Fully 3D Long-Term Simulation of the Coupling Resonance Experiments at the CERN PS

Ji Qiang and Robert Ryne, LBNL
Giuliano Franchetti, Ingo Hofmann, GSI
Elias Metral, CERN

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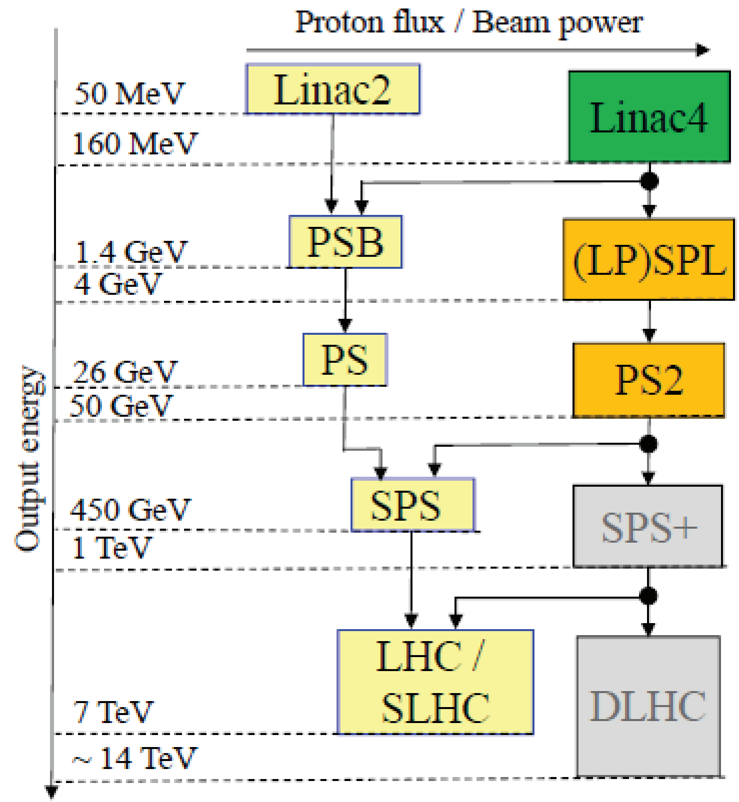
Outline

- Introduction
- Computational model
- Simulation of Montague resonance experiment at PS
- Summary

Introduction

- Proton-Synchrotron (PS) is amongst the LHC injectors the oldest, and will continue to serve the LHC at least for the next 25 years.
- Space-charge effects is a dominant factor limiting the bunch intensity.
- Montague Resonance:

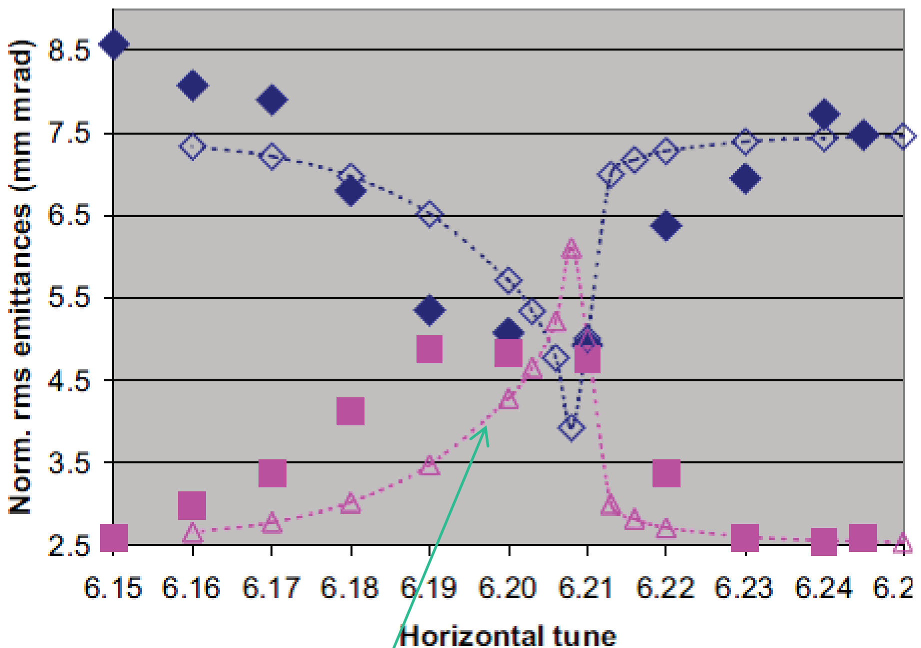
  $2\,Q_x - 2\,Q_y = 0$
- can cause particle due to unequal aperture size in horizontal and vertical dimensions.
- benchmark space-charge codes



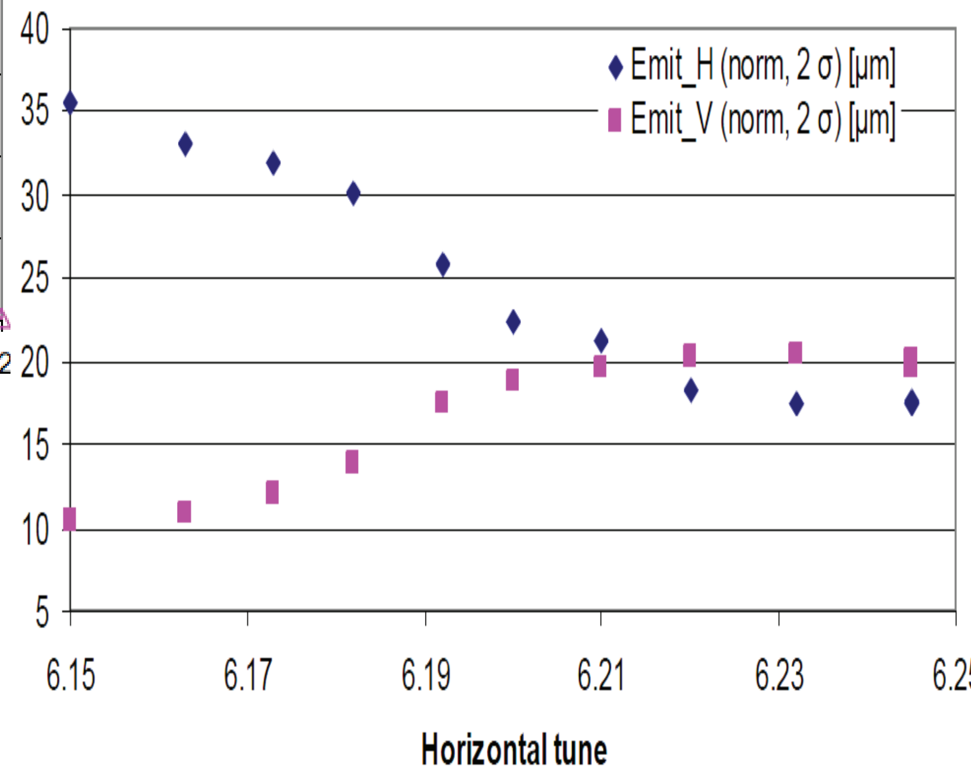
Refs: B. W. Montague, CERN-Report No. 68-38, CERN, 1968.
E. Metral et al., Proc. of EPAC 2004, p. 1894.
I. Hofmann et al., Proc. of EPAC 2004, p. 1960.

Static and Dynamics Montague Resonance Crossing at PS

Static Crossing



100 ms dynamic Crossing

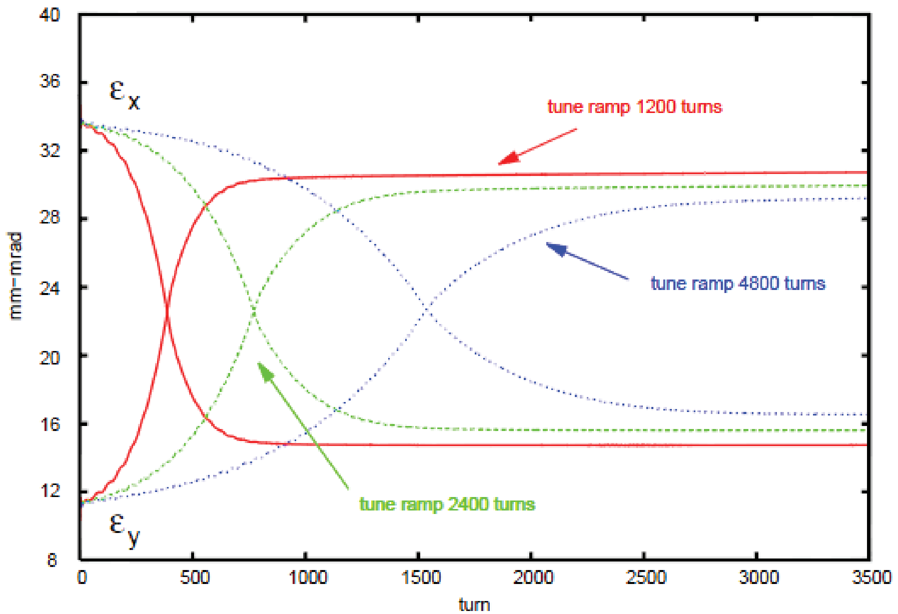


Simulations using constant focusing

Courtesy of E. Metral et al., Proc. EPAC04

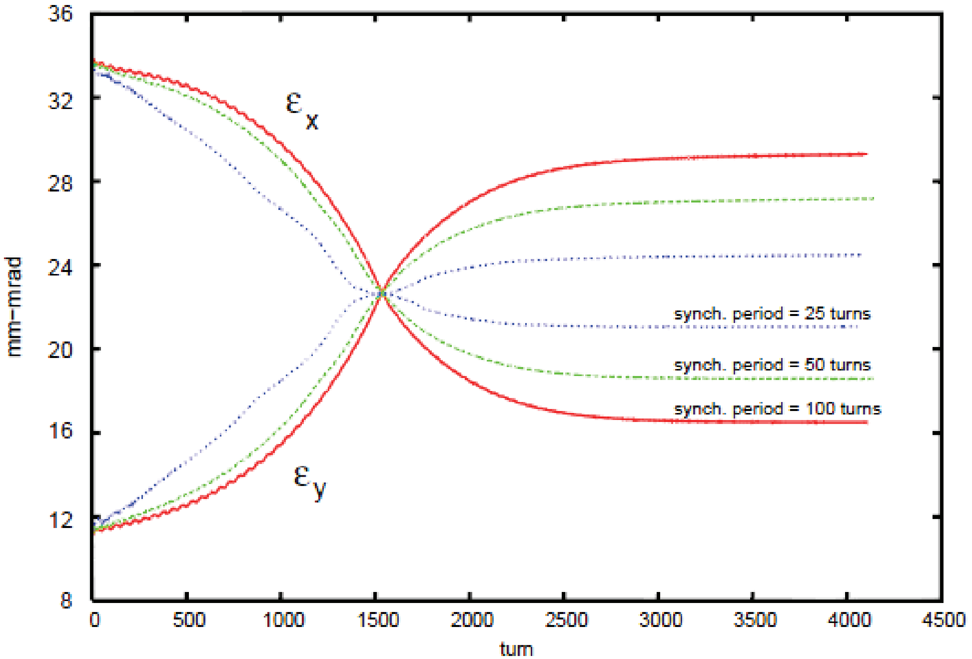
Dynamics Emittance Exchange in Constant Focusing Channel with Different Ramping Time and Synchrotron Oscillation Period

different ramping time but fixed synch. period



turn

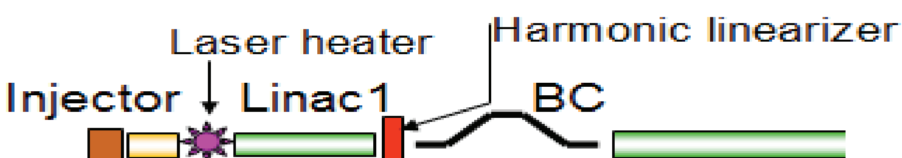
different synch. period but fixed ramping time



turn

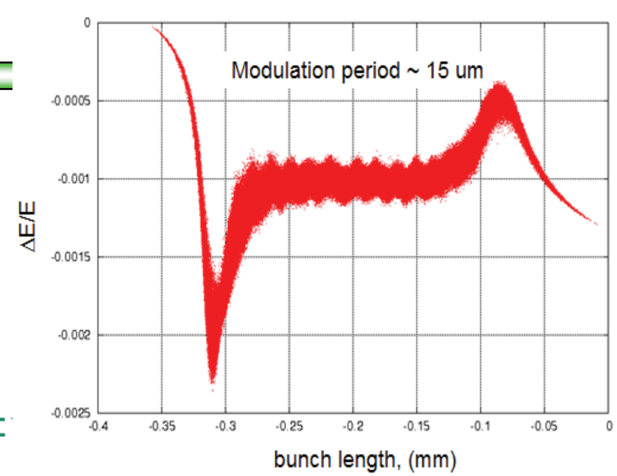
IMPACT Code Suite

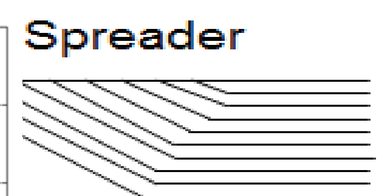
- IMPACT-Z: parallel PIC code (z-code)
- IMPACT-T: parallel PIC code (t-code)
- Envelope code, pre- and post-processors,…
- Optimized for parallel processing
- Applied to many projects: SNS, JPARC, RIA, FRIB, PS2, future light sources, advanced streak cameras,…
- Has been used to study photoinjectors for BNL e-cooling project, Cornell ERL, FNAL/A0, LBNL/APEX, ANL, JLAB, SLAC/LCLS



One Billion Macroparticle Simulation of an FEL Linac

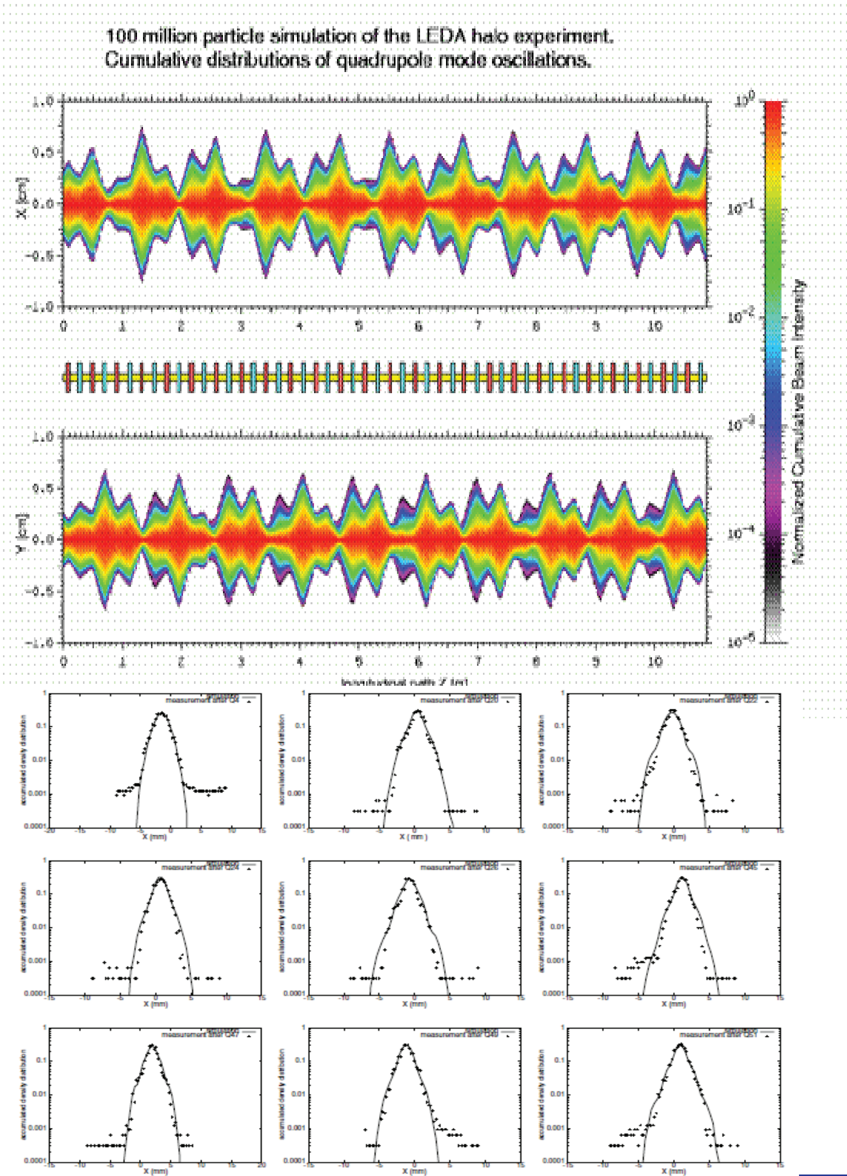
(~2 hrs on 512 processors)





IMPACT-Z

- Parallel PIC code using coordinate “z” as the independent variable
- Key Features
  - —Detailed RF accelerating and focusing model
  - —Multiple 3D Poisson solvers
    - Variety of boundary conditions
    - 3D Integrated Green Function
  - —Multi-charge state
  - —Machine error studies and steering
  - —Wakes
  - —CSR (1D)
  - —Run on both serial and multiple processor computers



IMPACT-Z for Space-Charge Study in Ring

Particle-in-cell simulation with split-operator method

- Particle-in-cell approach:
  - Charge deposition on a grid
  - Field solution via spectral-finite difference method with transverse rectangular conducting pipe and longitudinal open
  - Field interpolation from grid to particles
- Split-operator method with $H = H_{external} + H_{space\ charge}$
- Thin lens kicks for nonlinear elements
- Lumped space-charge at a number locations

Poison Solver Used in Space-Charge Calculation

$$\frac{\partial^2\phi}{\partial x^2}+\frac{\partial^2\phi}{\partial y^2}+\frac{\partial^2\phi}{\partial z^2}=-\frac{\rho}{\epsilon_0}$$

with boundary conditions

$$\begin{aligned}\phi(x=0,y,z)&=0,\\ \phi(x=a,y,z)&=0,\\ \phi(x,y=0,z)&=0,\\ \phi(x,y=b,z)&=0,\\ \phi(x,y,z=\pm\infty)&=0,\end{aligned}$$

$$\rho(x,y,z)=\sum_{l=1}^{N_l}\sum_{m=1}^{N_m}\rho^{lm}(z)\sin(\alpha_l x)\sin(\beta_m y),$$

$$\phi(x,y,z)=\sum_{l=1}^{N_l}\sum_{m=1}^{N_m}\phi^{lm}(z)\sin(\alpha_l x)\sin(\beta_m y),$$

where

$$\rho^{lm}(z)=\frac{4}{ab}\int_0^a\int_0^b\rho(x,y,z)\sin(\alpha_l x)\sin(\beta_m y),$$

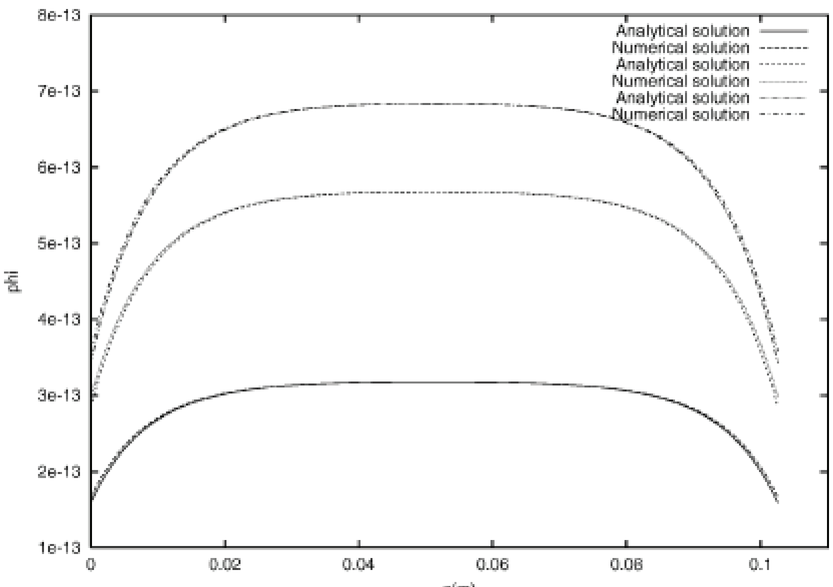
$$\phi^{lm}(z)=\frac{4}{ab}\int_0^a\int_0^b\phi(x,y,z)\sin(\alpha_l x)\sin(\beta_m y),$$

$$\frac{\partial^2\phi^{lm}(z)}{\partial z^2}-\gamma_{lm}^2\phi^{lm}(z)=-\frac{\rho^{lm}(z)}{\epsilon_0},$$

$$\frac{\phi_{n+1}^{lm}-2\phi_n^{lm}+\phi_{n-1}^{lm}}{h_z^2}-\gamma_{lm}^2\phi_n^{lm}=-\frac{\rho_n^{lm}}{\epsilon_0},$$

$$\begin{aligned}\phi_{-1}^{lm}&=\exp(-\gamma_{lm}h_z)\phi_0^{lm}, &\quad n&=0,\\ \phi_{N+1}^{lm}&=\exp(-\gamma_{lm}h_z)\phi_N^{lm}, &\quad n&=N.\end{aligned}$$

Numerical Solutions vs. Analytical Solutions



z (m)

Physical Parameters of PS

Physical parameters:

RF frequency = 3.5 MHz
RF voltage = 27 kV
Ek = 1.4 GeV
Emit_x = 7.5 mm-mrad
Emit_y = 2.5 mm-mrad
Rms bunch length = 45 ns
Rms dp/p = 1.7×10^{-3}

Horizontal tune: 6.15 – 6.245
Vertical tune: 6.21
Synchrotron period: 1.5 ms
Half Aperture = 7cm x 3.5cm
I = 1.0×10^{12}

Refs: B. W. Montague, CERN-Report No. 68-38, CERN, 1968.
E. Metral et al., Proc. of EPAC 2004, p. 1894.
I. Hofmann et al., Proc. of EPAC 2004, p. 1960.

Generation of Initial Matched Distribution

- Zero current match found using MaryLie normal form capabilities:
  - Normalize 1-turn map: $M=ANA^{-1}$

    A is the normalizing map

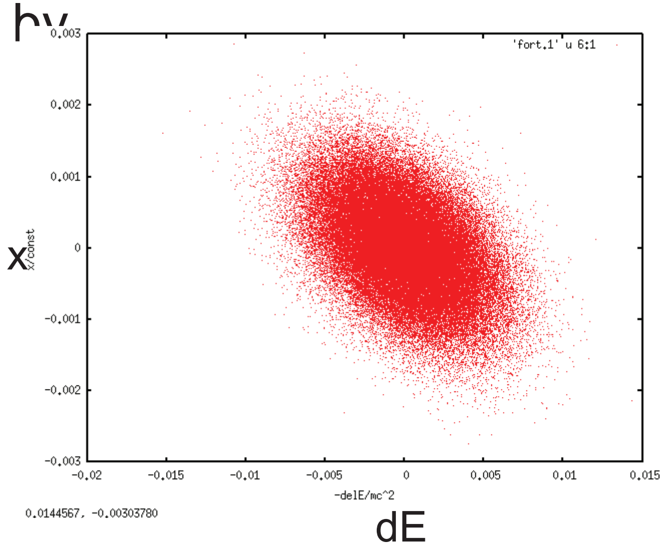
    N is the normal form which causes only rotations in phase space
  - Consider a function $g((x^2+p_x^2),(y^2+p_y^2),(t^2+p_t^2))$
  - Then $f(\zeta)=g(A\,(x^2+p_x^2),(y^2+p_y^2),(t^2+p_t^2))$ is a matched beam.

Proof: The distribution after one turn is given by

$f(M^{-1}\zeta)=g(AN\,A^{-1}A\,(x^2+p_x^2),(y^2+p_y^2),(t^2+p_t^2)) =$

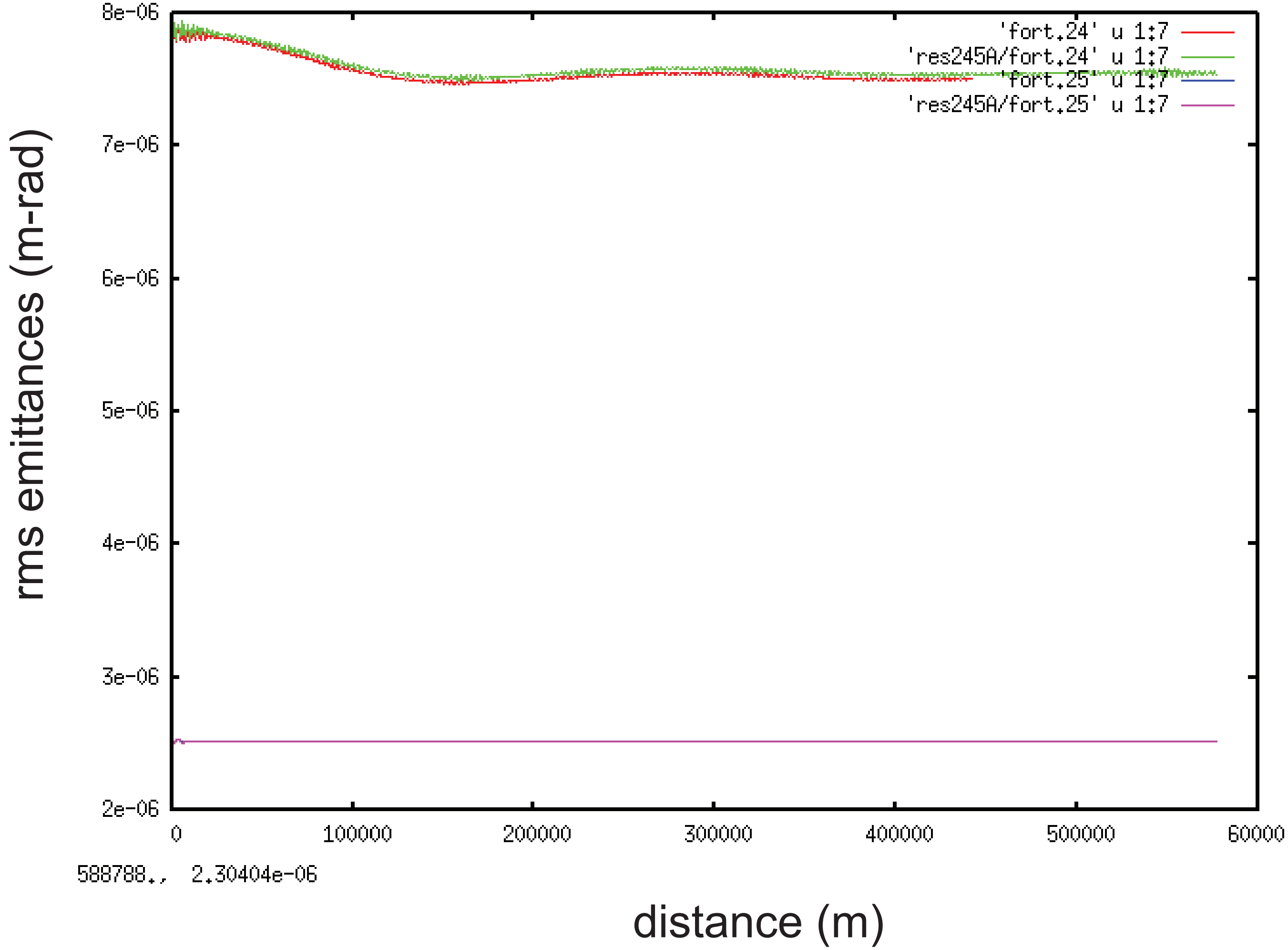
$g(AN\,(x^2+p_x^2),(y^2+p_y^2),(t^2+p_t^2))=$

$g(A\,(x^2+p_x^2),(y^2+p_y^2),(t^2+p_t^2))$



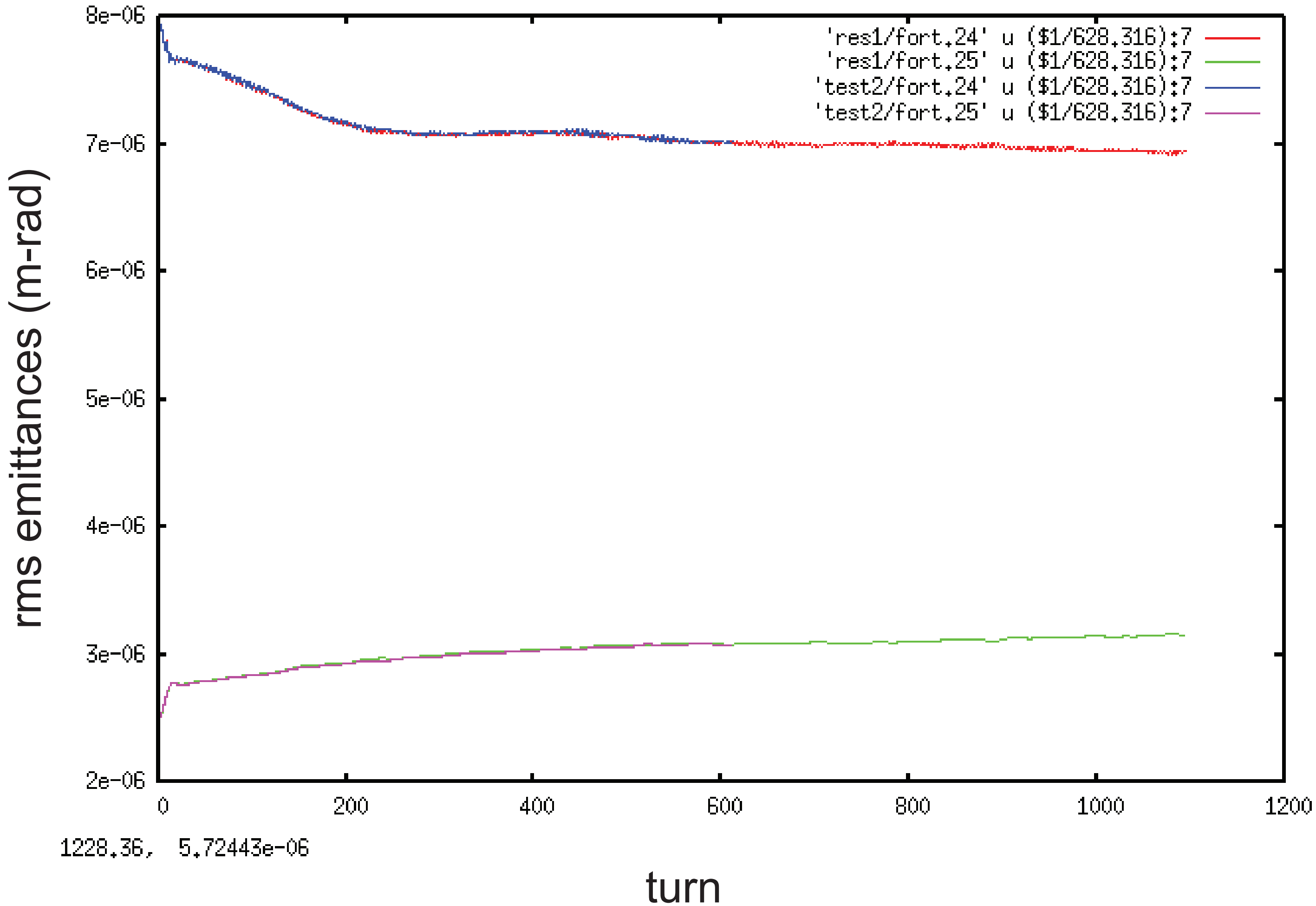
Numerical Parameters: Test of Convergence (1)

100k vs. 200k marco-particles

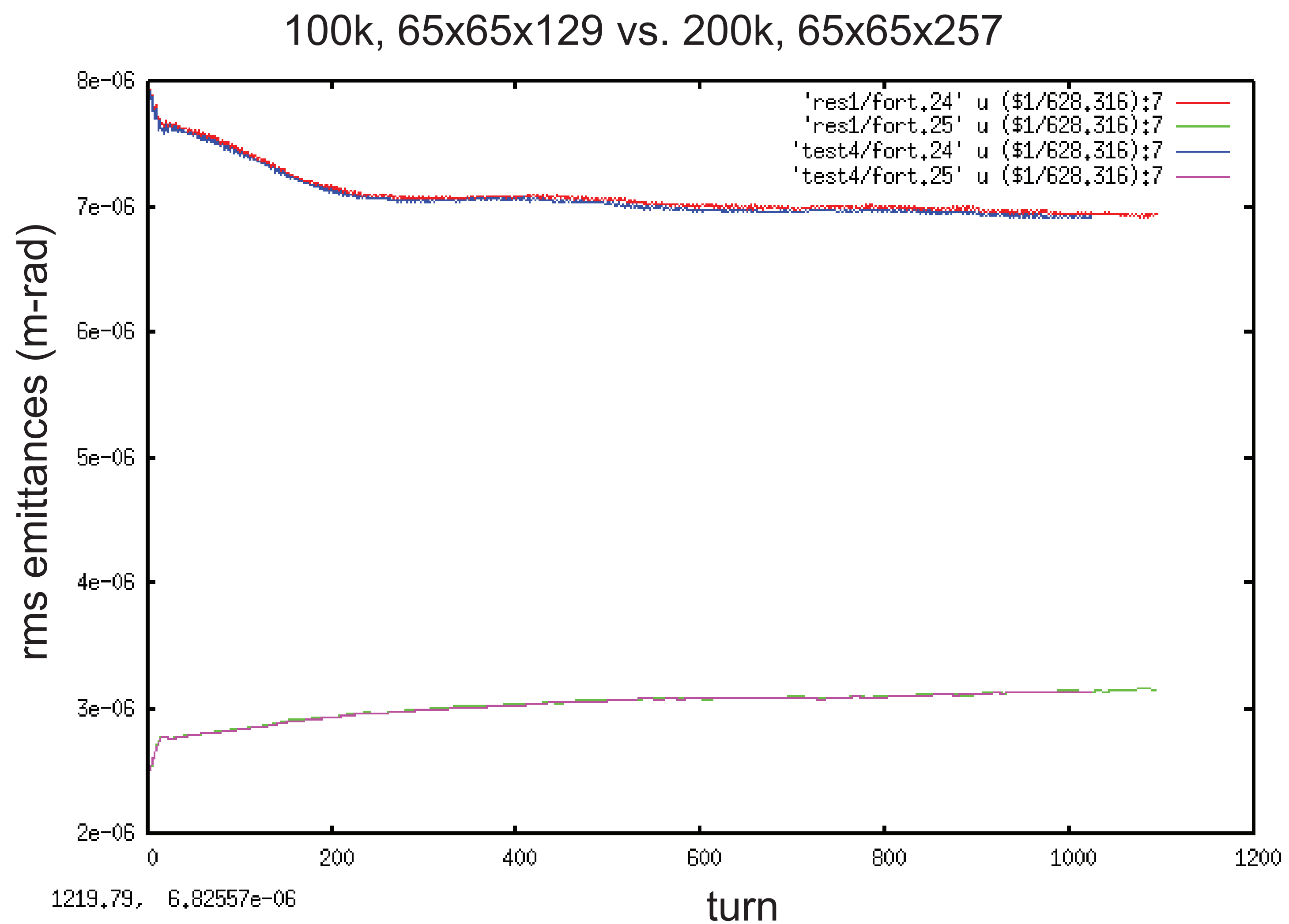


Numerical Parameters: Test of Convergence (2)

60 sc vs. 120 sc

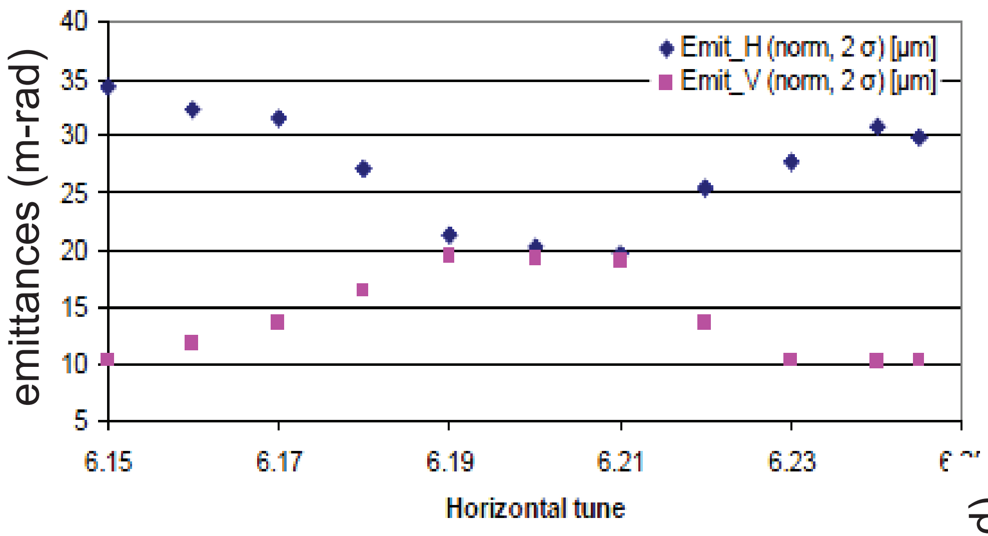


Numerical Parameters: Test of Convergence (3)

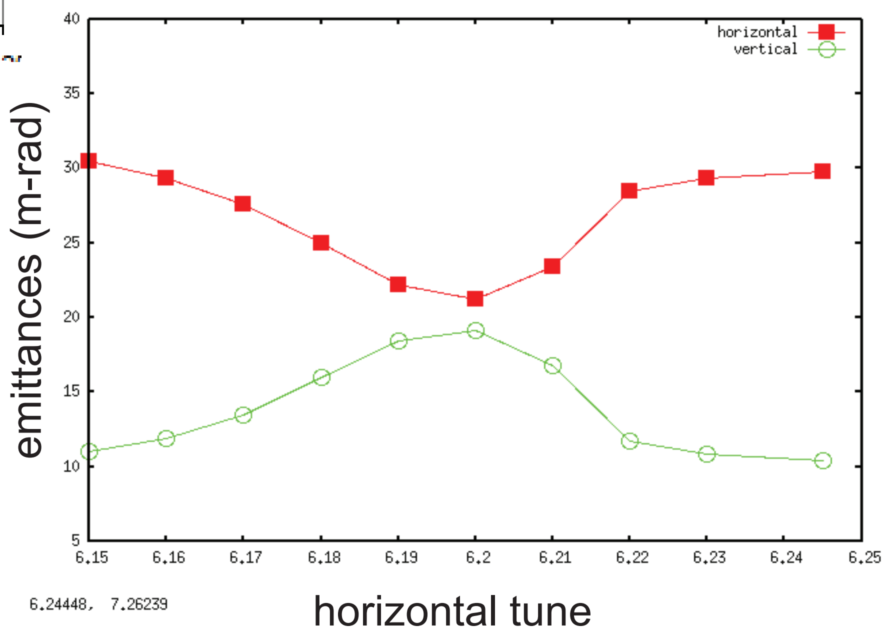


Static Montague Resonance Crossing at PS

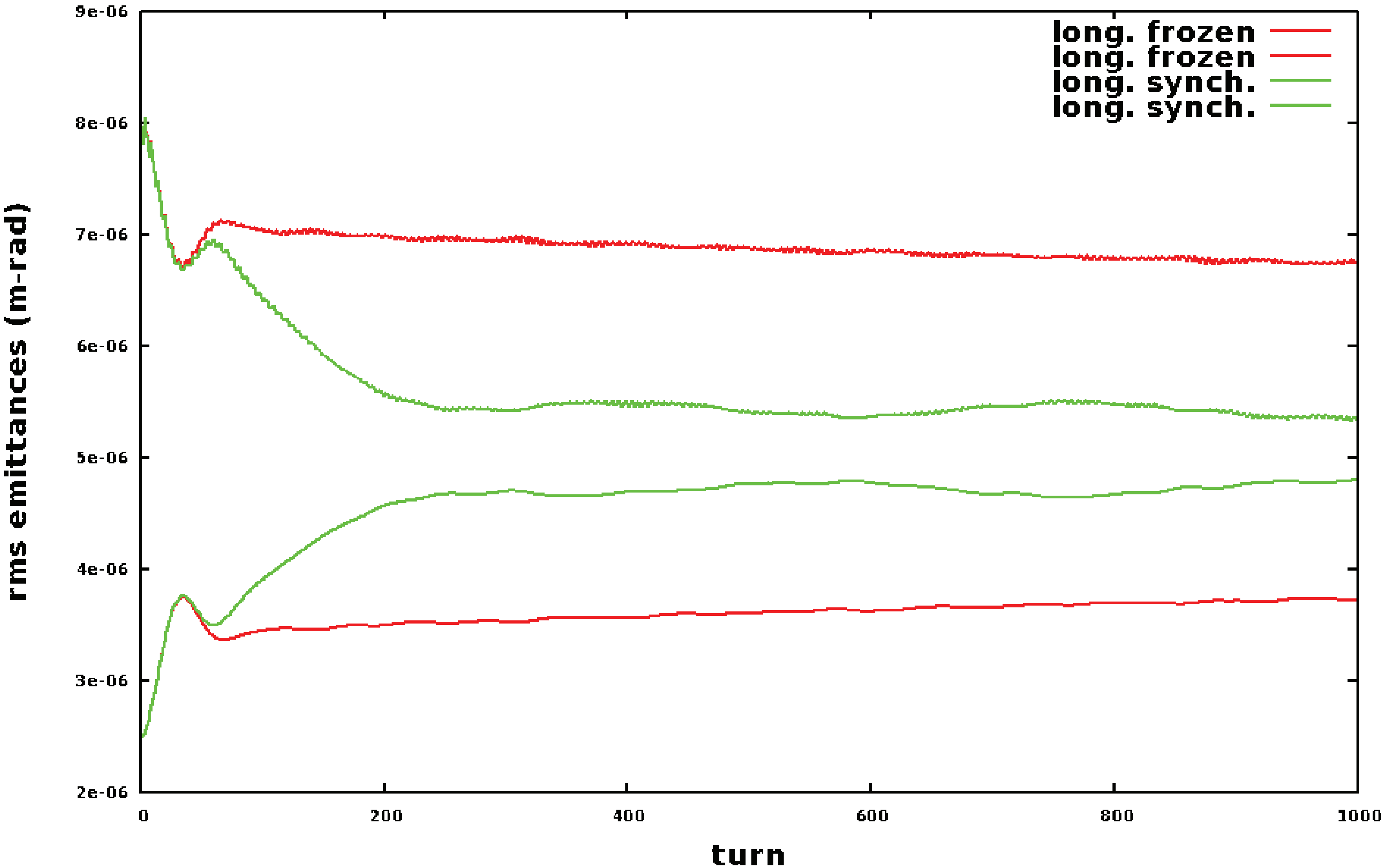
measurements



IMPACT simulation



Emittance Evolution w/o Longitudinal Synchrotron Motion (6.197,6.21)

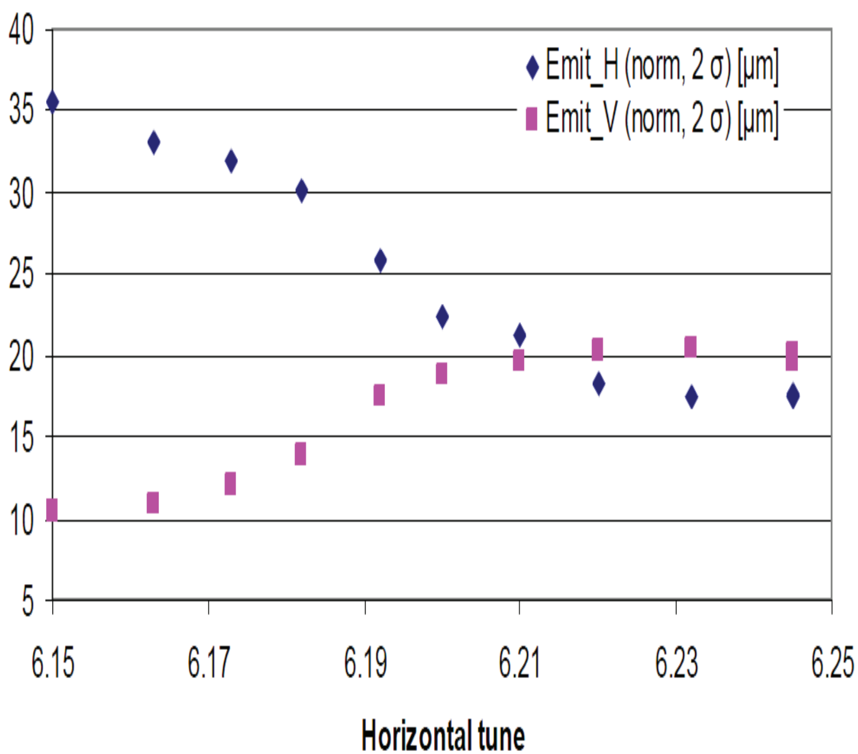


Synchrotron motion enhances the emittance exchange !

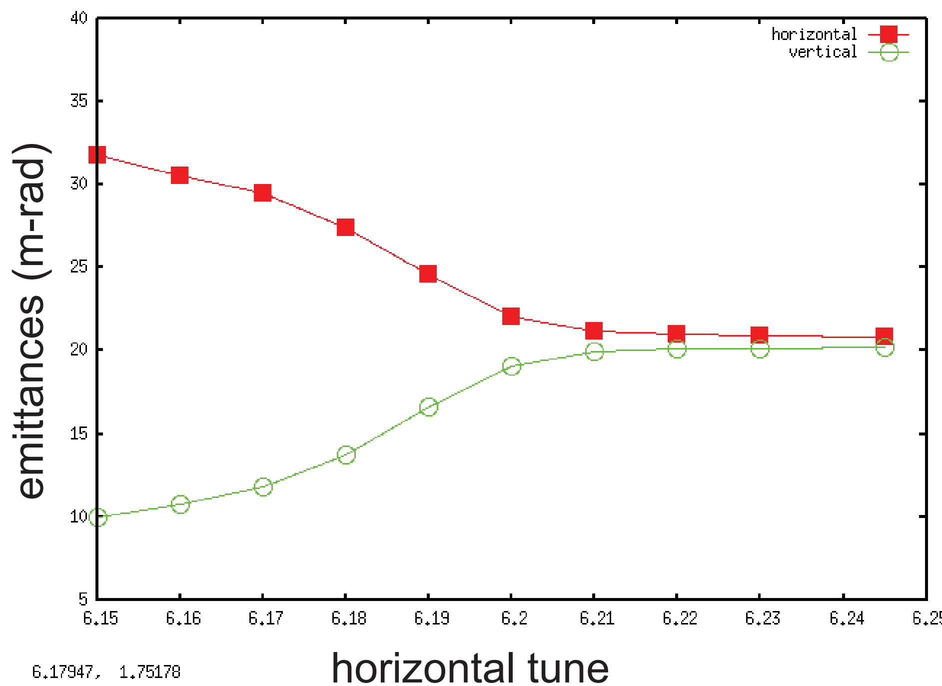
Dynamics Montague Resonance Crossing at PS (1)

100 ms dynamic Crossing

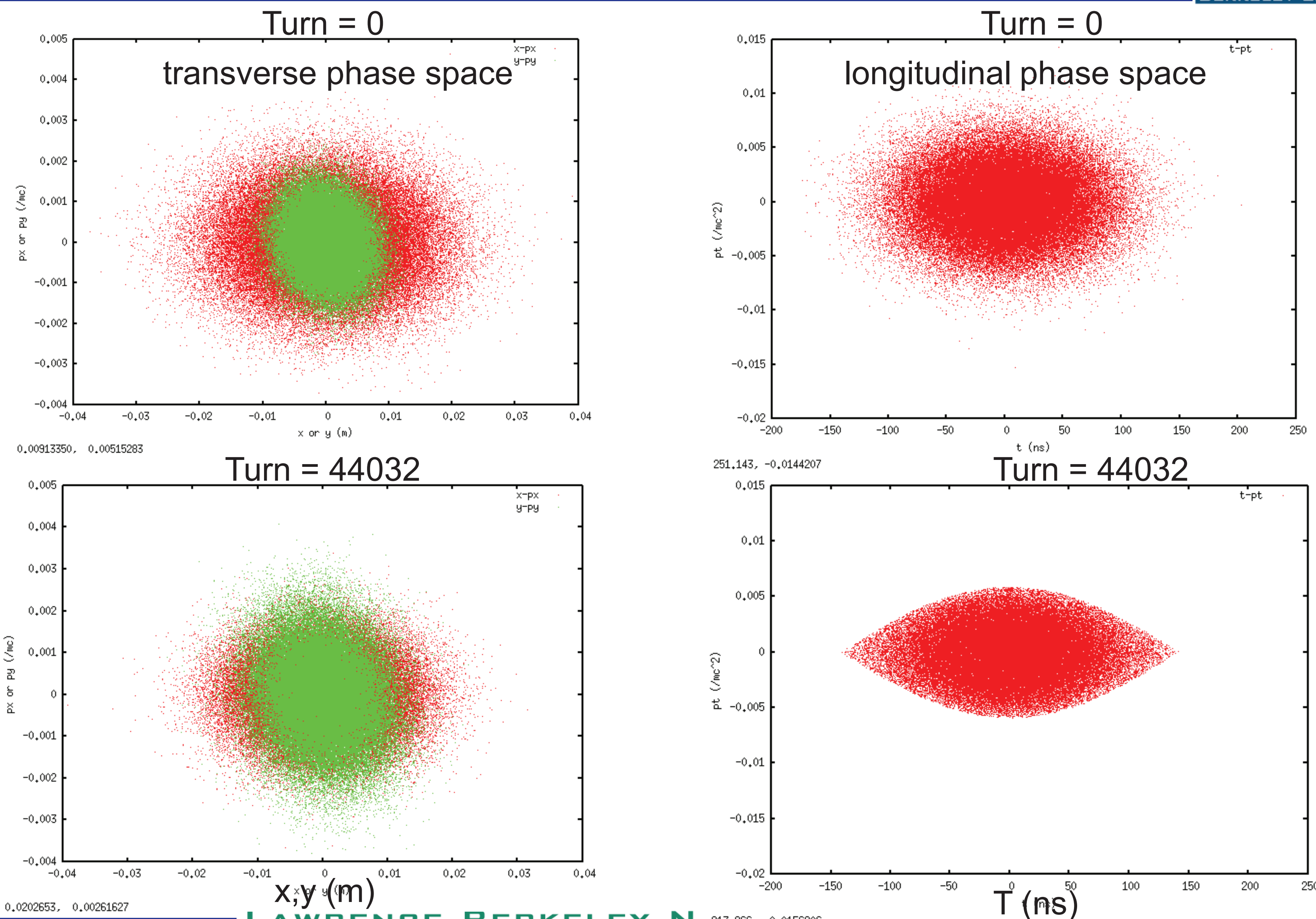
measurements



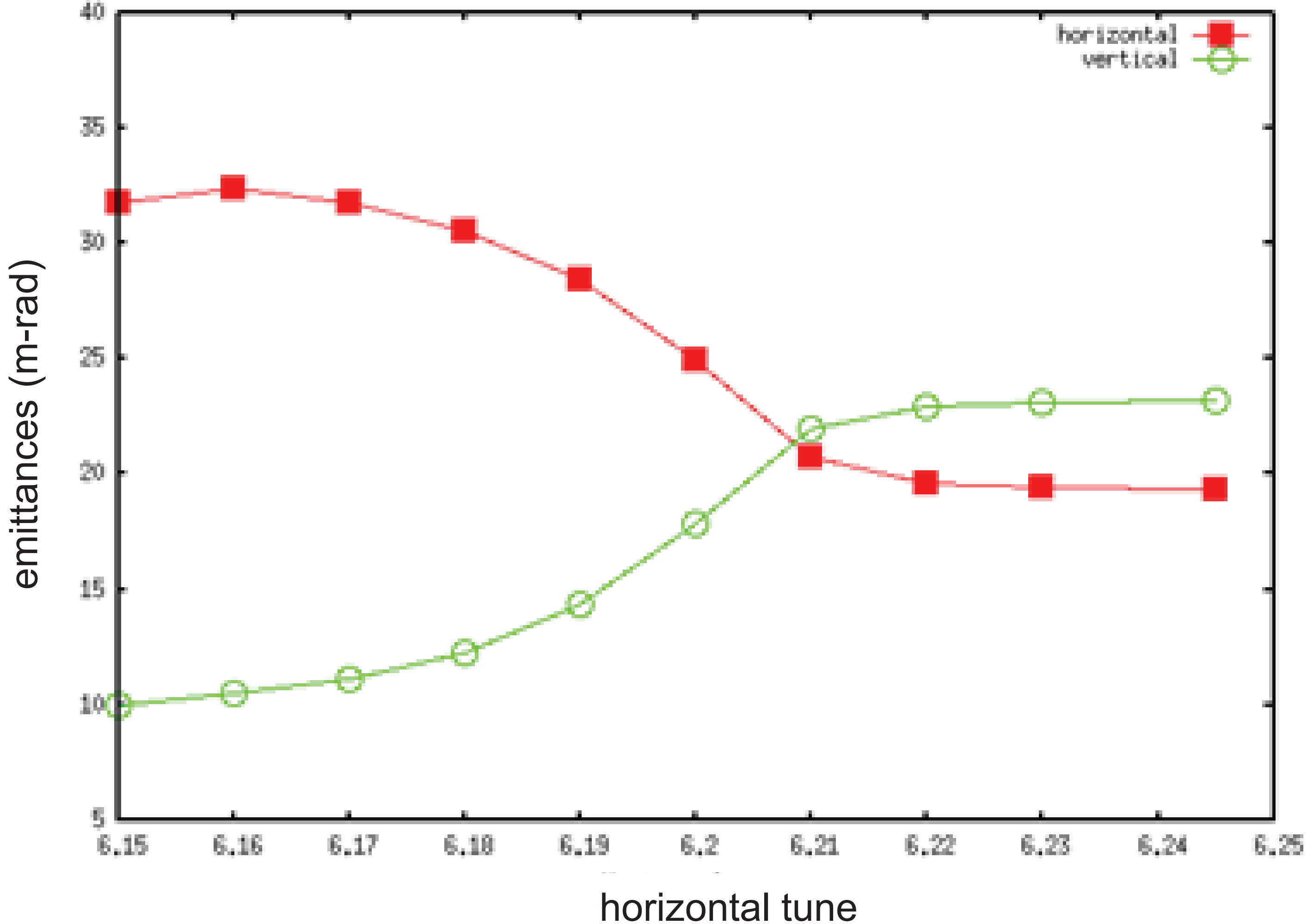
IMPACT simulation: fully 3D+nonlinear lattice



Initial and the Final Phase Space Distribution of the Dynamic Resonance Crossing



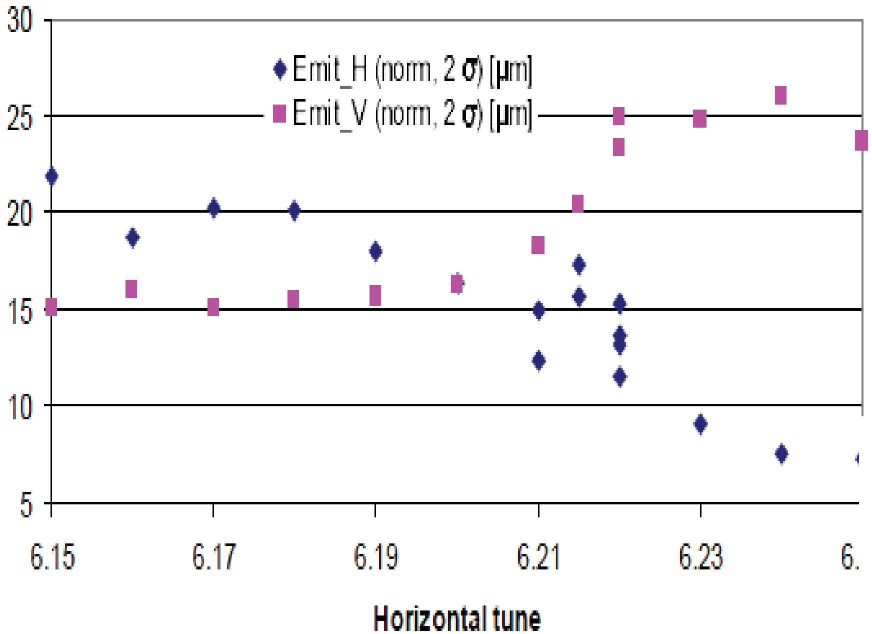
Simulation Dynamics Montague Resonance Crossing with Frozen Synchrotron Motion



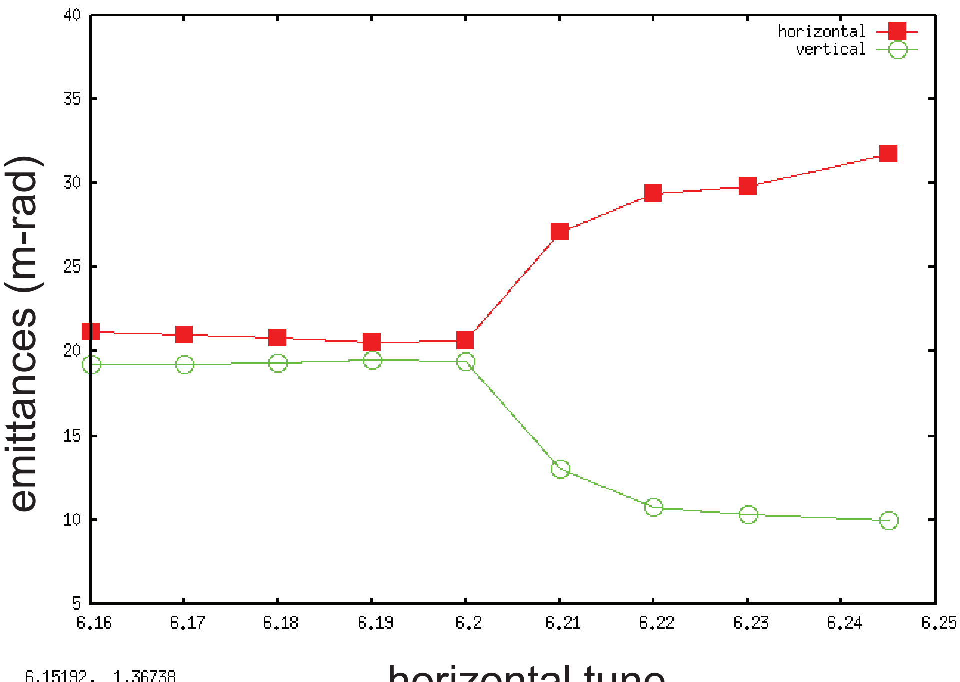
Dynamics Montague Resonance Crossing at PS (2)

100 ms dynamic Crossing

measurements



IMPACT simulation



Summary

- 3D self-consistent space-charge simulation reproduce the experiment data reasonably well
- Dynamic Montague resonance crossing shows no symmetry around the resonance stopband
- Longitudinal synchrotron motion helps the emittance exchange inside the resonance stopband