

Beam optics analysis of large-acceptance superconducting in-flight separator BigRIPS at RIKEN RI Beam Factory (RIBF)

- Magnetic spectrometer used for the production of radioactive isotope (RI) beams based on in-flight scheme
- Objective: study of exotic nuclei far from the stability using a variety of RI beams

Presented by **Hiroshi Suzuki**

RIKEN Nishina Center

Toshiyuki Kubo, Hiroyuki Takeda,
Kensuke Kusaka, Naohito Inabe,
Naoki Fukuda, & Daisuke Kameda

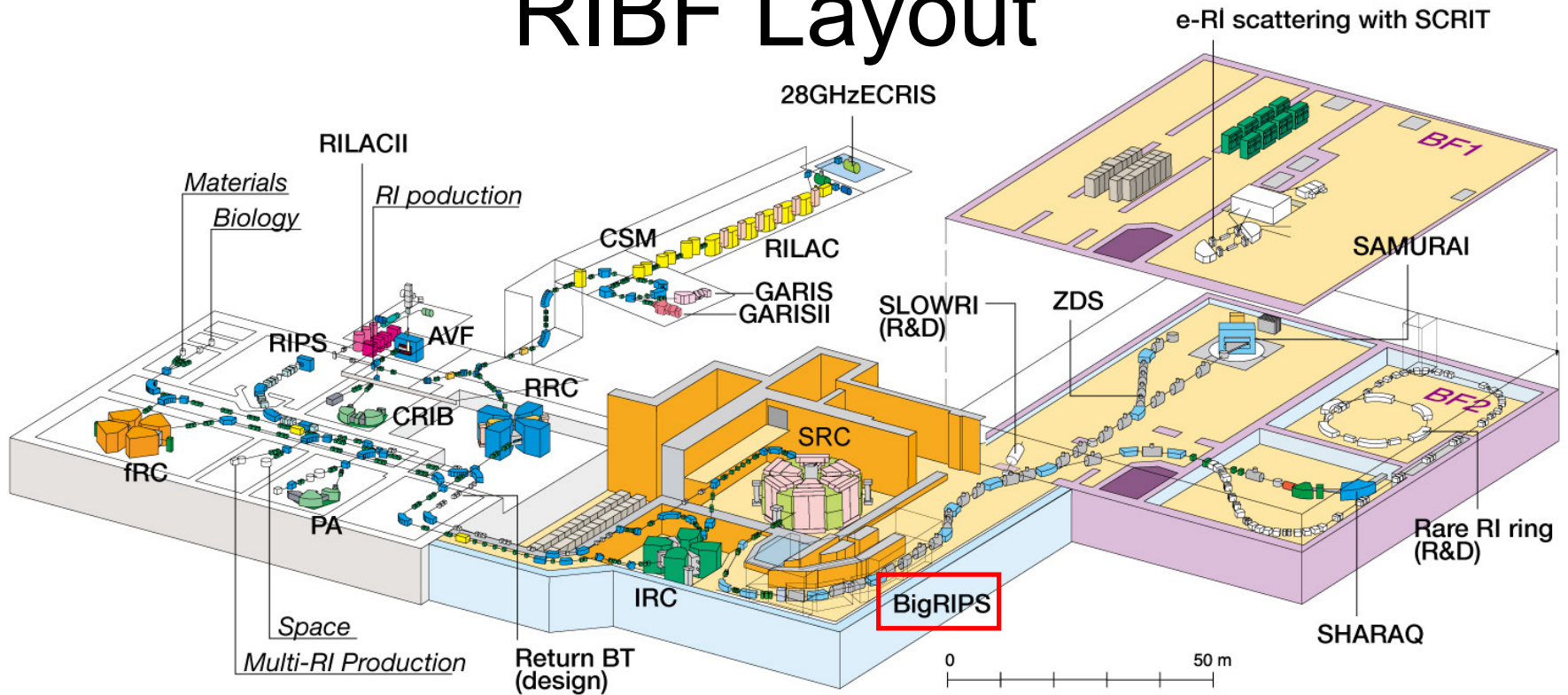


Outline of My Talk

- Introduction
 - Overview of BigRIPS separator, emphasizing its ion-optics issues
- Optics Calculation
 - Optics Calculation for BigRIPS, which is a large acceptance and large-aperture ion-optical system
 - Field map measurements
 - The procedure to deduce $b_{n,0}(z)$ from magnetic field vector
 - The procedure to fit the Enge function
 - Optics calculation using with COSY INFINITY
- Comparison with Measurement
 - Matrix terms
 - A/Q resolution from New-isotope Search Exp.
- Summary

Introduction

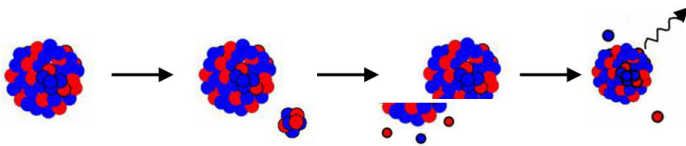
RIBF Layout



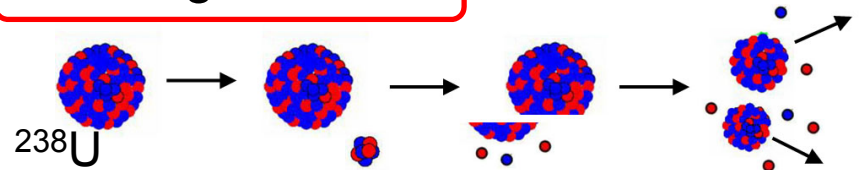
New-generation in-flight RI beam facility, Energy : 345 MeV/u up to ^{238}U ions

Reaction mechanism of RI production

- Projectile fragmentation



- In-flight fission



Very powerful for neutron-rich RIs in mid-heavy region

Features of BigRIPS Separator

- 1) **Large acceptances**
 - Comparable with angular / momentum spreads of in-flight fission at RIBF energy (± 50 mrad, $\pm 5\%$)
- 2) **Superconducting quads** with a **large aperture**
 - Pole tip radius: 17 cm
 - Max. pole tip field: 2.4 T
- 3) **Two-stage** separator scheme
 - 1st stage : 2 bend, $p/\Delta p = 1260$
 - 2nd stage : 4 bend, mirror sym. @ F5, $p/\Delta p = 3420$
 - Better resolution at 2nd stage for particle ID

Parameters:

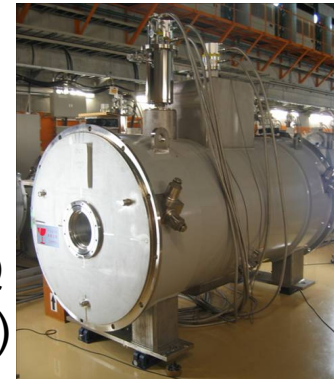
$$\Delta a = \pm 40 \text{ mrad}$$

$$\Delta b = \pm 50 \text{ mrad}$$

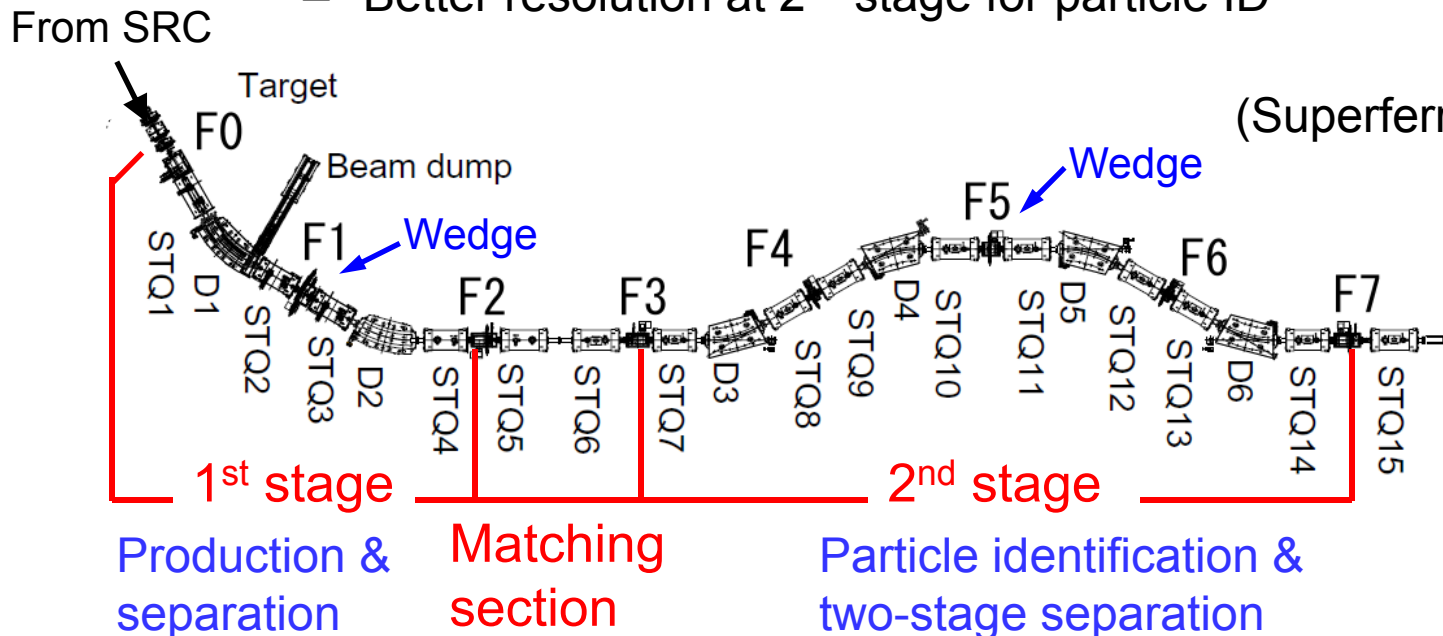
$$\Delta p/p = \pm 3 \%$$

$$B_p = 9 \text{ Tm}$$

$$L \sim 77 \text{ m}$$



STQ
(Superferric Q)



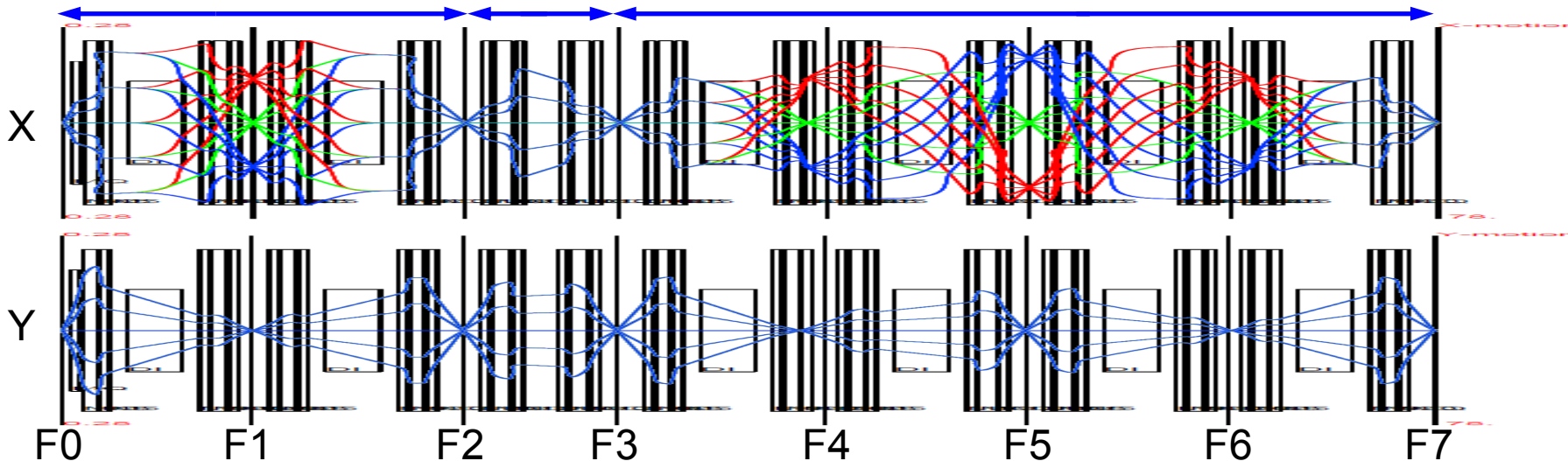
STQ1-14:
Superconducting
quad. triplets

D1-6: Room
temp. dipoles (30
deg)

F1-F7: focuses

Ion Optics of BigRIPS

1st stage Matching section 2nd stage (Mirror symmetry at F5)



→ F0F1

$$\begin{aligned} (x|x) &= -1.7, (x|a) = 0, \\ (y|y) &= -5.0, (y|b) = 0, \\ (x|\delta) &= -21.4 \text{ mm}/\%, (a|\delta) = 0 \end{aligned}$$

→ F3F4

$$\begin{aligned} (x|x) &= -1.40, (x|a) = -0.791, \\ (y|y) &= -3.45, (y|b) = -0.272, \\ (x|\delta) &= -22.1 \text{ mm}/\%, (a|\delta) = 0 \end{aligned}$$

$$\begin{aligned} P/\Delta P &= \\ &1260 \text{ (1st stage)} \\ &3420 \text{ (2nd stage)} \end{aligned}$$

→ F0F2

$$\begin{aligned} (x|x) &= 2.0, (x|a) = 0, \\ (y|y) &= 1.6, (y|b) = 0, \\ (x|\delta) &= 0 \text{ mm}/\%, (a|\delta) = 0 \end{aligned}$$

→ F3F5

$$\begin{aligned} (x|x) &= 0.92, (x|a) = 0, \\ (y|y) &= 1.06, (y|b) = 0, \\ (x|\delta) &= 31.7 \text{ mm}/\%, (a|\delta) = 0 \end{aligned}$$

Mirror symmetry
of F3-F5

→ F2F3

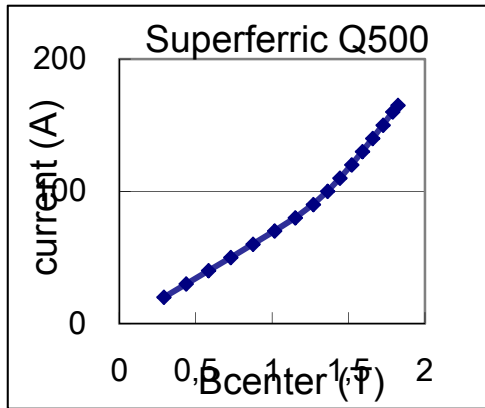
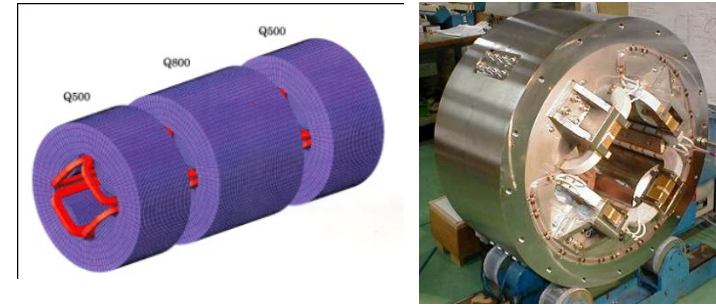
$$\begin{aligned} (x|x) &= -1.08, (y|y) = -1.18, \\ (x|a) &= (y|b) = (a|x) = (b|y) = 0 \end{aligned}$$

← F7F6

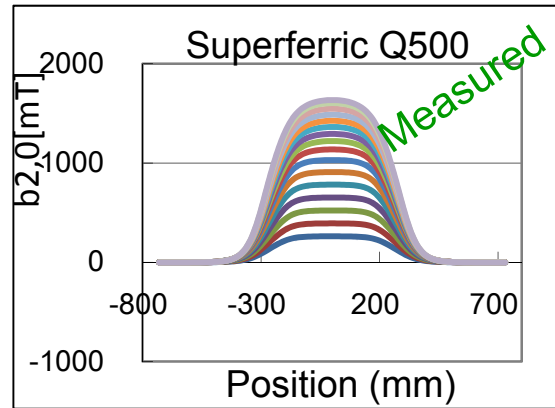
← F7F5

Large-Aperture, Short-Length Superconducting Quadrupole

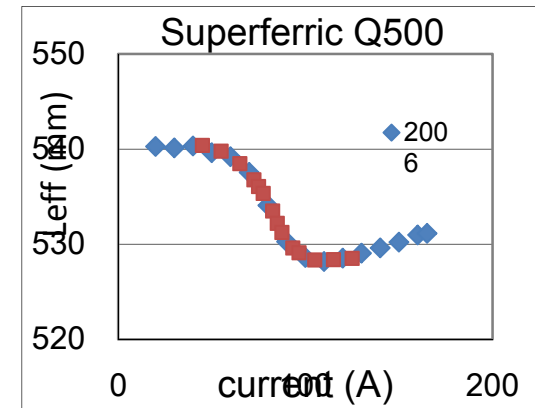
- Superferric (STQ2-26) : **iron dominated**



Excitation function



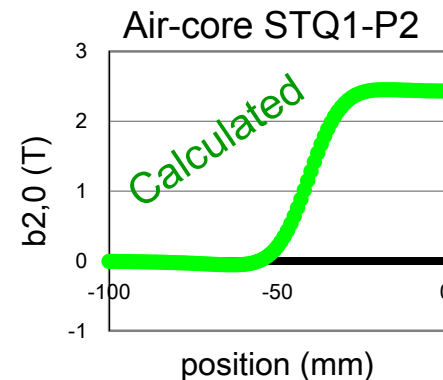
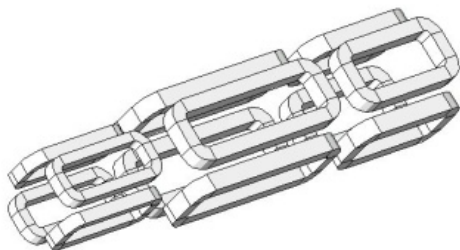
Field distribution



Effective length

Large fringe field regions and saturation effects!

- Air-core (STQ1)



Field distribution

Calculation for Optical Setting

Our goal: precise ion-optical setting, in which tuning is not needed.

Quadrupoles have large fringe field region and strong saturation effects. The **field distribution varies very much** with the magnet excitation.

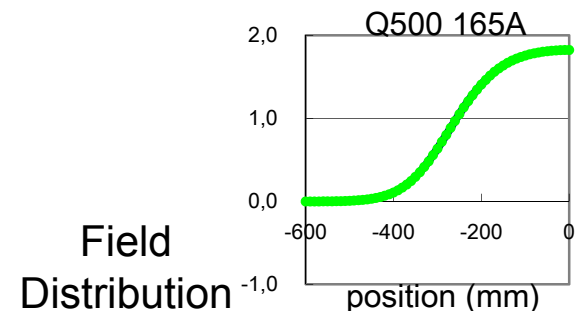


The effect of the varying distribution should be included in the simulation.

Procedure of the field & optics analysis

- Measure **detailed field-map** as a function of magnet current.
- Deduce $b_{n,0}(z,I)$ from the magnetic field map.
- Fit $b_{n,0}$ distribution by **Enge function**. Its **Enge coefficients** are the function of magnet current.
- Make detailed ion-optical calculation using the deduced Enge coefficients and **COSY INFINITY** code.
- Search **magnet current setting**, which satisfies the ion optical setting.

$$F(z) = \frac{1}{1 + \exp \left[a_1 + a_2 (z/D) + \dots + a_6 (z/D)^5 \right]}$$



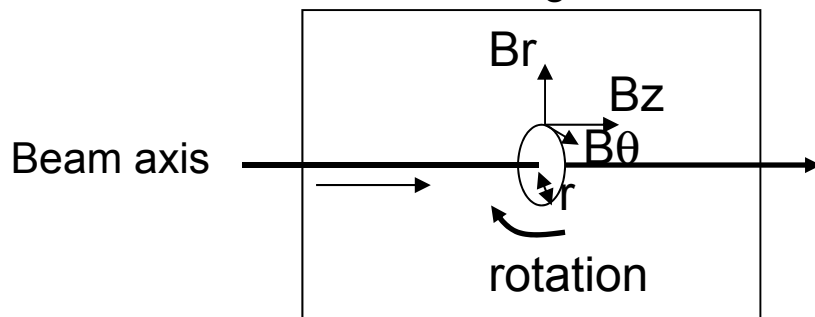
Optics Calculation

Field Map Measurement

- Quadrupole & Sextupole

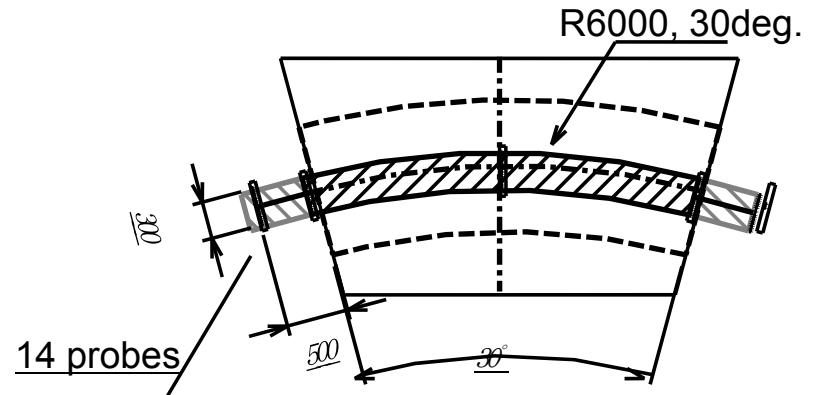
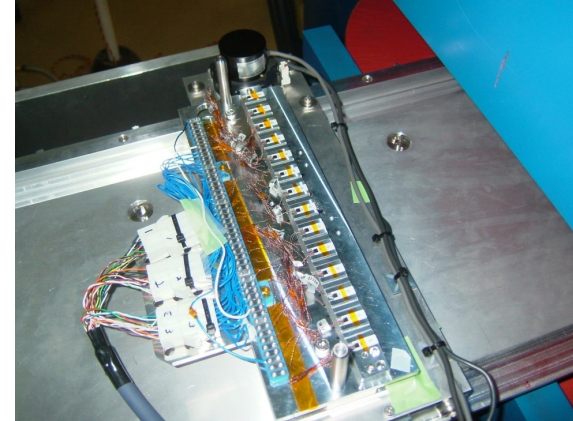


STQ magnet



Radius : $r = 81,94,107$ mm
 Step :
 $\Delta z = 10$ mm
 $\Delta\theta = 9$ degree (for quadrupole)
 3 degree (for sextupole)

- Dipole

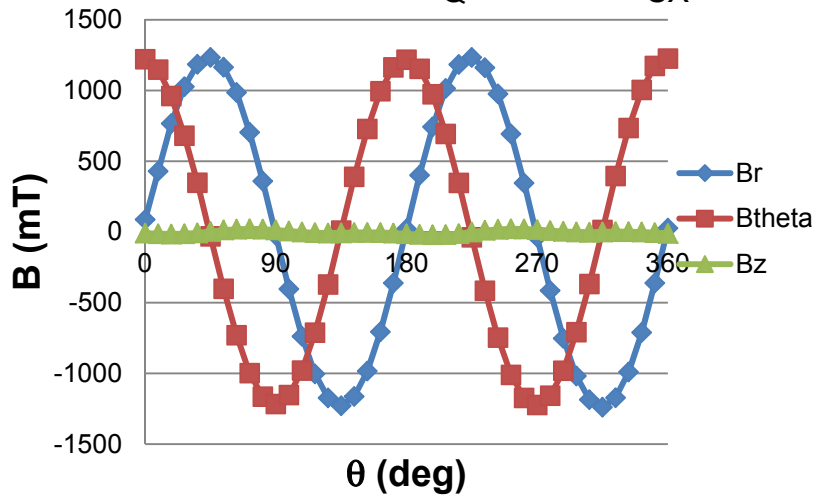


Range : outside ± 500 mm
 Step : 20 mm (center : 10 mm)
 Plane : mid-plane, $\pm 10, 20, 30, 40$ mm
 (Gap : ± 70 mm)

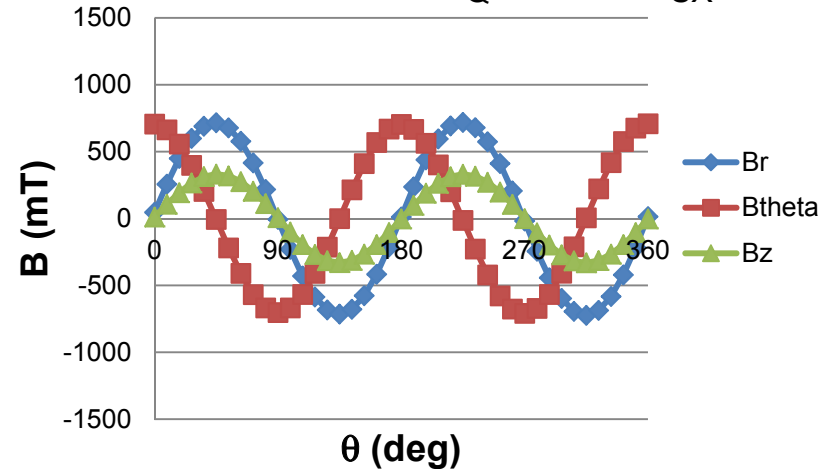
Magnetic Field in θ Direction

Quadrupole

Q500, $z=2230\text{mm}$, $I_Q=100\text{A}$, $I_{SX}=0\text{A}$

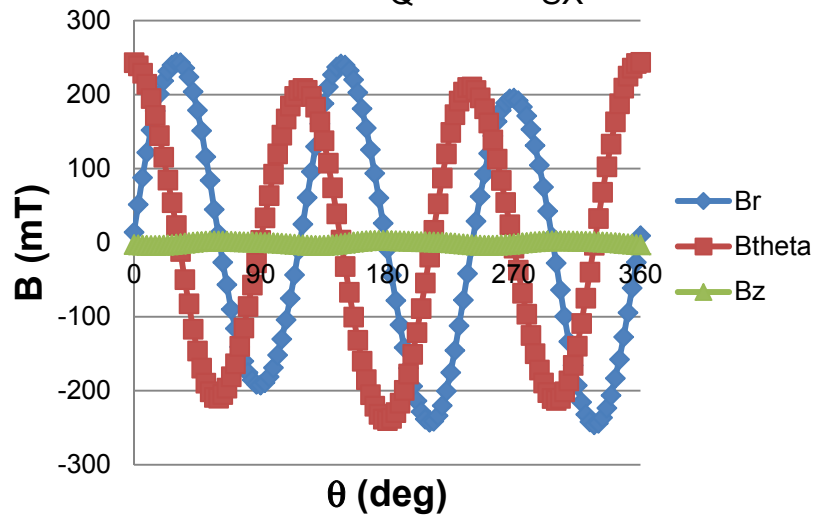


Q500, $z=1980\text{mm}$, $I_Q=100\text{A}$, $I_{SX}=0\text{A}$



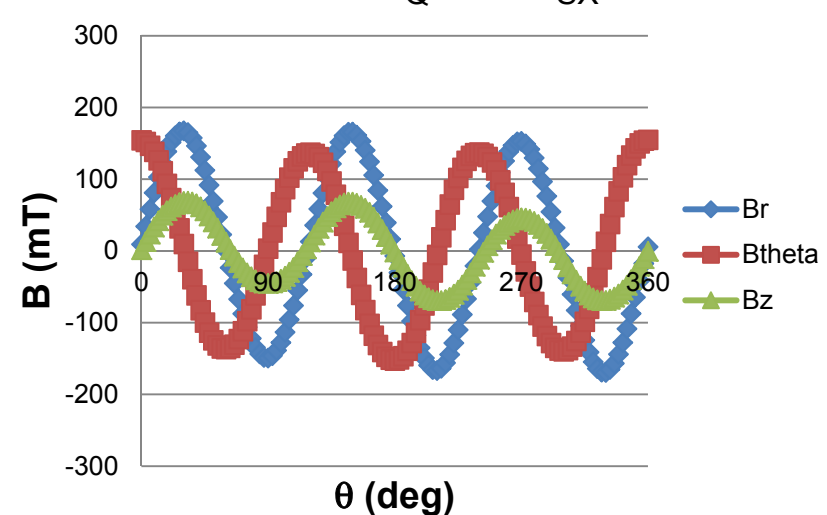
Sextupole

SX, $z=2230\text{mm}$, $I_Q=0\text{A}$, $I_{SX}=46\text{A}$



magnet center

SX, $z=1980\text{mm}$, $I_Q=0\text{A}$, $I_{SX}=46\text{A}$



field boundary region (edge of mag.)

Multipole Analysis of 3D Mag. Field

Magnetic field vector $(B_r, B_\theta, B_z(r, \theta, z))$ is expressed by a scalar $b_{n,0}(z)$.

measurement

$$\begin{cases} B_r(r, \theta, z) \\ B_\theta(r, \theta, z) \\ B_z(r, \theta, z) \end{cases} = \begin{cases} \sum_{n=1}^{\infty} B_{r,n}(r, z) \sin n\theta, \\ \sum_{n=1}^{\infty} B_{\theta,n}(r, z) \cos n\theta, \\ \sum_{n=1}^{\infty} B_{z,n}(r, z) \sin n\theta. \end{cases}$$

1st step (Fourier Analysis)

(w/o skew components)

$n=1$: dipole
 $n=2$: quadrupole
 $n=3$: sextupole
 ...

2nd step (Deducing $b_{n,0}$)

$$\begin{cases} B_{r,n}(r, z) \\ B_{\theta,n}(r, z) \\ B_{z,n}(r, z) \end{cases} \equiv \begin{cases} \left(\frac{r}{r_0}\right)^{n-1} \sum_{m=0}^{\infty} b_{n,m}(z) \left(\frac{r}{r_0}\right)^{2m}, \\ \left(\frac{r}{r_0}\right)^{n-1} \sum_{m=0}^{\infty} \frac{n}{n+2m} b_{n,m}(z) \left(\frac{r}{r_0}\right)^{2m}, \\ \left(\frac{r}{r_0}\right)^n \sum_{m=0}^{\infty} \frac{r_0}{n+2m} \frac{\partial}{\partial z} b_{n,m}(z) \left(\frac{r}{r_0}\right)^{2m}. \end{cases}$$

$$b_{n,m}(z) = -\frac{r_0^2}{4m(n+m)} \frac{n+2m}{n+2(m-1)} \frac{\partial^2}{\partial z^2} b_{n,m-1}(z).$$

Fourier Transform of Differential

Eq.

$$b_{n,m}(z) = -\frac{r_0^2}{4m(n+m)} \frac{n+2m}{n+2(m-1)} \frac{\partial^2}{\partial z^2} b_{n,m-1}(z). \quad (m>0)$$

Fourier
transform



$$\tilde{b}_{n,m}(k) = \int_{-\infty}^{\infty} b_{n,m}(z) e^{-ikz} dz$$

$$\frac{\partial}{\partial z} \rightarrow -ik$$

z derivative can be translated into simple algebraic calculation by FT

$$\begin{aligned} \tilde{b}_{n,m}(k) &= -\frac{r_0^2}{4m(n+m)} \frac{n+2m}{n+2(m-1)} (-ik)^2 \tilde{b}_{n,m-1}(k) \\ &= \frac{(r_0 k)^2}{4m(n+m)} \frac{n+2m}{n+2(m-1)} \tilde{b}_{n,m-1}(k) \\ &= q_m \tilde{b}_{n,m-1}(k) \quad q_m \\ &= q_m q_{m-1} \tilde{b}_{n,m-2}(k) \\ &\vdots \\ &= q_m q_{m-1} \cdots q_1 \tilde{b}_{n,0}(k) \\ &= p_m \tilde{b}_{n,0}(k) \quad \left(p_m \equiv \prod_{i=1}^m q_i \right) \end{aligned}$$

Procedure to Deduce $b_{n,0}$ from $B_{r,n}$

$$B_{r,n}(r, z) = \left(\frac{r}{r_0}\right)^{n-1} \sum_{m=0}^{\infty} b_{n,m}(z) \left(\frac{r}{r_0}\right)^{2m} \quad (\text{diff. eq.})$$

$$B_{r,n}(r = r_0, z) = \sum_{m=0}^{\infty} b_{n,m}(z) \quad (\text{diff. eq.})$$

Fourier tr.

$$\tilde{B}_{r,n}(k) = \int_{-\infty}^{\infty} B_{r,n}(r = r_0, z) e^{-ikz} dz$$

decomposed from measured data

$$\begin{aligned} \tilde{B}_{r,n}(k) &= \sum_{m=0}^{\infty} \tilde{b}_{n,m}(k) \\ &= \sum_{m=0}^{\infty} p_m \tilde{b}_{n,0}(k) \\ \tilde{b}_{n,0}(k) &= \tilde{B}_{r,n}(k) / \sum_{m=0}^{\infty} p_m \end{aligned}$$

$$\begin{aligned} \tilde{B}_{\theta,n}(k) &= \sum_{m=0}^{\infty} \frac{n}{n+2m} \tilde{b}_{n,m}(k) \\ &= \sum_{m=0}^{\infty} \frac{n}{n+2m} p_m \tilde{b}_{n,0}(k) \\ \tilde{b}_{n,0}(k) &= \tilde{B}_{\theta,n}(k) / \sum_{m=0}^{\infty} \frac{n p_m}{n+2m} \end{aligned}$$

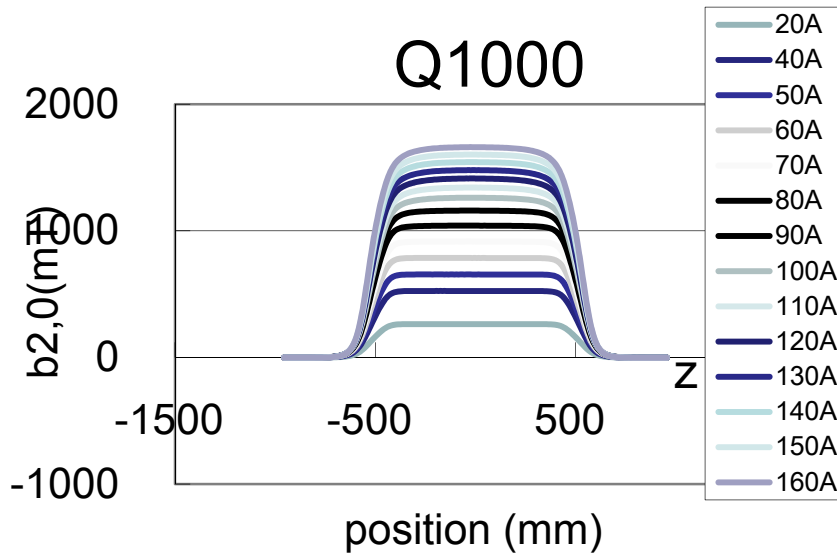
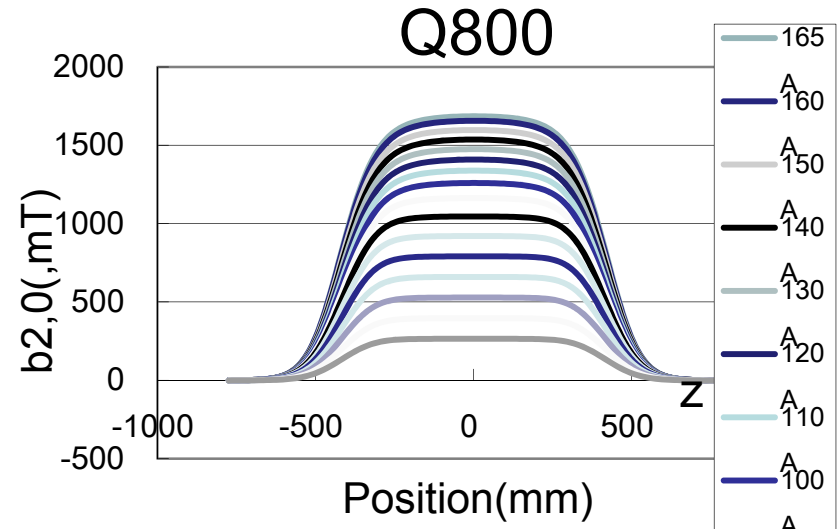
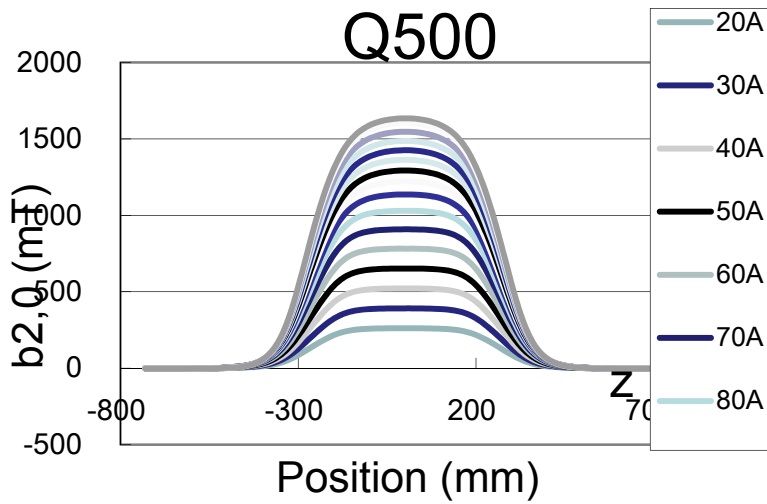
$b_{n,0}$ from $B_{\theta,n}$

Inv. Fourier tr.

$$b_{n,0}(z) = \frac{1}{2\pi} \int_{-\infty}^{\infty} \tilde{b}_{n,0}(k) e^{+ikz} dk$$

Using the procedure of Fourier tr. and inverted Fourier tr., $b_{n,0}(z)$ is obtained from $B_{r,n}(r, z)$, without solving the high differential equation.

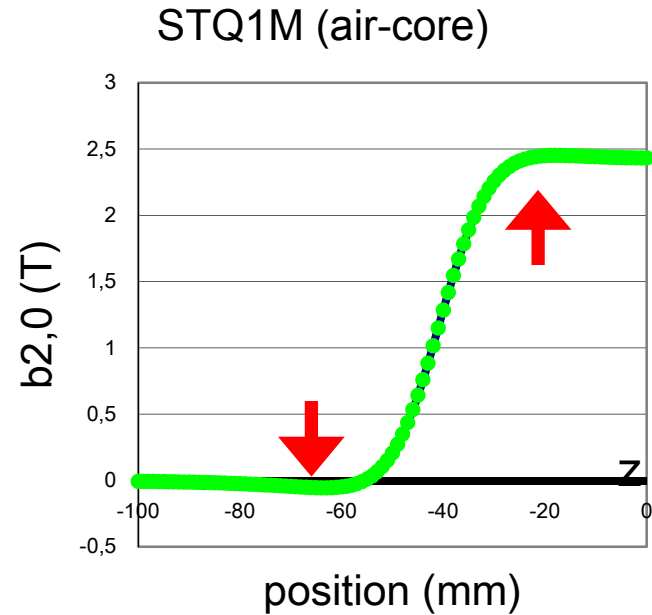
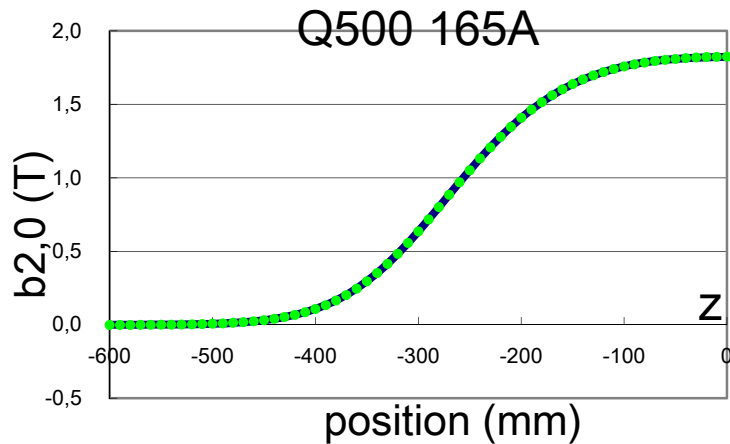
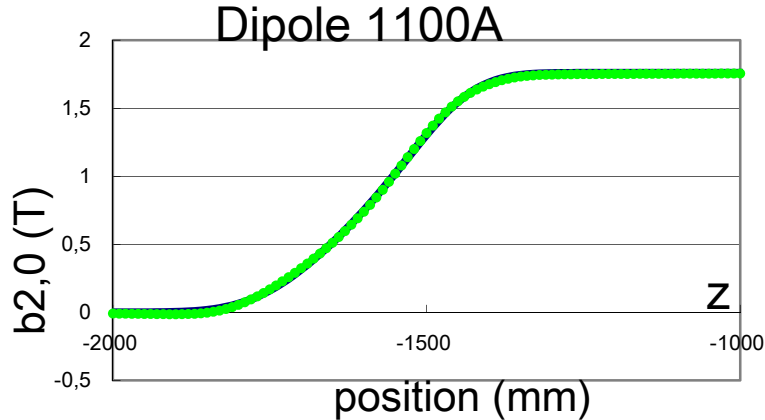
$b_{2,0}(z)$ Distribution along the Axis



Deduced from B_r ($r=107$ mm)

- The fringe region is very **large**.
- The shape of the **distribution varies** much with the excitation.

Engel Function for Fringe of $b_{n,0}$



Overshooting & undershooting part
 → Second term is introduced (a_7 - a_{11})

$$F(z) = \frac{1}{1 + \exp(a_1 + a_2(z/D) + \dots + a_6(z/D)^5)}$$

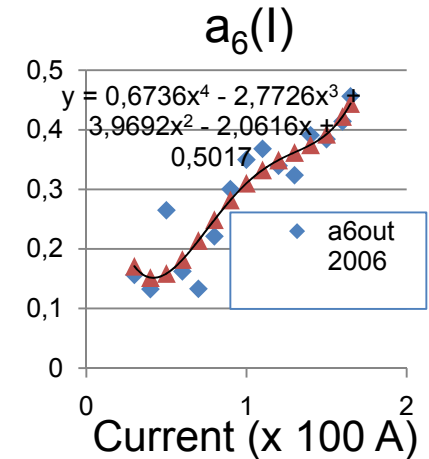
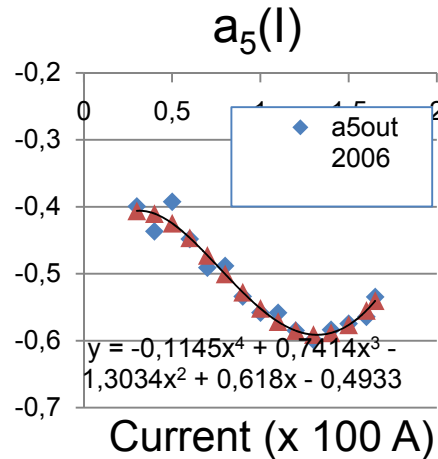
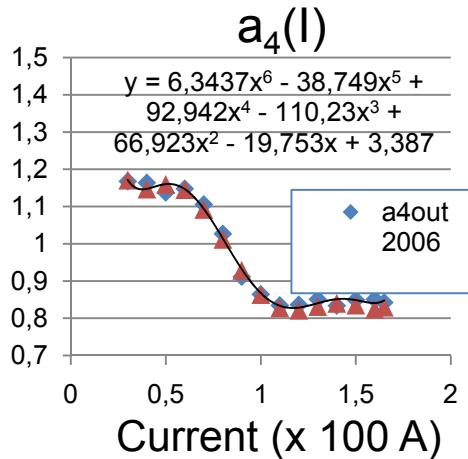
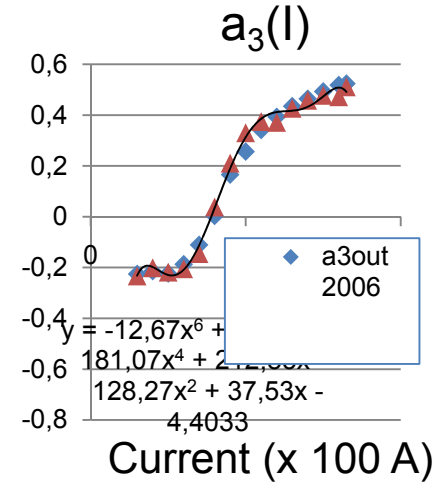
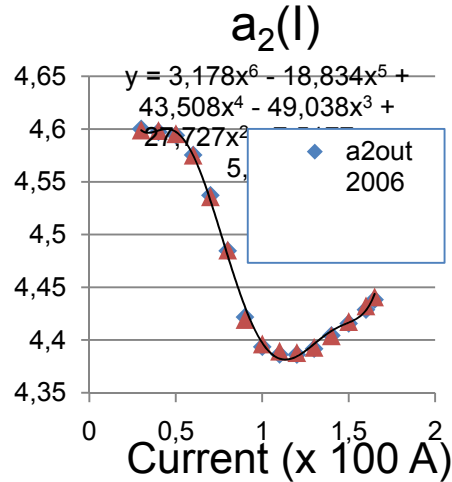
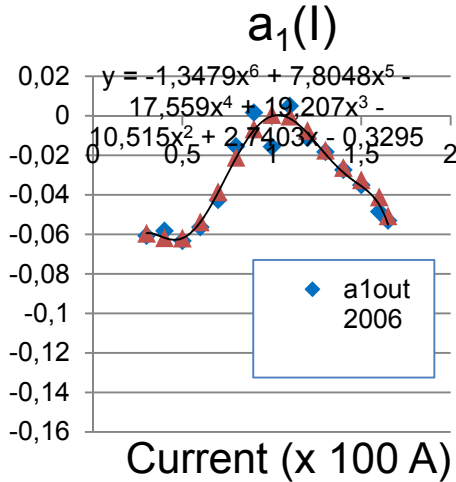
D : Pole tip diameter

a_1 - a_6 : parameter

$$F(z) = \frac{1}{1 + \exp(a_1 + a_2(z/D) + \dots + a_6(z/D)^5)} + a_7 \times \tanh(a_8 + a_9(z/D)) \times \exp\left(-\frac{((z/D) + a_{10})^2}{a_{11}^2}\right)$$

Enge Coefficients

As a function of magnet current (Q500, inner side)

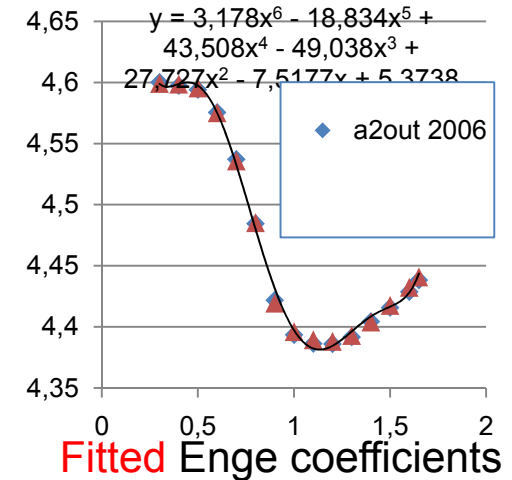


Enge coefficients are fitted with polynomal function.
→ Fitted Enge coefficients are used in our optics calculation.

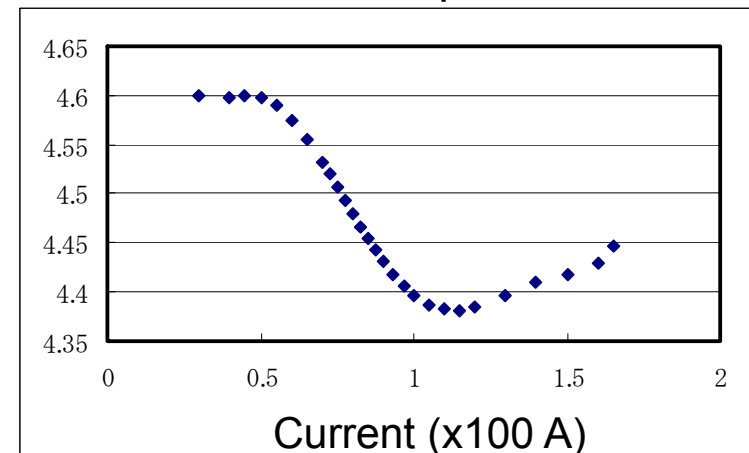
Optics Search using COSY INFINITY

e.g. a_2 for Q500 outer side

- Optics search using **symplectic transfer maps** that allow symplectic scaling is made.
- Symplectic transfer maps are calculated beforehand using the **fitted Enge coefficients** for discrete values of magnet current (see the lower plot).
- During the search, symplectic transfer maps whose magnet current is closest are chosen and used for optics calculation applying the **symplectic scaling**.
- This scheme allows **fast search**, saving computational time.



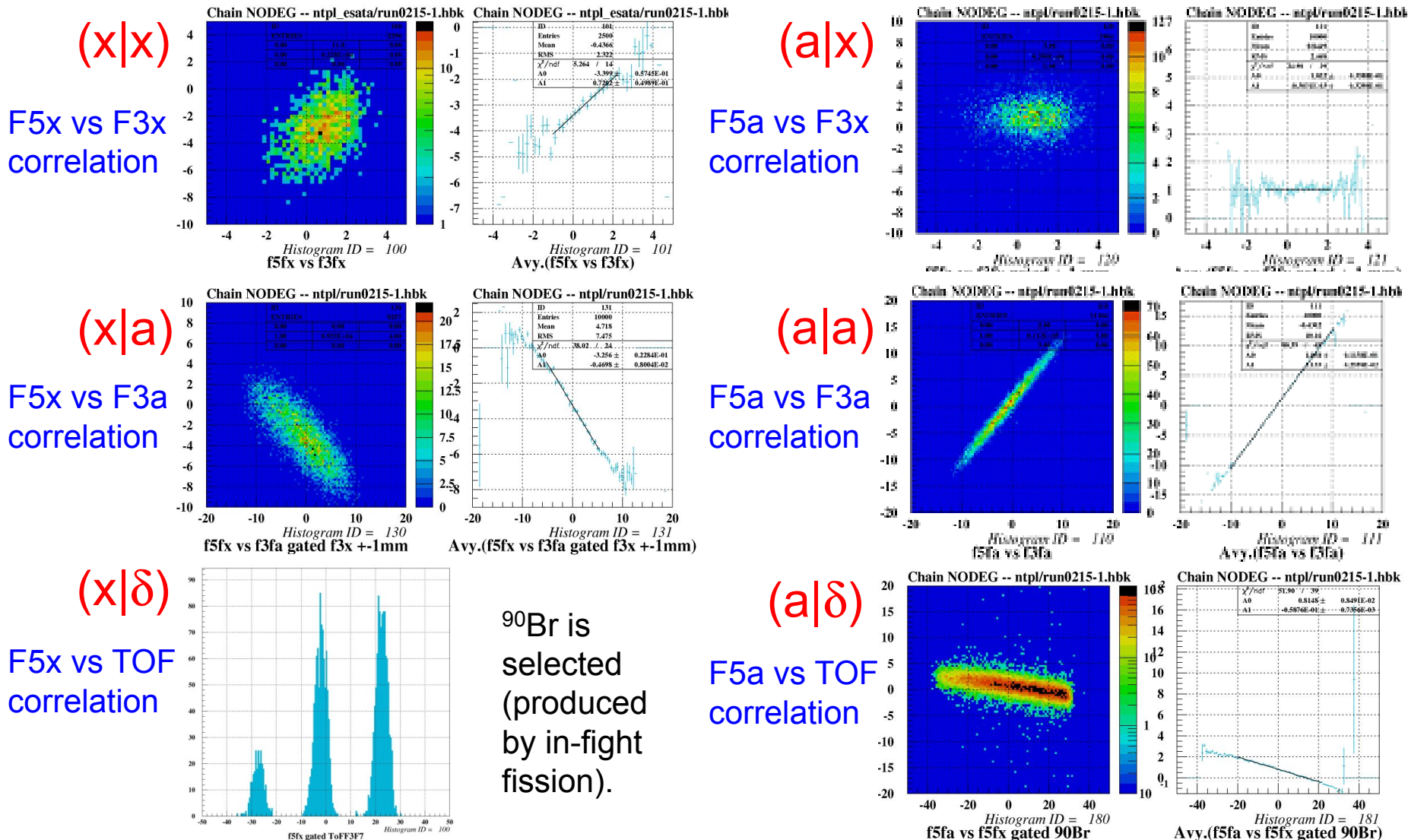
Symplectic transfer maps are calculated for the points below.



Comparison with measurements

Determination of matrix terms from 2ndary beam

1st order matrix elements from F3 to F5



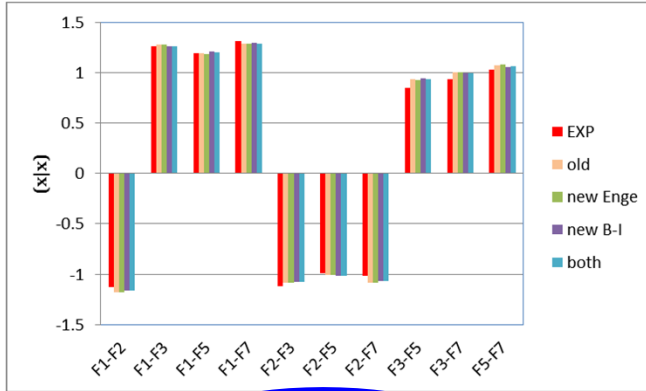
⁹⁰Br is selected (produced by in-flight fission).

F3x: ±1mm, F3a: ±1mrad gates are applied. δ is gated with TOF37: ±1ns.

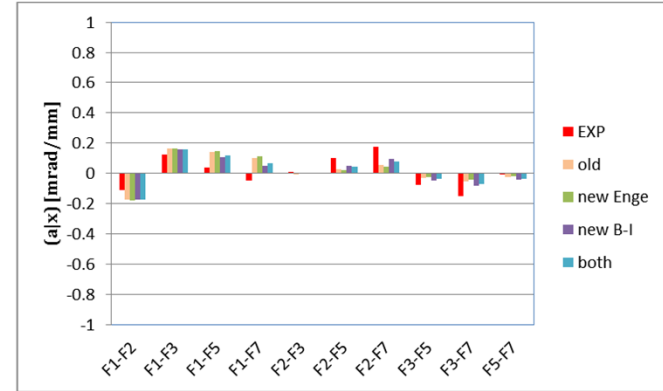
Comparison for the matrix terms

measured

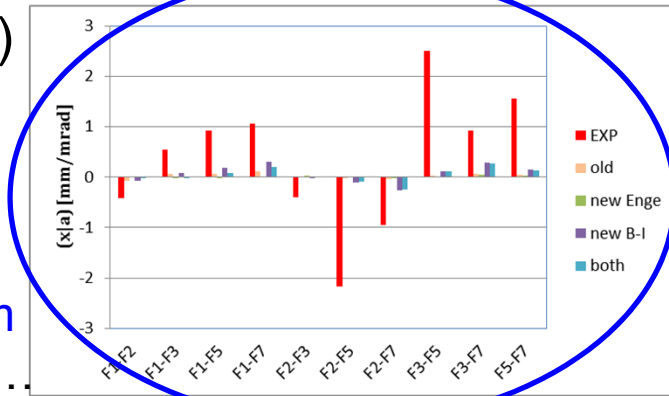
$(x|x)$



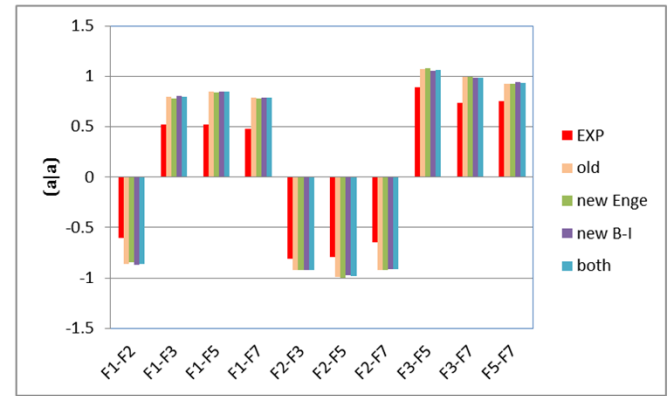
$(a|x)$



$(x|a)$

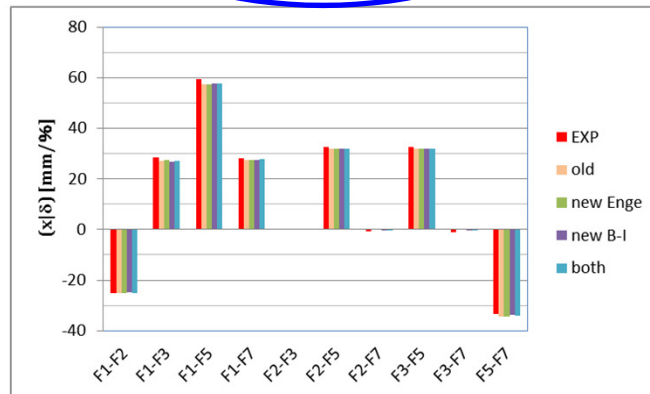


$(a|a)$

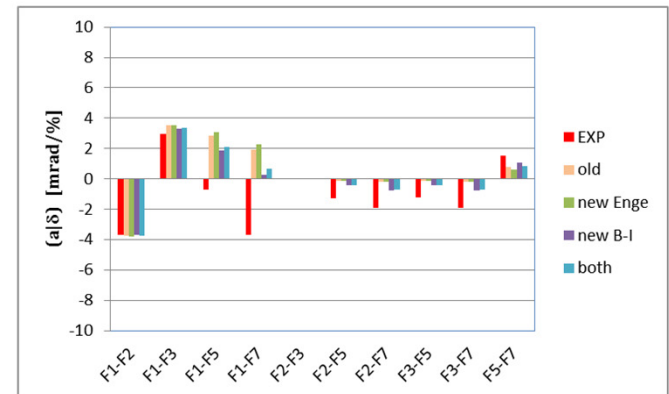


Focusing term
Not sufficient...

$(x|\delta)$



$(a|\delta)$



Particle Identification in 2nd Stage

TOF-B ρ - ΔE method with track reconstruction

→ Improve the B ρ and TOF resolution

Measure β , B ρ , ΔE @ 2nd stage

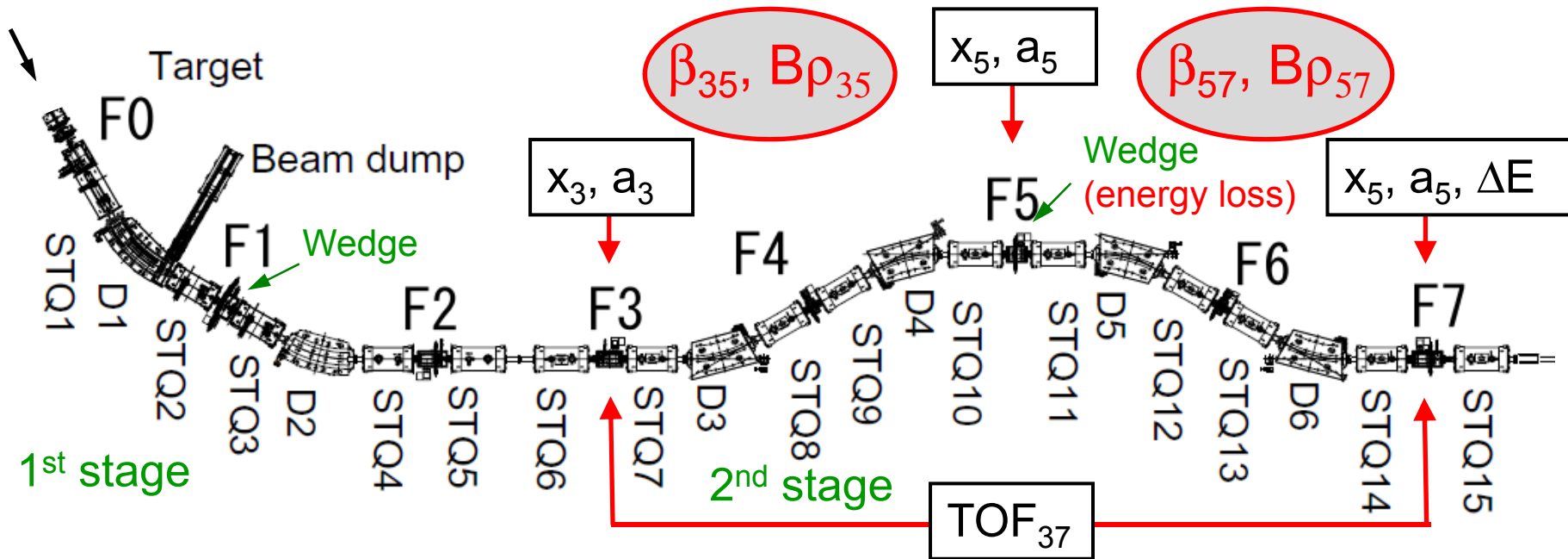
+ isomeric
 γ -rays
 $Z, A/Q$

$$Z \leftarrow -dE/dx = f(Z, \beta)$$

$$A/Q = \frac{B\rho}{c\beta\gamma}$$

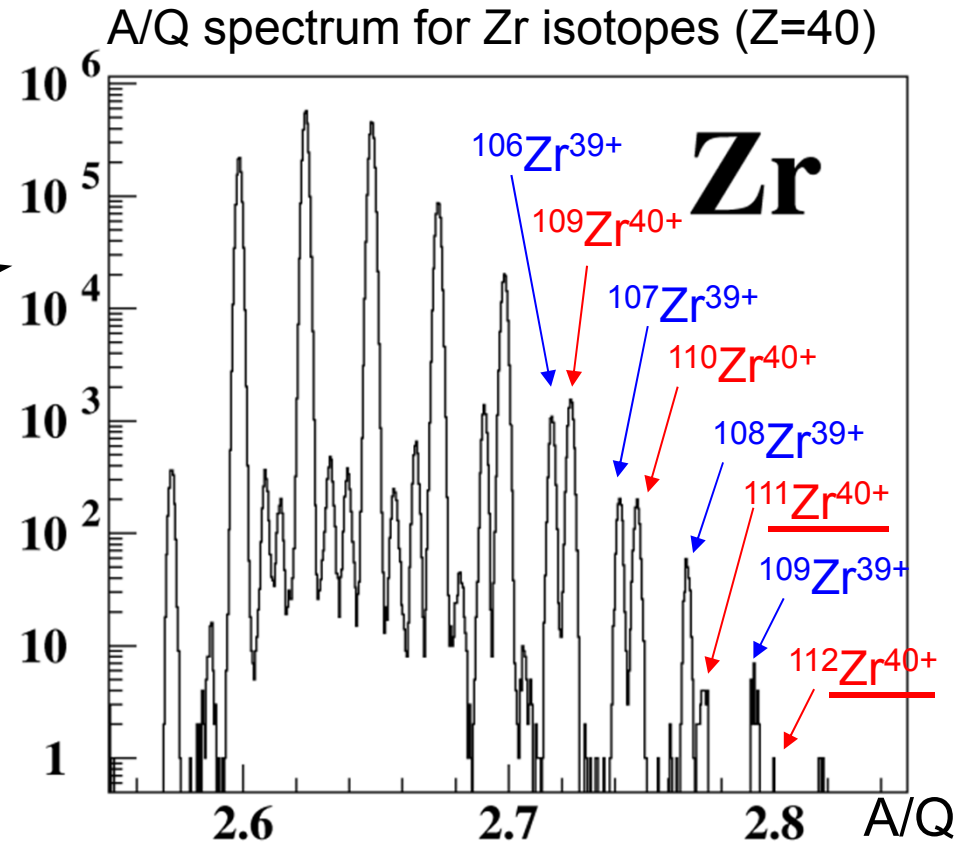
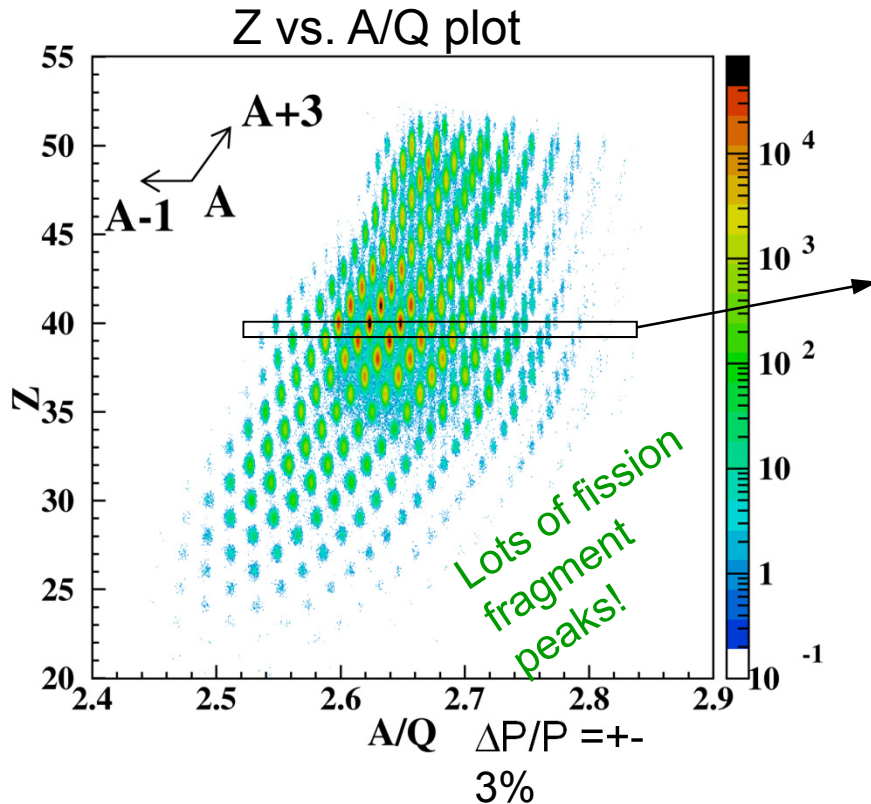
- B ρ \leftarrow by track reconstruction.
 - $x_3, a_3, x_5, a_5 \rightarrow B\rho_{35}$
 - $x_7, a_7, x_5, a_5 \rightarrow B\rho_{57}$ (ion optics)
- β \leftarrow by the couple equations.
 - $TOF_{37} = L_{35}/\beta_{35}c + L_{57}/\beta_{57}c$
 - $A/Q = B\rho_{35} / c\beta_{35}\gamma_{35}$
 - $A/Q = B\rho_{57} / c\beta_{57}\gamma_{57}$

a: θ (angle in horizontal)



PID Power for Fission Fragments

High enough to well identify charge states.
thanks to the track reconstruction!



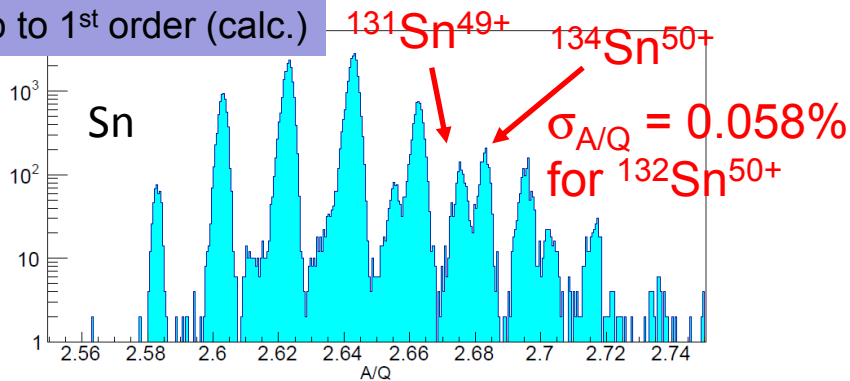
U-beam+2.9-mm Be, $B\rho_{01} = 7.990 \text{ Tm}$
F1 deg: 2.18-mm Al, $\Delta p/p: \pm 3\%$, G3 setting (Z~40)
J. Phys. Soc. Jpn. 79 (2010) 073201.

r.m.s. A/Q resolution: **0.035 %**

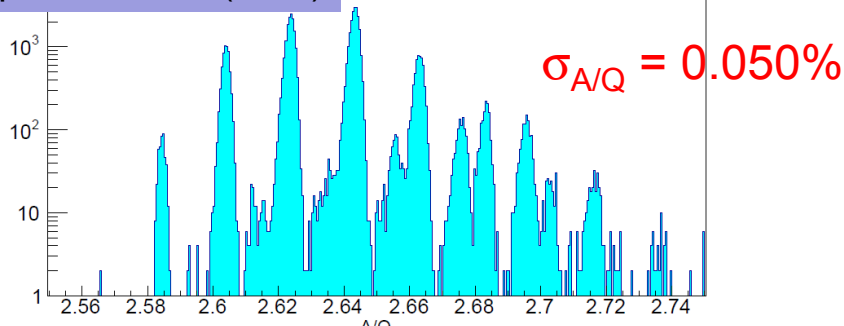
Improvement of PID Power

Sn isotopes produced by in-flight fission of ^{238}U

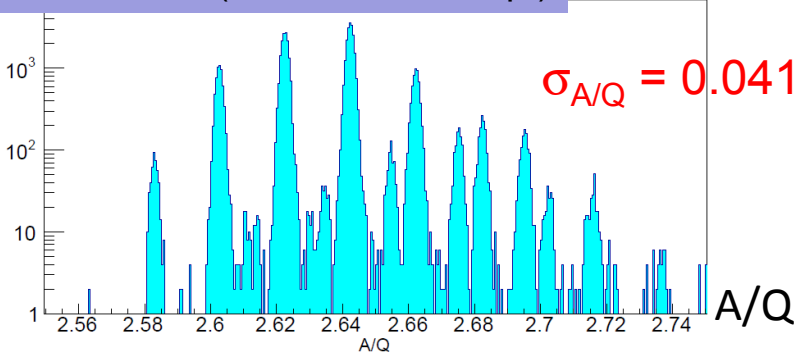
Up to 1st order (calc.)



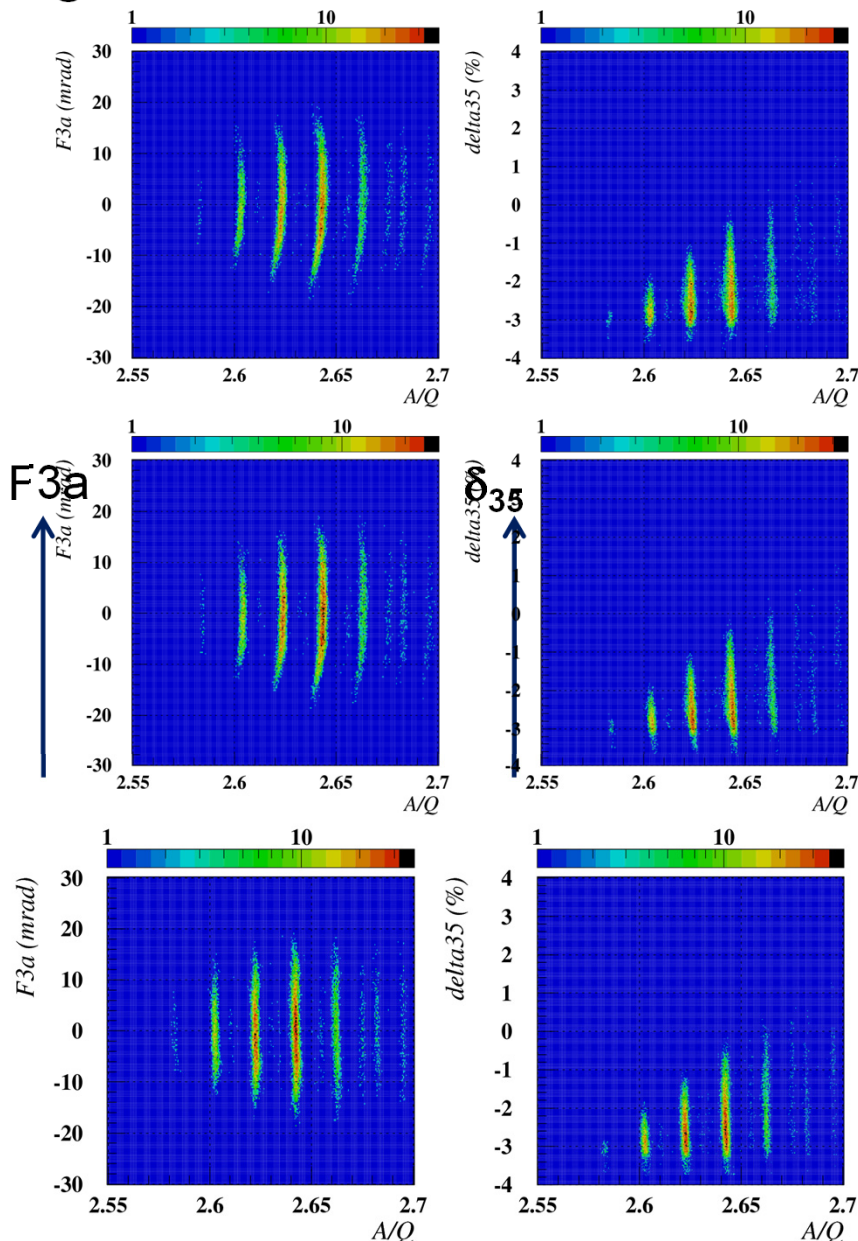
Up to 3rd order (calc.)



Up to 3rd order (deduced from exp.)



Reconstructed δ and F3a vs A/Q



Issues

- COSY predictability improvement
 - Improvement of magnetic field measurement
 - Magnetic field distribution
 - Cross talk between Q and SX (not only $Q \rightarrow SX$ but also $SX \rightarrow Q$)
 - Better analysis of measured magnetic field-maps
 - B-I curve quality
 - Fitting $b_{n,0}$ distribution with Enge function (the function of z)
 - Fitting Enge coefficient (the function of I)
- allowing us to achieve our goal: precise optics setting, in which any tuning is not needed.
- allowing us to achieve excellent track reconstruction without using experimentally-determined transfer maps.

Summary

- Introduction
 - BigRIPS has large acceptance and large aperture for the **fission fragments of ^{238}U** beam.
 - For this feature, **Superconducting quadrupoles** are used.
 - The **field distribution** of STQ **varies very much** with the magnet excitation.
- Optics Calculation
 - Goal: **precise ion-optical setting** is calculated, in which tuning is not needed.
 - To achieve this goal, the **varying field distribution** should be included in the optics calculation.
 - The procedure of the magnetic field analysis is shown.
 - For deducing $b_{n,0}$, **a new approach** using Fourier Transform is shown.
- Comparison with measurement
 - Matrix term: the agreement of $(x|a)$ term is **not sufficient**.
 - A/Q resolution: there is room for improvement.

Thank you for your attention!