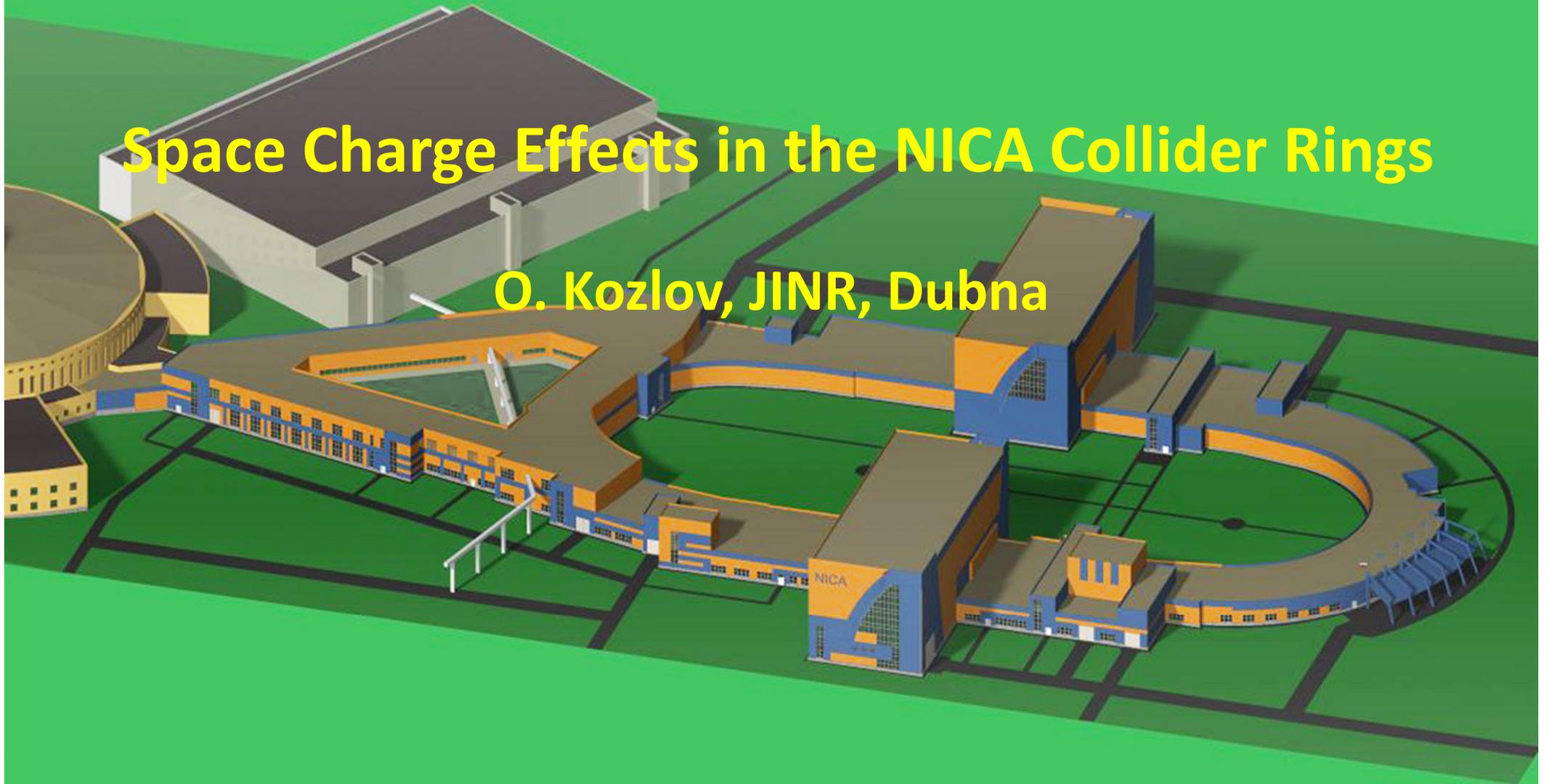


# Space Charge Effects in the NICA Collider Rings

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# Contents

1. Introduction: The goal of the project
2. Facility scheme and operation scenario
3. Collider Luminosity
4. Beam preparation scheme
5. Beam accumulation
6. Stochastic cooling
7. Electron cooling
8. Conclusion

# Introduction: The goal of the project

The goal of the project is

construction at JINR of a new accelerator facility that provides

1a) Heavy ion colliding beams  $^{197}\text{Au}^{79+} \times ^{197}\text{Au}^{79+}$  at

$$\sqrt{s_{\text{NN}}} = 4 \div 11 \text{ GeV} \text{ (} 1 \div 4.5 \text{ GeV/u ion kinetic energy )}$$

$$\text{at } L_{\text{average}} = 1\text{E}27 \text{ cm}^{-2}\cdot\text{s}^{-1} \text{ (at } \sqrt{s_{\text{NN}}} = 9 \text{ GeV)}$$

1b) Light-Heavy ion colliding beams of the same energy range and luminosity

2) Polarized beams of protons and deuterons in collider mode:

$$p\uparrow p\uparrow \sqrt{s_{\text{pp}}} = 12 \div 27 \text{ GeV} \text{ (} 5 \div 12.6 \text{ GeV kinetic energy )}$$

$$d\uparrow d\uparrow \sqrt{s_{\text{NN}}} = 4 \div 13.8 \text{ GeV} \text{ (} 2 \div 5.9 \text{ GeV/u ion kinetic energy )}$$

$$L_{\text{average}} \geq 1\text{E}30 \text{ cm}^{-2}\cdot\text{s}^{-1} \text{ (at } \sqrt{s_{\text{pp}}} = 27 \text{ GeV)}$$

3) The beams of light ions and polarized protons and deuterons for fixed target

experiments:

$$\text{Li} \div \text{Au} = 1 \div 4.5 \text{ GeV /u ion kinetic energy}$$

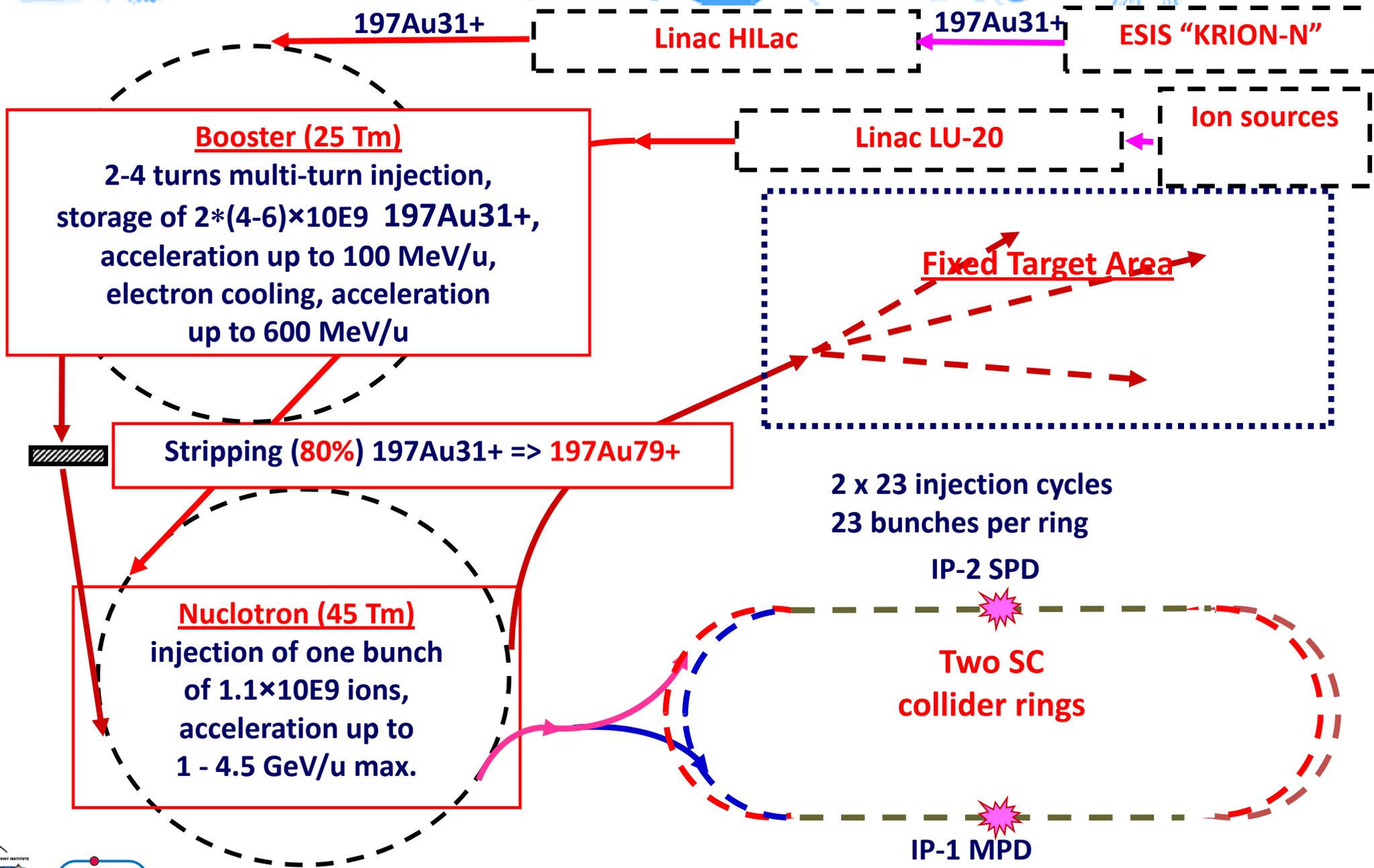
$$p, p\uparrow = 5 \div 12.6 \text{ GeV kinetic energy}$$

$$d, d\uparrow = 2 \div 5.9 \text{ GeV/u ion kinetic energy}$$

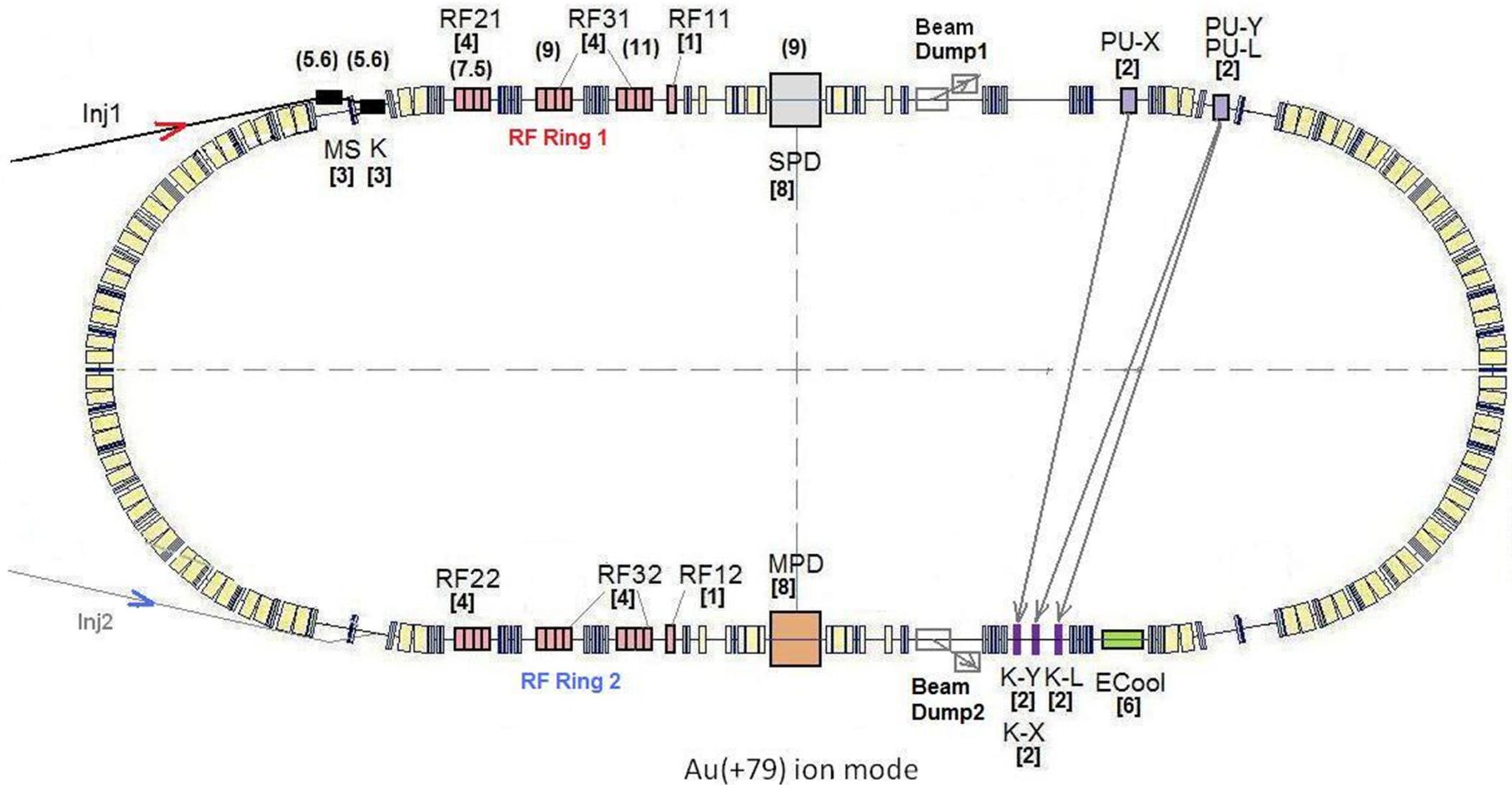
4) Applied research on ion beams at kinetic energy

from 0.5 GeV/u up to 12.6 GeV (p) and 4.5 GeV /u (Au)

# Facility scheme and operation scenario



# Collider Ring Composition. Ion Mode



# Collider Luminosity

## *NICA collider parameters and boundary conditions*

Ring circumference, m	503,04		
Number of bunches	23		
Rms bunch length, m	0.6		
Beta-function in the IP, m	0.35		
Betatron tunes, Qx/Qy	9.44/9.44		
Ring acceptance	40 $\pi \cdot \text{mm} \cdot \text{mrad}$		
Long. acceptance, dp/p	$\pm 0.010$		
Gamma-transition, $\gamma_{\text{tr}}$	7.091		
Ion energy, GeV/u	1.0	3.0	4.5
Ion number per bunch	$2.75 \cdot 10^8$	$2.4 \cdot 10^9$	$2.2 \cdot 10^9$
Rms dp/p, $10^{-3}$	0.62	1.25	1.65
Rms beam emittance, h/v, (unnormalized), $\pi \cdot \text{mm} \cdot \text{mrad}$	1.1/ 1.01	1.1/ 0.89	1.1/ 0.76
Luminosity, $\text{cm}^{-2}\text{s}^{-1}$	1.1e25	1e27	1e27
IBS growthe time, sec	190	700	2500

- 1. Beam emittance**  
(unnormalized)  $\varepsilon_b \leq 1$   
 $\pi \cdot \text{mm} \cdot \text{mrad}$ , limited by the  
ring acceptance
- 2.  $L(E_i) \geq 1E27 \text{ cm}^{-2}\cdot\text{s}^{-1}$  at  $3.5 < E_i < 4.5 \text{ GeV/u}$  – physics requirement**
- 3. Ion number per bunch is limited by injection chain and ion storage time duration:  $N_b \leq 2E9$  per bunch**

# Collider Luminosity

For identical round colliding bunches  
the peak luminosity :

$$L = \frac{N_b^2}{4\pi\epsilon\beta^*} F_C f_{HG}(\sigma_s, \beta^*),$$

Bunch length has to be small enough to  
decrease “hour-glass” effect and to  
provide luminosity concentration in the  
detector center, but very small length  
increases tune shift and coherent  
instability:

$$f_{HG}(\sigma_s / \beta^*) = \frac{1}{\sqrt{\pi}} \int_{-\infty}^{+\infty} \frac{\exp(-u^2) du}{1 + (u\sigma_s / \beta^*)^2}$$

Beam intensity is limited by space  
charge effects – “Tune shift criteria”:

$$\Delta Q = \frac{Z^2 r_p}{A} \frac{N_b}{4\pi\beta^2 \gamma^3 \epsilon} F_{SC} F_b, \quad F_b = \frac{C_{Ring}}{\sqrt{2\pi\sigma_s}}$$

1. The Laslett tune shift – most strong:
2. Beam-beam parameter:

$$\xi = \frac{Z^2 r_p N_b (1 + \beta^2)}{A 4\pi\beta^2 \gamma \epsilon}$$

For practical estimates the numerical  
criterion for beam stability is used:

$$\Delta Q_{total} = \Delta Q + n_\xi \xi \leq 0.05,$$

$$n_\xi = 2 - \text{number of IPs}$$

# Collider Luminosity

From the Formulae above one can derive the simple relations between parameters:

$$\left. \begin{aligned} L &\propto \frac{N_b^2}{\varepsilon} \cdot f_1(E_i) \cdot f_{HG} \\ \Delta Q &\propto \frac{N_b}{\varepsilon} \cdot f_2(E_i) \end{aligned} \right\} \Rightarrow L \propto \Delta Q^2 \cdot \varepsilon \cdot f_3(E_i) \cdot f_{HG} \quad N_b \propto \Delta Q \cdot \varepsilon \cdot f_4(E_i)$$

At fixed  $\Delta Q = \Delta Q_{max} \approx 0.05$  maximum luminosity is achieved when all acceptance is filled with ions!

“Space Charge Dominated Regime” (SCD Regime)

$$\tau_{cool} < \tau_{IBS}$$

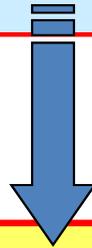


# Collider Luminosity

Then at fixed Luminosity:

$$\left. \begin{aligned} L &\propto \frac{N_b^2}{\varepsilon} \cdot f_1(E_i) \cdot f_{HG} \\ \Delta Q &\propto \frac{N_b}{\varepsilon} \cdot f_2(E_i) \end{aligned} \right\} \Rightarrow \text{if } L = \text{const} = 10^{27} \Rightarrow$$

$$N_{ion} \propto \sqrt{L \cdot \varepsilon} \cdot f_4(E_i, \beta^*, \sigma_s), \quad \Delta Q \propto \sqrt{\frac{L}{\varepsilon}} \cdot f_5(E_i, \beta^*, \sigma_s) < \Delta Q_{\max} = 0.05$$



If luminosity can be limited (for some “not beam related” reasons  
– e.g., detector performance) one can have

***IBS Dominated Regime:***

$$\tau_{IBS} = \tau_{cooling}$$

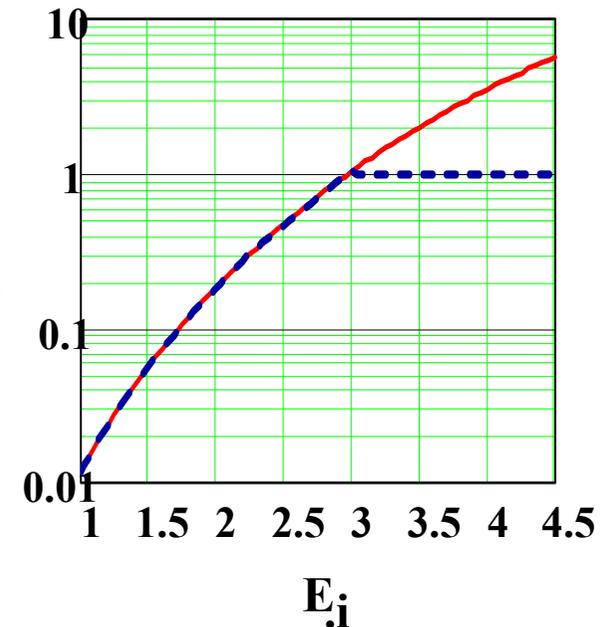
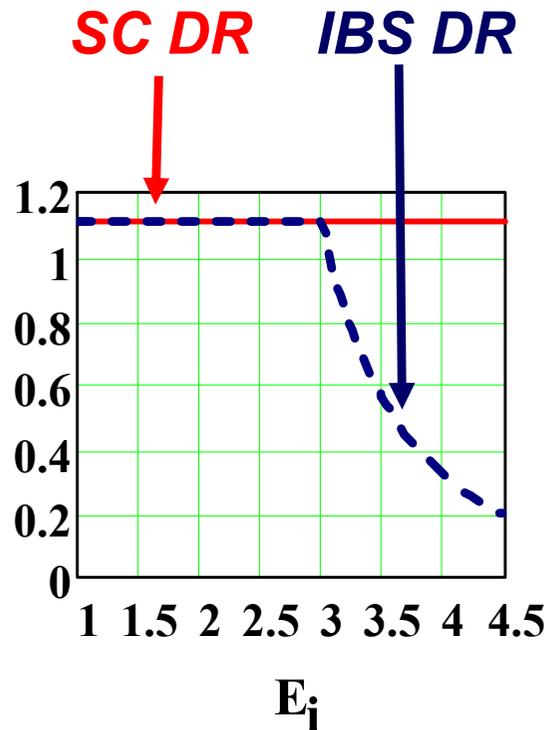
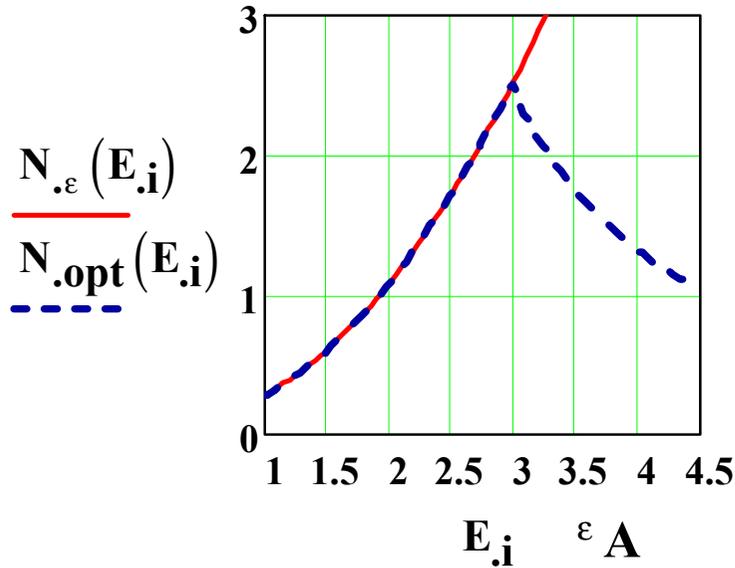


# Collider Luminosity

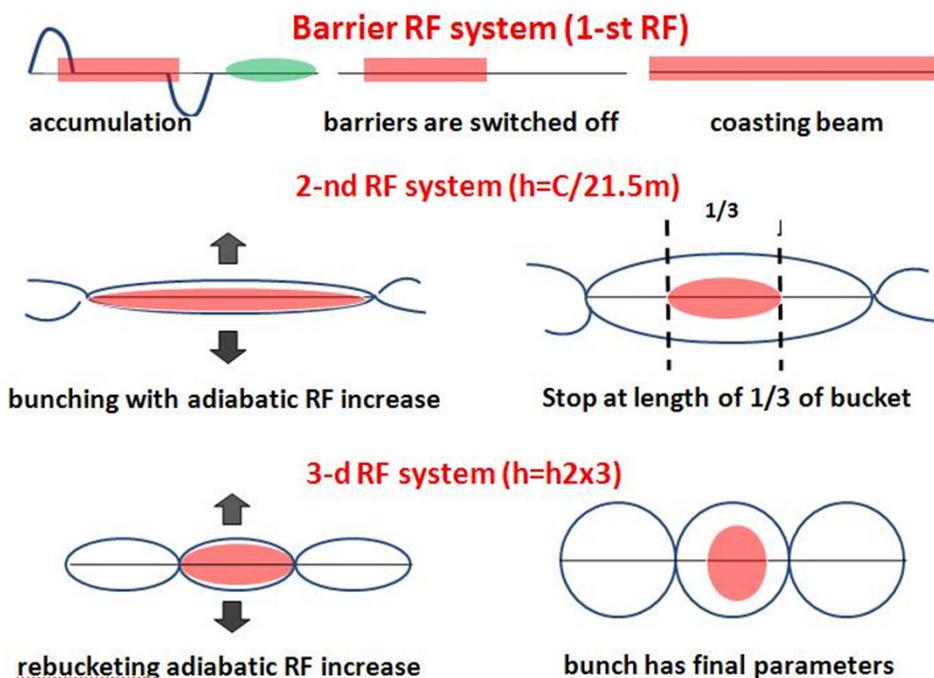
## Energy Ranges of Two Regimes

— **A) Acceptance is filled with ions up to  $\Delta Q = \Delta Q_{max} = 0.05$ ,  $L = L_{max}$**

- - - **B) Optimal regime:  $L = \begin{cases} L_{max} & \text{at } 1 \leq E_i \leq 3 \text{ GeV/u} , \\ 1E27 = \text{const} & \text{at } 3 \leq E_i \leq 4.5 \text{ GeV/u} . \end{cases}$**



# Beam preparation scheme



## Beam storage at the experiment energy :

- 1. RF barrier bucket system (RF1)**  
allowing storage of the required beam intensity
- 2. 1<sup>st</sup> narrow-band RF system (RF2)**  
operating at harmonics of revolution frequency corresponding to the bunch number; it provides the beam bunching.
- 3. 2<sup>nd</sup> narrow-band RF system (RF3)**  
operating at harmonics number larger than the 1<sup>st</sup> one, that provides the bunch length necessary for collision experiments.

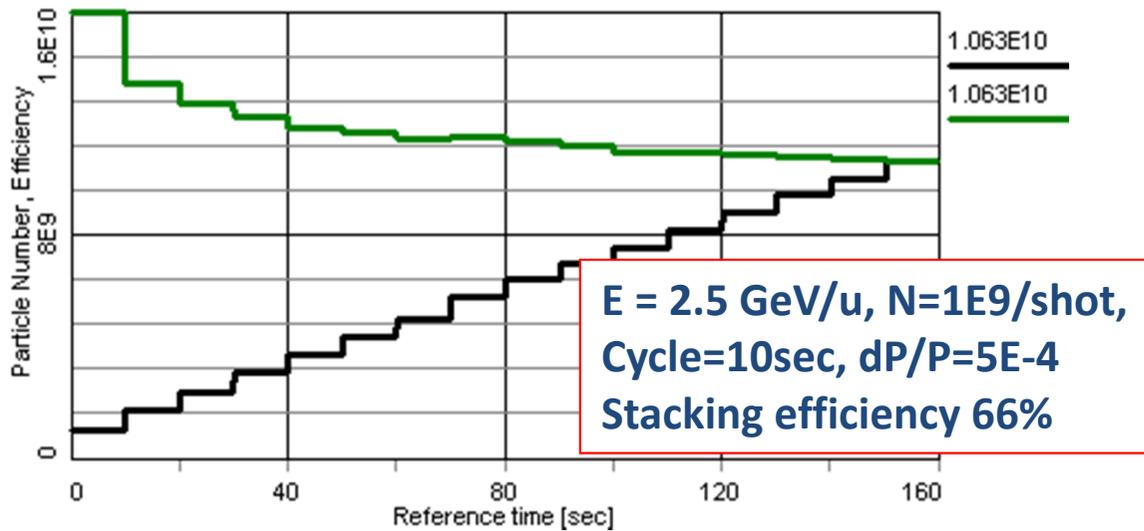
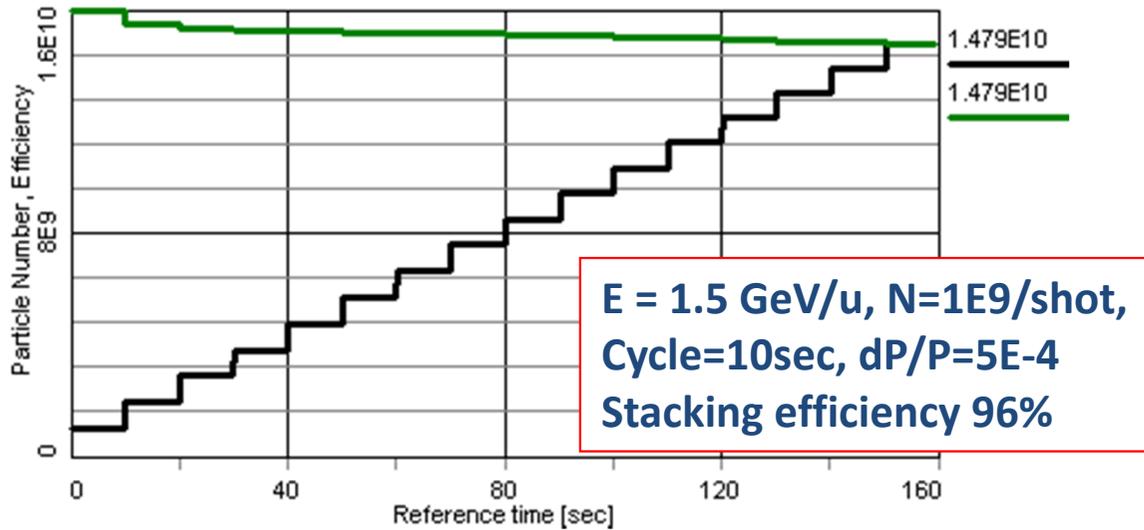
All stages are provided with cooling

## Main parameters of RF systems

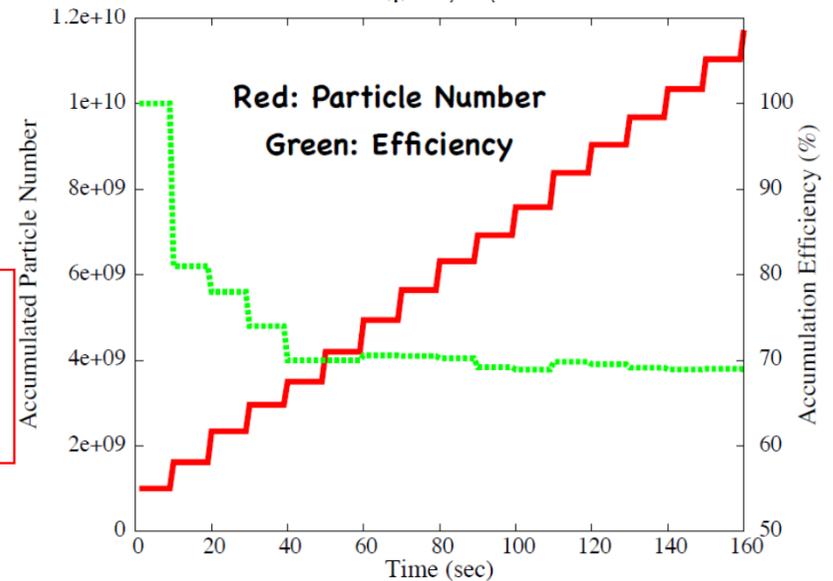
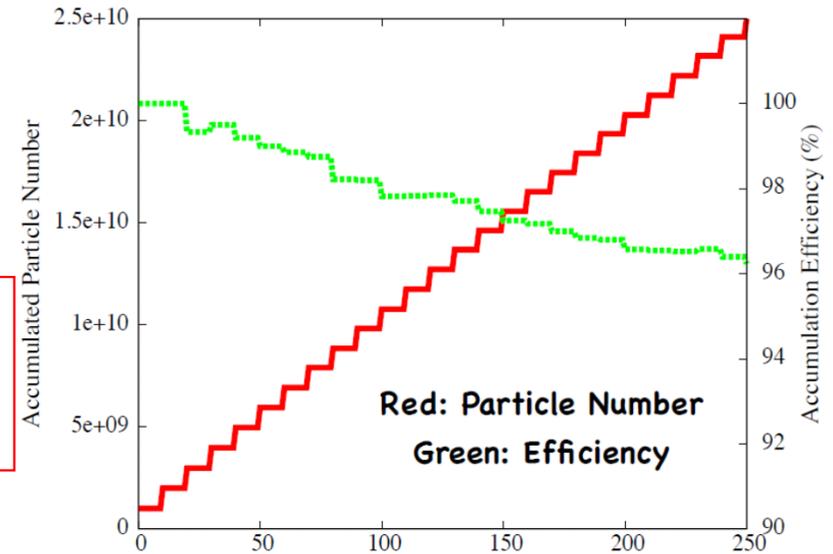
	RF1	RF2	RF3
Frequency, MHz	BB	11.4-12.8	34.2-38.4
Total voltage ampl., kV	5	100(50)	1000
Voltage/resonator, kV	5	25	125
Number of resonators	1	4	8
Resonator length, m	0.8	1.1	1.1
Total length, m	0.8	4.4	8.8

# Beam stacking with electron cooling

**A.Smirnov (Betacool)**

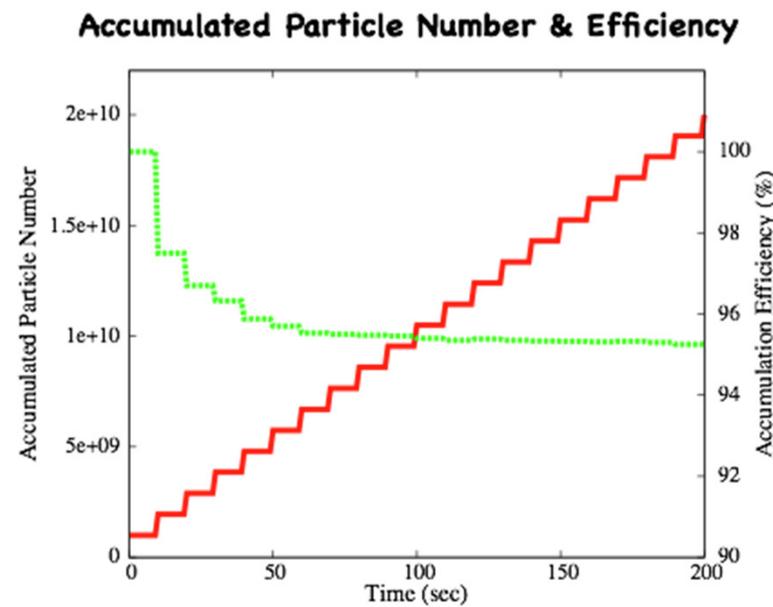
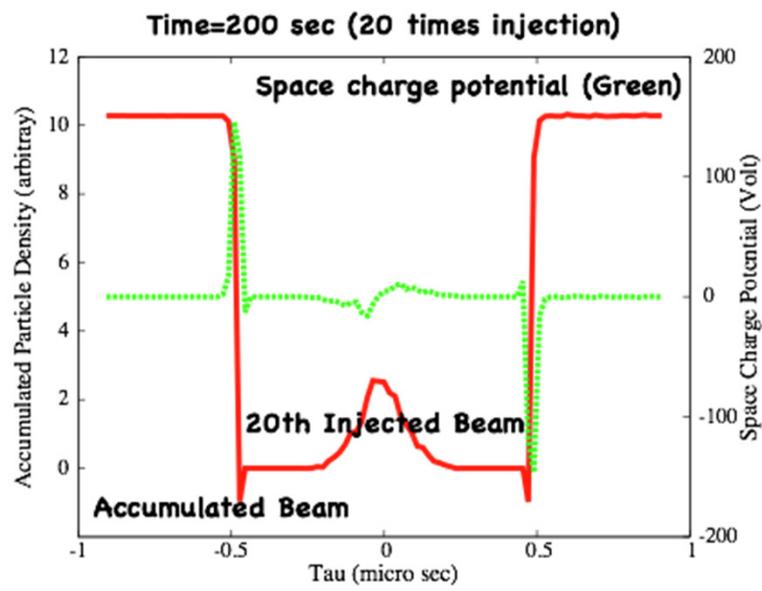
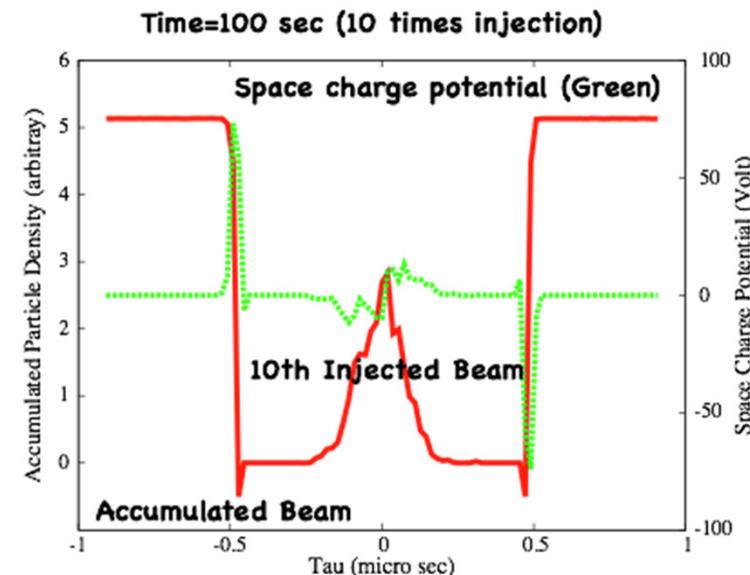
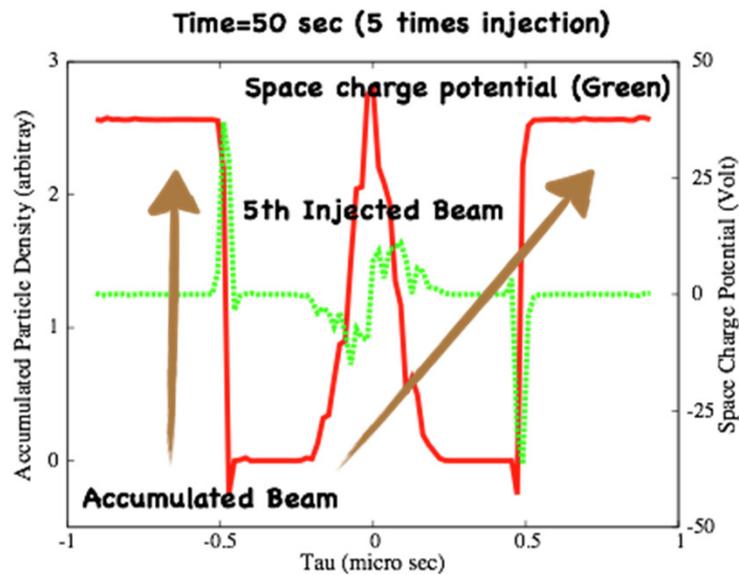


**T.Katayama**



# Space charge effect during stacking and bunching

(T.Katayama)

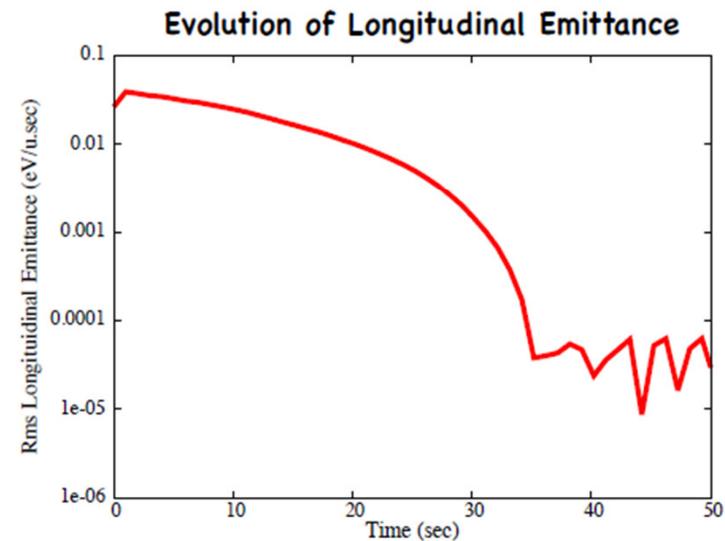
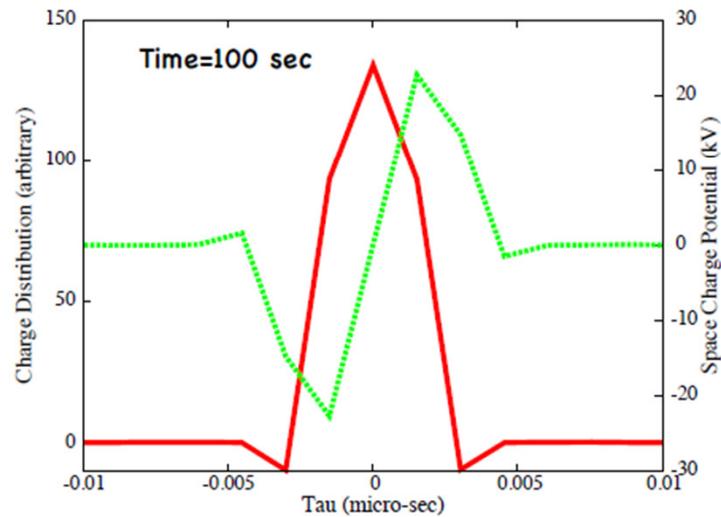
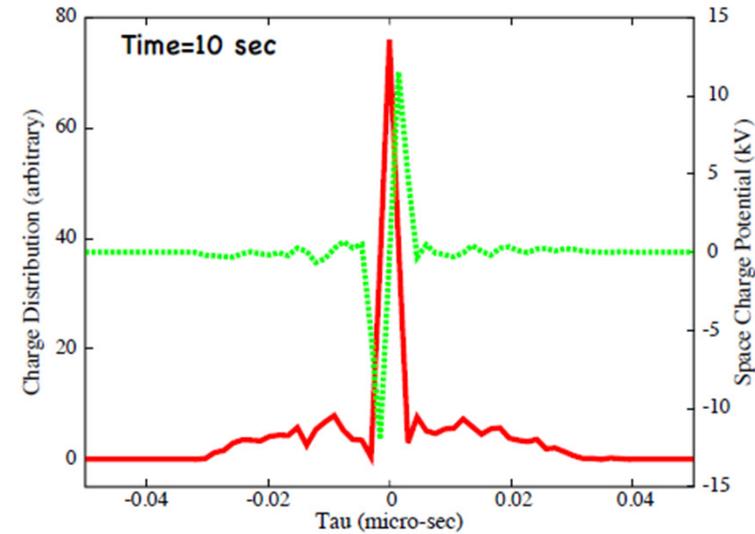
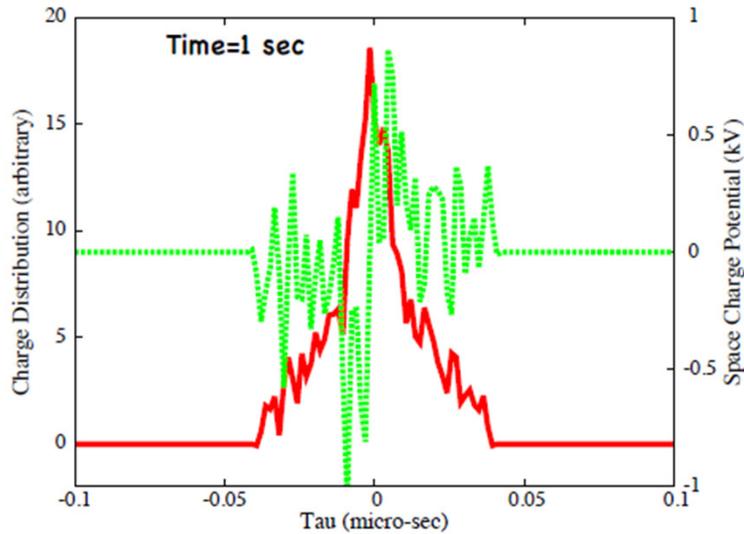


1.5 GeV/u

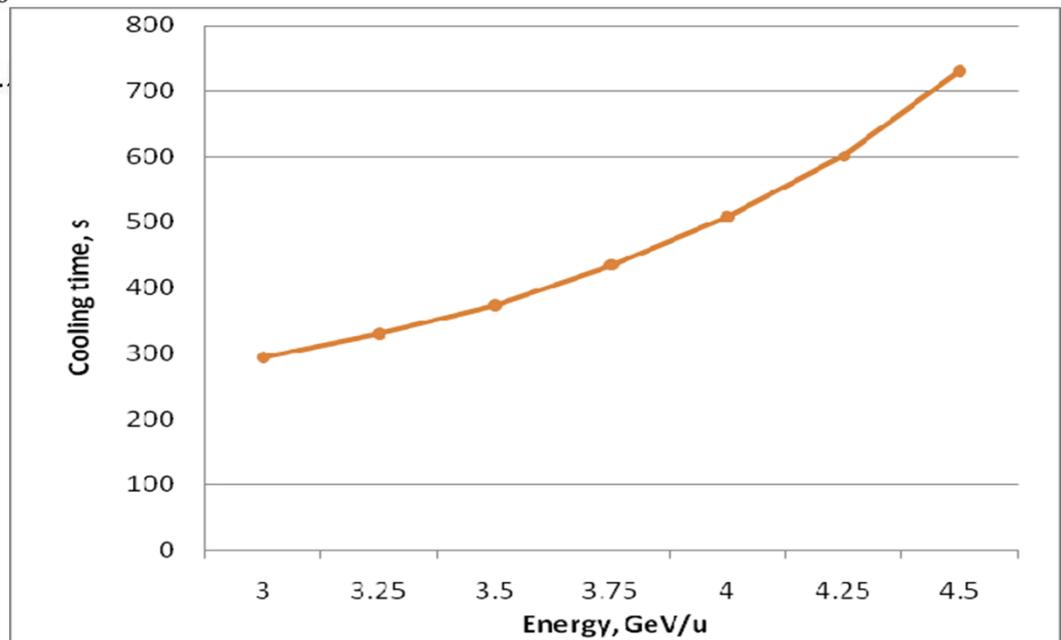
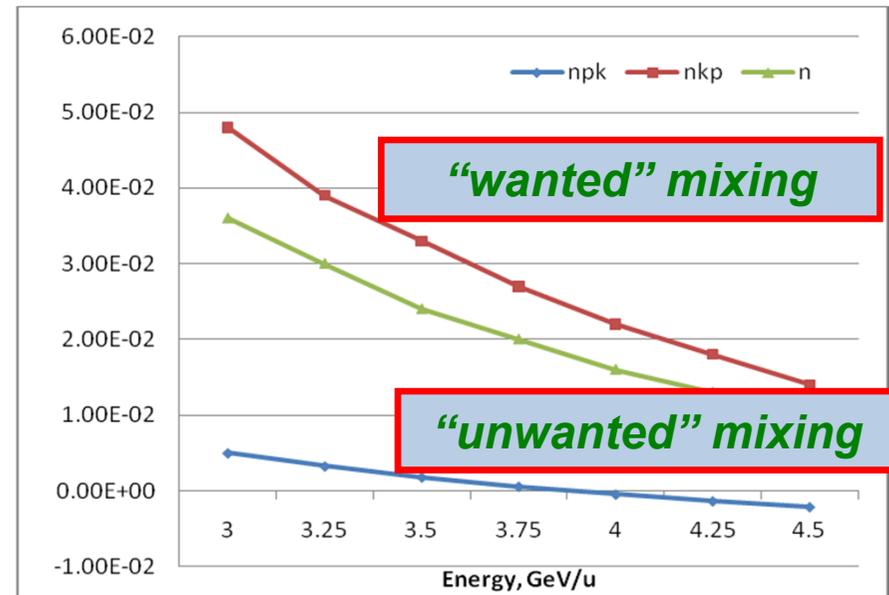
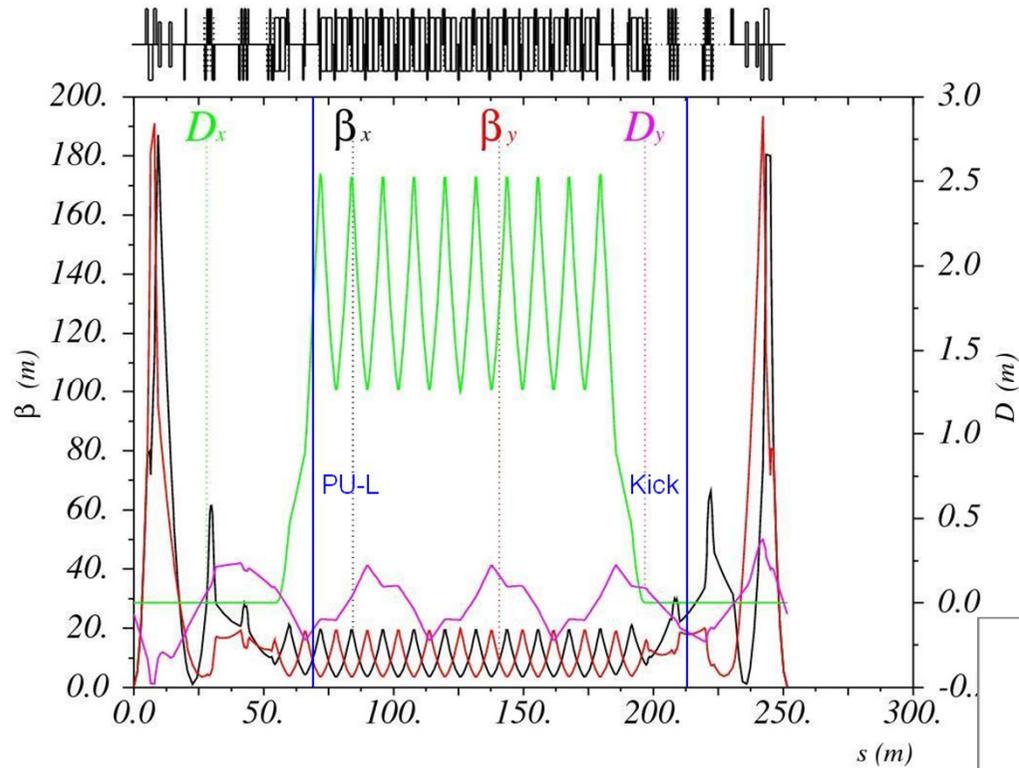
# Formation of the bunch shape

T.Katayama

$E_k=1.5$  GeV/u,  $N=1e9$ , RF voltage=200kV,  $\eta=0.1268$ ,  $dp/p(\text{initial})=5e-4(\text{rms})$  (Gaussian)



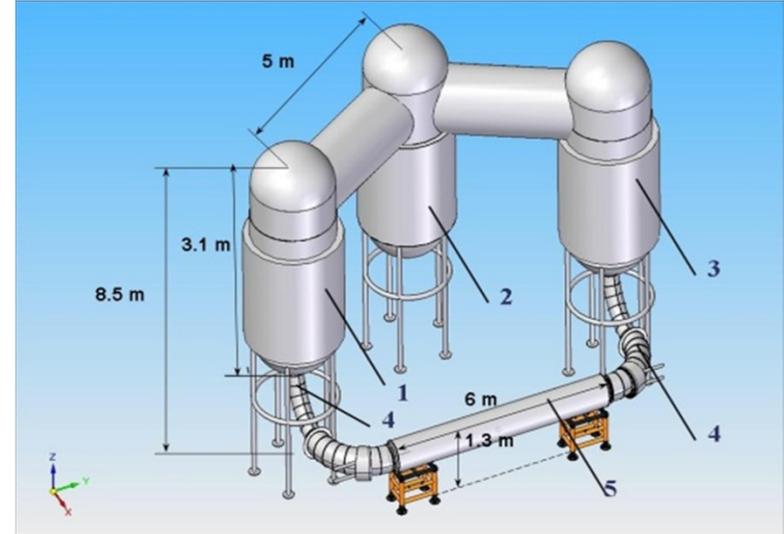
# Stochastic cooling (3-4.5 GeV/u)



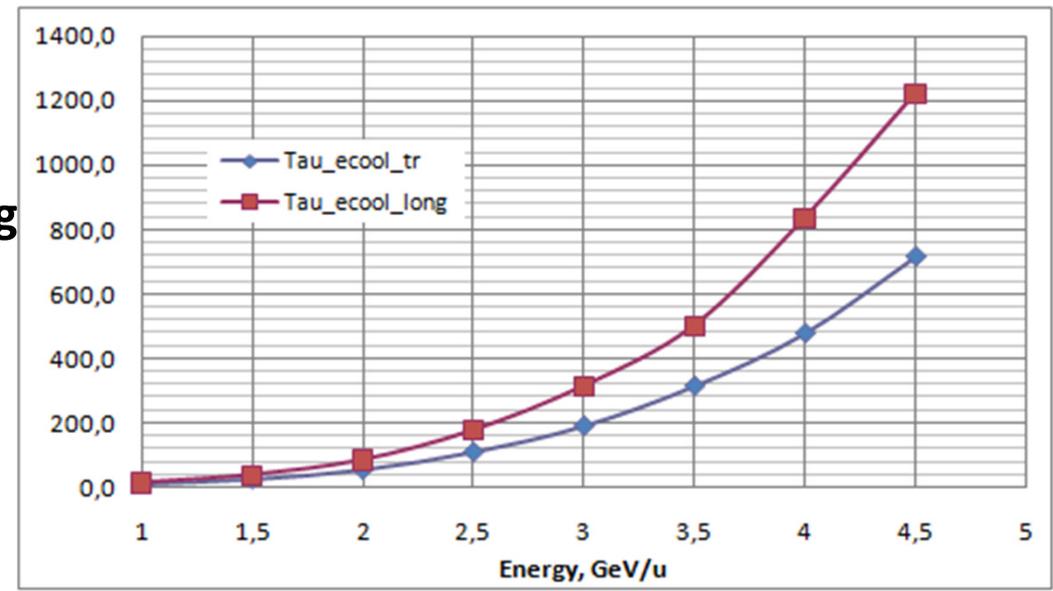
**Bandwidth from 3 to 6 GHz**  
**Cooling times varies by about 2 times**  
**In the energy range from 3 to 4.5 GeV/u**

# Electron cooling

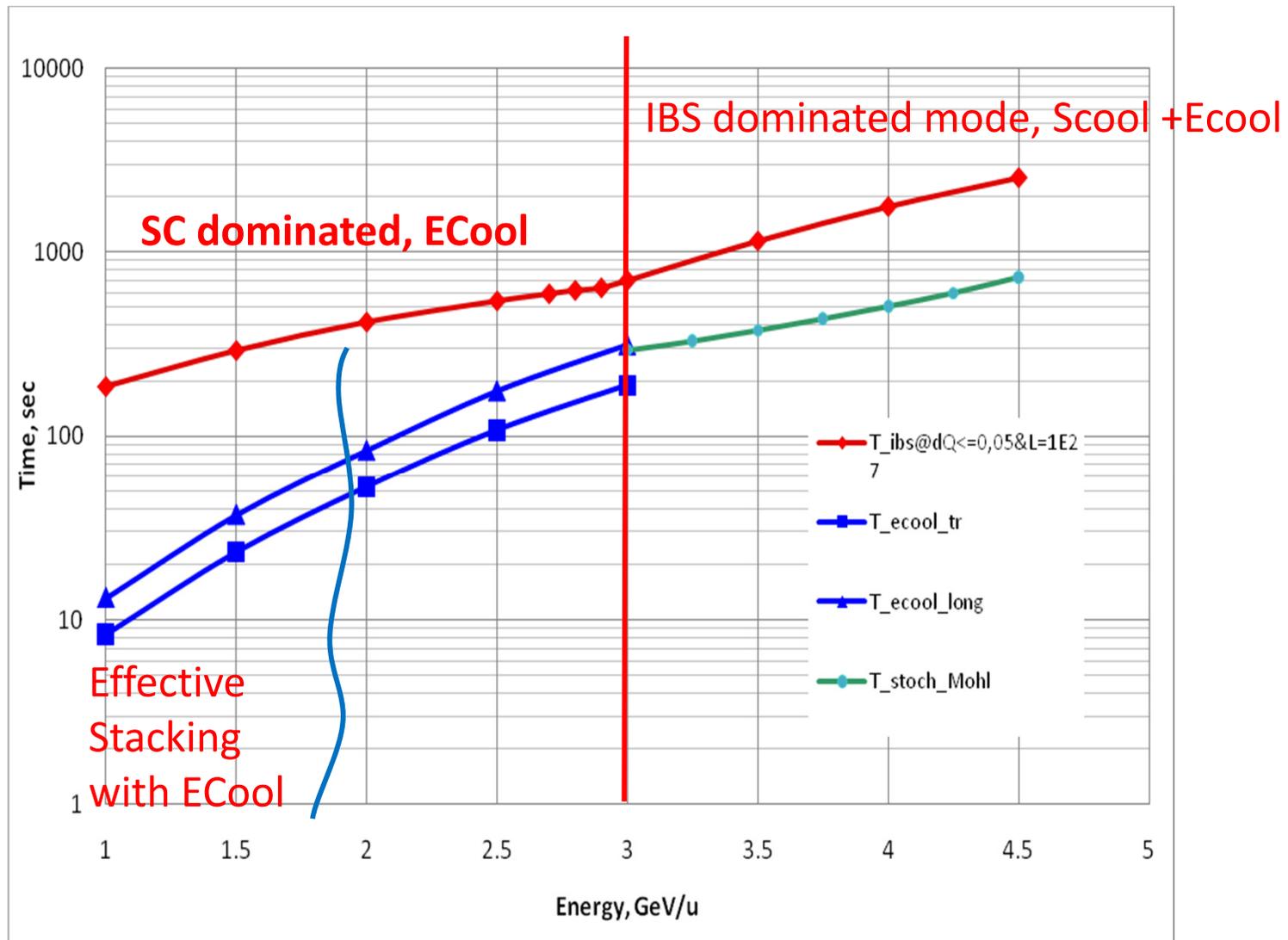
Maximum electron energy, MeV	2.5
Cooling section length, m	6.0
Electron beam current, A	1
Electron beam radius, cm	1
Magnetic field in cooling section, T	0.2
Magnetic field imperfection in cooling section	$2 \times 10^{-5}$
Beta functions in cooling section, m	16
Longitudinal electron temperature meV	5.0



**At higher energies 3-4.5 GeV/u:**  
**ECooling times comparable with IBS heating times and SCooling times;**  
**At lower energies 1-3 GeV/u:**  
**ECooling times ~20 times shorter than IBS heating times**



# Strategy of the cooling at experiment



IBS is calculated for equal rates in 3 degrees of freedom

# Conclusion

1. Collider has 2 modes of operation: Space Charge Dominated Regime (1-3 GeV/u) and IBS Dominated Regime (3-4.5 GeV/u)
2. Beam Cooling techniques are used for formation of high intensity and low emittance ion beams, and for providing the required luminosity life time
3. Stochastic cooling sufficient for IBS suppression is sufficient for beam stacking also
4. Electron cooling can be used for cooling at experiment in the total energy range
5. Electron cooling can provide effective stacking at small energy only
6. At energy larger than 3 GeV/u the experiment can be provided using electron cooling as well as stochastic, or combination of both methods
7. At energy below 3 GeV/u the experiment is provided using electron cooling. Possibility to increase of luminosity at minimum energy is related with space charge dominated mode

**Thank you for your attention!**