch stability for the bunch of the 480 x 1 run:



Starting vertical emittance:  $\varepsilon_y = 20$  pm rad

e-cloud:

- uniform distribution,
- density:  $\rho_e = 1 \cdot 10^{11}, 5 \cdot 10^{11}, 2 \cdot 10^{12}, 5 \cdot 10^{12}$  [ $N_e/m^3$ ]
- Beam pipe radius: 5mm length: 10mm
- Represented by unit charges

positron bunch:

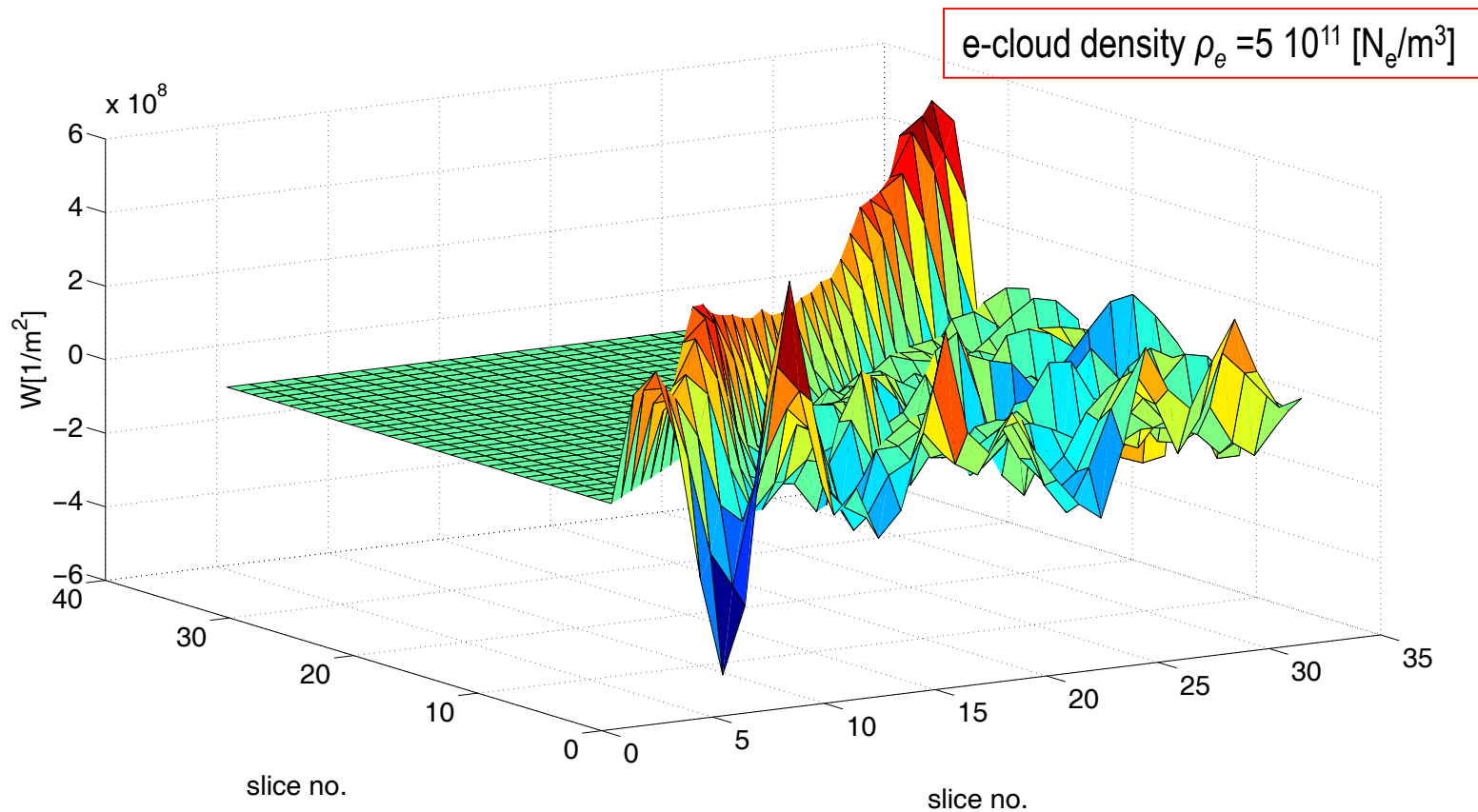
- represented by  $10^6$  macro-particles;
- Gaussian distribution;
- longitudinally spreads from  $-3\sigma_z$  to  $+3\sigma_z$
- virtually sliced in  $M = 40$  slices\*

Beam Current	$I$	100 mA
Beam Charge	$Q$	769 nC
Bunch Charge	$Q_b$	1.6 nC
Positrons per Bunch	$N_b$	$10^{10}$
Mean $\beta$ function	$\beta_{x/y}$	15 m
Transverse beam size (rms)	$\sigma_x$	122.47 $\mu\text{m}$
	$\sigma_y$	17.321 $\mu\text{m}$

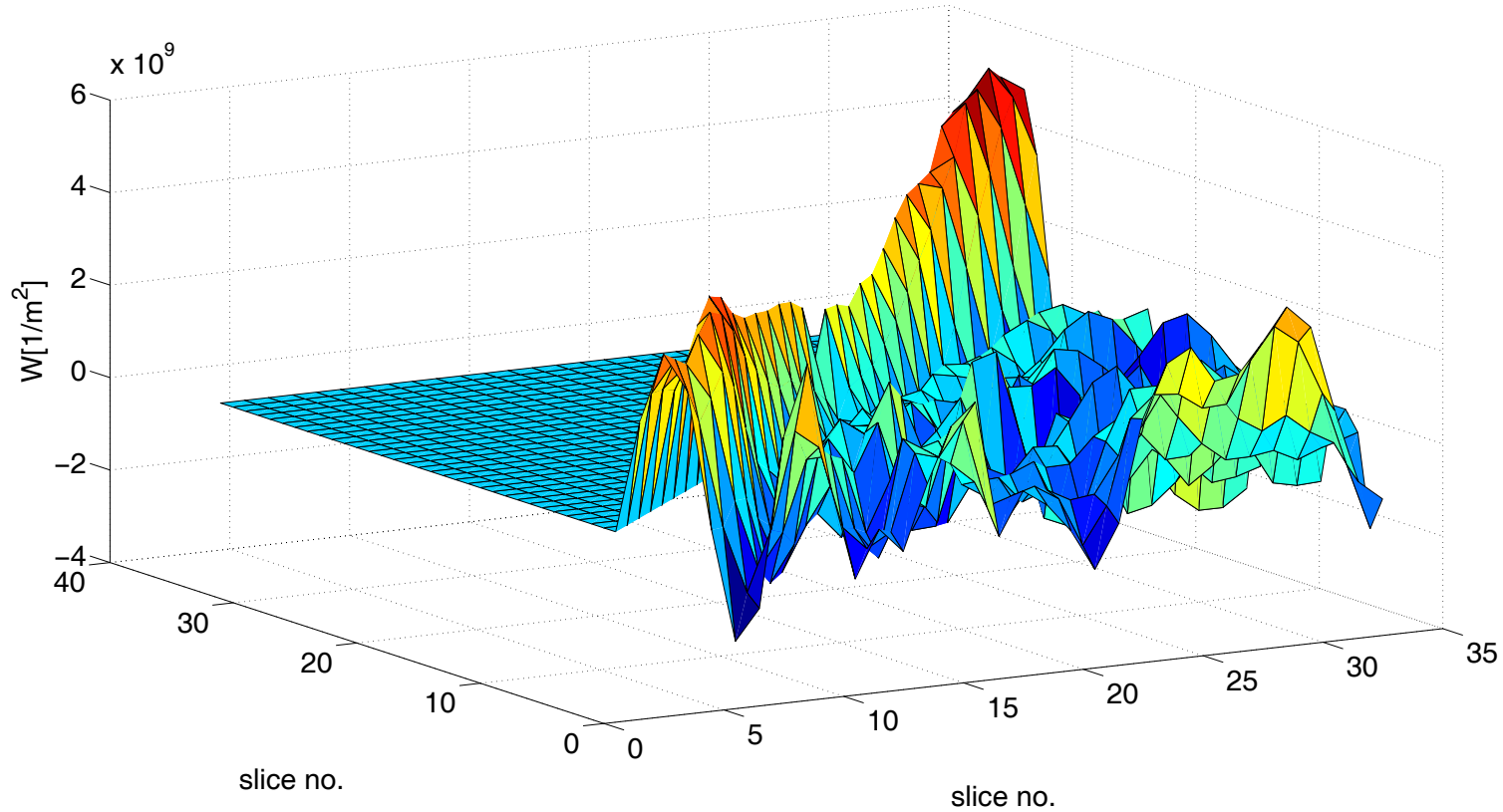
The time step used for the interaction simulation is 1 ps.

\* The thickness of the slices in the lab frame corresponds to the time which the electrons on the beam axis need to change their vertical position for one  $\sigma_y$ .

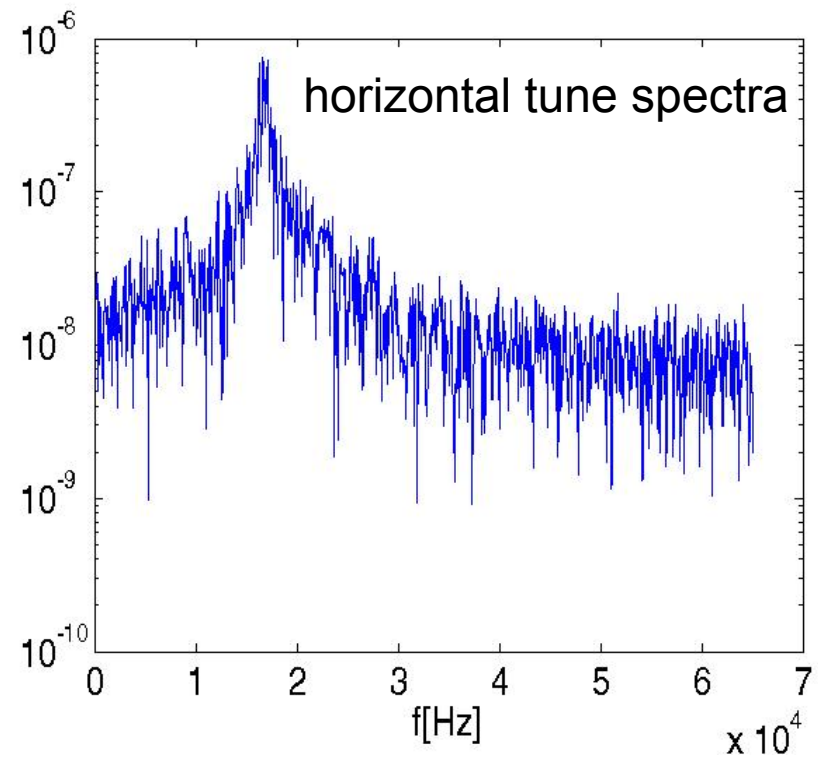
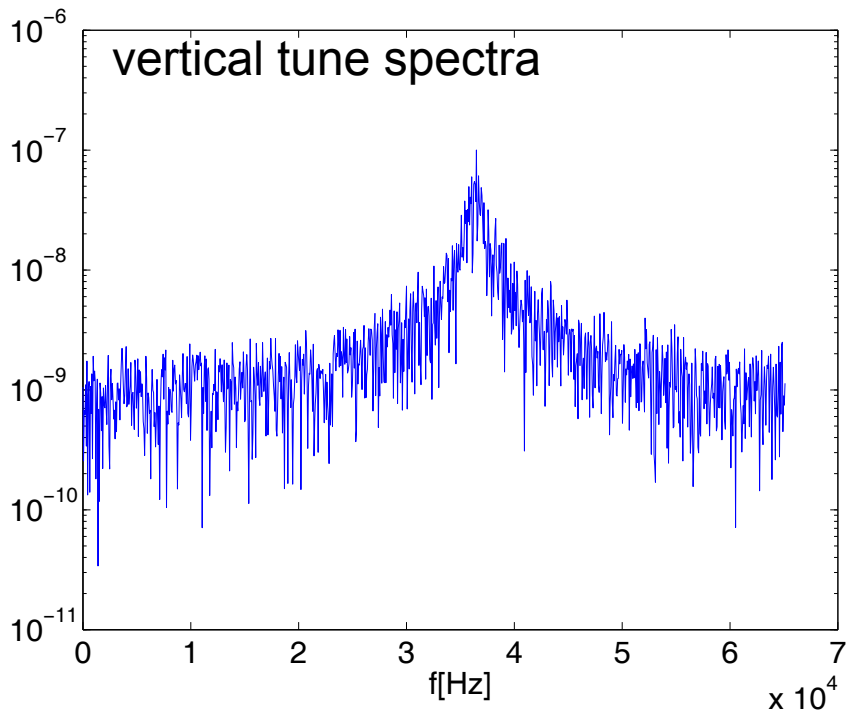
## Wake matrix computed by MOEVE-PIC TRACK



e-cloud density  $\rho^e = 5 \cdot 10^{12} \text{ [N}_e/\text{m}^3]$

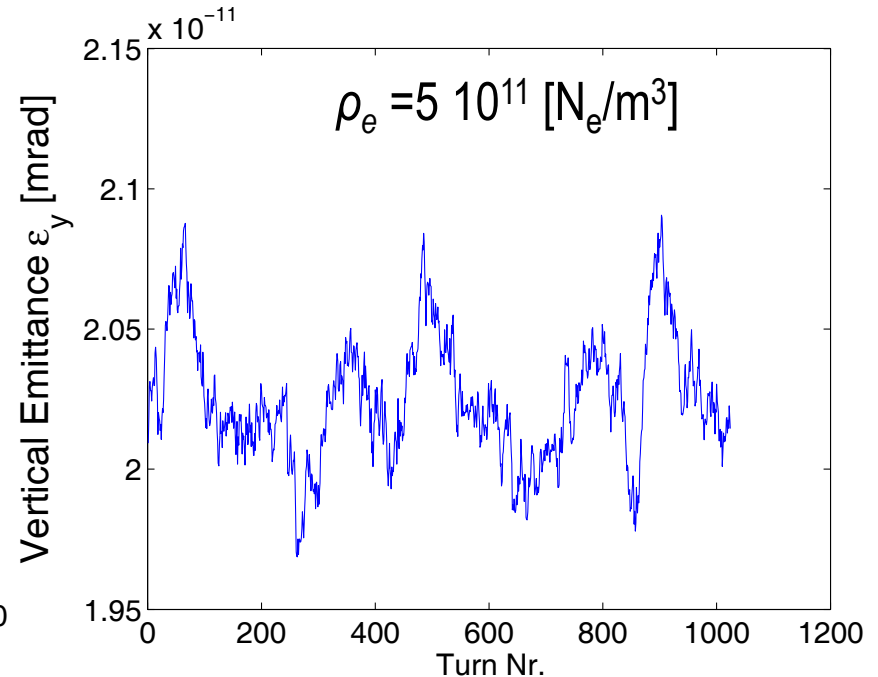
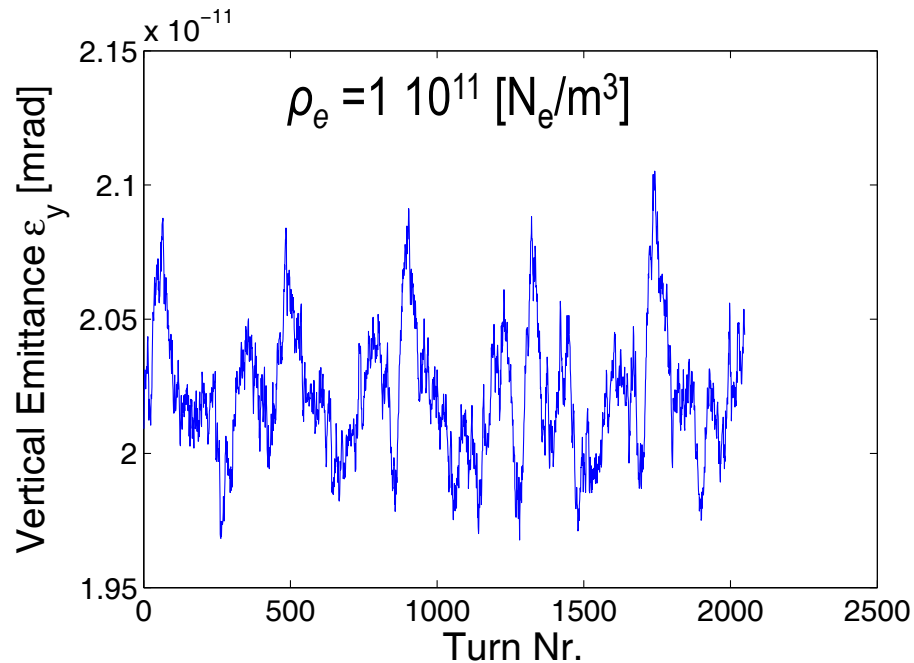


## Tune spectra for e-cloud density $\rho_e = 5 \cdot 10^{11} \text{ [N}_e/\text{m}^3]$





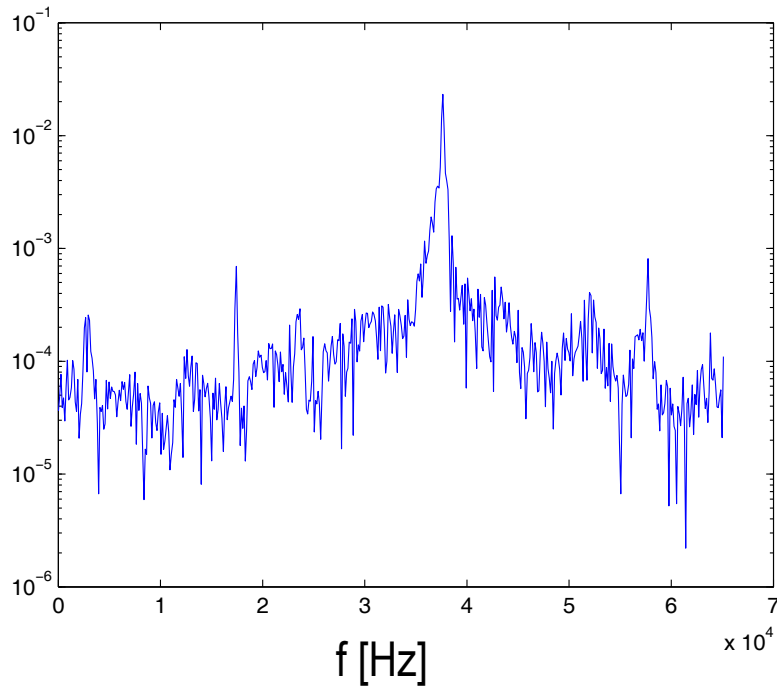
Vertical emittances... e-cloud density < threshold:  $\rho_e = 1.4 \cdot 10^{12} \text{ [N}_e/\text{m}^3]$ \*



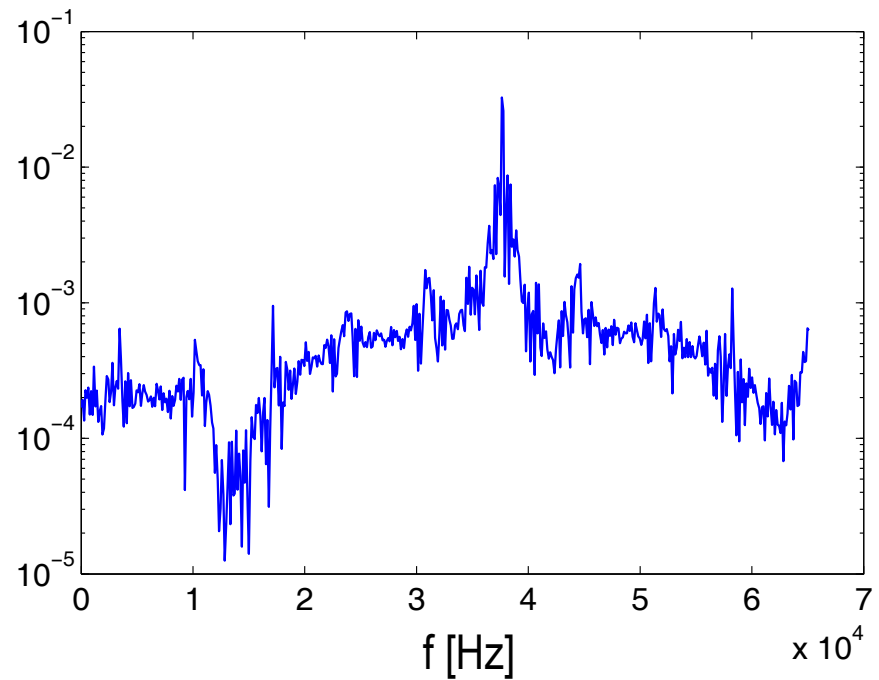
\*computed by R.Wanzenberg according to the expression from: K. Ohmi: Electron Cloud Effect in Damping Rings of Linear Colliders 31st ICFA Advanced Beam Dynamics Workshop on Electron-Cloud Effects "E-CLOUD'04"

Vertical tune spectra    e-cloud density > threshold:  $\rho_e = 1.4 \cdot 10^{12} \text{ [N}_e/\text{m}^3]$

$$\rho_e = 2 \cdot 10^{12} \text{ [N}_e/\text{m}^3]$$

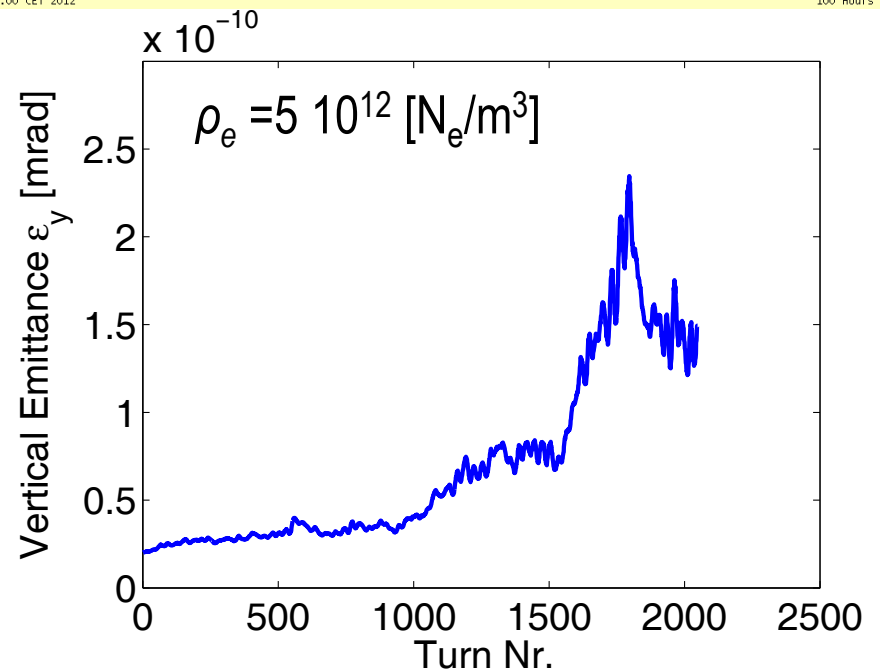
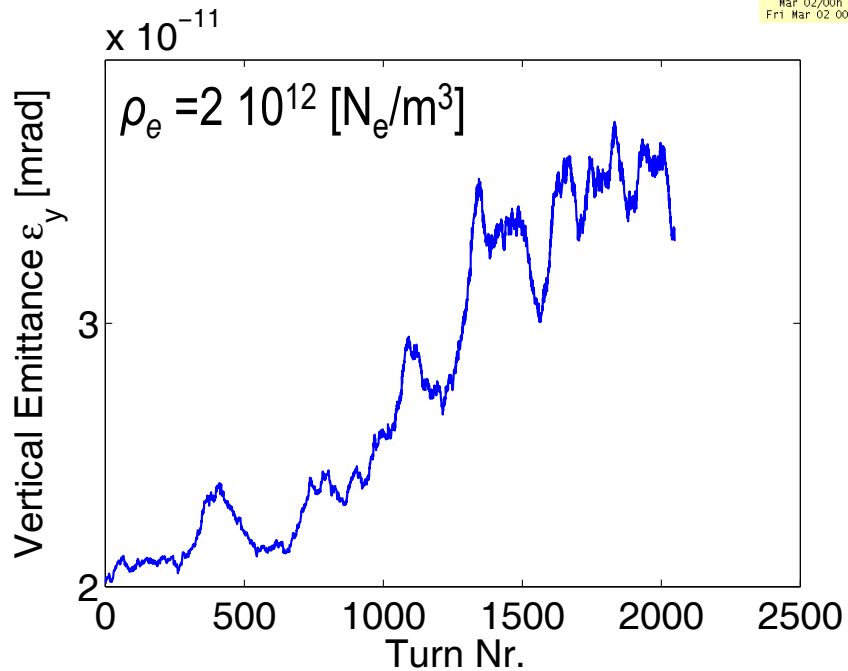
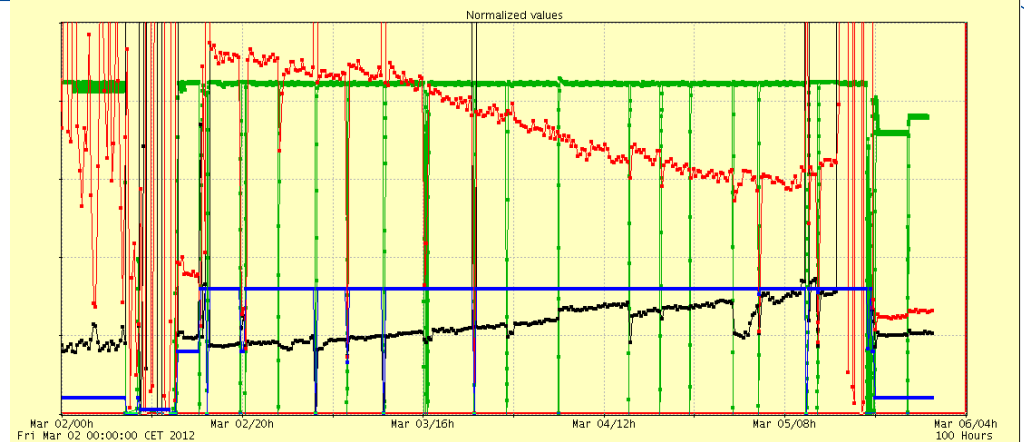


$$\rho_e = 5 \cdot 10^{12} \text{ [N}_e/\text{m}^3]$$



## Vertical emittances...

Run: 480 x 1 Beam Scrubbing, March 3 / 4, 2012  
**Vert. Emittance** ~140 pm rad ( for 20 h),  
 than dropping to 97 pm rad



## Summary and conclusion

- 3D computation of single-bunch induced electron-cloud wake fields
- Simulation of single bunch instabilities due to the interaction with the electron clouds by tracking with a 2D Wake-Function.
- Investigation of the stability for different beam and cloud parameters
- The tracking simulation using the pre-computed wake matrix for the given bunch was able to predict the instability.
- As in the measurements the simulation for e-cloud densities above threshold show also sidebands in the betatron tune spectra.
- The simulated emittance growth seems realistic, even more the emittance from the simulation with  $\rho_e = 5 \cdot 10^{12} \text{ N}^e/\text{m}^3$  seems to match the measured long time emittance ( $\sim 140 \text{ pm}$ ) from the run with 480 bunches.
- Although further validation of the procedure is needed it seems that such a simulation may also be used to numerically estimate the threshold e-cloud density.



## Acknowledgment

We would like to thank K. Ohmi for letting us use his program and R. Wanzenberg for sharing his knowledge with us regarding e-cloud effects in the PETRAIII ring.