

# Studies of a scheme for low emittance muon beam production from positrons on target

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# Outline

- Introduction: Muons case
- Proposal for a novel technique for muon production
- $e^+$  ring with target
- Multi-turn simulations
- Conclusion and Perspectives

# Muon based Colliders

- A  $\mu^+\mu^-$  collider offers an ideal technology to extend lepton high energy frontier in the multi-TeV range:
  - No synchrotron radiation (limit of  $e^+e^-$  circular colliders)
  - No beamstrahlung (limit of  $e^+e^-$  linear colliders)
  - but muon lifetime is  $2.2 \mu\text{s}$  (at rest)
- Best performances in terms of luminosity and power consumption
- Great potentiality if the technology proves its feasibility:
  - Muon source
  - Fast muon cooling
  - Fast acceleration
  - $\mu$  Collider
  - Radiation Safety (muon decay in accelerator and detector)

# Idea for low emittance $\mu$ beam

Conventional production: from **proton on target**

$\pi$ , K decays from proton on target have typical  $P_\mu \sim 100 \text{ MeV}/c$   
( $\pi$ , K rest frame)

whatever is the boost,  $P_T$  will stay in Lab frame  $\rightarrow$

**very high emittance** at  $\mu$  production point  $\rightarrow$  **cooling** needed!

Novel proposal: **direct  $\mu$  pair production:  $e^+e^- \rightarrow \mu^+\mu^-$**

just above the  $\mu^+\mu^-$  production threshold ( $\sqrt{s} \approx 0.212 \text{ GeV}$ ) with minimal muon energy spread, with direct annihilation of  $\approx 45 \text{ GeV}$   $e^+$  with atomic  $e^-$  in a thin target  $O(0.01 \text{ radiation length})$

**very small emittance** at  $\mu$  production point  $\rightarrow$  **no cooling** needed!

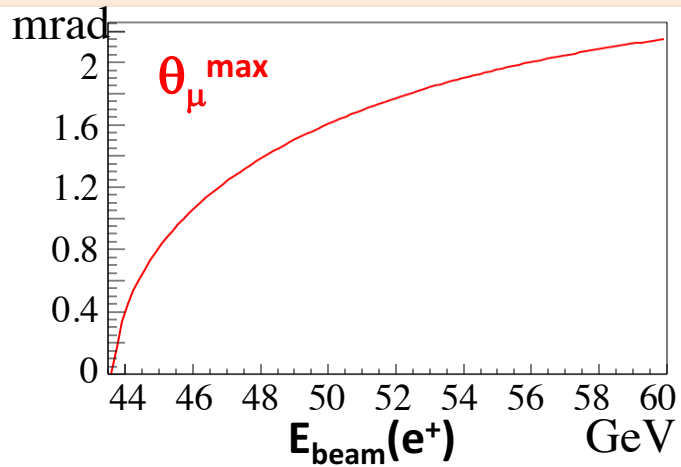
## Advantages:

- 1. Low emittance possible:**  $\theta_\mu$  is tunable with  $\sqrt{s}$  in  $e^+e^- \rightarrow \mu^+\mu^-$   
 $\theta_\mu$  can be **very small** close to the  $\mu^+\mu^-$  threshold
- 2. Low background:** Luminosity at low emittance will allow low background and low  $\nu$  radiation (easier experimental conditions, can go up in energy)
- 3. Reduced losses from decay:** muons can be produced with a relatively high boost in asymmetric collisions
- 4. Energy spread:** muon energy spread **also small at threshold**, it gets larger as  $\sqrt{s}$  increases

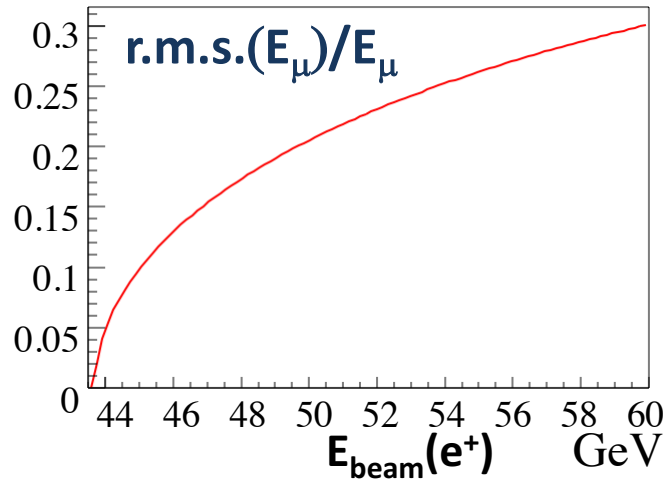
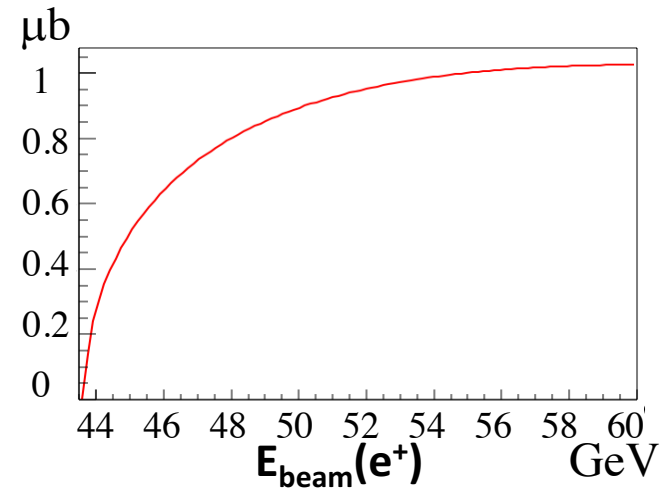
## Disadvantages:

- Rate:** much smaller cross section wrt protons ( $\approx$  mb)  
$$\sigma(e^+e^- \rightarrow \mu^+\mu^-) \approx 1 \mu\text{b} \quad \text{at most}$$

# Parametric behaviours



$$\sigma(e^+e^- \rightarrow \mu^+\mu^-)$$



# Criteria for target design

- minimize emittance → thin target
- maximize rate → maximize density (high Z)
- minimize positron loss (brem.) → low Z

- **Heavy materials, thin target**

- to minimize  $\varepsilon_\mu$ : thin target ( $\varepsilon_\mu \propto \text{length}$ ) with high density  $\rho$   
Copper: MS and  $\mu^+\mu^-$  production give about same contribution to  $\varepsilon_\mu$

- BUT high  $e^+$  loss (Bremsstrahlung is dominant) so

- $\sigma(e^+\text{loss}) \approx \sigma(\text{Brem}+\text{bhabha}) \approx (Z+1)\sigma(\text{Bhabha}) \rightarrow$

- low maximal  $\mu^+\mu^-$  production efficiency (infinite length target)

- $\text{Eff}_{\text{max}} \approx \sigma_\mu / [(Z+1)\sigma(\text{Bhabha})] \sim 10^{-7}$

- **Very light materials, thick target**

- maximize  $\mu^+\mu^-$  production efficiency  $\sim 10^{-5}$  (enters quad) →  $\text{H}_2$

- Even for liquid targets O(1m) needed →  $\varepsilon_\mu$  increase

- **Not too heavy materials (Be, C, Li)**

- Allow low  $\varepsilon_\mu$  with small  $e^+$  loss  $\text{Eff}_{\text{max}} \approx 10^{-6}$

**not too heavy and thin in combination with stored positron beam  
to reduce the requests on positron source**

# Preliminary scheme for low emittance $\mu$ beam production

## Goal:

$$@T \approx 10^{11} \mu/s$$

Efficiency  $\approx 10^{-7}$  (with Be 3mm)  $\rightarrow$

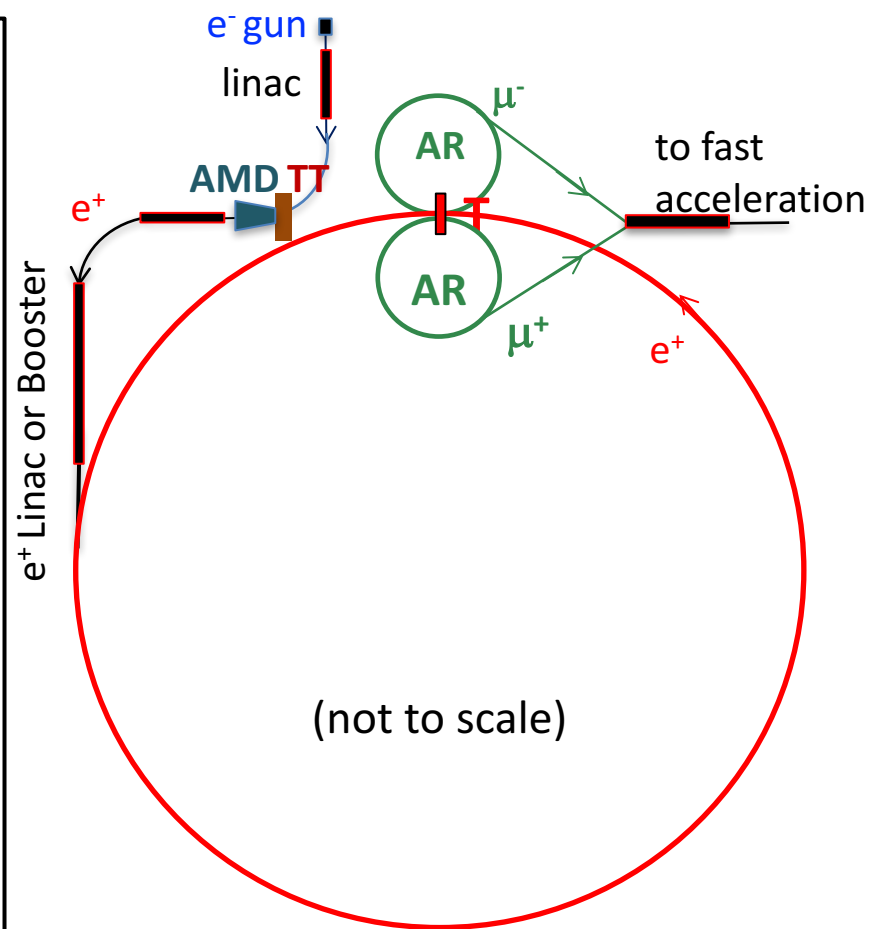
$10^{18} e^+/s$  needed @T  $\rightarrow$

$e^+$  stored beam with T

need the largest possible lifetime to minimize positron source rate

LHeC like  $e^+$  source required rate with lifetime( $e^+$ )  $\approx 250$  turns [i.e. 25% momentum aperture]  $\rightarrow$

$$n(\mu)/n(e^+ \text{ source}) \approx 10^{-5}$$





# Preliminary scheme for low emittance $\mu$ beam production

## from $e^+$ SOURCE to RING:

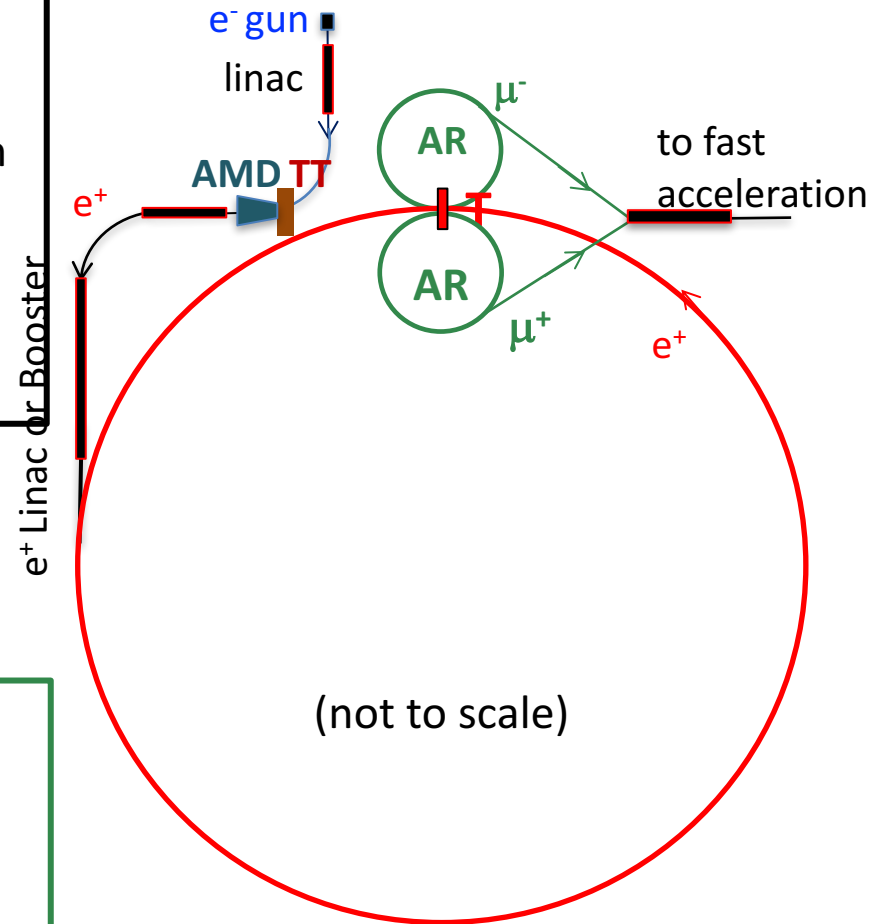
- $e^-$  on conventional Heavy Thick Target (TT) for  $e^+e^-$  pairs production.
- possibly with  $\gamma$  produced by  $e^+$  stored beam on T  $\rightarrow$
- Adiabatic Matching Device (AMD) for  $e^+$  collection  $\rightarrow$
- acceleration (linac / booster), injection  $\rightarrow$

## $e^+$ RING:

- 6.3 km 45 GeV storage ring with target T for muon production

## from $\mu^+ \mu^-$ production to collider

- produced by the  $e^+$  beam on target T with  $E(\mu) \approx 22 \text{ GeV}$ ,  $\gamma(\mu) \approx 200 \rightarrow \tau_{\text{lab}}(\mu) \approx 500 \mu\text{s}$
- AR: 60 m isochronous and high mom. acceptance rings will recombine  $\mu$  bunches for  $\sim 1 \tau_{\mu}^{\text{lab}} \approx 2500$  turns
- fast acceleration
- muon collider



# Preliminary scheme for low emittance $\mu$ beam production

## from $e^+$ SOURCE to RING:

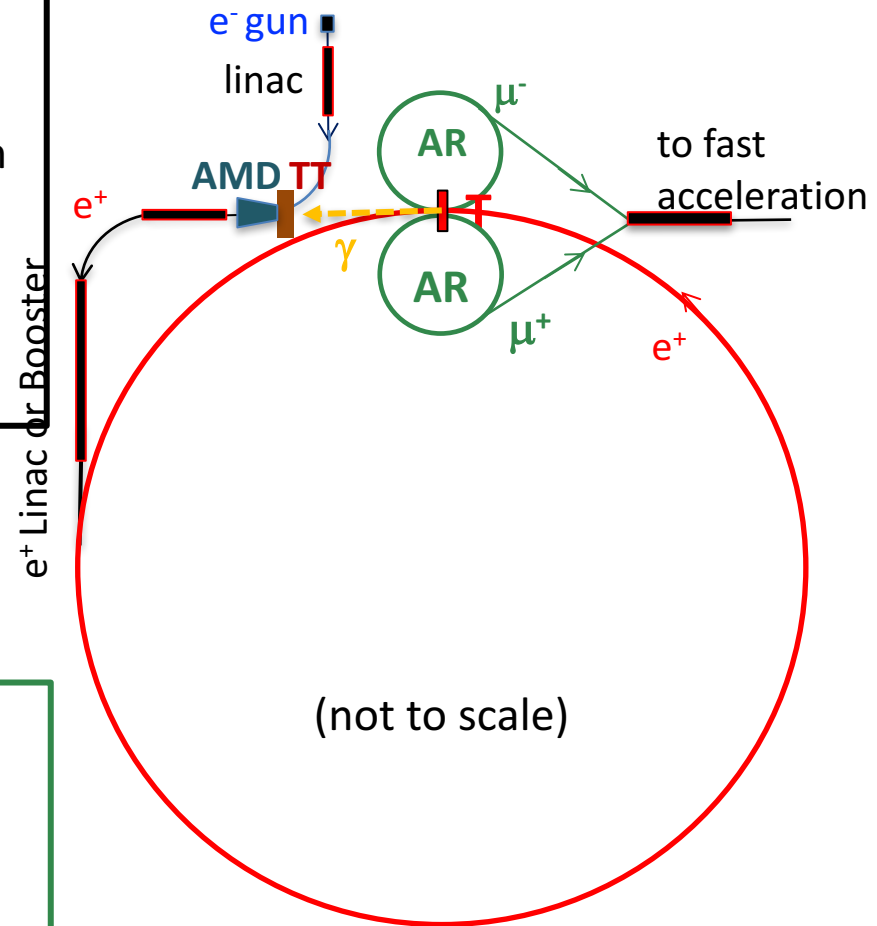
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- possibly with  $\gamma$  produced by  $e^+$  stored beam on T  $\rightarrow$
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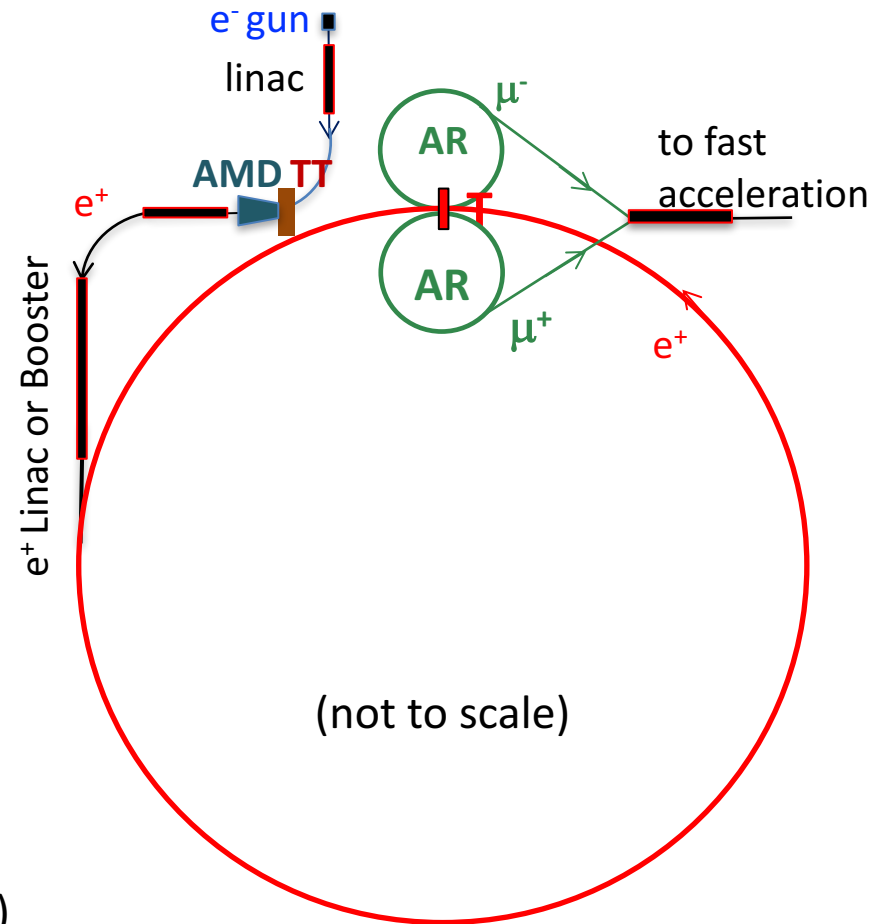
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- fast acceleration
- muon collider



# Preliminary scheme for low emittance $\mu$ beam production

e <sup>+</sup> ring parameter	unit	
Circumference	km	6.3
Energy	GeV	45
bunches	#	100
e <sup>+</sup> bunch spacing = T <sub>rev</sub> (AR)	ns	200
Beam current	mA	240
N(e <sup>+</sup> )/bunch	#	3 · 10 <sup>11</sup>
U <sub>0</sub>	GeV	0.51
SR power	MW	120



(also 28 km foreseen to be studied as an option)

# 6 TeV $\mu$ collider draft Parameters

no lattice yet

$\mu^+\mu^-$  rate =  $9 \cdot 10^{10}$  Hz [ NIM A 807  
 $\epsilon_N = 40$  nm 101-107 (2016)]

if: LHeC like  $e^+$  source

with 25% mom. accept.  $e^+$  ring  
 and  $\epsilon$  dominated by  $\mu$  production

thanks to very small  
 emittance (and lower beta\*)  
 comparable luminosity with  
 lower  $N\mu$ /bunch  
 ( $\rightarrow$  lower background)

Of course, a design study  
 is needed to have a  
 reliable estimate of  
 performances

Parameter	Units	LEMC-6TeV
LUMINOSITY/IP	$\text{cm}^{-2} \text{s}^{-1}$	5.09E+34
Beam Energy	GeV	3000
Hourglass reduction factor		1.000
Muon mass	GeV	0.10566
Lifetime @ prod	sec	2.20E-06
Lifetime	sec	0.06
c*tau @ prod	m	658.00
c*tau	m	1.87E+07
1/tau	Hz	1.60E+01
Circumference	m	6000
Bending Field	T	15
Bending radius	m	667
Magnetic rigidity	T m	10000
Gamma Lorentz factor		28392.96
N turns before decay		3113.76
$\beta_x$ @ IP	m	0.0002
$\beta_y$ @ IP	m	0.0002
Beta ratio		1.0
Coupling (full current)	%	100
Normalised Emittance x	m	4.00E-08
Emittance x	m	1.41E-12
Emittance y	m	1.41E-12
Emittance ratio		1.0
Bunch length (zero current)	mm	0.1
Bunch length (full current)	mm	0.1
Beam current	mA	0.048
Revolution frequency	Hz	5.00E+04
Revolution period	s	2.00E-05
Number of bunches	#	1
N. Particle/bunch	#	6.00E+09
Number of IP	#	1.00
$\sigma_x$ @ IP	micron	1.68E-02
$\sigma_y$ @ IP	micron	1.68E-02
$\sigma_x$ @ IP	rad	8.39E-05
$\sigma_y$ @ IP	rad	8.39E-05

# Radiological hazard due to neutrinos from a muon collider

Colin Johnson, Gigi Rolandi and Marco Silari

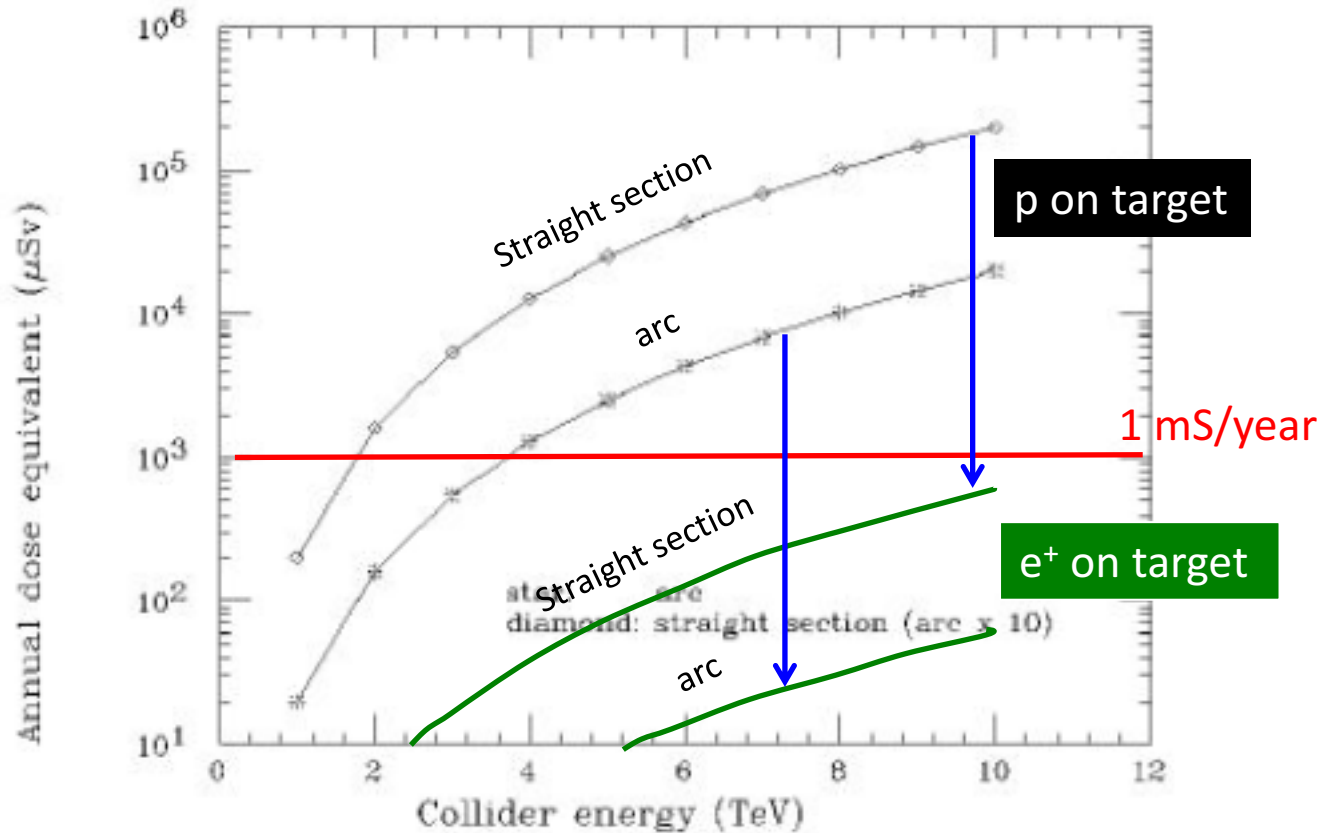


Fig. 1. Dose equivalent due to neutrino radiation at 36 km distance (collider at 100 m depth)

muon rate: p on target option  $3 \cdot 10^{13} \mu/\text{s}$

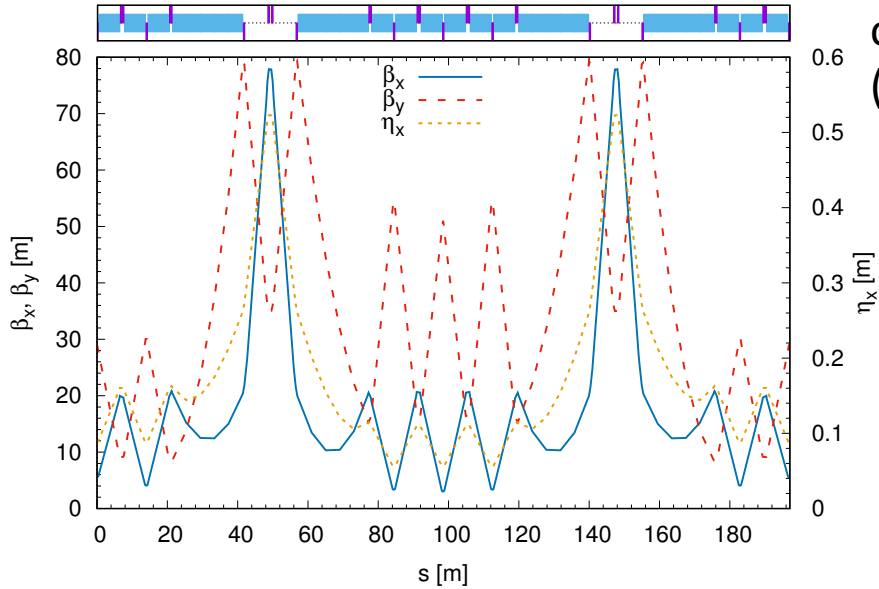
**e+ on target option  $9 \cdot 10^{10} \mu/\text{s}$**

# Key topics for this scheme

- **Low emittance and high momentum acceptance 45 GeV  $e^+$  ring**
- **$O(100 \text{ kW})$  class target in the  $e^+$  ring for  $\mu^+ \mu^-$  production**
- **High rate positron source**
- **High momentum acceptance muon accumulator rings**

# Low emittance 45 GeV positron ring

cell

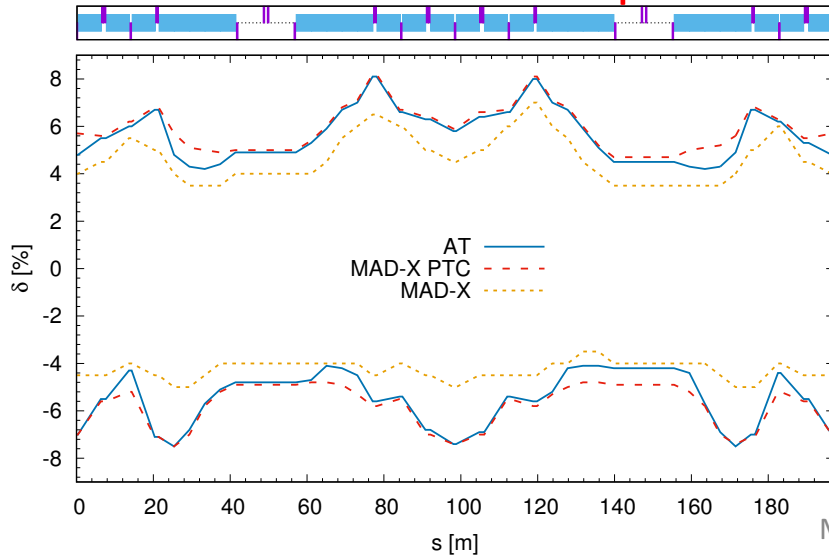


circumference 6.3 km: 197 m x 32 cells  
(no injection section yet)

## Table e+ ring parameters

Parameter	Units	
Energy	GeV	45
Circumference	m	6300
Coupling(full current)	%	1
Emittance x	m	$5.73 \times 10^{-9}$
Emittance y	m	$5.73 \times 10^{-11}$
Bunch length	mm	3
Beam current	mA	240
RF frequency	MHz	500
RF voltage	GV	1.15
Harmonic number	#	10508
Number of bunches	#	100
N. particles/bunch	#	$3.15 \times 10^{11}$
Synchrotron tune		0.068
Transverse damping time	turns	175
Longitudinal damping time	turns	87.5
Energy loss/turn	GeV	0.511
Momentum compaction		$1.1 \times 10^{-4}$
RF acceptance	%	$\pm 7.2$
Energy spread	dE/E	$1 \times 10^{-3}$
SR power	MW	120

## momentum acceptance



Physical aperture=5 cm constant

no errors

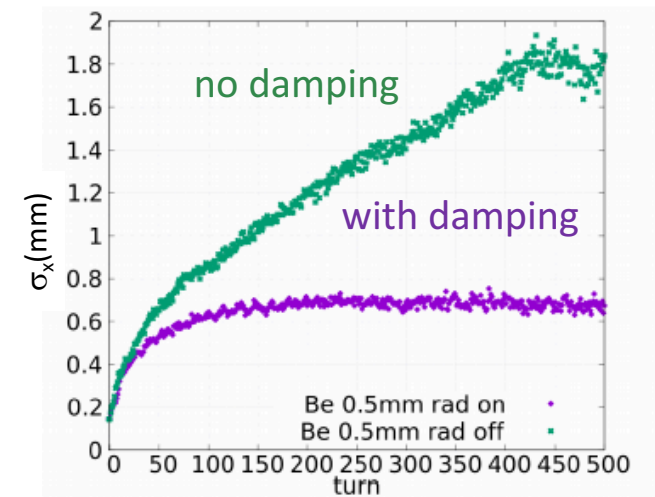
Good agreement between **MADX PTC** / **Accelerator Toolbox**,  
both used for particle tracking in our studies

# Multi-turn simulations

1. Initial 6D distribution from the equilibrium emittances
2. 6D  $e^+$  distribution tracking up to the target (AT and MAD-X PTC)
3. tracking through the target (with Geant4beamline and FLUKA and GEANT4)
4. back to tracking code

At each pass through the muon target the  $e^+$  beam

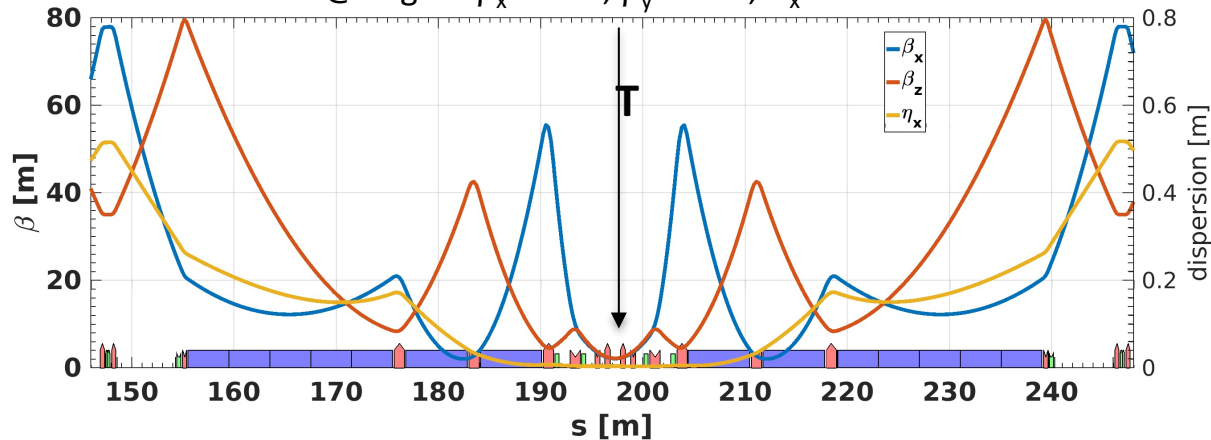
- gets an angular kick due to the **multiple Coulomb scattering**, so at each pass changes  $e^+$  beam divergence and size, resulting in an emittance increase.
- undergoes **bremsstrahlung energy loss**: to minimize the beam degradation due to this effect,  $D_x=0$  at target
- in addition there is natural radiation **damping** (it prevents an indefinite beam growth)





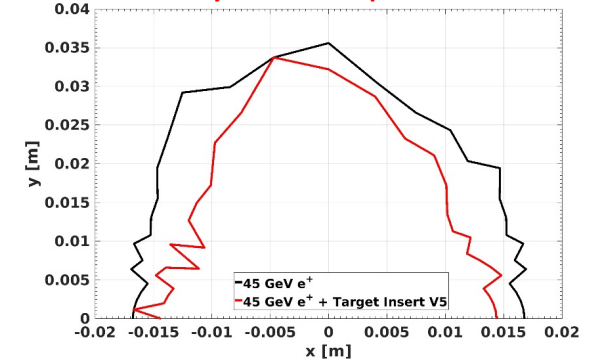
# Preliminary low- $\beta$ IR for muon target insertion

@target:  $\beta_x=1.6\text{m}$ ;  $\beta_y=1.7\text{m}$ ;  $D_x=5.4\text{mm}$

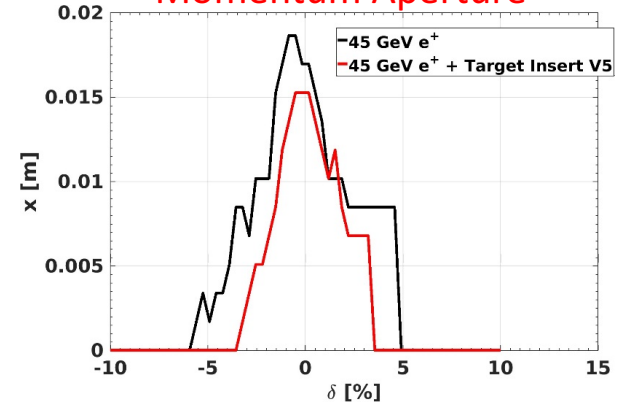


- @target location:
  - $D_x \approx 0$
  - low- $\beta$
- Further optimizations are underway:
  - match the transverse minimum beam size with constraints of target thermo-mechanical stress
  - match with other contributions to muon emittance (production, accumulation)
  - dynamic and momentum aperture can be optimized

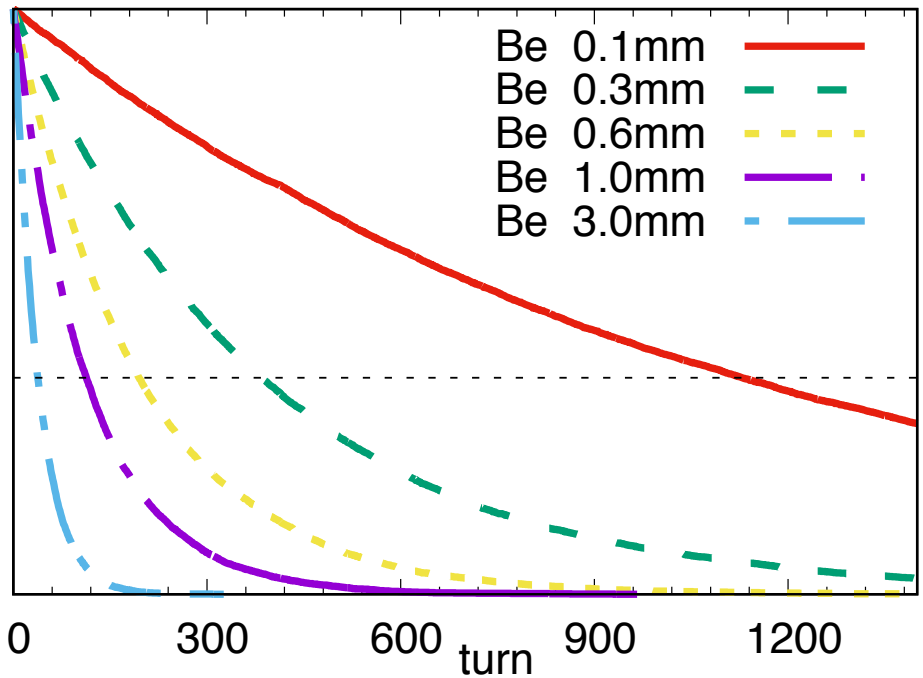
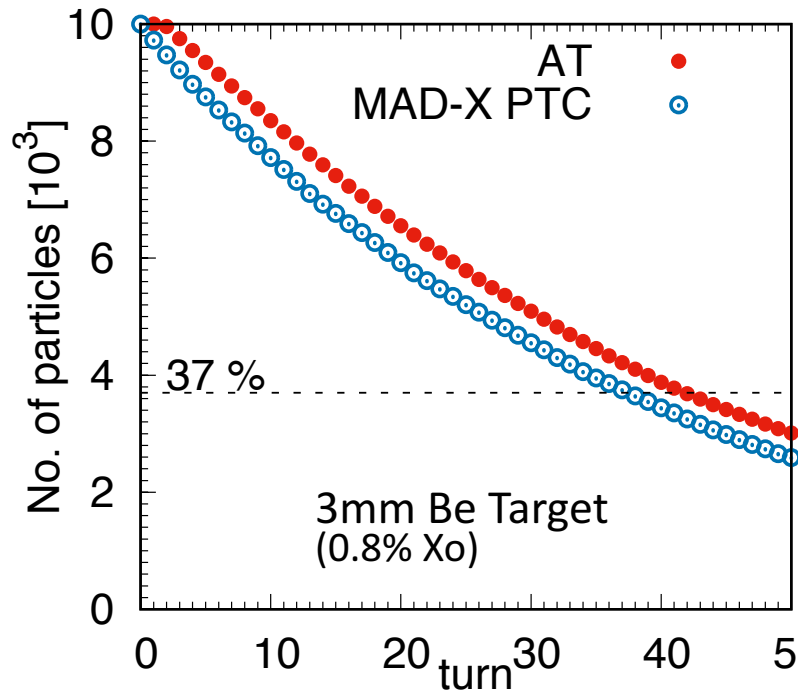
## Dynamic Aperture



## Momentum Aperture

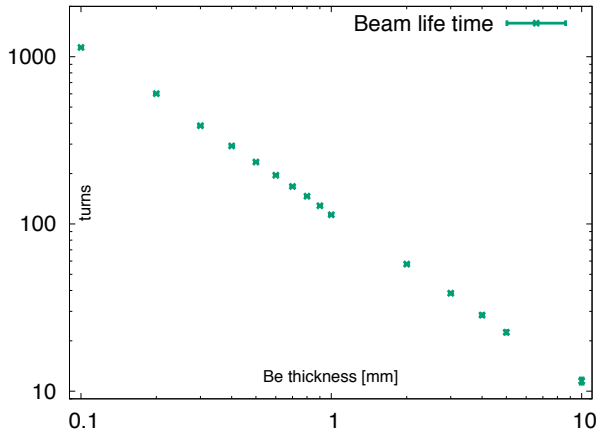
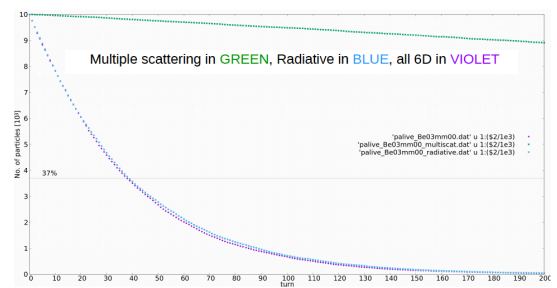


# e+ lifetime with Be target



determined by **bremstrahlung** and **momentum acceptance**  
 Lifetime with  $\sim 40$  turns  
 agreement within 10%

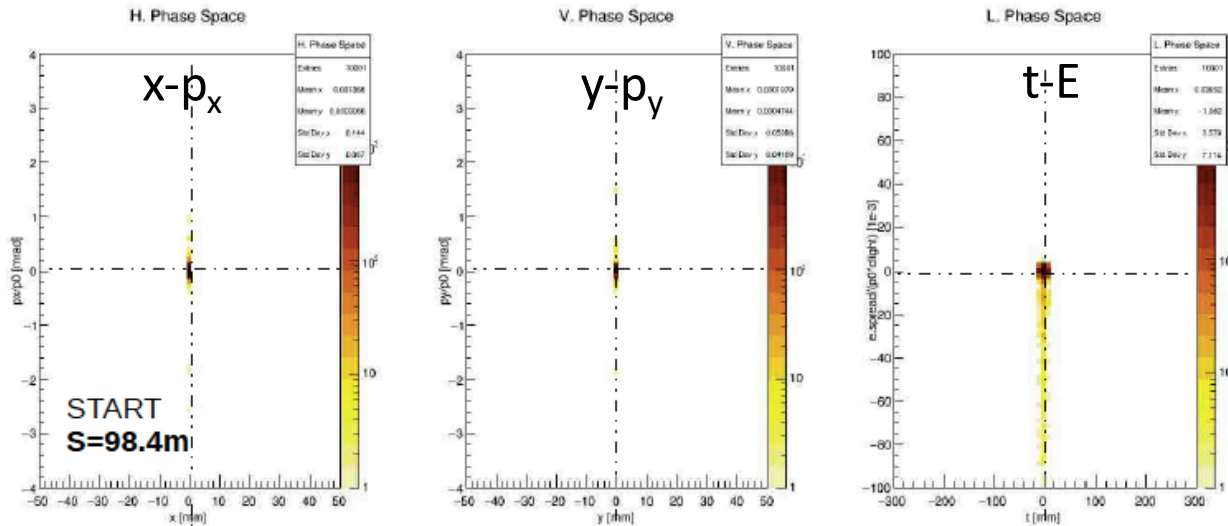
Lifetime  $\propto 1/\text{thickness}$  as expected



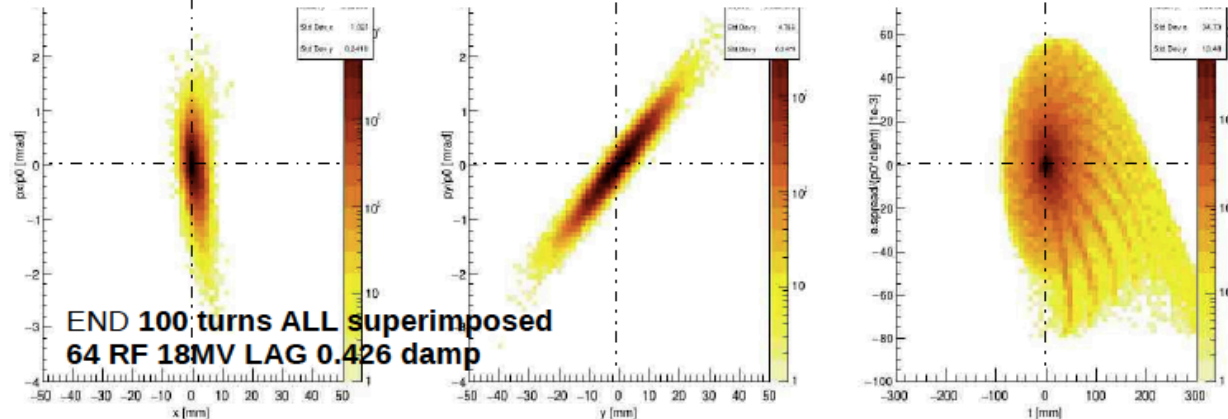
2-3% e+ losses happen in the first turn Boscolo, IPAC17

# e+ ring with target: beam evolution in the 6D phase space

before target,  
starting point



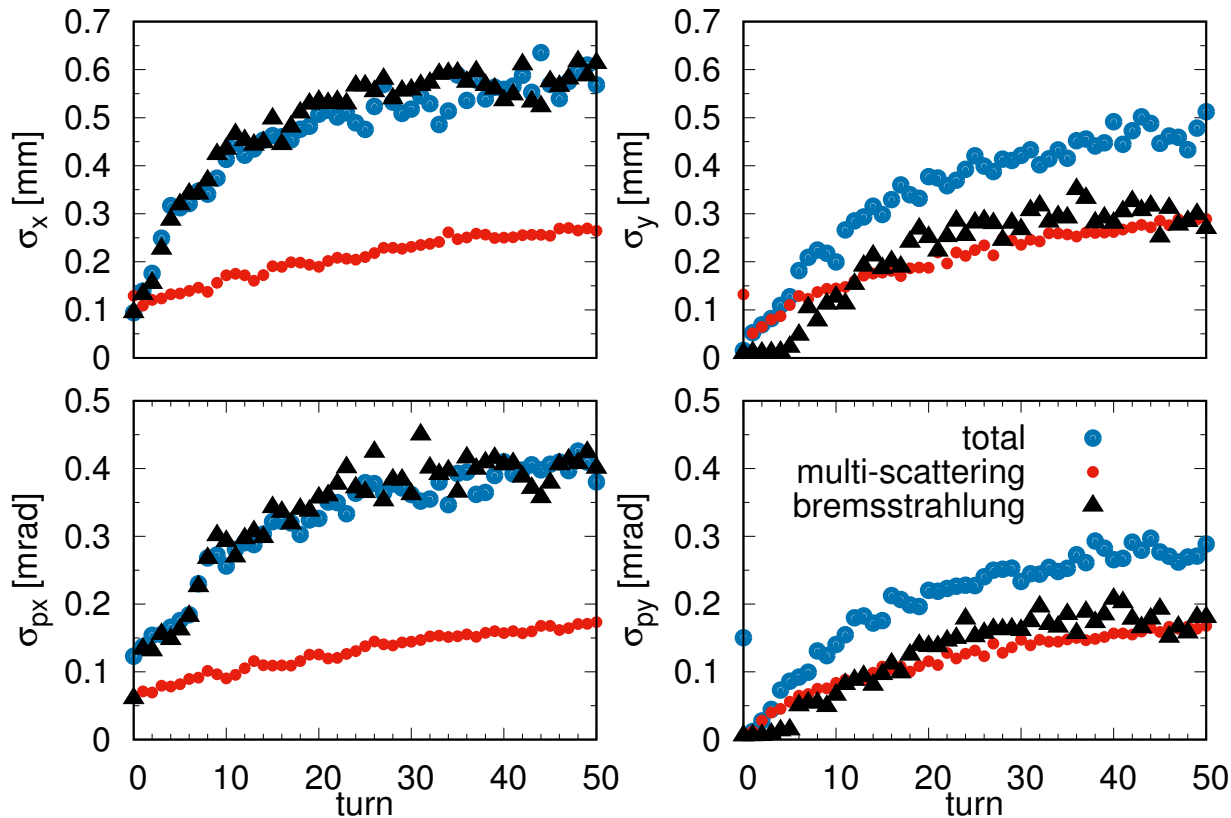
after 40 turns



MAD-X PTC & GEANT4 6-D tracking simulation of e+ beam with 3 mm Be target along the ring (not at IR center in this example)

# Evolution of e+ beam size and divergence

3mm Be Target (0.8% Xo) at center of IR



bremsstrahlung and multiple scattering artificially separated by considering alternatively effects in longitudinal (dominated by **bremsstrahlung**) and transverse (dominated by **multiple scattering**) phase space due to target; in **blue** the combination of both effects (realistic target)

Some bremsstrahlung contribution due to residual dispersion at target  
 multiple scattering contribution in line with expectation:  $\sigma_{MS} = \frac{1}{2} \sqrt{n_D} \sigma'_{MS} \beta$   
 one pass contribution due to the target:  $\sigma'_{MS} = 25 \mu\text{rad}$

# Muon emittance

$$\varepsilon(\mu) = \varepsilon(e^+) \oplus \varepsilon(\text{MS}) \oplus \varepsilon(\text{rad}) \oplus \varepsilon(\text{prod}) \oplus \varepsilon(\text{AR})$$

would like all contributions of same size  
knobs:

$\varepsilon(e^+)$  =  $e^+$  emittance

$\varepsilon(\text{MS})$  = multiple scattering contribution

$\varepsilon(\text{rad})$  = energy loss (brem.) contribution

$\varepsilon(\text{prod})$  = muon production contribution

$\varepsilon(\text{AR})$  = accumulator ring contribution

$\beta_x \beta_y$  @target & target material

$\beta_x \beta_y D_x$  @target & target material

$E(e^+)$  & target thickness

AR optics & target

with constraints from target survival

now:  $\varepsilon(\mu)$  dominated by  $\varepsilon(\text{MS}) \oplus \varepsilon(\text{rad})$  -> lower dispersion & lower  $\beta$ -functions at target  
with beam spot at the limit of the target survival

also test different material

- crystals in channeling better:  $\varepsilon(\text{MS})$ ,  $\varepsilon(\text{rad})$ ,  $\varepsilon(\text{prod})$  (also gain in lifetime)
- light liquid jet target better:  $\varepsilon(\text{MS})$ ,  $\varepsilon(\text{rad})$   
(also gain in lifetime & target thermo-mechanical characteristics)

# $\mu$ Accumulator Rings considerations

isochronous optics with high momentum acceptance ( $\delta \gtrsim 10\%$ )  
optics to be designed

**Multiple Scattering effect  
using one-turn matrix** →

**beam divergence:**

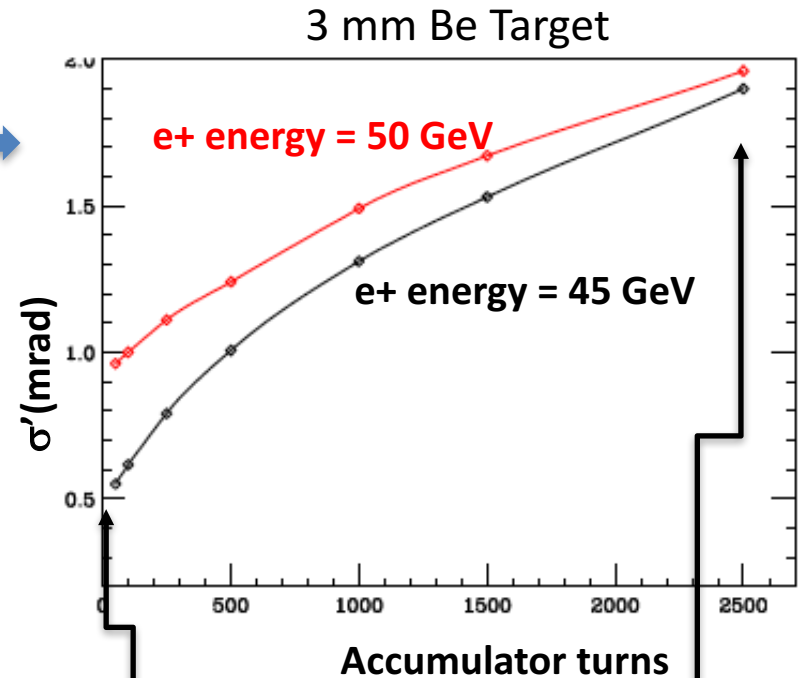
a factor 3-2 increase at 45-50 GeV w.r.t. muon  
production angle contribution

**beam size:**

depends on optics need low- $\beta$  to suppress size  
increase

this contribution can be strongly reduced with  
crystals in channeling

better performances at 50 GeV provided  
>15% momentum acceptance



muon  
production  
angle

muon  
production  
angle + MS  
contribution

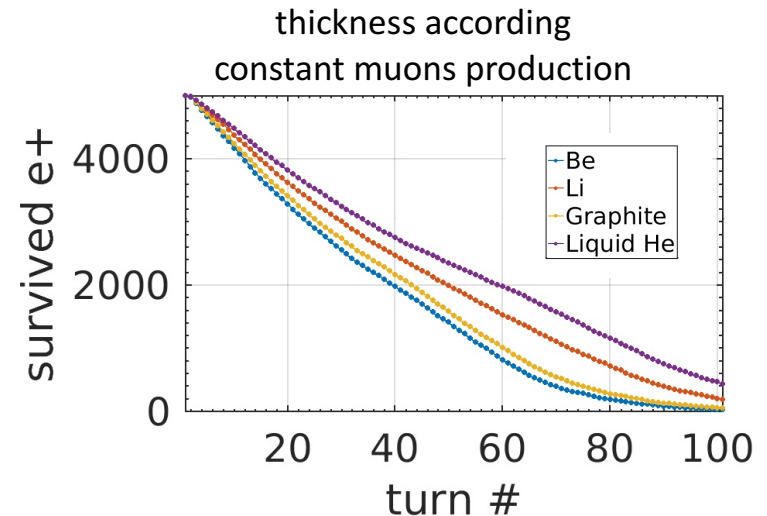
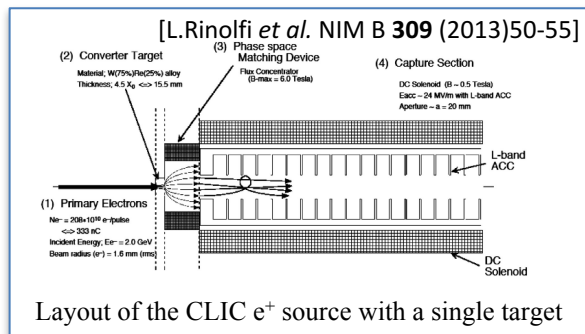
# Target considerations

Beam size as small as possible (matching various emittance contribution), but

- constraints for **power removal (200 kW)** and **temperature rise**
- to contrast the **temperature rise**  
**move target (for free with liquid jet)** and  
**e<sup>+</sup> beam bump** every 1 bunch muon accumulation
- **Solid target:** simpler and better wrt temperature rise
  - **Be, C**  
[Kavin Ammigan 6<sup>th</sup> High Power Targetry Workshop]
    - Be target: @HIRadMat safe operation with extracted beam from SPS, beam size 300 μm, N=1.7x10<sup>11</sup> p/bunch, up to 288 bunches in one shot
- **Liquid target:** better wrt power removal (200kW)
  - **Li**, difficult to handle lighter materials (H, He)
    - **LLi jets examples from neutron production, Tokamak divertor (200 kW beam power removal seems feasible) , minimum beam size to be understood**

# Conclusion and Perspectives

- First design of low emittance  $e^+$  ring with preliminary studies of beam dynamics
- Optimization requires other issues to be preliminary addressed:
  - target material & characteristics
  - $e^+$  accelerator complex



- muon accumulator rings design

Preliminary studies for a low emittance muon source are promising

We will continue to optimize all the parameters, lattices, targets, etc. in order to assess the ultimate performances of a muon collider based on this concept



# References

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# Tests with e<sup>+</sup> beam

Use tertiary 45 GeV e<sup>+</sup> beam in CERN North area (H4)  
(1 week of beam time July 2017, funded by CSN1-INFN)

- **Low intensity** (one by one e<sup>+</sup> tracking) with crystals and amorphous targets:
  - measure beam degradation (emittance energy spectrum)
  - measure produced photons flux and spectrum
- **High intensity** (up to  $5 \times 10^6$  /spill) with amorphous targets:
  - measure muon production rate and
  - muons kinematic properties