

# *Emittance control in the presence of collective effects in the FERMI@Elettra FEL linac driver*

**S. Di Mitri, on behalf of *FERMI Commissioning Team***

## Outline

- FERMI FEL and importance of *projected* transverse emittance
- Sources of emittance growth. Beam matrix formalism.
- Coherent synchrotron radiation (CSR) {  
in magnetic compressor  
in high energy transfer line}
- Geometric transverse wakefield (GTW) {  
in collimator  
in RF linac}
- 4-D e-beam brightness in presence of CSR and GTW:  
model, validation and optimization studies
- FERMI linac emittance budget



Elettra  
Sincrotrone  
Trieste

is a nonprofit shareholder company of **national interest**, established in Trieste, Italy in 1987 to **construct and manage synchrotron light sources as international facilities**.

**FERMI (Free Electron Laser):  
100 – 4 nm HGHG, fully funded.**

- $E = 0.9 - 1.5 \text{ GeV}$
- $Q \leq 500 \text{ pC}$
- $I \geq 400 \text{ A}$
- $\varepsilon_n \text{ slice} \approx I \text{ } \mu\text{m rad}$

**ELETTRA (Synchrotron Light Source);  
up to 2.4 GeV, top-up mode,  
~800 proposals from 40 countries every year**



## FEL requirements for electron beam

- Compactness and high intensity of FEL require high 6-D e-beam brightness,  $Q/(\varepsilon_x \varepsilon_y \varepsilon_z)$ , on the scale length of the *FEL slippage*:

$$P_{FEL}(z) \sim e^{z \frac{\rho}{\lambda_u}} \sim e^{z \left( \frac{I_{pk}}{\sigma_{\perp}} \right)^{1/3}}$$

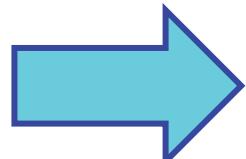
$$\varepsilon_n \leq \frac{\gamma \lambda}{4\pi}$$

$$\sigma_{\delta} < \rho$$

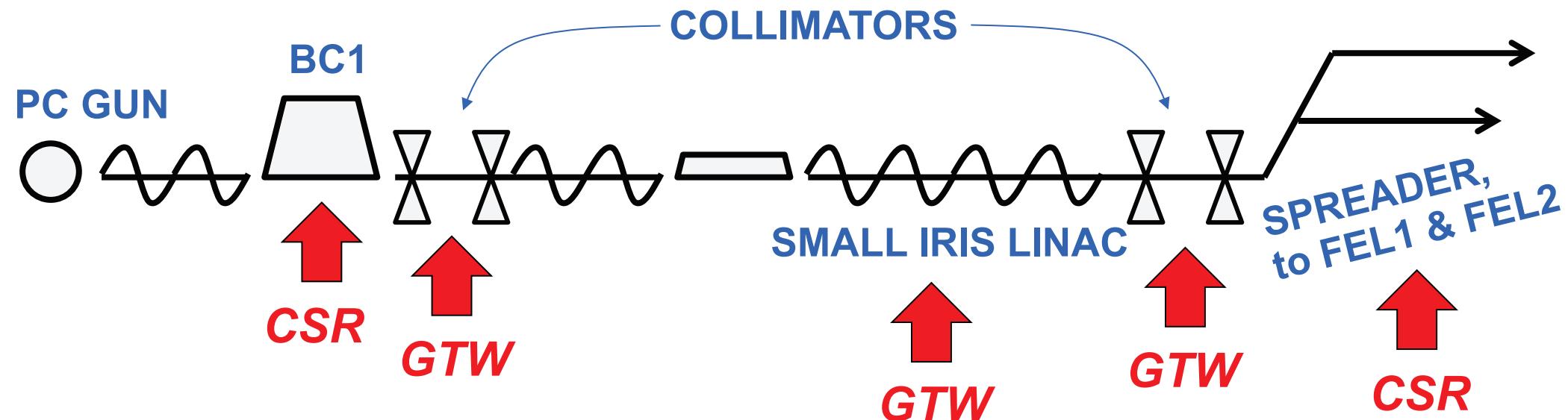
However...

- Collective effects may establish correlations between slices' coordinates (i.e., projected emittance growth) that affect the FEL wavelength and bandwidth [G. Andonian et al., PRL 95, 054801 (2005); G.Penn et al., ST/F-TN-06/01 (2006)].
- Control of e-beam size and angular divergence requires optics matching (i.e., projected Twiss functions).

**Control of FEL and e-beam slice parameters is inferred by the measurement and control of e-beam projected values.**



## Sources of transverse emittance growth



Particle distribution is assumed to be locally kicked by  $\Delta^2 = \langle \Delta x'^2 \rangle$ .  
The perturbed emittance is estimated with the beam matrix:

$$\tilde{\varepsilon} = \sqrt{\det \begin{pmatrix} \langle x^2 \rangle & \langle xx' \rangle \\ \langle xx' \rangle & \langle x'^2 \rangle + \langle \Delta x'^2 \rangle \end{pmatrix}} = \sqrt{\det \varepsilon \begin{pmatrix} \beta & -\alpha \\ -\alpha & \gamma + \Delta^2 \end{pmatrix}} = \sqrt{\varepsilon^2 \left( 1 + \frac{\beta \Delta^2}{\varepsilon} \right)} \quad (1)$$

[M. Dohlus, T. Limberg, PAC'05; Emma, ICFA 38 (2005)]

It may work for CSR in a dipole and GTW in a collimator .

Transverse emittance preservation during bunch compression in the Fermi free electron laser

S. Di Mitri,\* E. M. Allaria, P. Craievich, W. Fawley, L. Giannessi, A. Lutman, G. Penco, S. Spampinati, and M. Trovo

Sincrotrone Trieste, Trieste, Italy

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# CSR in magnetic compressor (BC1)

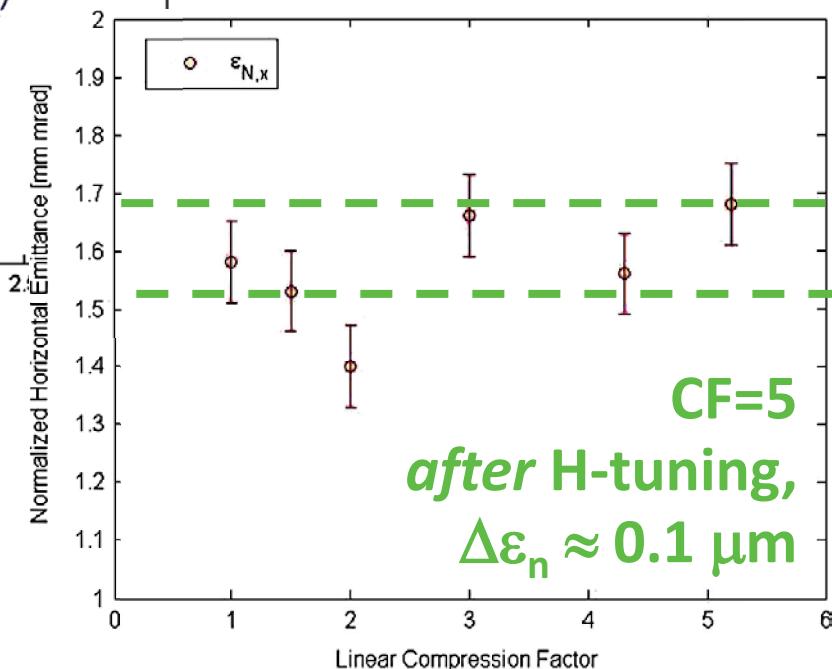
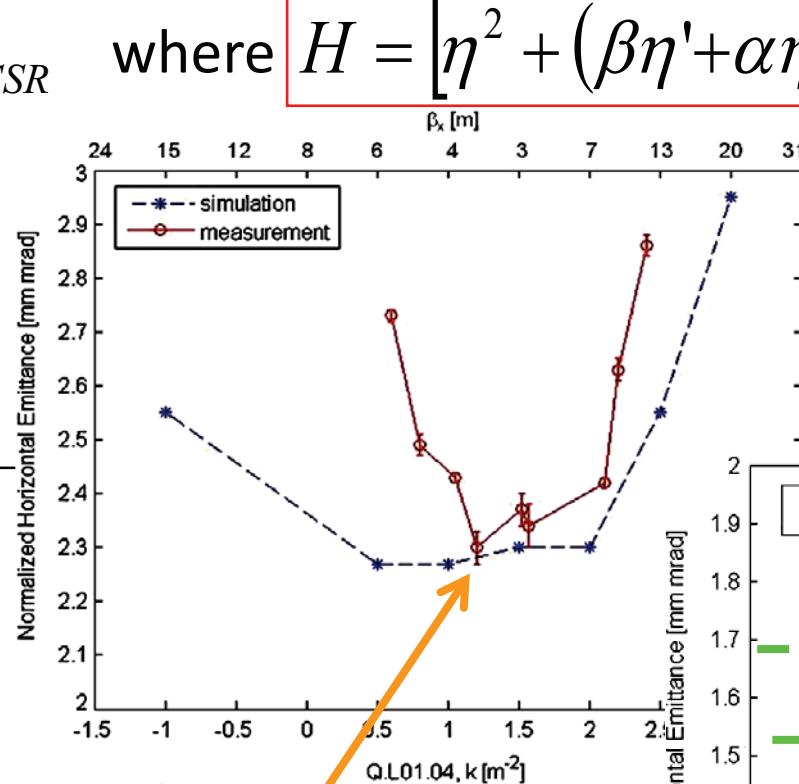
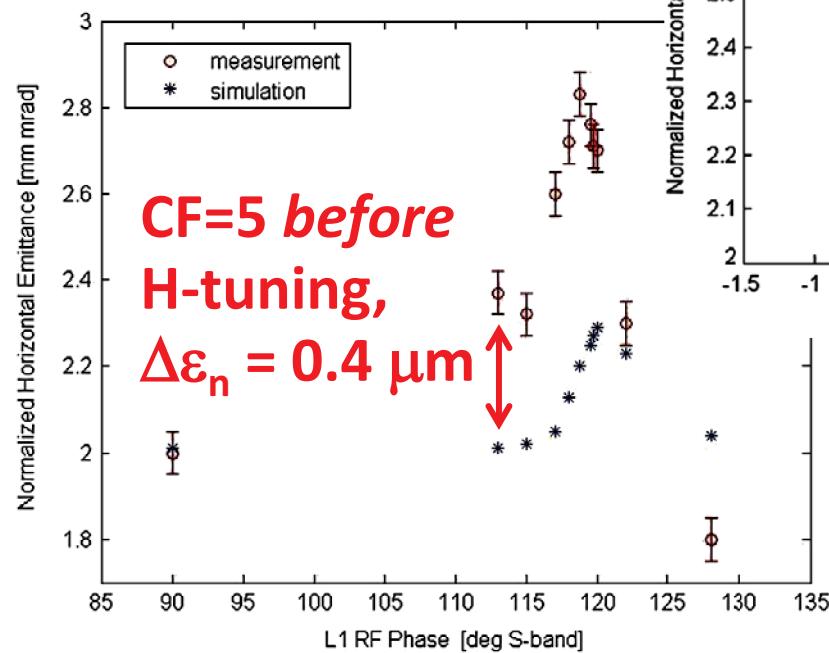
Assume  $\varepsilon$ -growth is dominated by CSR in the last dipole magnet.

$$\beta\Delta^2 \text{ in Eq.1} \rightarrow H\sigma_{\delta,CSR}^2$$

$$\text{where } H = \left[ \eta^2 + (\beta\eta' + \alpha\eta)^2 \right] / \beta,$$

$$\sigma_{\delta,CSR} \propto 1/\sigma_z^{4/3}$$

From injector:  
200pC, 6ps FWHM



## Cancellation of Coherent Synchrotron Radiation Kicks with Optics Balance

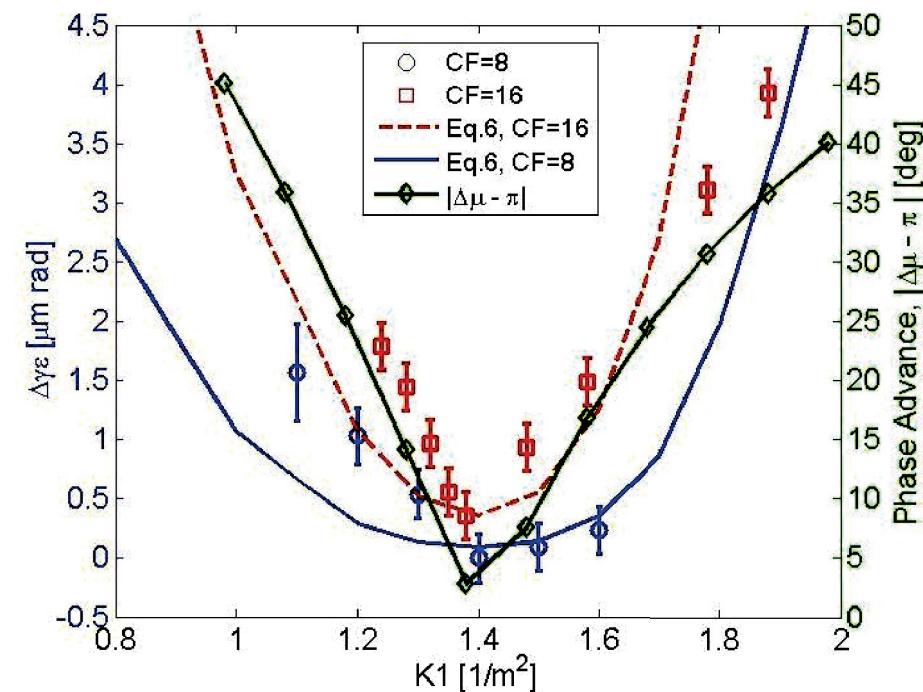
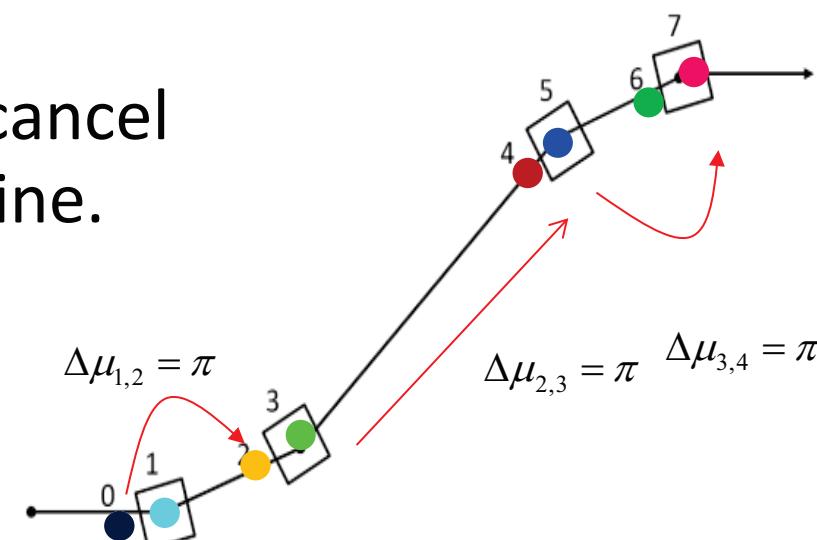
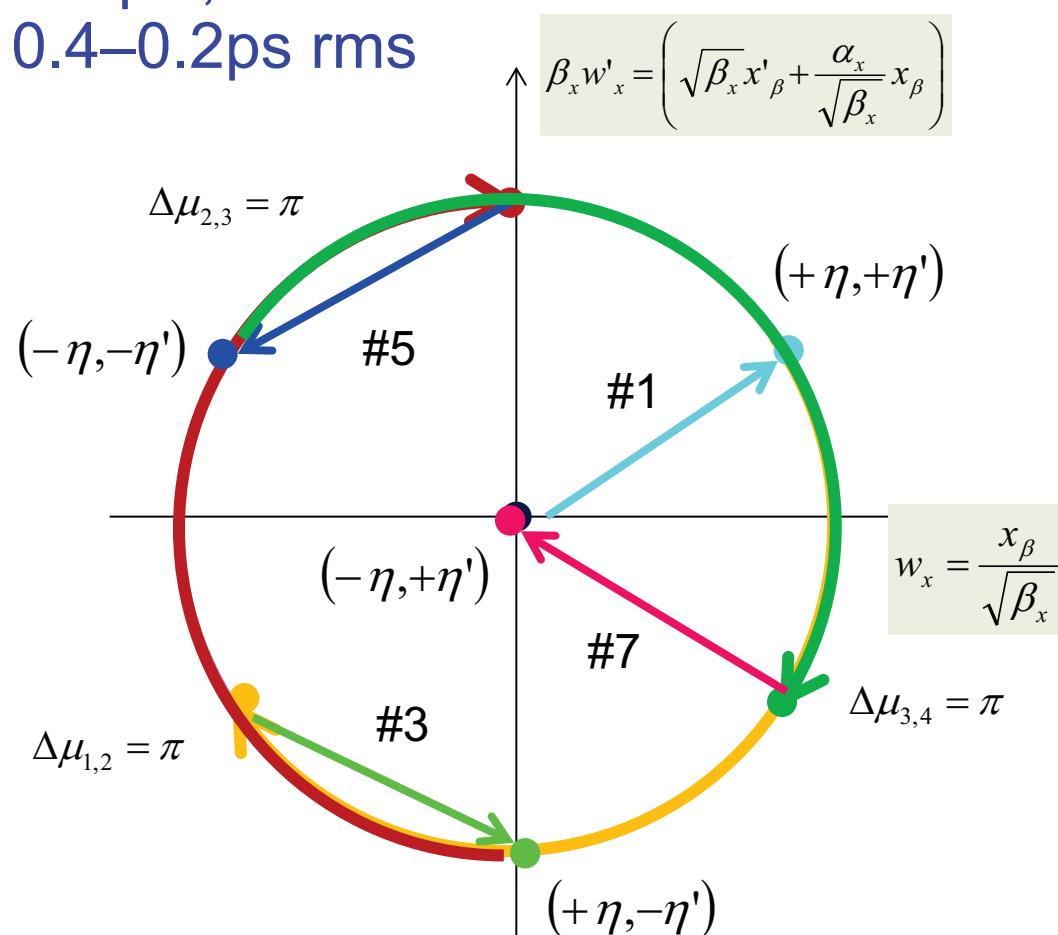
S. Di Mitri,<sup>1</sup> M. Cornacchia,<sup>1</sup> and S. Spampinati<sup>2</sup><sup>1</sup>Elettra-Sincrotrone Trieste S.C.p.A., 34149 Basovizza, Trieste, Italy<sup>2</sup>University of Nova Gorica, SI-5000 Nova Gorica, Slovenia

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## CSR in high energy transfer line (Spreader)

Sum of CSR kicks in all dipoles finally cancel by virtue of optics balance along the line.

500pC,  
0.4–0.2ps rms



## Influence of longitudinally tapered collimators on a high brightness electron beam

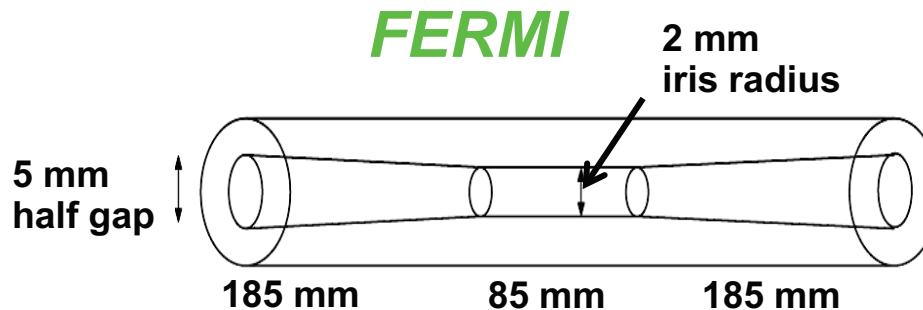
S. Di Mitri, L. Froehlich, and E. Karantzoulis

Sincrotrone Trieste, 34149 Basovizza, Trieste, Italy

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**GTW in collimator**

$\Delta^2$  in Eq.1 is here the GTW's rms kick,  $\Delta = hQ\kappa_{rms}/E$

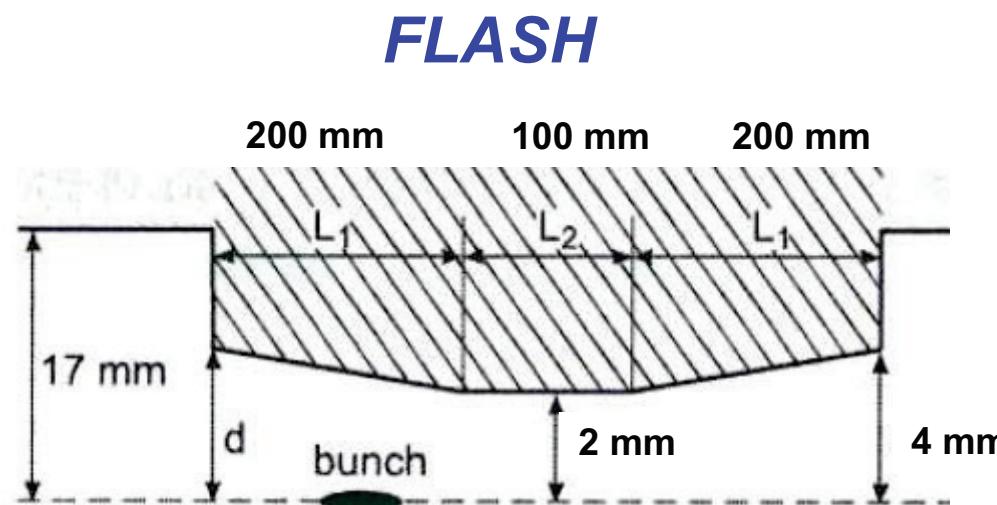


$$\kappa_{fit} = 2.20 \text{ } V / pC / mm$$

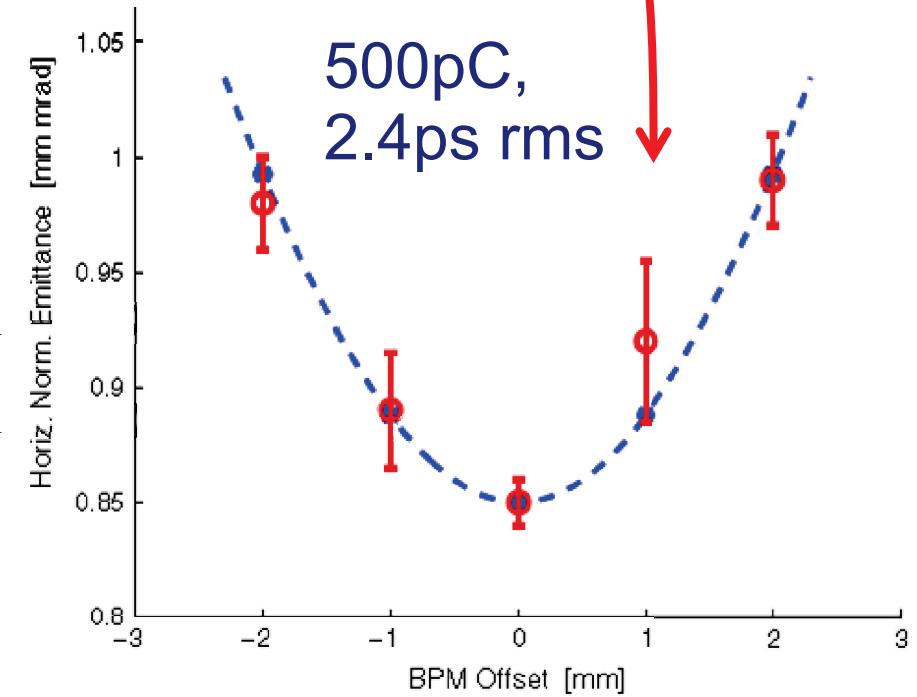
$$\kappa_{ABCi} < 4 \text{ } V / pC / mm$$

$$\bar{\kappa}_{theor} = 2.19 \text{ } V / pC / mm$$

[P. Craievich, C. Bontoiu, PAC09]

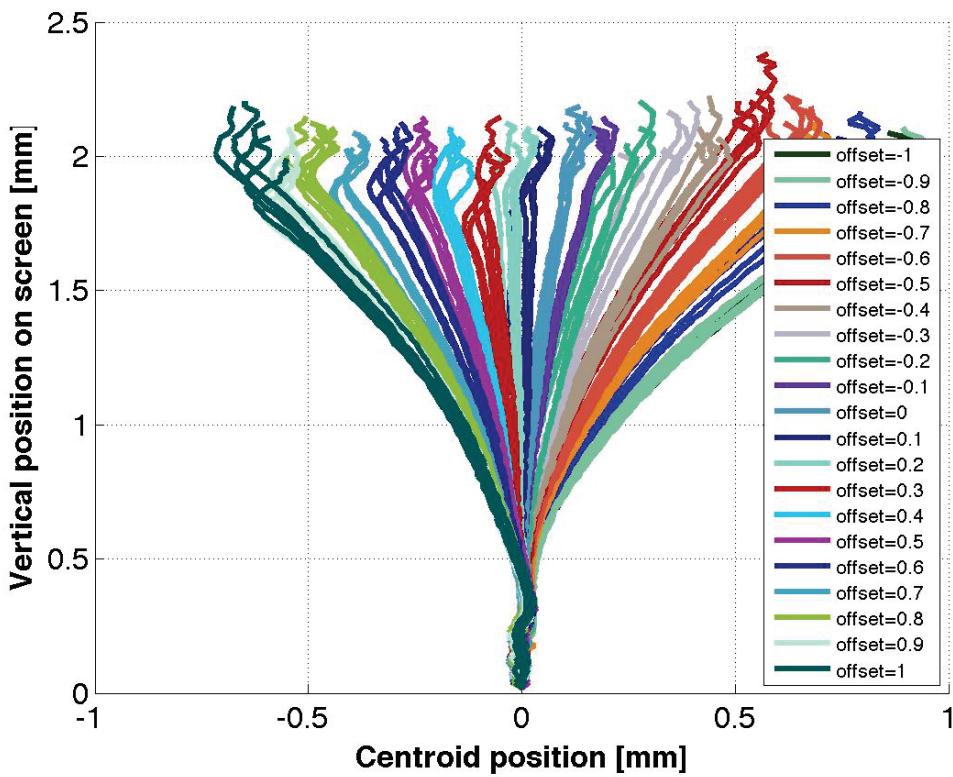


[A. Tsakanian et al., NIM A 659 (2011) 9]



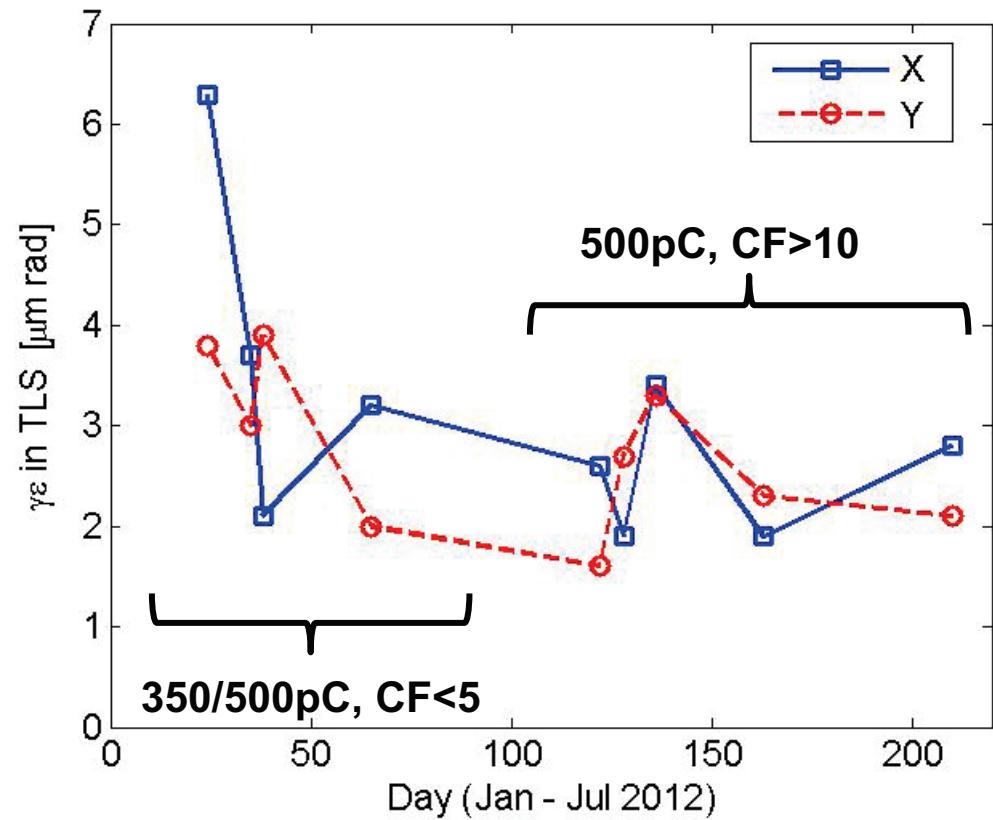
Trajectory bumps along last linac section (small iris structures) allow control of banana shape (*i.e.*, projected emittance) at the linac's end.

**Banana shape vs. BPM offsets**



[E. Ferrari, O. Kalberg,  
G. Penco, 2013]

**Final Emittance vs. working point**

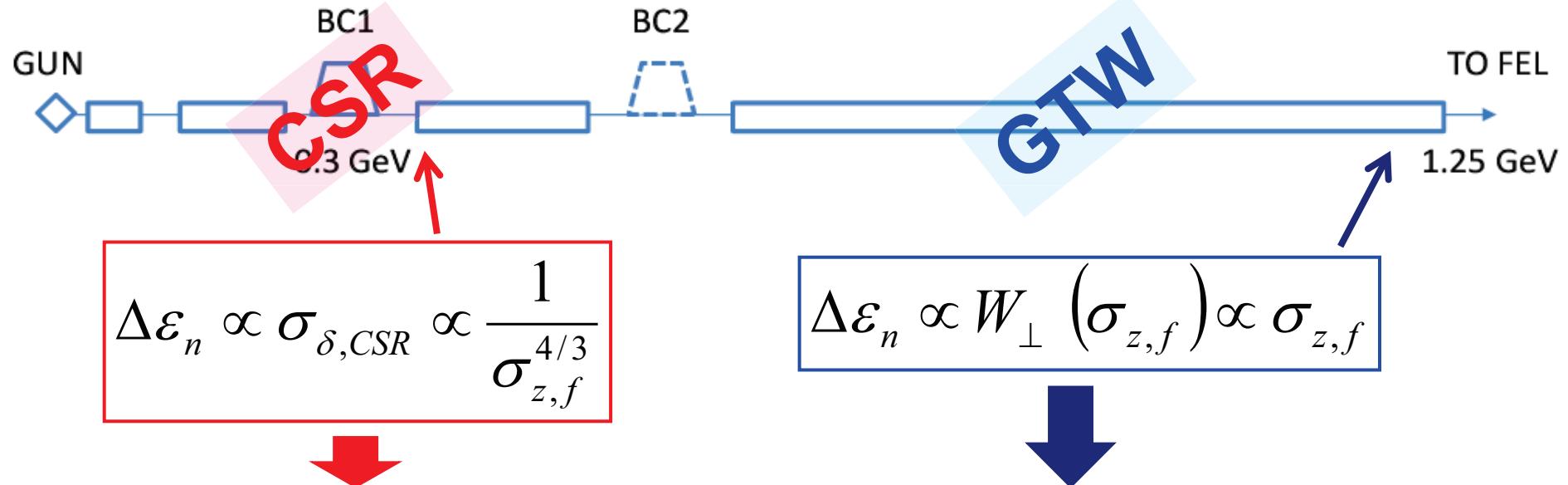


Maximum brightness of linac-driven electron beams in the presence of collective effects

S. Di Mitri

Elettra-Sincrotrone Trieste S.C.p.A., 34149 Basovizza, Trieste, Italy  
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# 4-D Brightness in presence of CSR and GTW

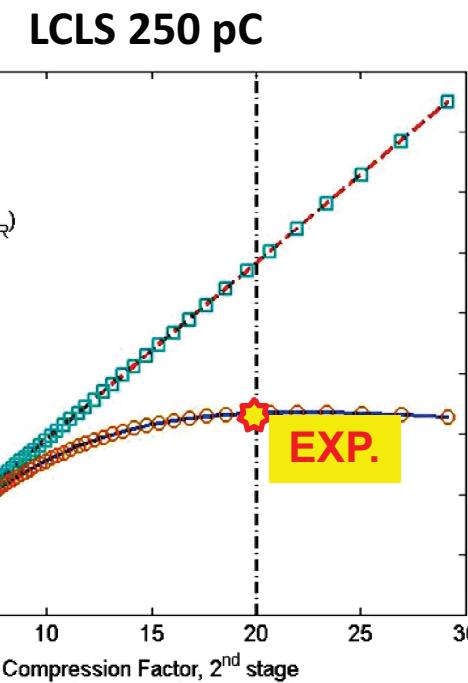
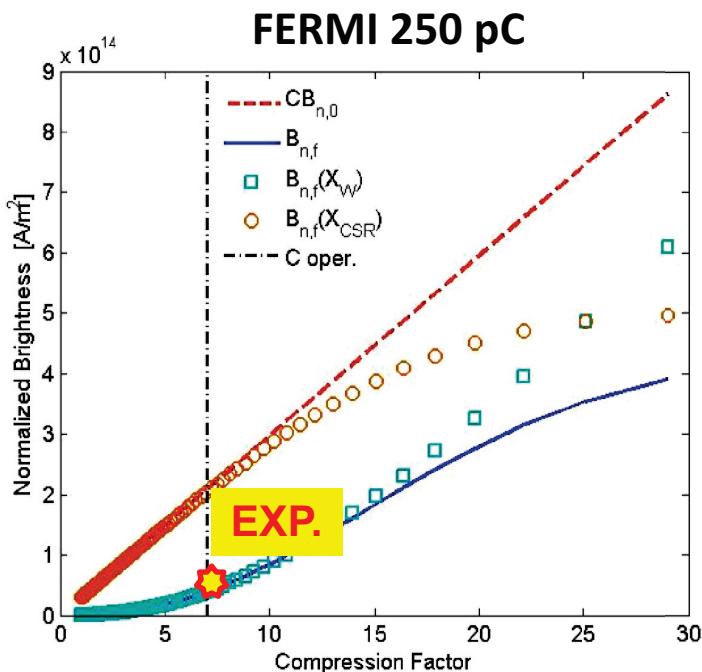


$$B_{n,f} \equiv \frac{I}{\gamma_f^2 \epsilon_{x,f} \epsilon_{y,f}} = \frac{CI_0}{(\gamma_0 \epsilon_{i,0})^2 \sqrt{(1+X_W)(1+X_{CSR}+X_W)}} \equiv \frac{CB_{n,0}}{\sqrt{(1+X_W)(1+X_{CSR}+X_W)}}$$

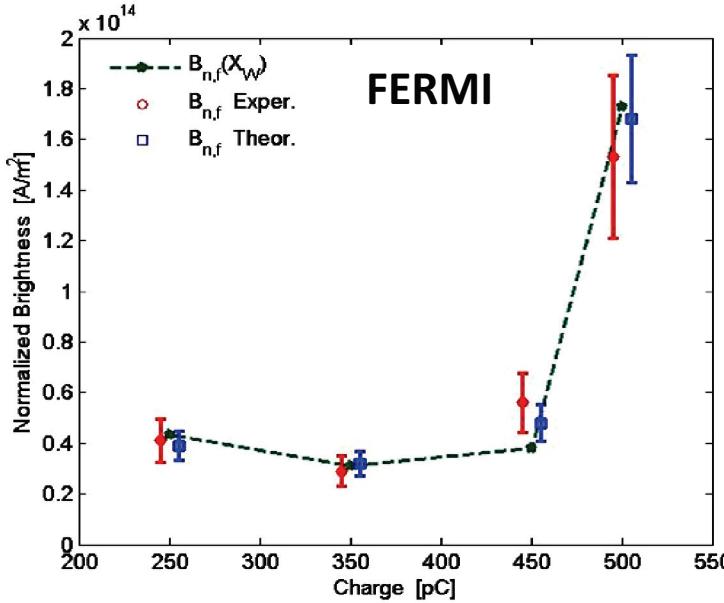
**There must be an optimum (compressed) bunch length that minimizes the combined effect of CSR and GTW on the final  $\epsilon_{n,f}$ .**

**Longitudinal dynamics and effects on FEL in the next talks by Penco, Ferrari and Allaria.**

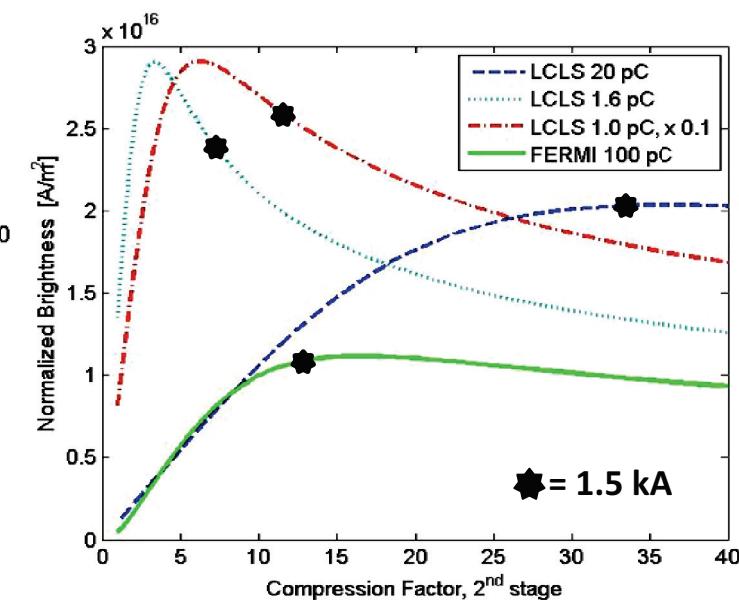
# Validation and optimization studies



The model identifies the dominant source of  $\varepsilon$ -growth.

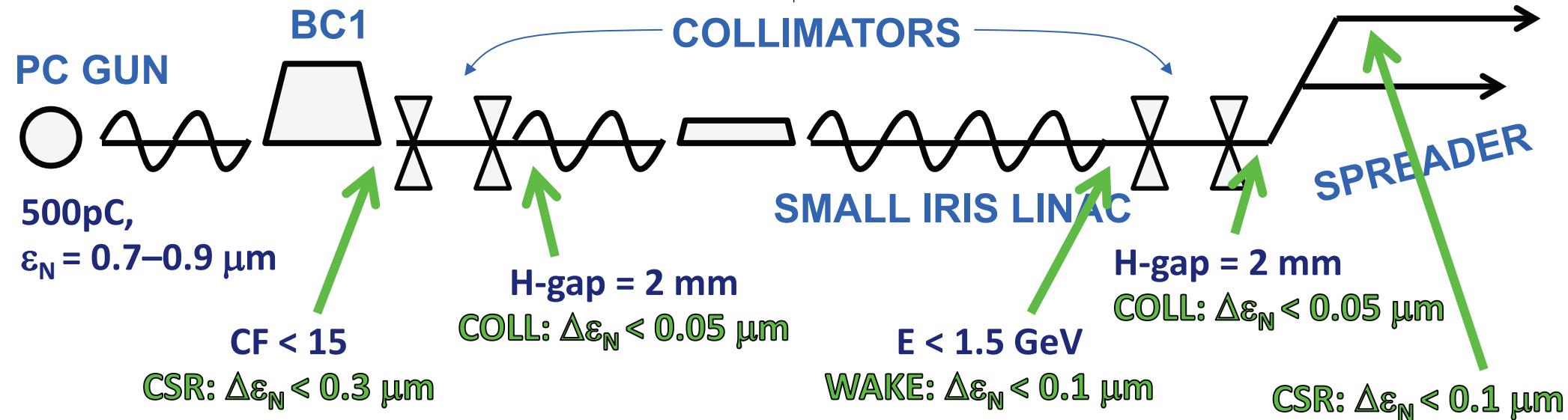


The model works well with different charges and CFs



Local maximum of  $B_{4D,n}$  can be used for optimization studies

## Current FERMI Linac emittance budget



- Best 500pC projected norm. emittance is 1.5  $\mu\text{m}$  in front of undulator. Slice emittance is estimated at 1  $\mu\text{m}$  level. This meets the FEL requirements and allows lasing within users' specs.
- Interplay of residual CSR and GTW effect still requires manual tuning to minimize the final emittance. Annoying, but not critical.
- 4-D brightness model agrees with experimental data and promises further optimizations of FERMI's working point.

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## AUTHORS:

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## CONTRIBUTORS:

P. Cinquegrana, M. B. Danailov, G. D'Auria, A. Demidovitch, B. Diviacco, M. Ferianis, G. Gaio, O. Kalberg, R. Ivanov, B. Mahieu, N. Mahne, I. Nikolov, L. Raimondi, C. Scafuri, P. Sigalotti, C. Svetina, M. Zangrandi, M. Svandrlik

*Thank you for your kind attention*