

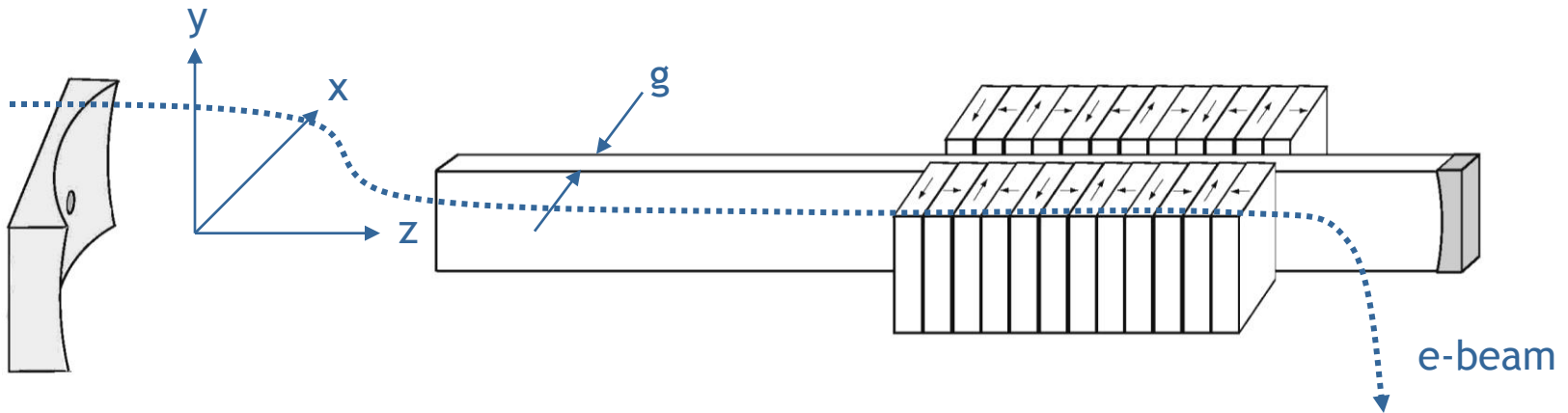


Tuning gaps in the FELIX long-wavelength FEL

Dick Oepts and [Lex van der Meer](#)



Partial-waveguide resonator

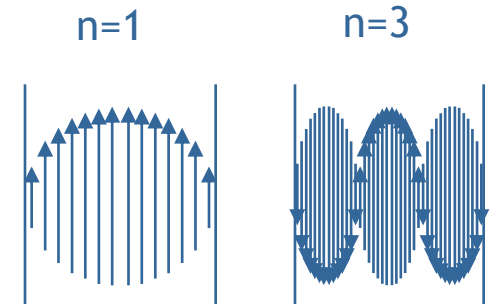


Eigenmodes are a combination of TE and Hermit-Gaussian modes:

$$\Psi_n(x, y, z) = \cos\left(\frac{nx\pi}{g}\right) \exp\left(\frac{-y^2}{w^2(z)} + i\left(\frac{k_n^z y^2}{2R(z)} - \frac{1}{2} \tan^{-1} \frac{z}{z_r}\right)\right)$$

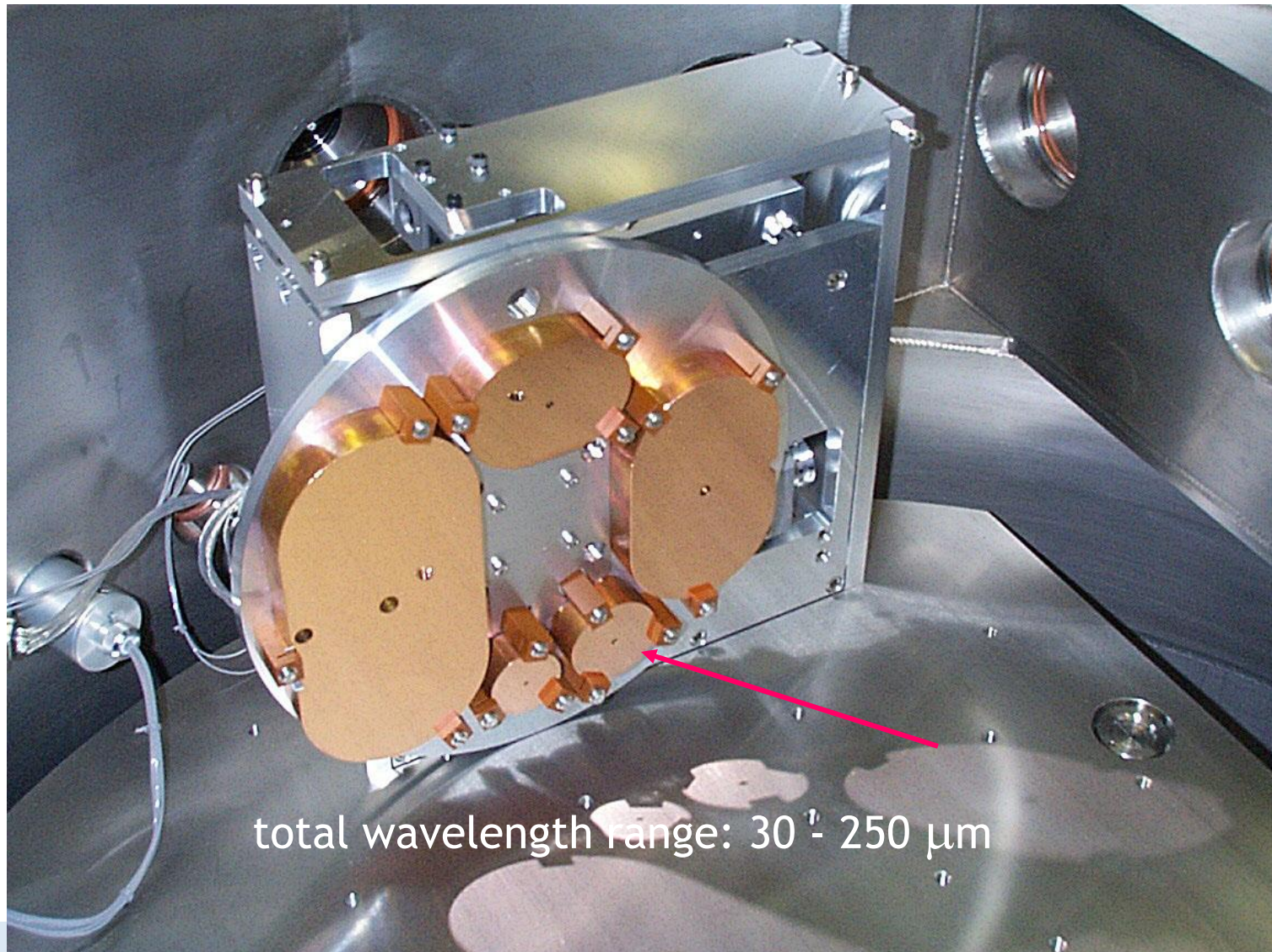
with $w(z) = w_0 \cdot \sqrt{1 + \frac{z^2}{z_r^2}}$, $k_n^z = \sqrt{k^2 - n^2 k_\perp^2}$, $R(z) = z + \frac{z_r^2}{z}$

and $k_\perp = \frac{\pi}{g}$, where k is the wave vector in vacuum, z_r the Rayleigh range and w_0 the waist





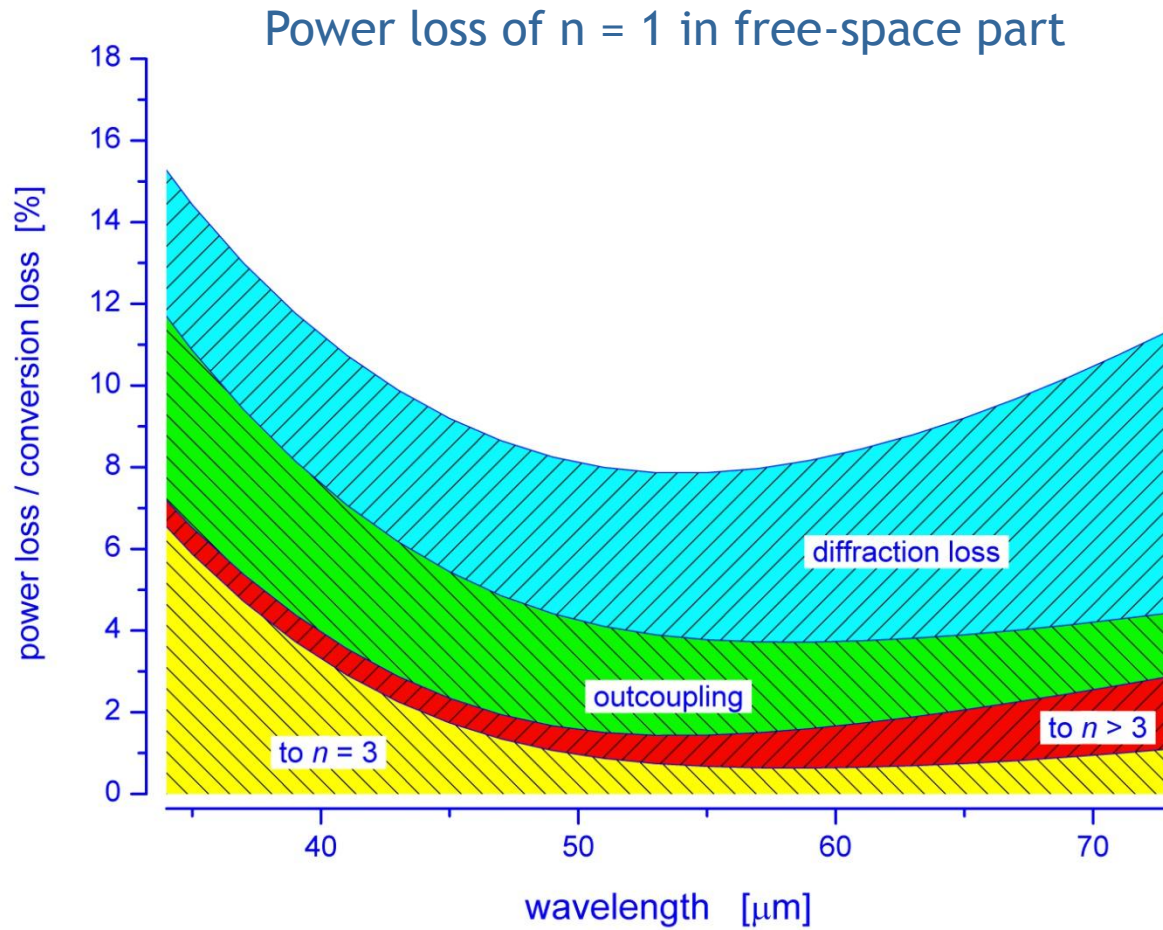
Mirror carousel



total wavelength range: 30 - 250 μm

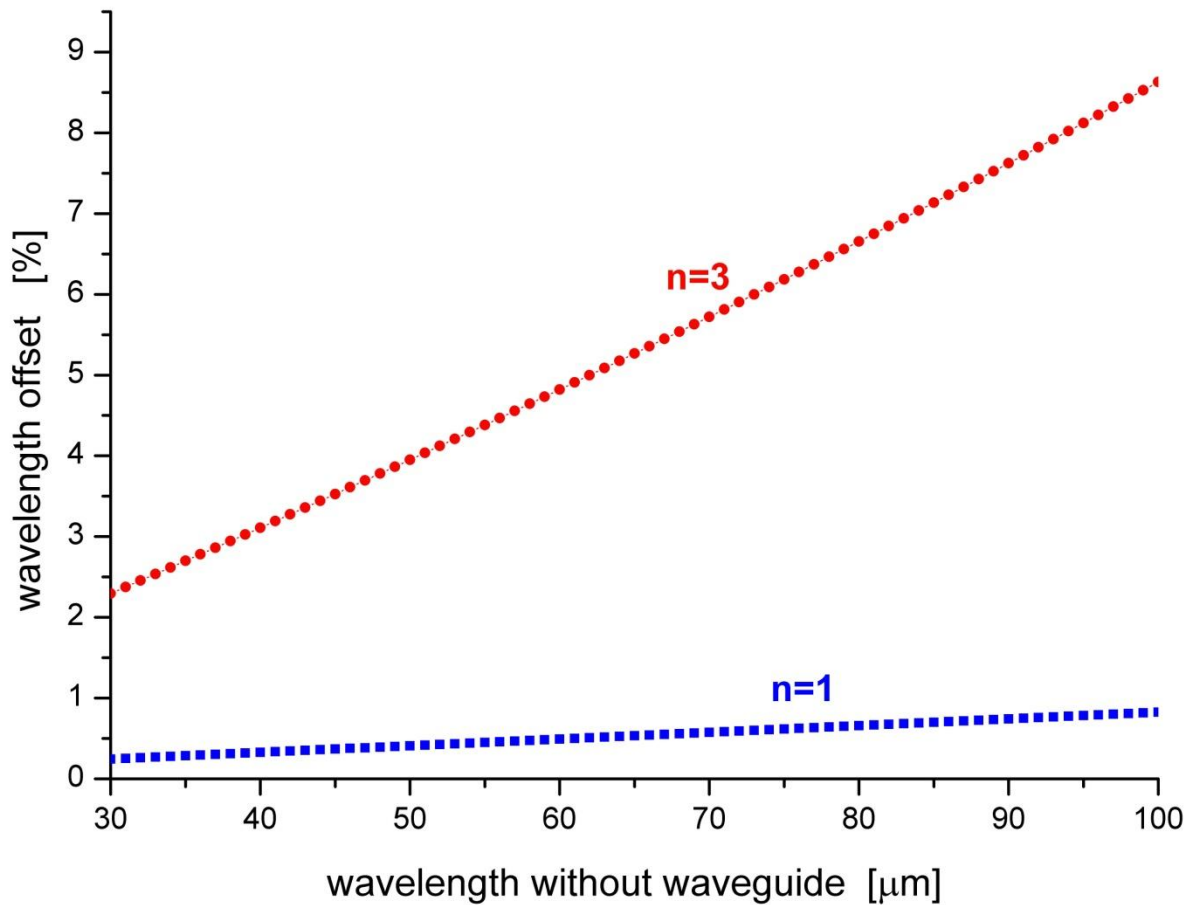


Mode conversion in free-space part



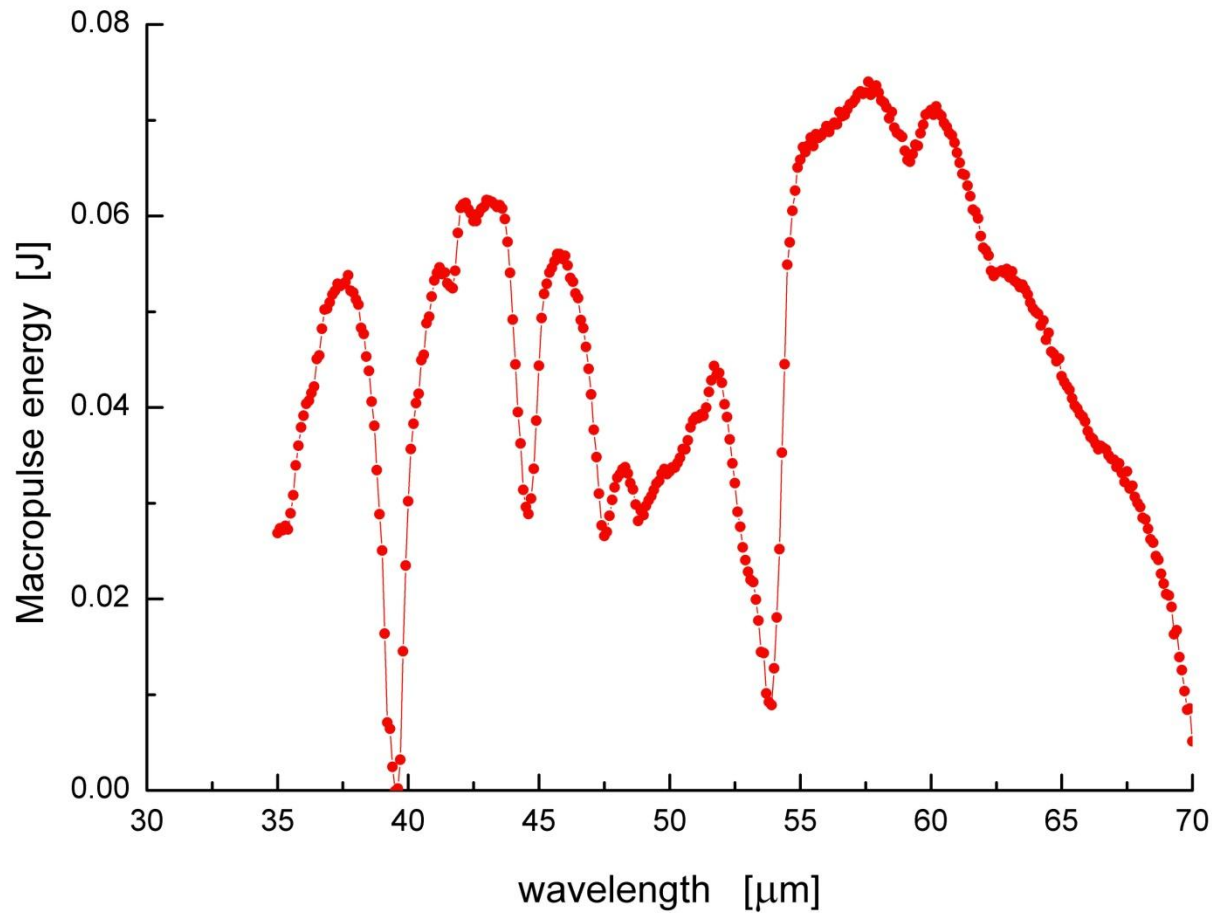


Frequency offset between $n=1$ and $n=3$



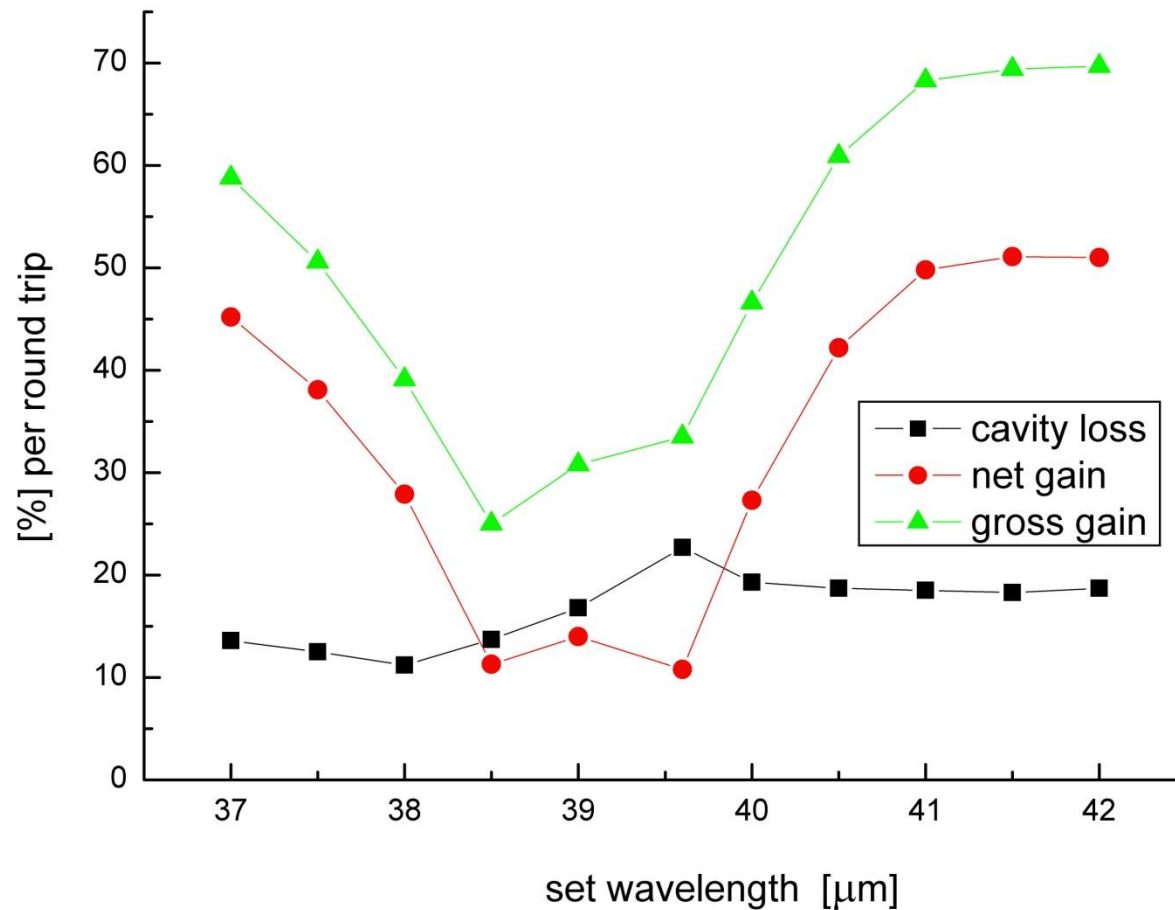


Typical tuning curve



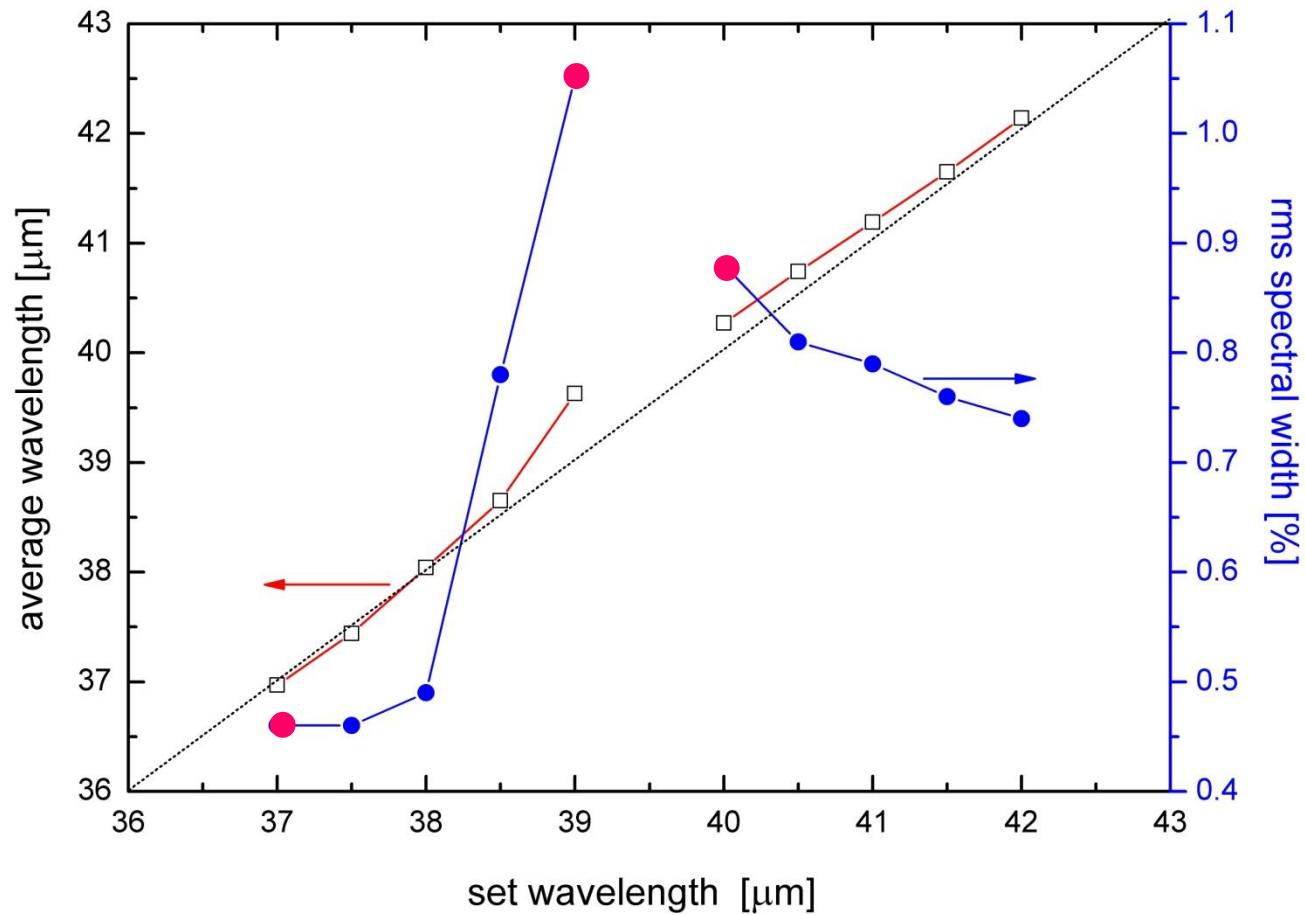


measured roundtrip gain and loss



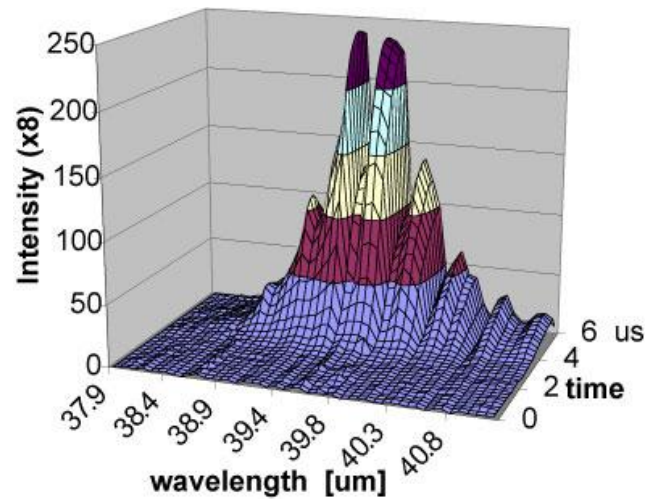
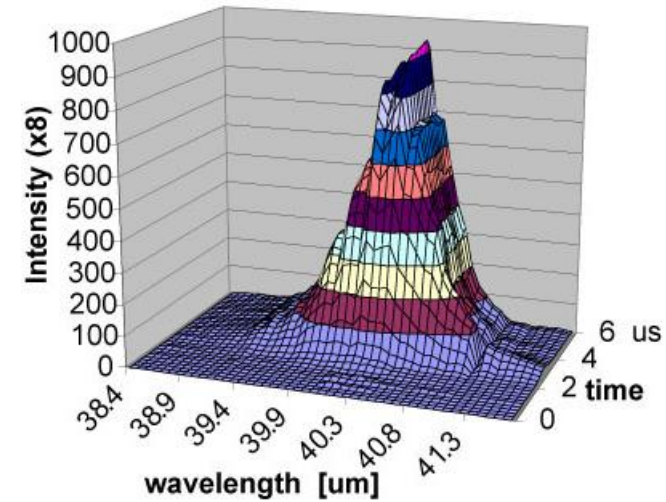
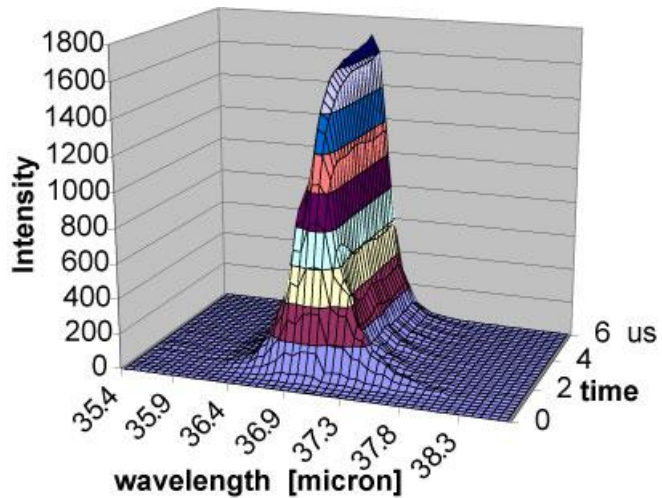


measured spectral characteristics



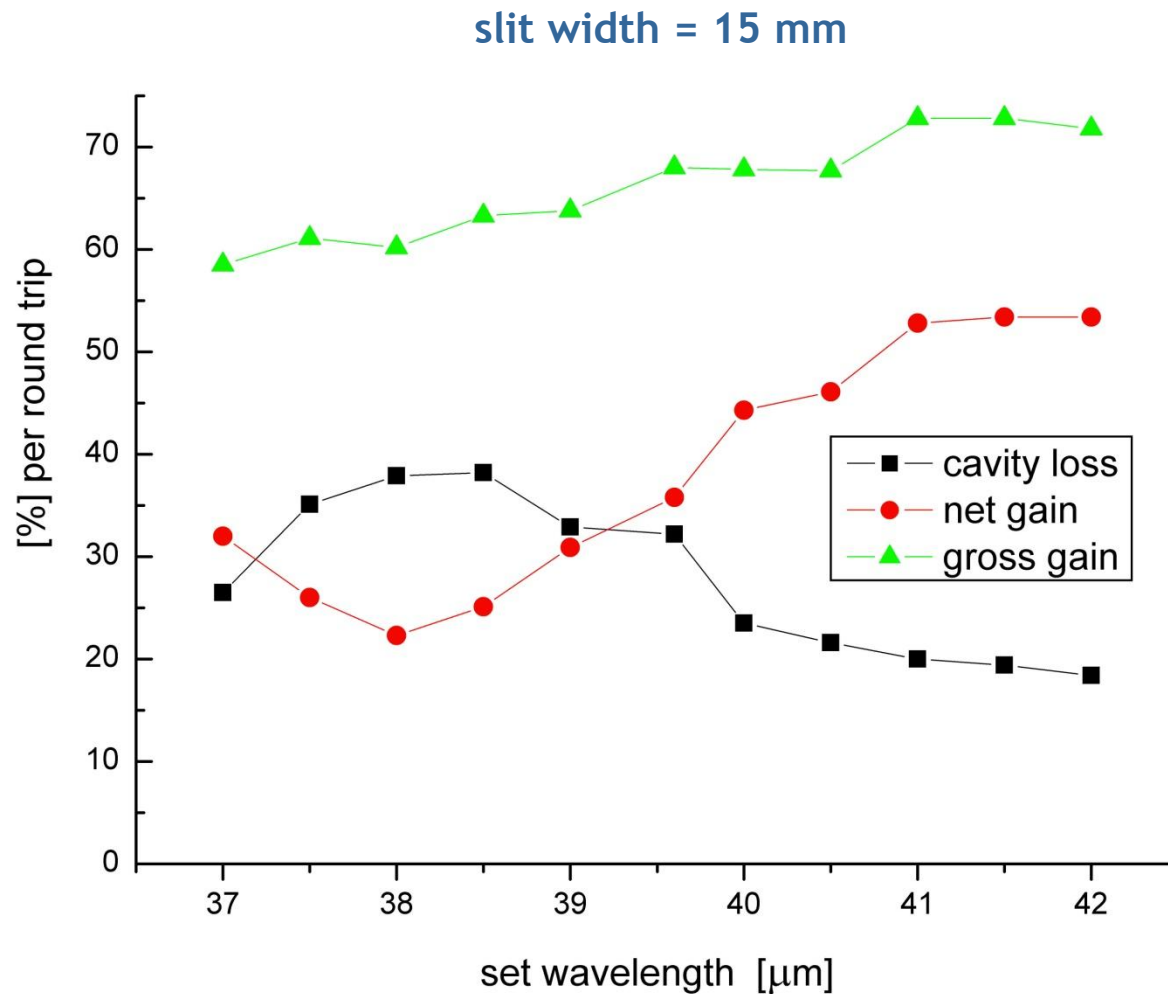


measured spectral characteristics cont.



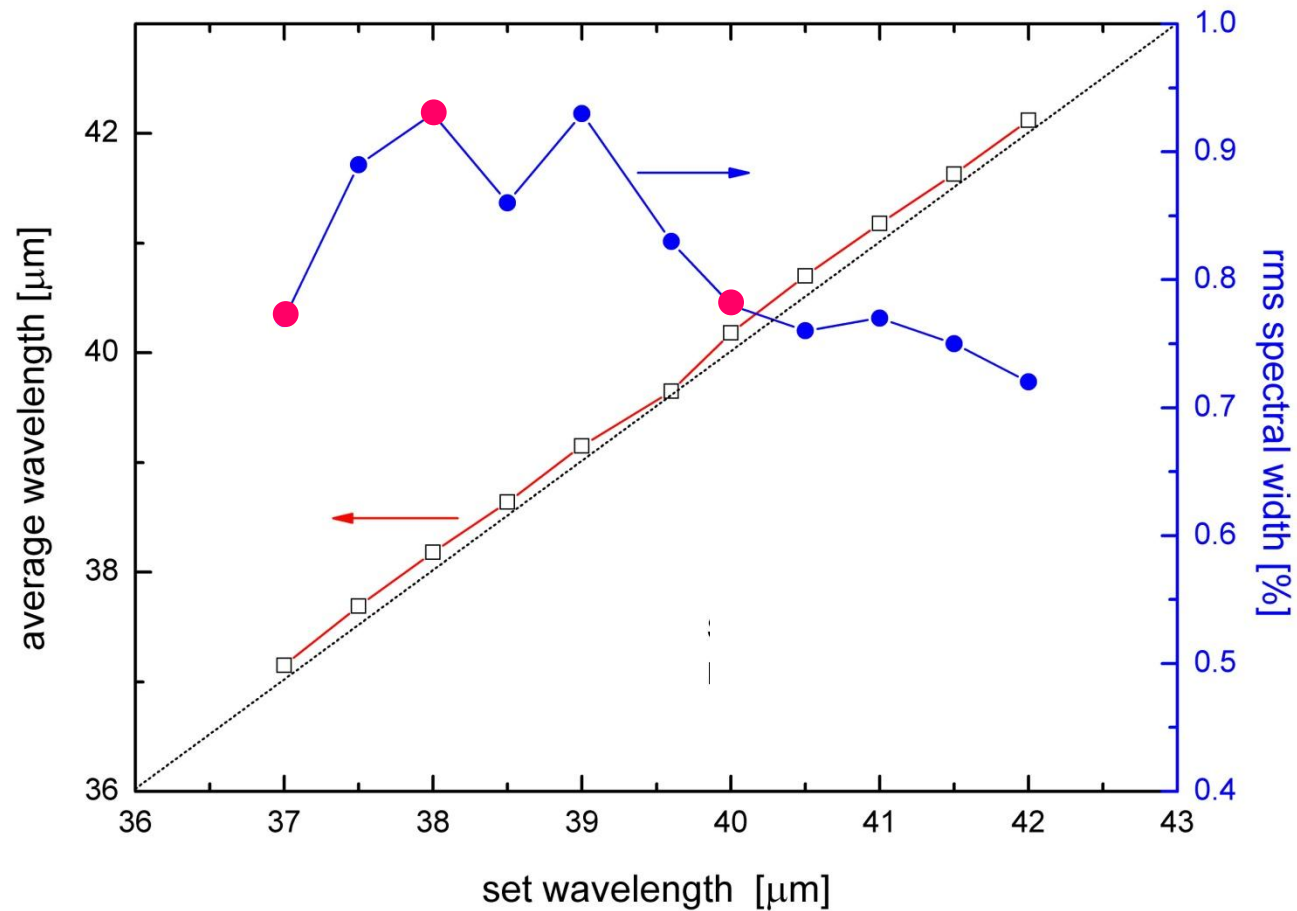


measured roundtrip gain and loss cont.



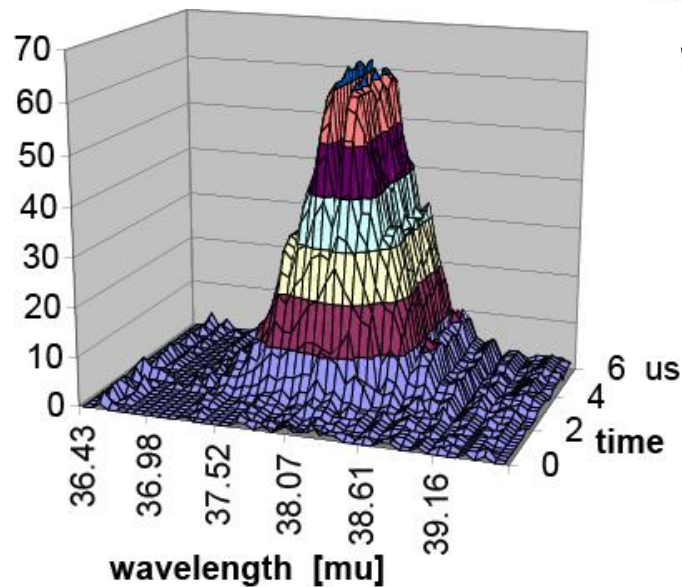
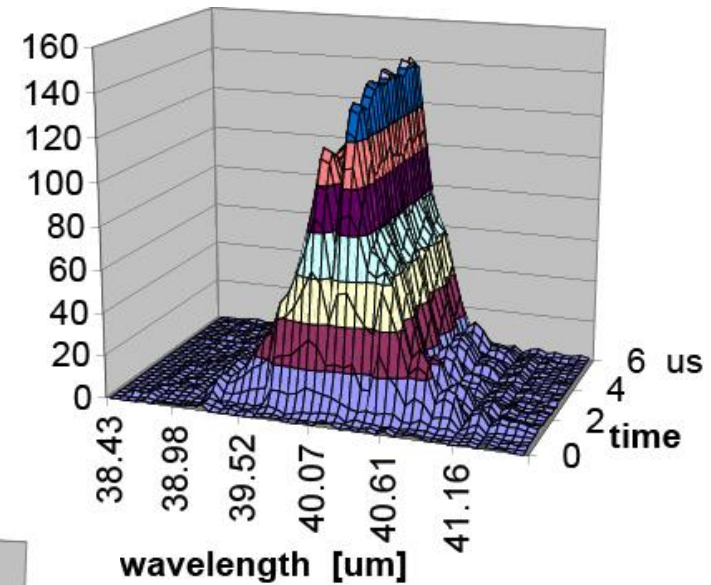
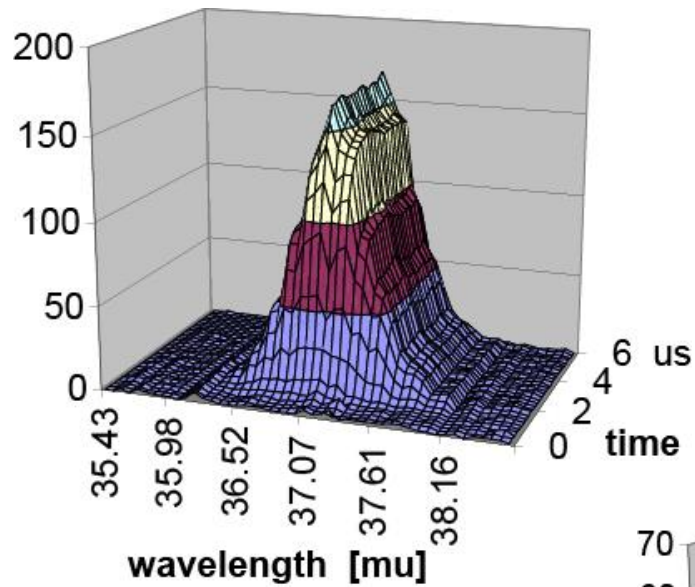


measured spectral characteristics cont.



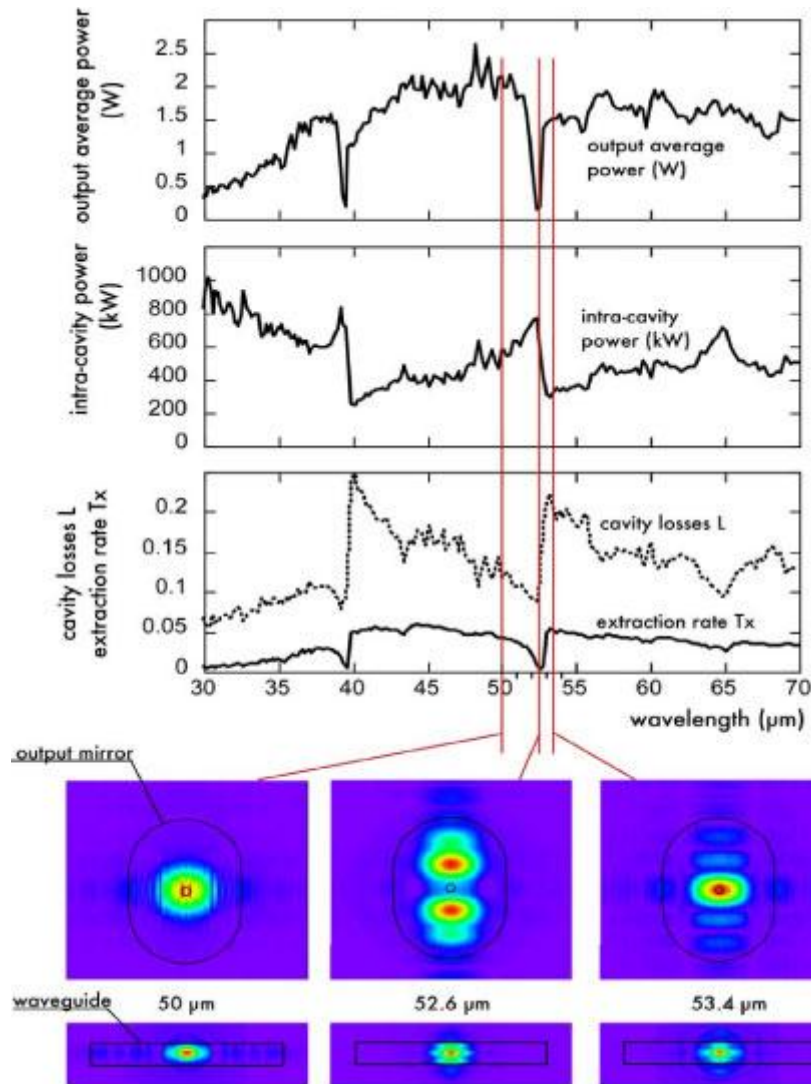


measured spectral characteristics cont.





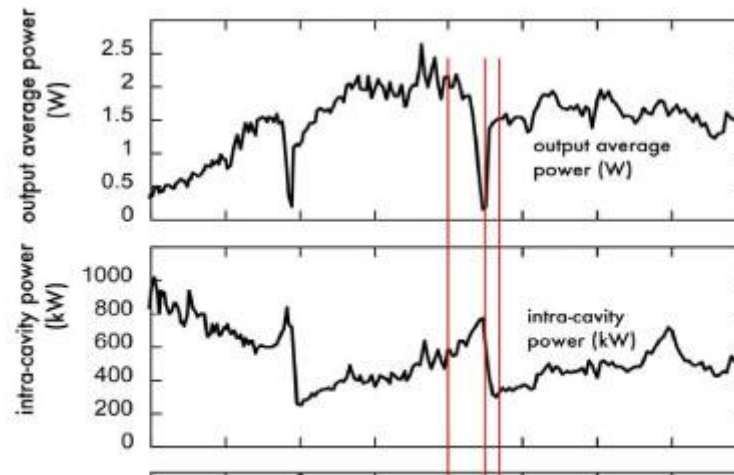
Simulations by Prazeres et al.



Prazeres et al.,
PRST Accel. Beams
12 (2009) 010701



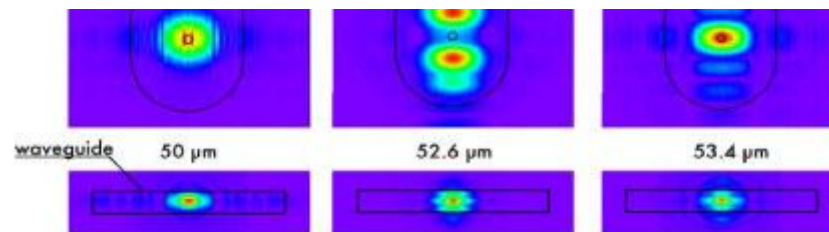
Simulations by Prazeres et al.



Prazeres et al.,
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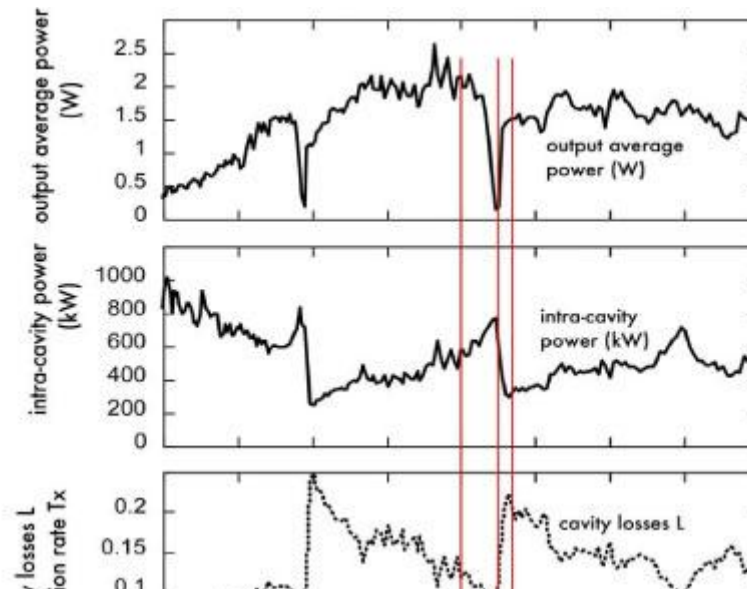
Limitations of the model used:

- single frequency
- no start-up
- gain evaluation only halfway the undulator





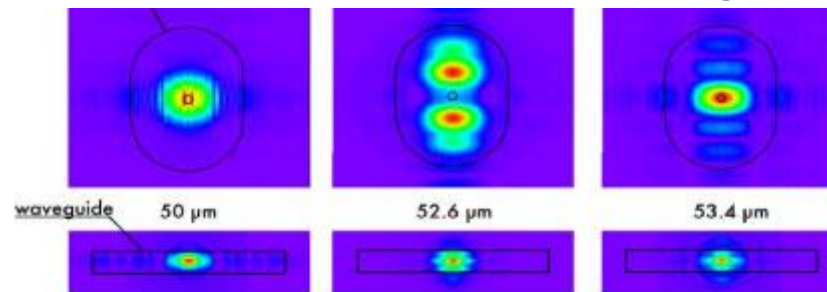
Simulations by Prazeres et al.



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PRST Accel. Beams
12 (2009) 010701

Conjecture:

spacing of gaps given by $\Delta\Phi^w_1 - \Delta\Phi^w_3 = 2\pi$





Our model

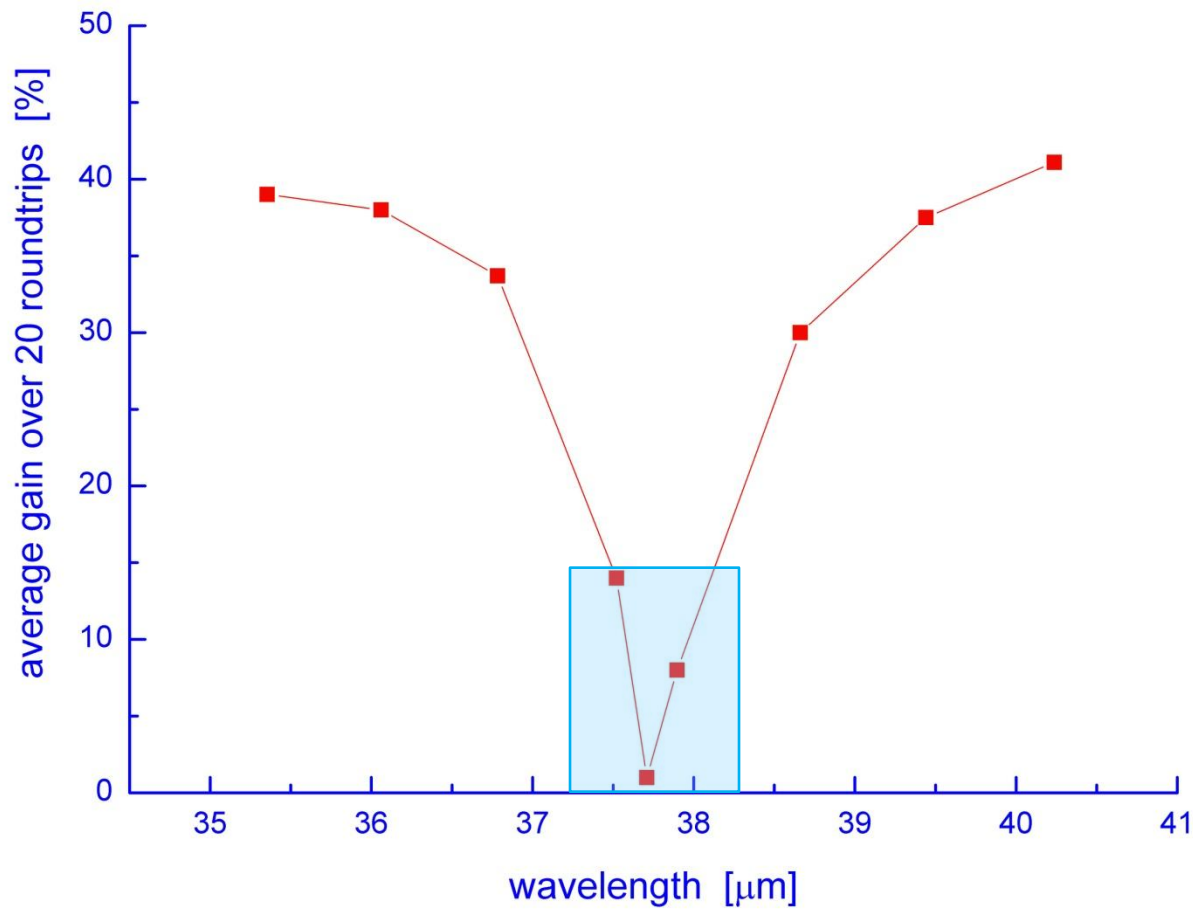
Modification of the model by Prazeres:

- single transverse coordinate (x), so no hole
- multi frequency, short pulse
- distributed, frequency dependent gain

(stepwise integration of small-signal, low-gain FEL equation along the undulator and across the e-beam profile)

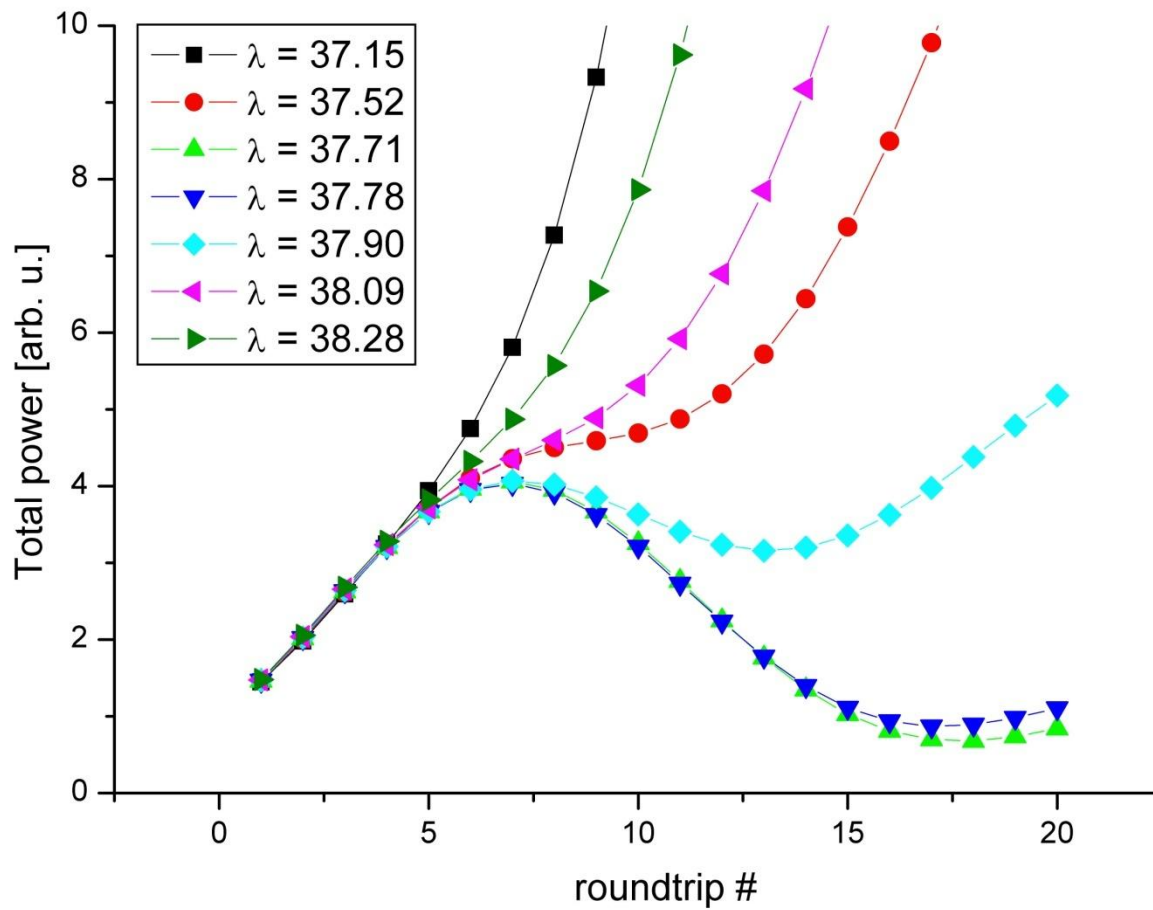


Our simulation results



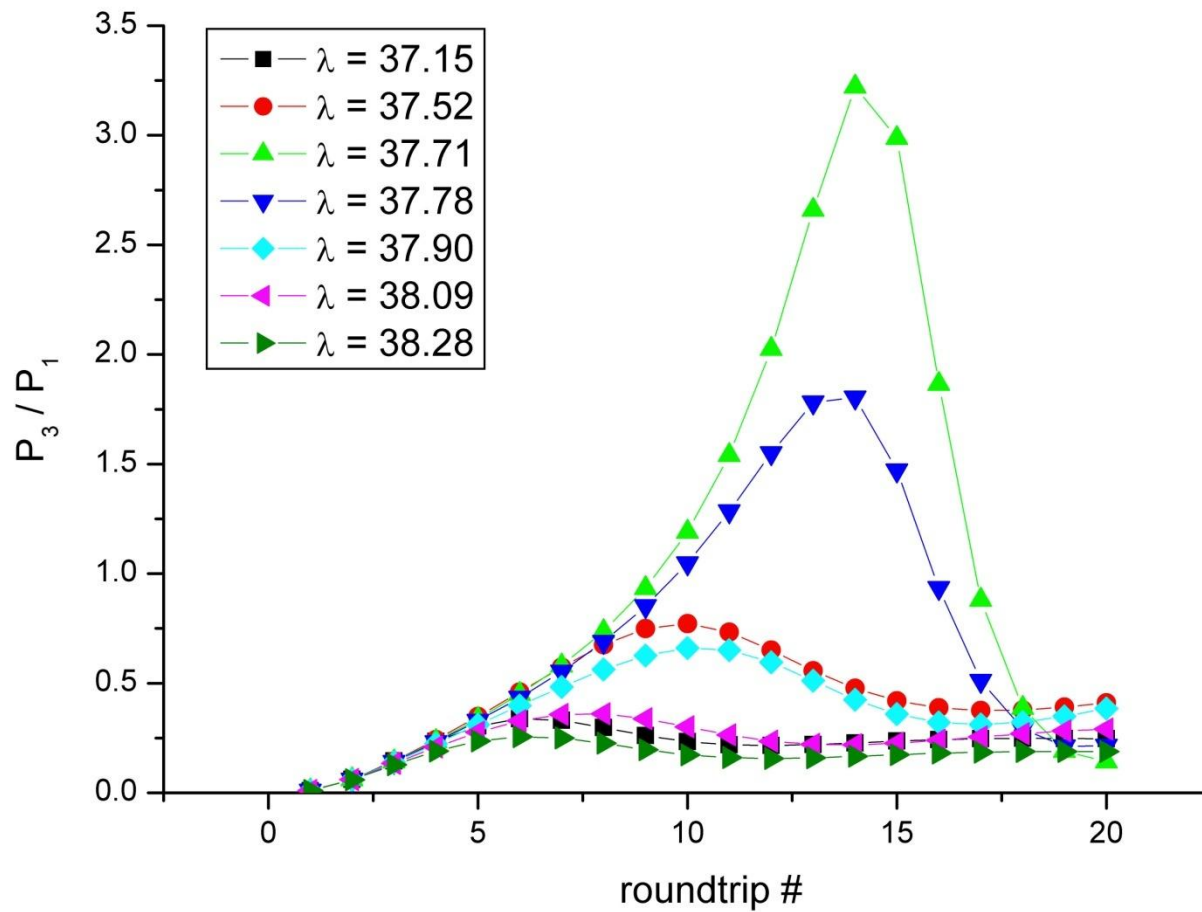


Our simulation results



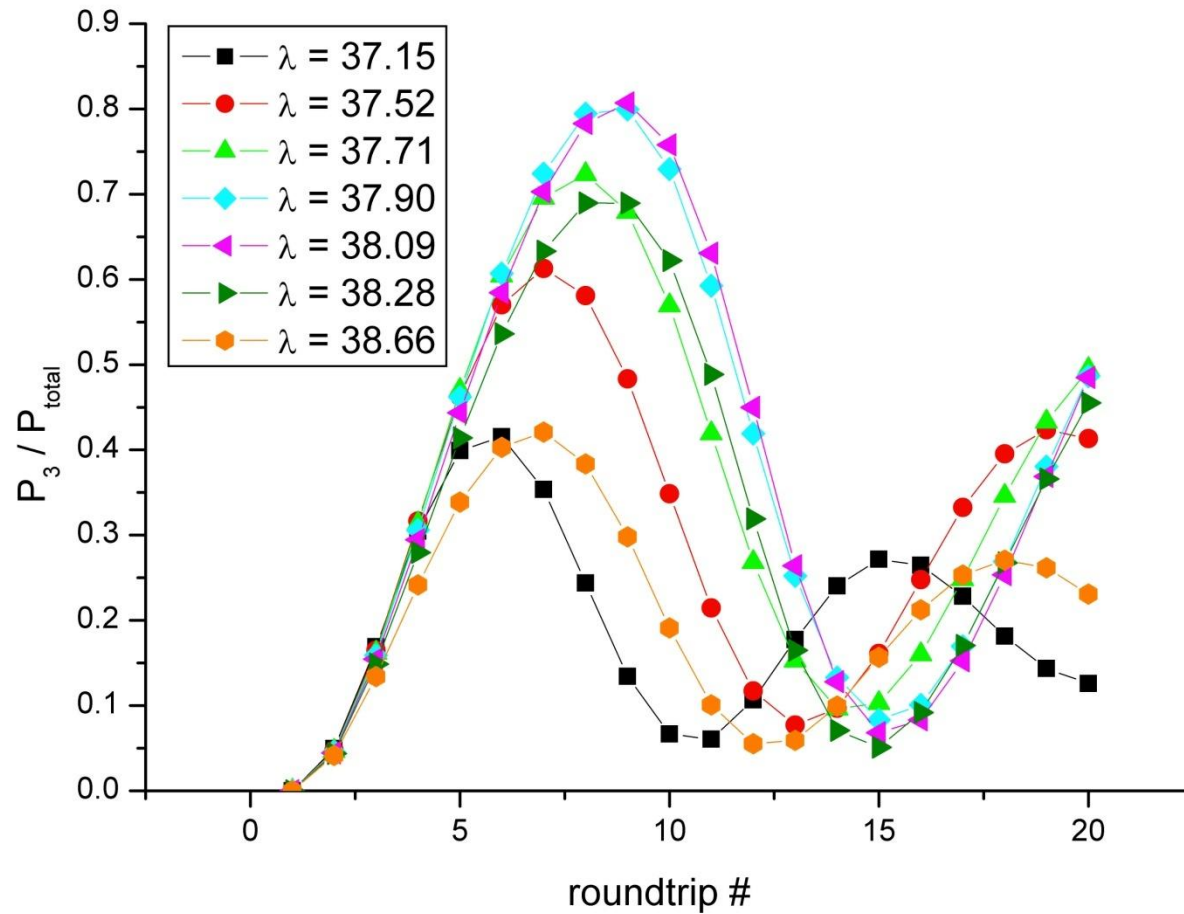


Our simulation results cont.



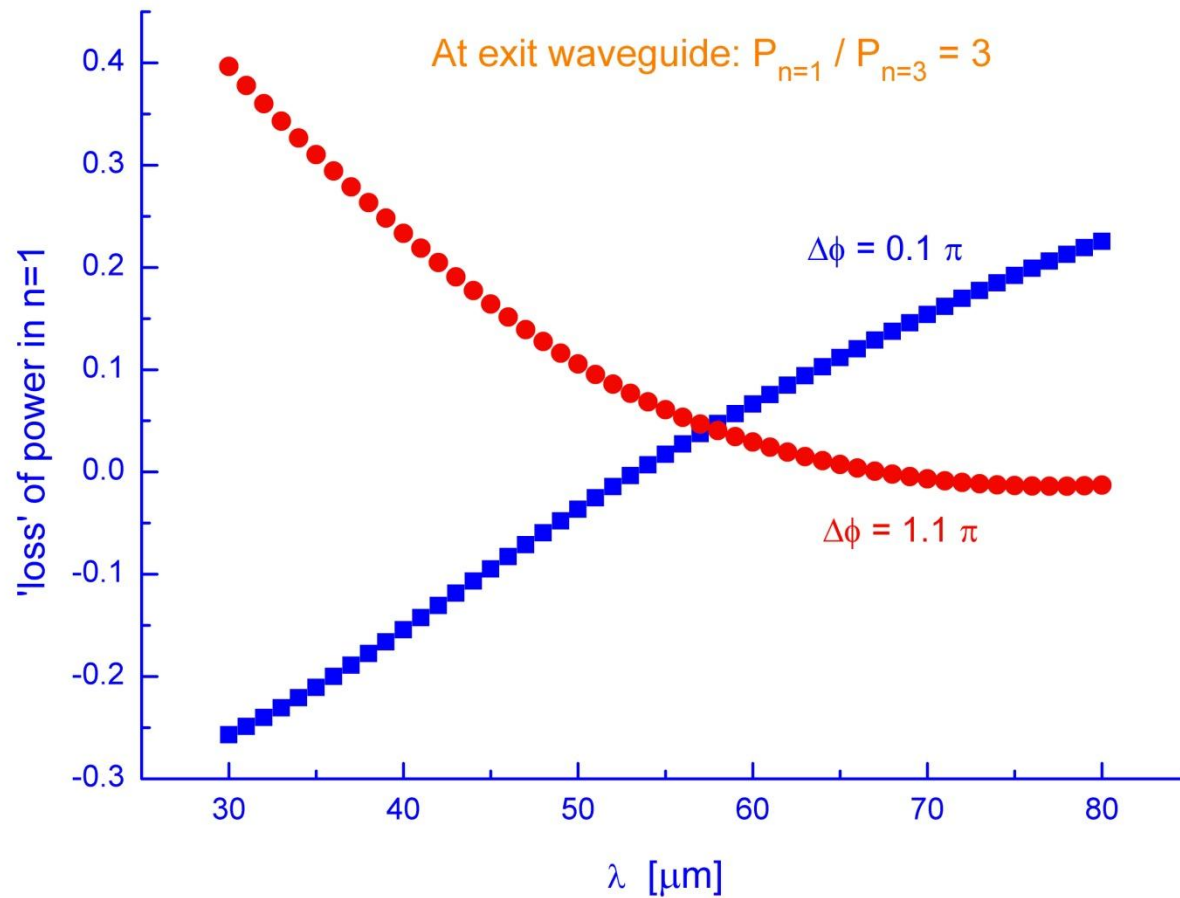


Our simulation results cont.



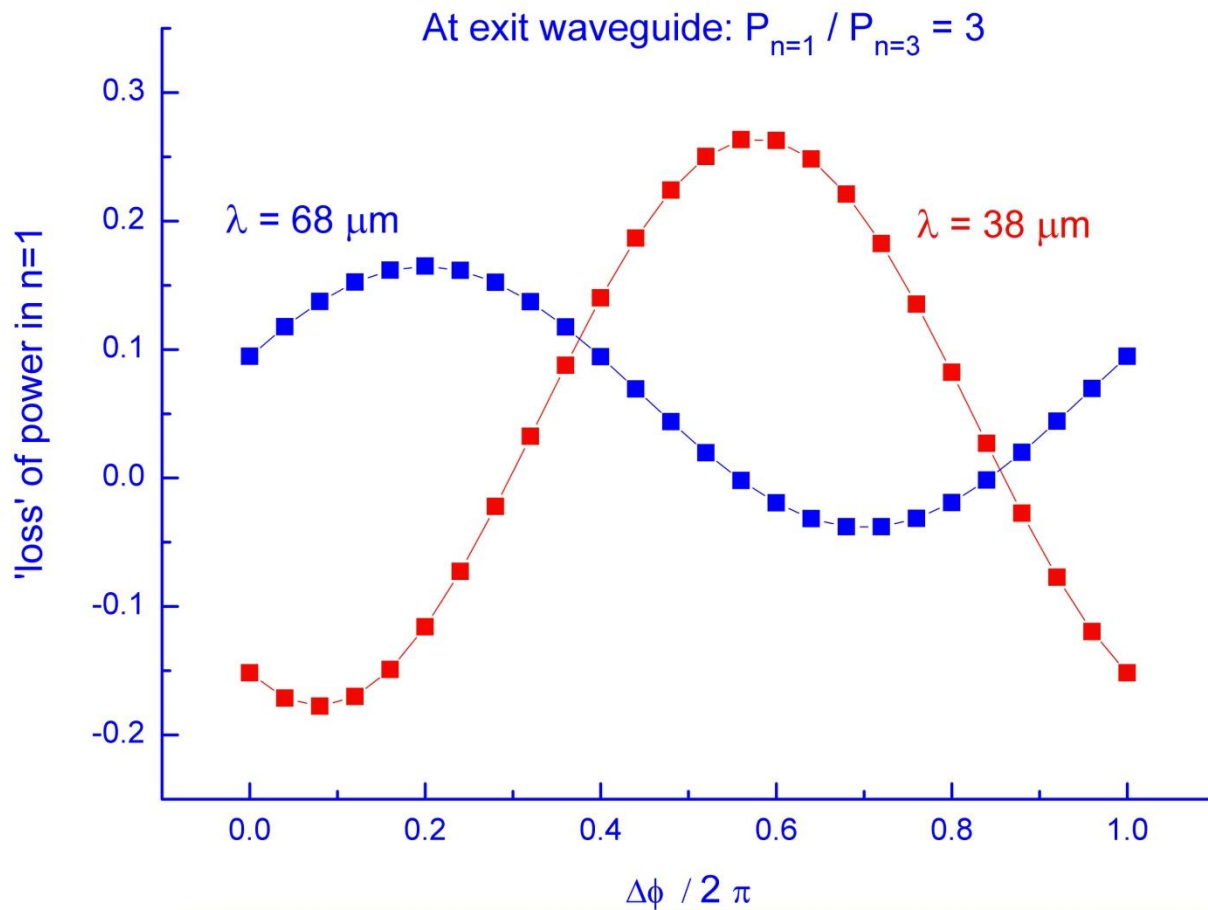


conversion in free space with $P_{n=3}$ present



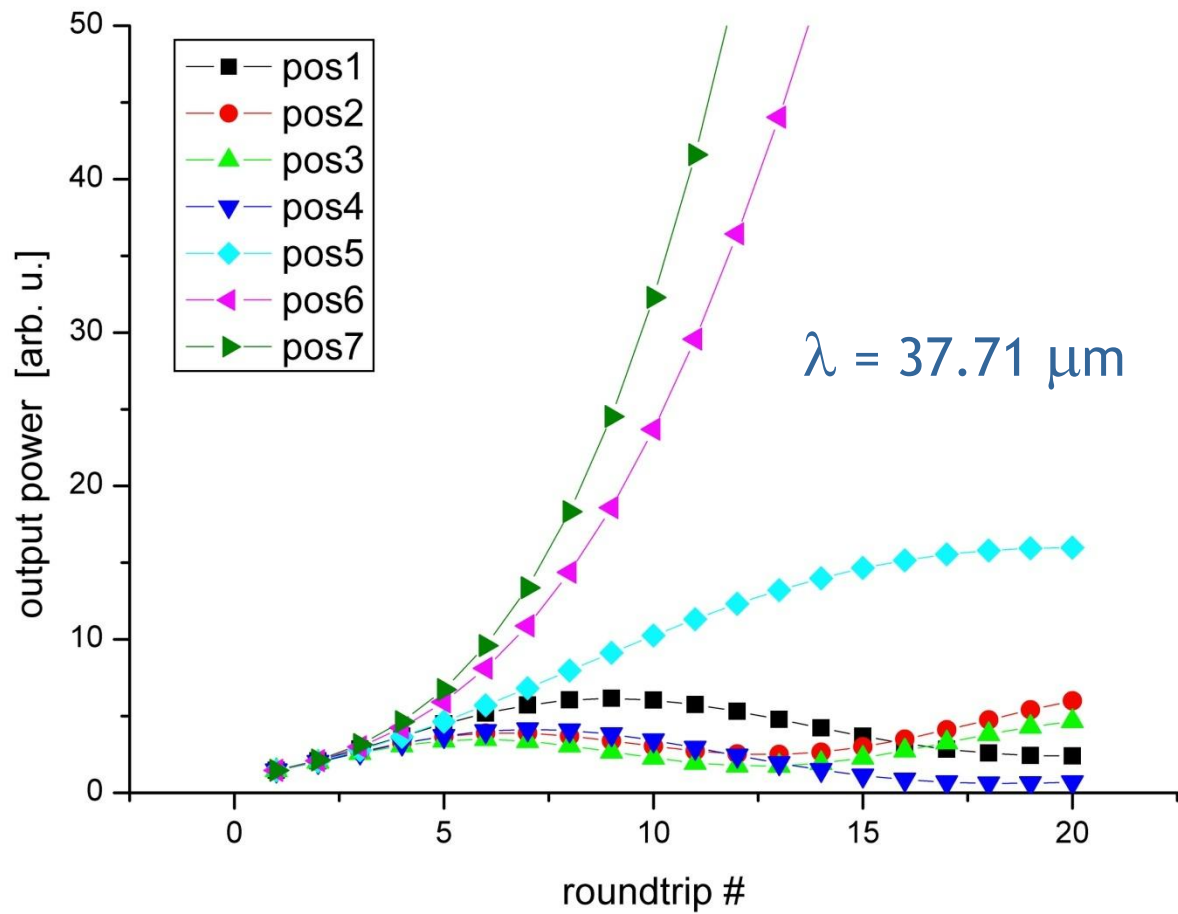


conversion in free space with $P_{n=3}$ present



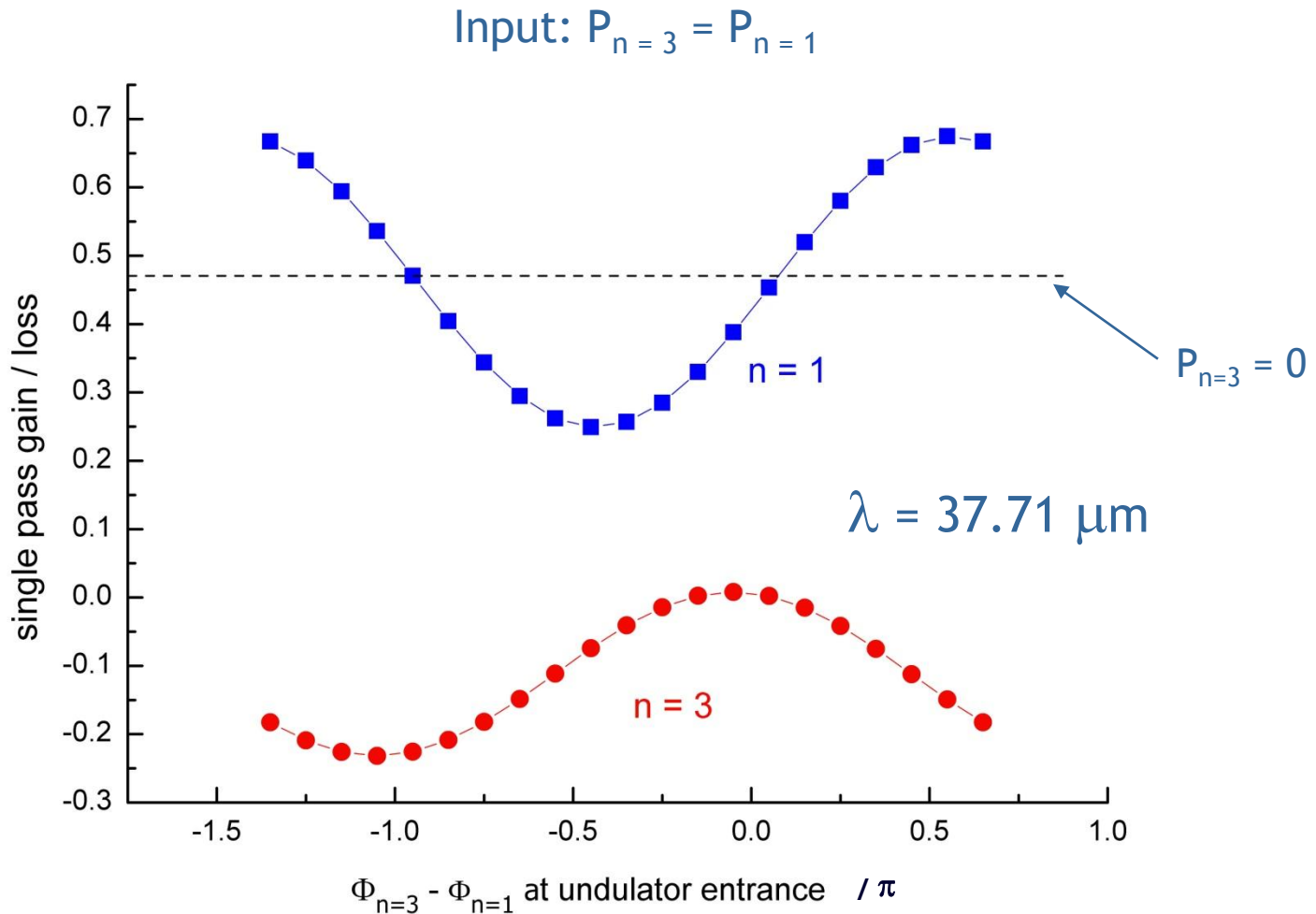


Gain vs. undulator position



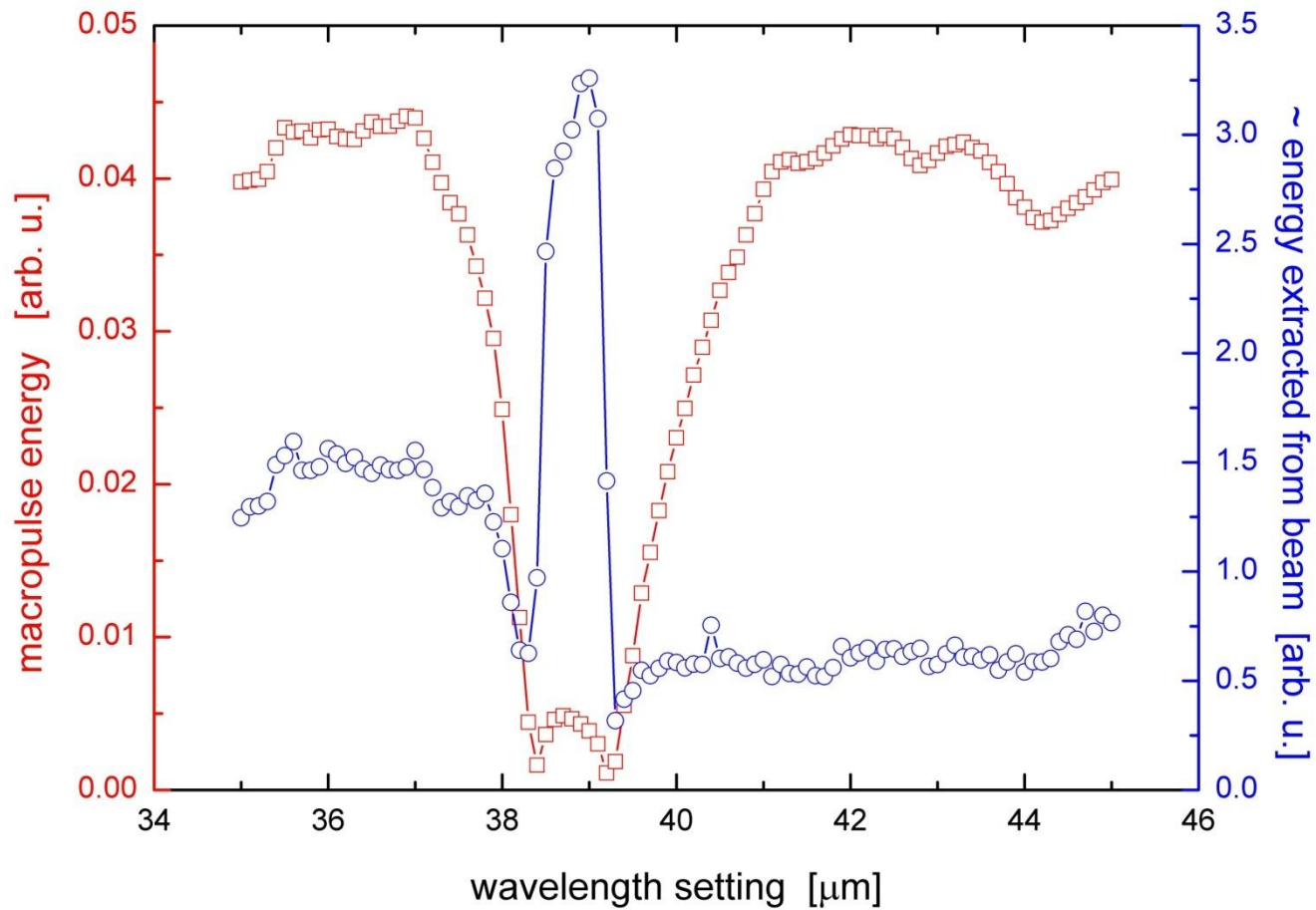


Single pass undulator gain vs. relative phase





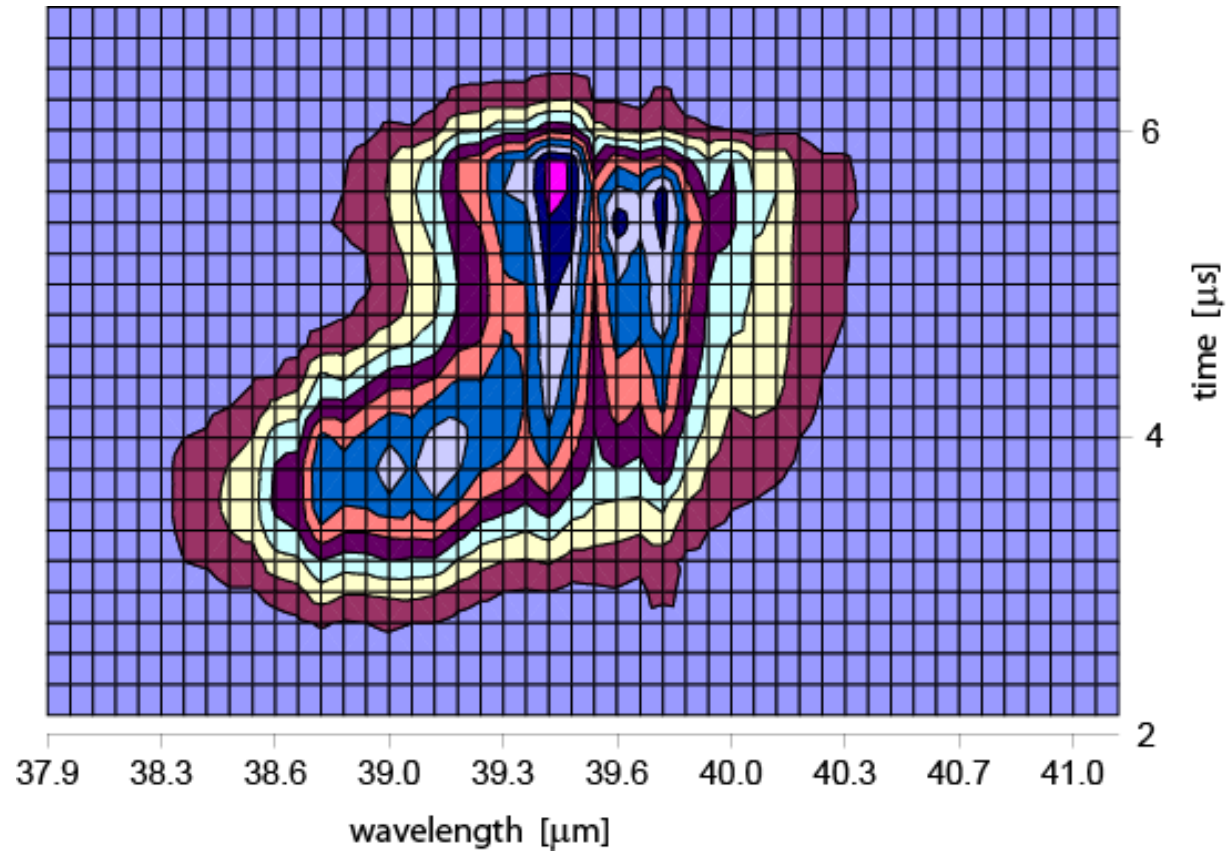
Example of low outcoupling





Example of low outcoupling

wavelength setting: 39 μm





Conclusions

Start-up problem and power gaps are caused by

1. the resonant mode conversion from the $n = 1$ mode to higher-order modes between waveguide exit and entrance when the relative, roundtrip phase shift is a multiple of 2π
2. the dependence of the gain of the $n = 1$ mode on the relative phases of the higher-order transverse modes along the undulator