

# Diverse Beam Profile Shapings through Nonlinear Focusing of Multipole Magnets in a Beam Transport Line

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# Feasibility of beam profile shaping using the nonlinear focusing force

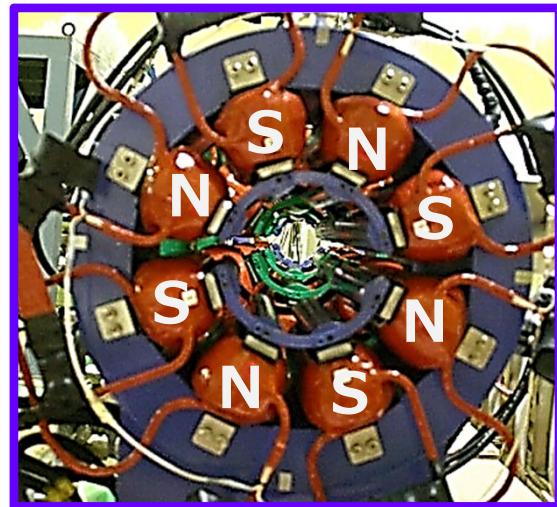
- Equation of motion in the horizontal and vertical directions:

$$\begin{cases} x'' + K_{\text{QUAD}}(s)x + \frac{K_{\text{SXT}}(s)}{2!}(x^2 - y^2) + \frac{K_{\text{OCT}}(s)}{3!}(x^3 - 3xy^2) + \dots = 0 \\ y'' - K_{\text{QUAD}}(s)y - \frac{K_{\text{SXT}}(s)}{2!}(2xy) + \frac{K_{\text{OCT}}(s)}{3!}(y^3 - 3x^2y) + \dots = 0 \end{cases}$$

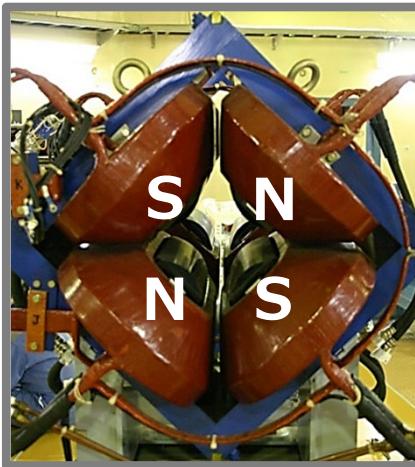
**Quadrupole      Sextupole      Octupole**

- Controlling the complicated particle motion properly,
  - ➡ It should be possible to generate unique beam profiles that can never be realized by linear focusing.
    - ✓ Uniform profile (NSRL@BNL, J-PARC, etc.)
    - ✓ Hollow profile

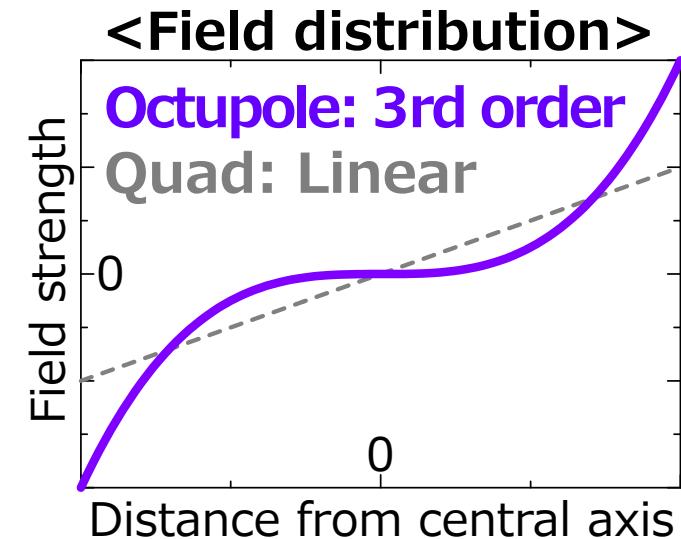
# Beam shaping using octupole magnets



Octupole magnet

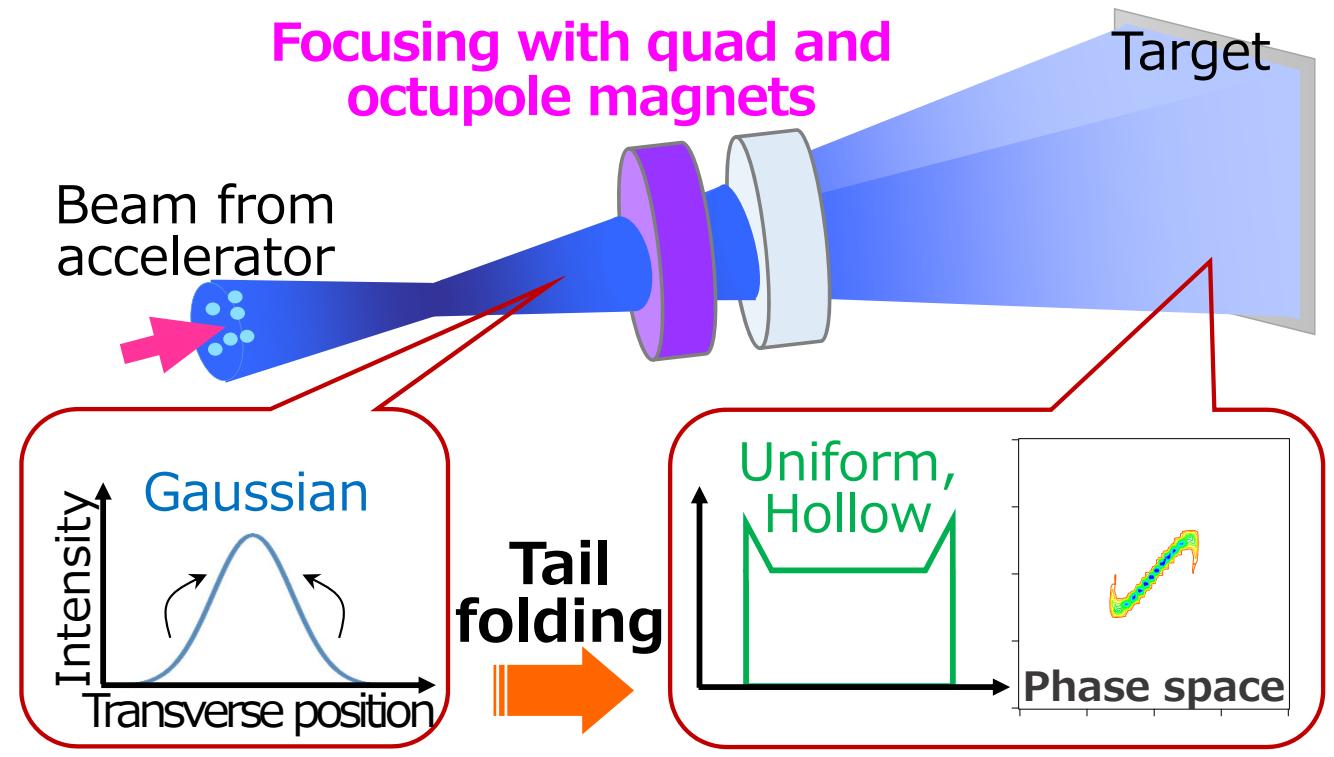


Quadrupole magnet



## 【Principle】

- The tail of the distribution can be folded by the nonlinear force.
- The phase-space profile is deformed into an "S"-shape.



# QST Takasaki's Cyclotron Facility

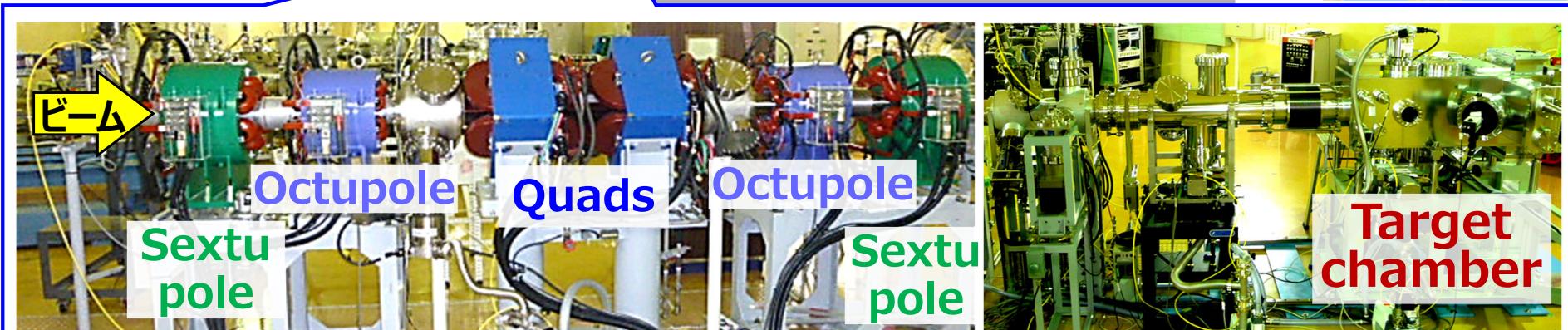
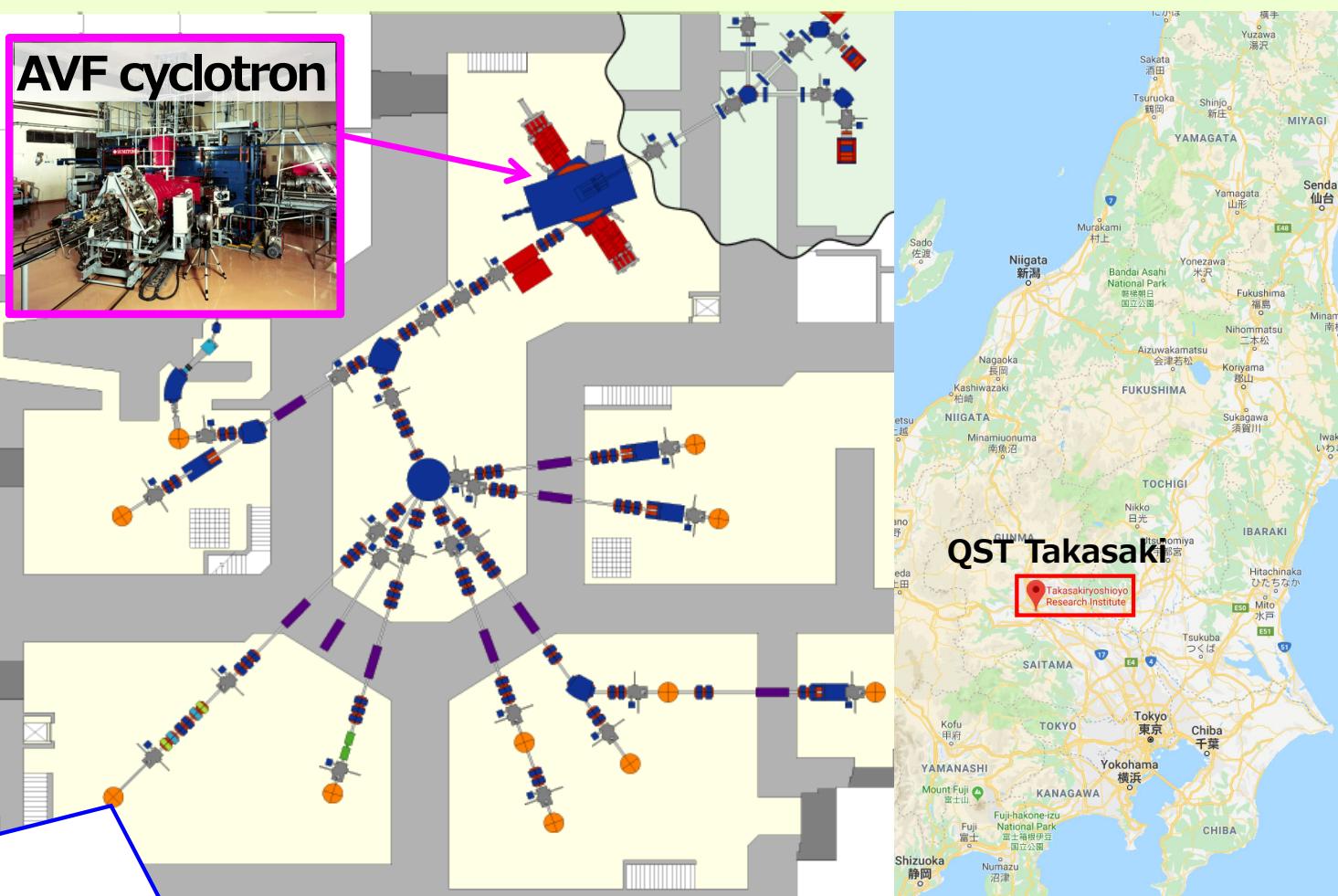
Bending limit  $K_b$  110 MeV

Ion species    Energy [MeV]

H	10 ~ 90
He	20 ~ 107
C	75 ~ 320
Ar	107 ~ 520
Kr	210 ~ 520
Xe	320 ~ 560

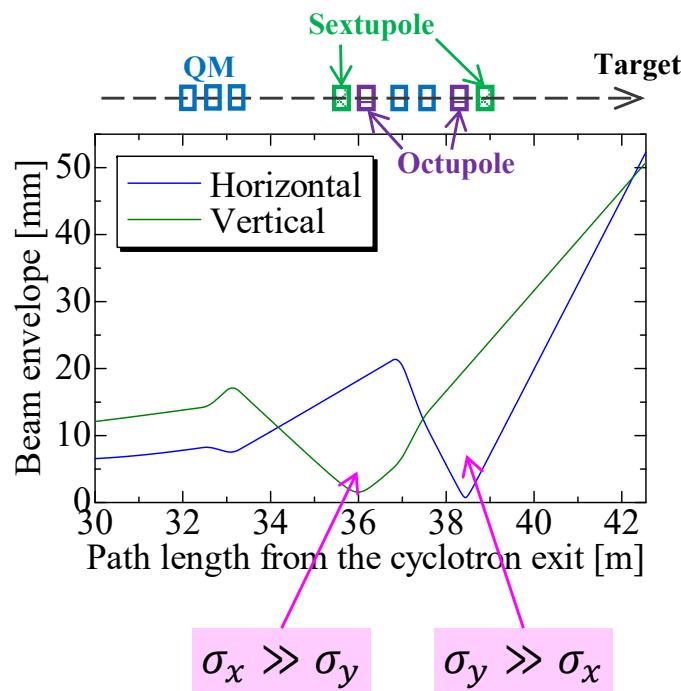
## Main applications

- RI production
- Mutagenesis of plants
- Material modification
- Radiation testing of devices



# Existing nonlinear beam shaping: Uniform beam formation

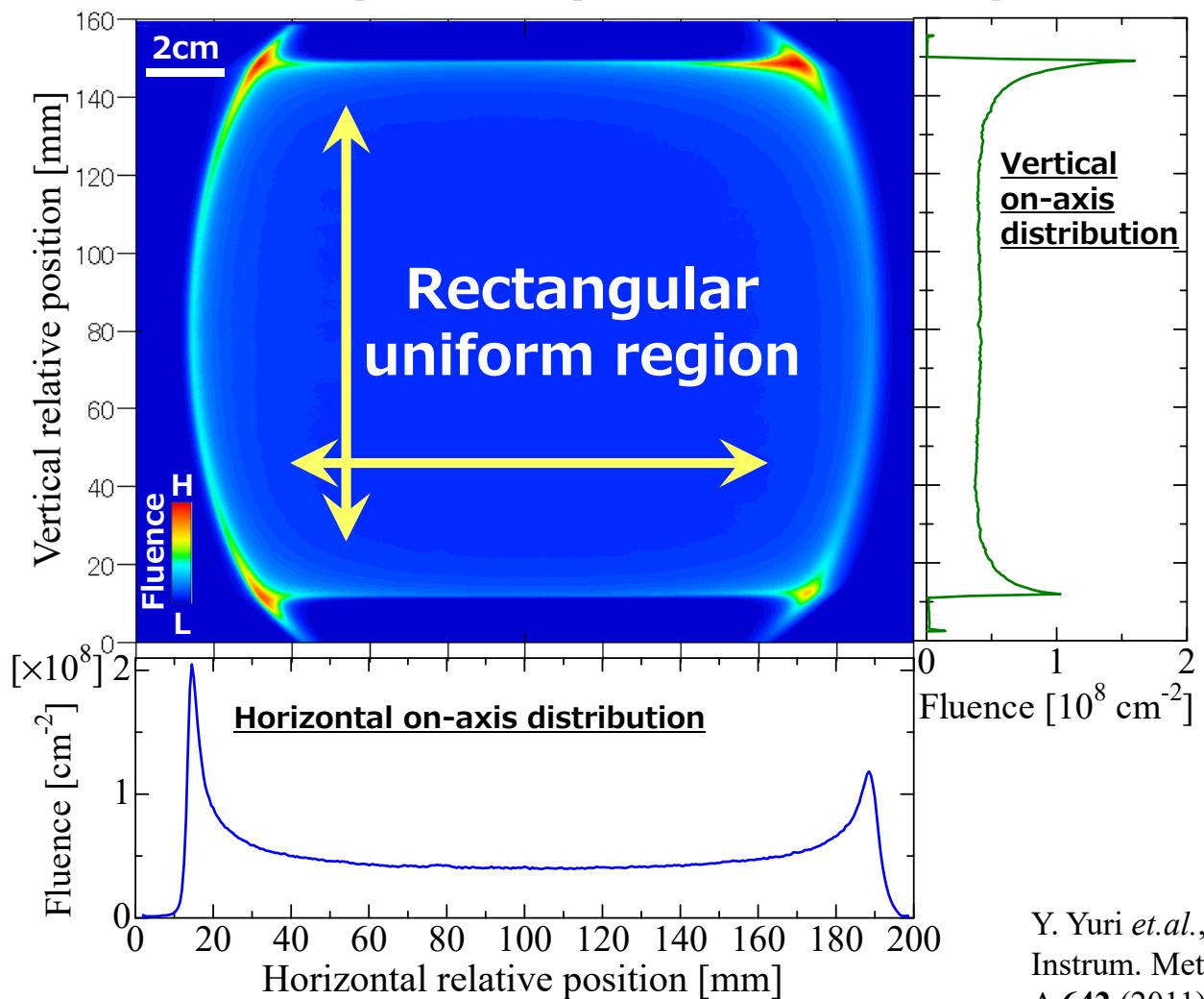
## [Beam optics]



X-Y coupling is reduced at OCTs

Large-area uniform beam realized using octupole magnets

[2D profile (560MeV  $^{129}\text{Xe}$ ) ]



Y. Yuri *et.al.*, Nucl. Instrum. Methods A 642 (2011) 10.

- ✓ Ion species: H, He, C, Ar, Xe
- ✓ Area:  $20 \sim 200 \text{ cm}^2$
- ✓ Uniformity < 10%

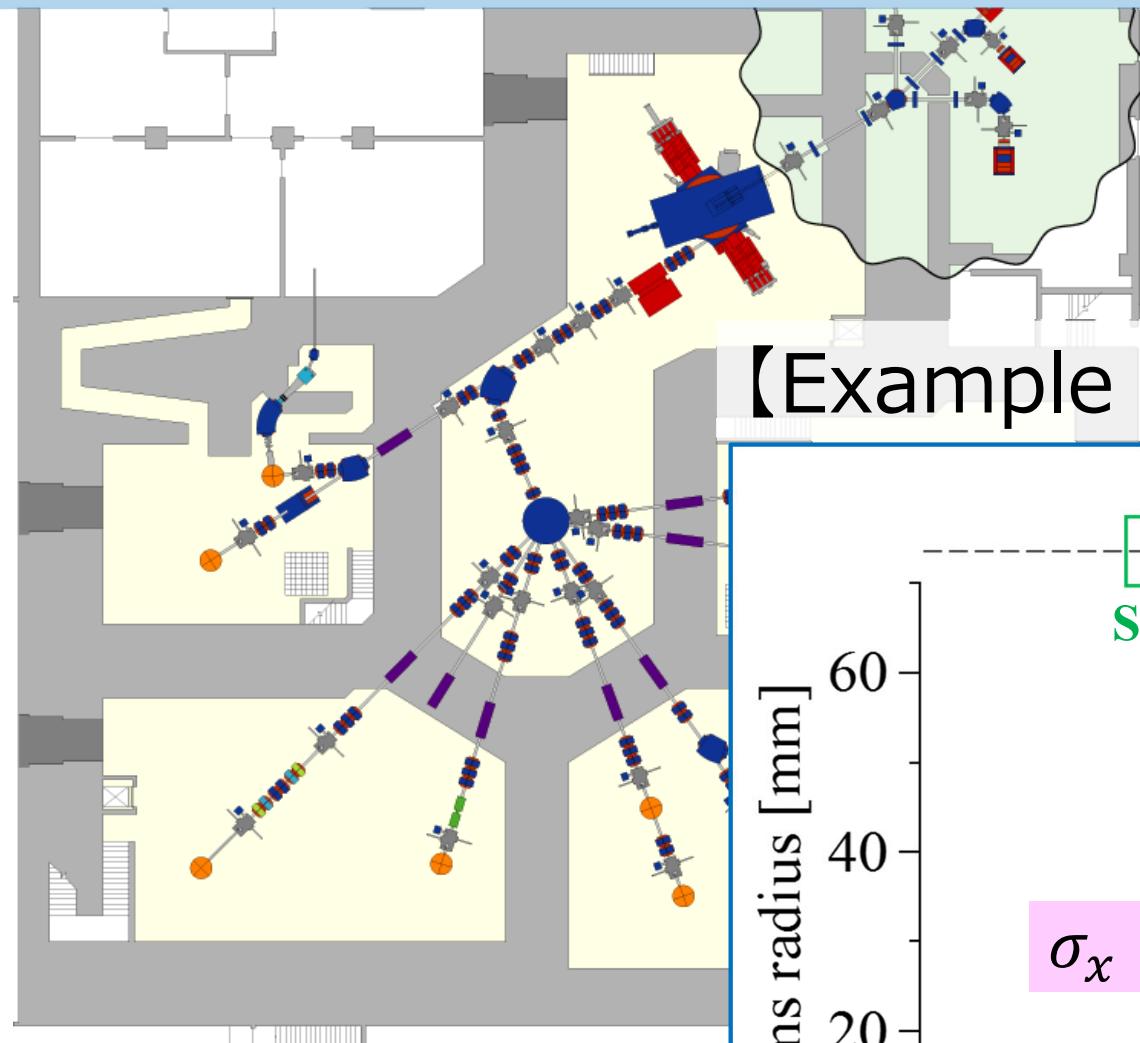
# Diverse beam shaping: Hollow beam formation

- Existing method (uniform beam formation)
  - ✓ The peak is generated at the edge of the beam.  
⇒ Central uniform region is used for uniform irradiation.
  - ✓ Horizontal-vertical coupling is suppressed.  
⇒ Rectangular cross-sectional shape

## ■ New scheme

- ✓ Raise the intensity around the edge  
⇒ **Distribution can be made “hollow.”**
- ✓ Betatron coupling  
⇒ **Various cross-sectional shapes**  
(other than a rectangle)

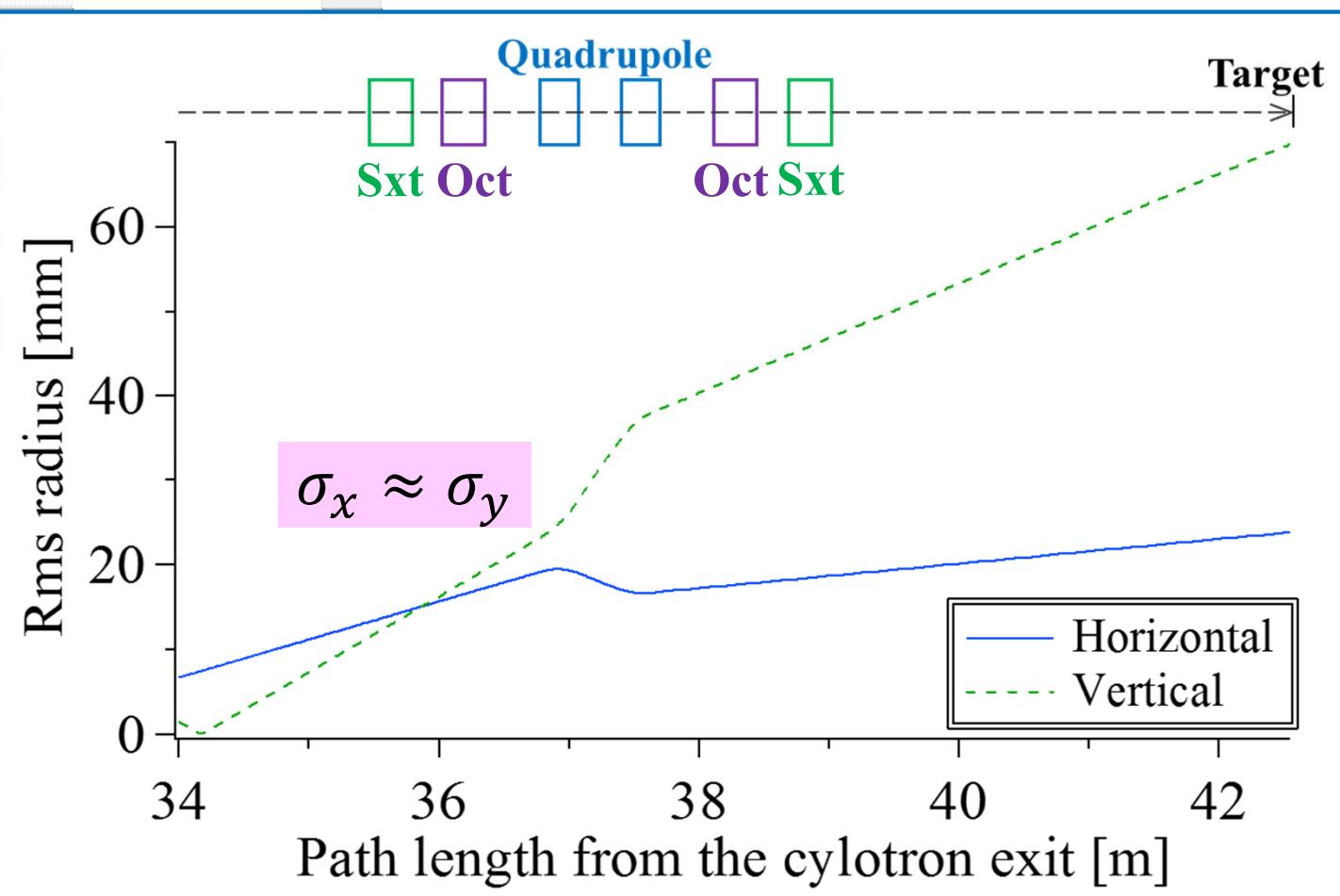
# Beam experiment at QST Takasaki



【Main conditions】

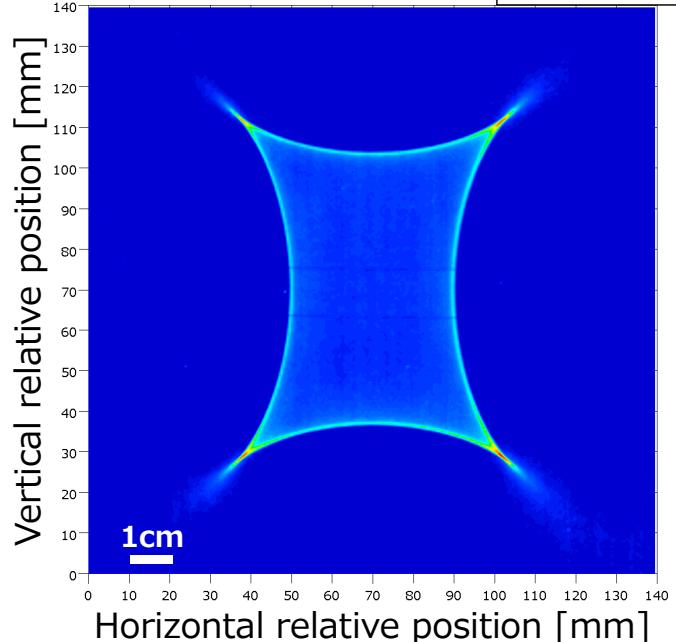
- ✓ Ion species: 10 MeV proton  
( $B\beta=0.46$  Tm,  $\beta=0.144$ ,  $\gamma=1.011$ )
- ✓  $I \sim 1$  nA (No space-charge effect)

【Example of the linear beam optics】

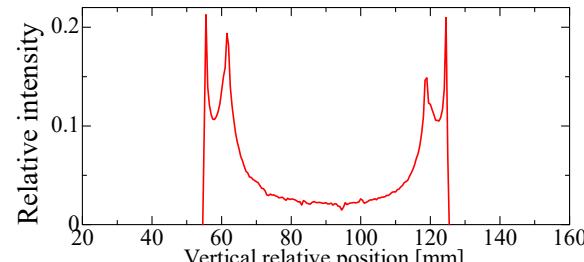
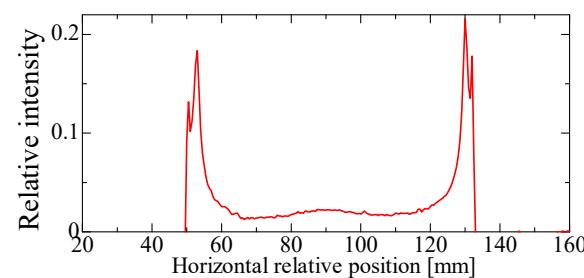
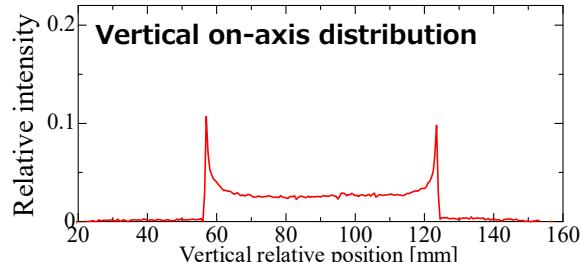
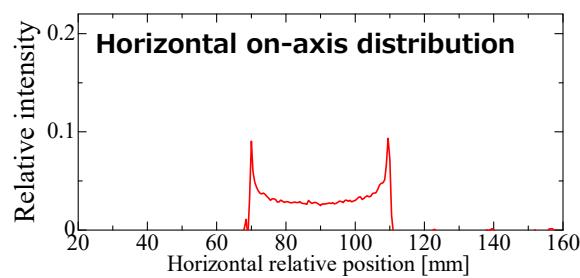
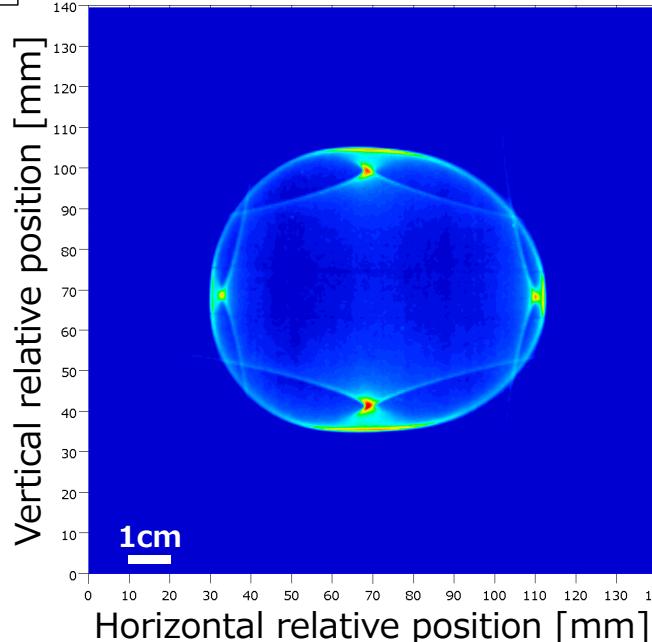


# Experimental results (1)

One octupole: ON



Two octupoles: ON



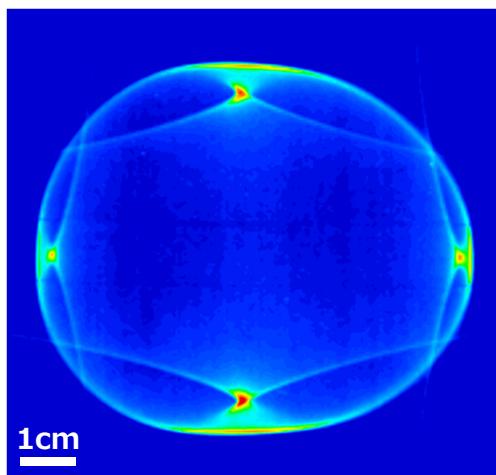
**Size~8cm x 7cm  
Peak width~1mm  
Contrast~14 (max)**

**Hollow-beam formation demonstrated!!**

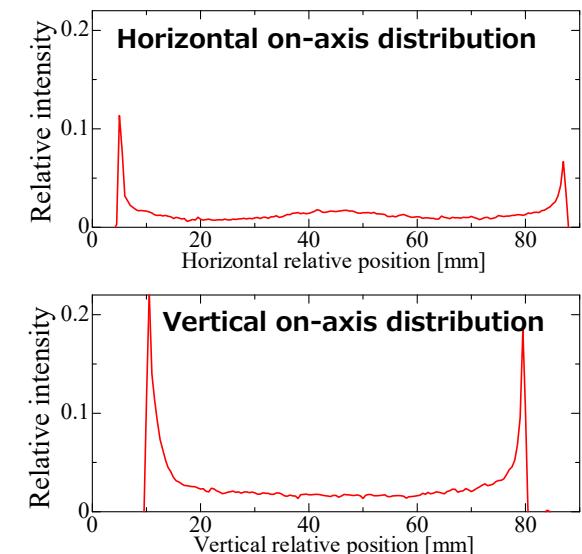
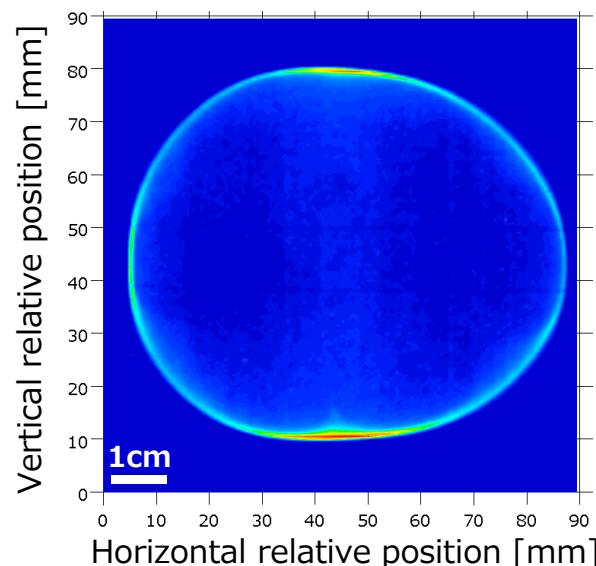
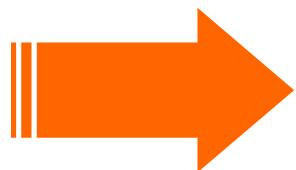
# Experimental results (2)

$$K_{OCT1} = -10,500 \text{ [m}^{-4}]$$
$$K_{OCT2} = 3,100 \text{ [m}^{-4}]$$

Tail collimation using beam slits  
before octupole magnets



**"Streaks"**

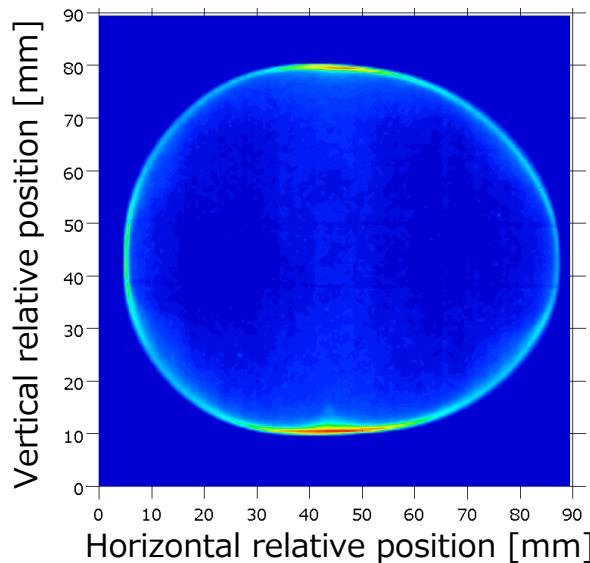


- ✓ The streaks have been suppressed.
- ✓ These streaks are induced by strong X-Y coupling.
- ✓ Clearly hollow profile!!

# Experimental results (3)

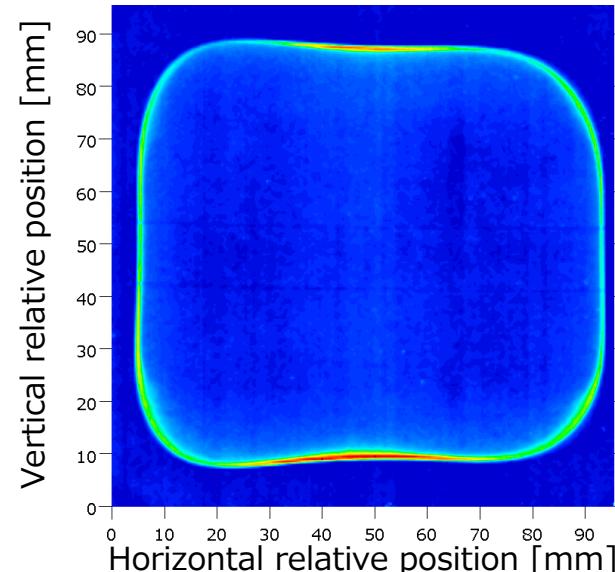
The cross-sectional shape changes depending on the octupole strength.

$$\begin{aligned}K_{\text{OCT1}} &= -10,500 [\text{m}^{-4}] \\K_{\text{OCT2}} &= 3,100 [\text{m}^{-4}]\end{aligned}$$



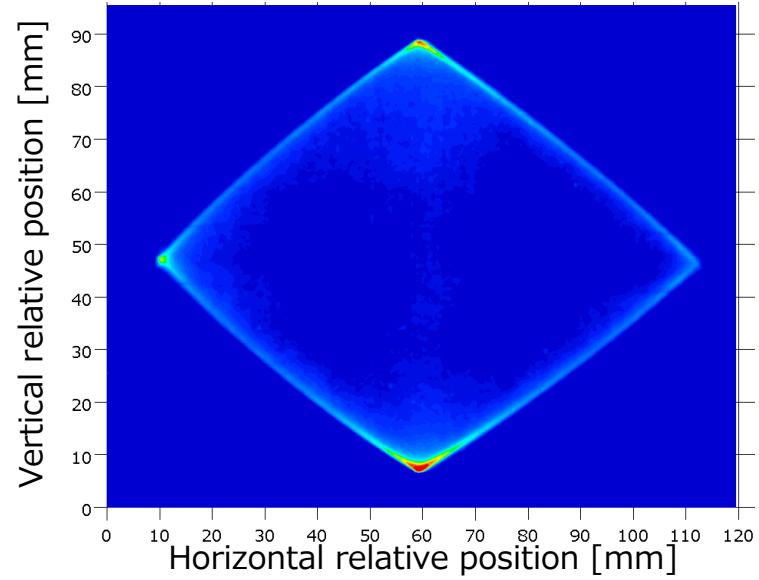
*Ellipse*

$$\begin{aligned}K_{\text{OCT1}} &= -6,700 [\text{m}^{-4}] \\K_{\text{OCT2}} &= 2,400 [\text{m}^{-4}]\end{aligned}$$



*Rounded rectangle*

$$\begin{aligned}K_{\text{OCT1}} &= -11,300 [\text{m}^{-4}] \\K_{\text{OCT2}} &= 2,300 [\text{m}^{-4}]\end{aligned}$$



*Rhombus*

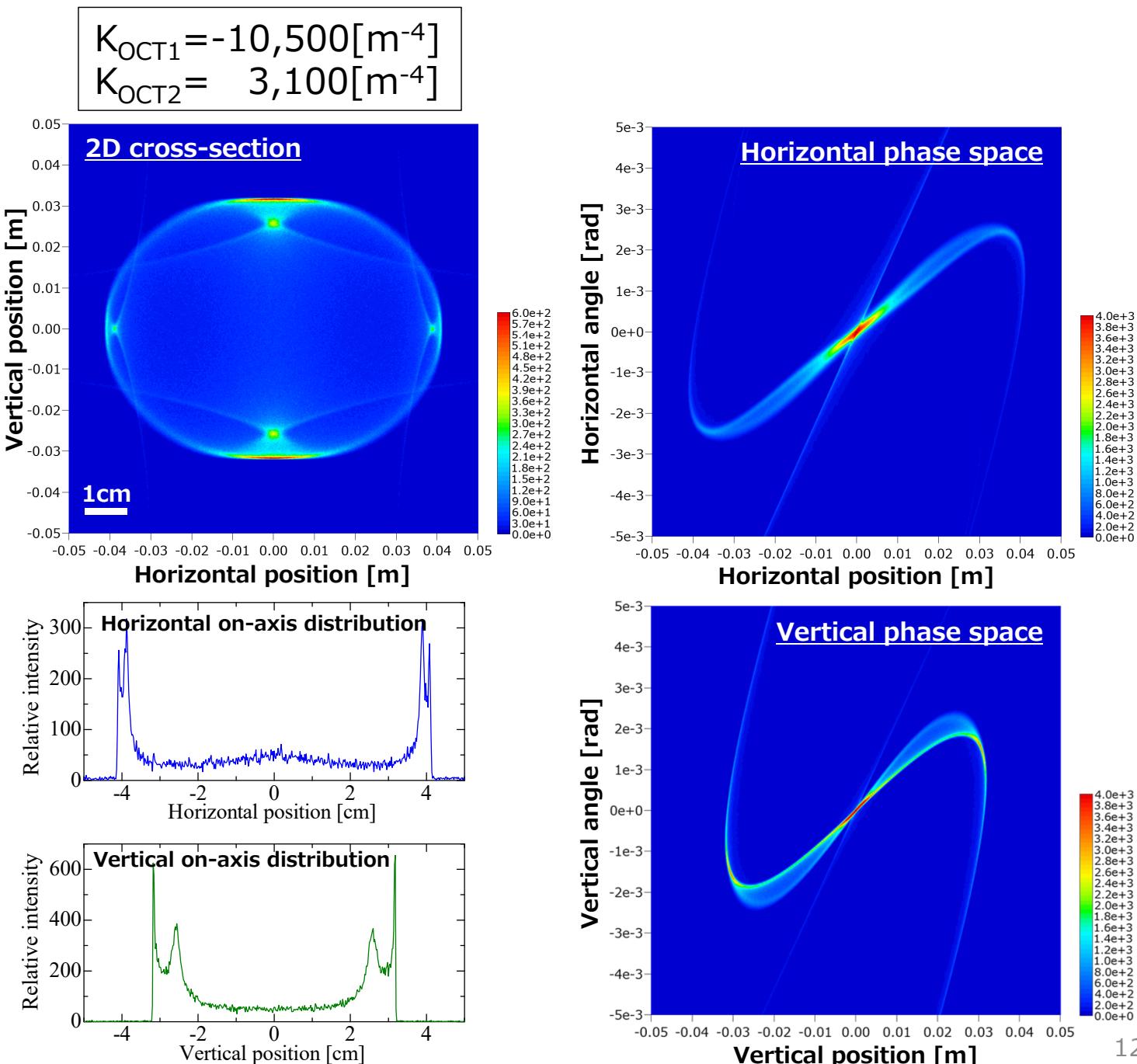
Hollow beams of various cross-sectional shapes can be generated easily using multipole magnets.

# Particle tracking simulation

## Numerical integration of EoM

- ✓ Beam optics same as that of the experiment
- ✓ Ion species: 10MeV proton
- ✓ Initial conditions:  
Gaussian trans. distribution
- ✓ RMS emittance:  
Hori.  $2\pi$  mm.mrad  
Vert.  $1\pi$  mm.mrad
- ✓  $d\mathbf{p}/\mathbf{p}=0$
- ✓ No space charge

**Contrast: 6~17**  
**Edge peak width~1mm**



# Simulation results

$$\begin{aligned}K_{\text{OCT1}} &= -10,500 \text{ m}^{-4} \\K_{\text{OCT2}} &= 3,100 \text{ m}^{-4}\end{aligned}$$

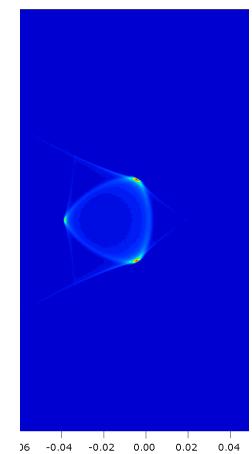
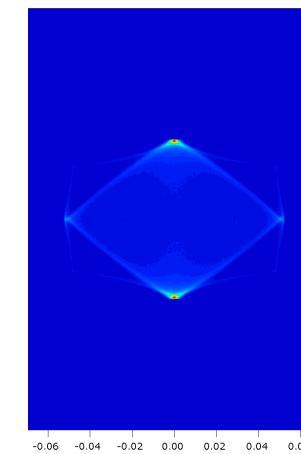
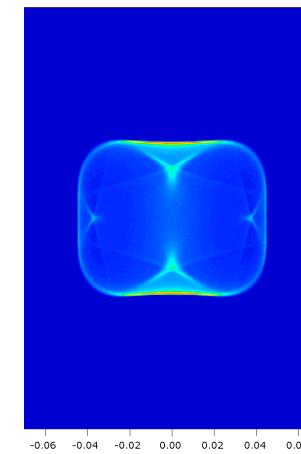
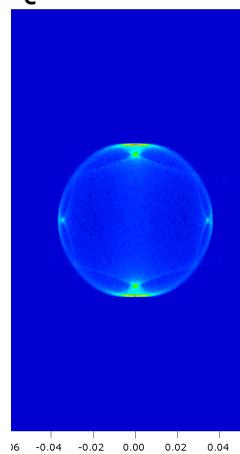
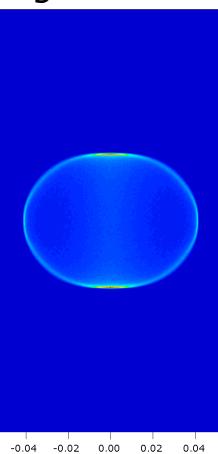
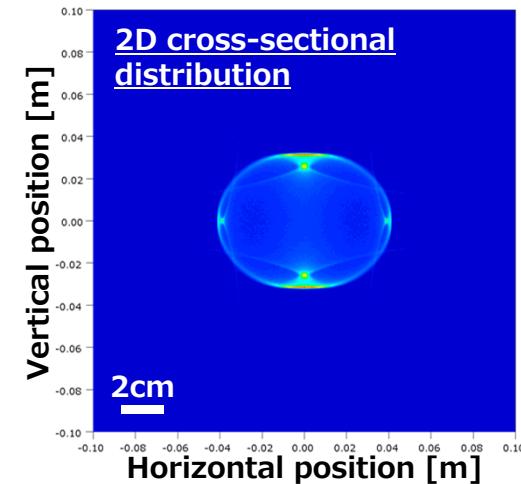
Tail collimation  
before octupole  
magnets

Circular profile  
by adjusting  
QMs

$$\begin{aligned}K_{\text{OCT1}} &= -6,700 \text{ m}^{-4} \\K_{\text{OCT2}} &= 2,400 \text{ m}^{-4}\end{aligned}$$

$$\begin{aligned}K_{\text{OCT1}} &= -11,300 \text{ m}^{-4} \\K_{\text{OCT2}} &= 2,300 \text{ m}^{-4}\end{aligned}$$

$$\begin{aligned}K_{\text{SXT1}} &= 150 \text{ m}^{-3} \\K_{\text{SXT2}} &= -37 \text{ m}^{-3}\end{aligned}$$



**Octupole focusing**  
→ Ellipse ~ Rectangle ~ Rhombus

**Sextupole  
focusing**  
→ Triangle

**Experimental results have been well reproduced.**

Diverse beam profile shaping is possible,  
depending on the order and strength of multipole magnets.

# Summary

- ✓ We have demonstrated the formation of a hollow beam through the nonlinear force of multipole magnets.

Y. Yuri *et.al.*, Prog. Theor. Exp. Phys. **2019** (2019) 053G01.

- ✓ Different characteristics have been revealed:

- Steep, narrow peak at the edge
- The cross-sectional shape depends on the order and strength of multipole magnets.

Rectangle ~ Ellipse ~ Rhombus for octupole focusing  
Triangle-like for sextupole focusing

- ✓ The proper use of the nonlinear force enables us to achieve unique beam shaping that cannot be realized by conventional linear focusing.

- Applicable to various beams of different parameters (species, energy, bunched or coasting, current, etc.) as the source of the nonlinear force is the magnetostatic field.

- ✓ As an application of a hollow beam, irradiation of the hollow beam is now investigated toward efficient production of low-energy muons at RCNP, Osaka Univ.



National Institutes for Quantum and  
Radiological Science and Technology



# Thank you for your attention!!

This work was supported in part by grant-in-aid programs in Japan.

- ✓ JSPS KAKENHI (JP18K11934)
- ✓ JST OPERA (Quantum Innovation for Safe and Smart Society)

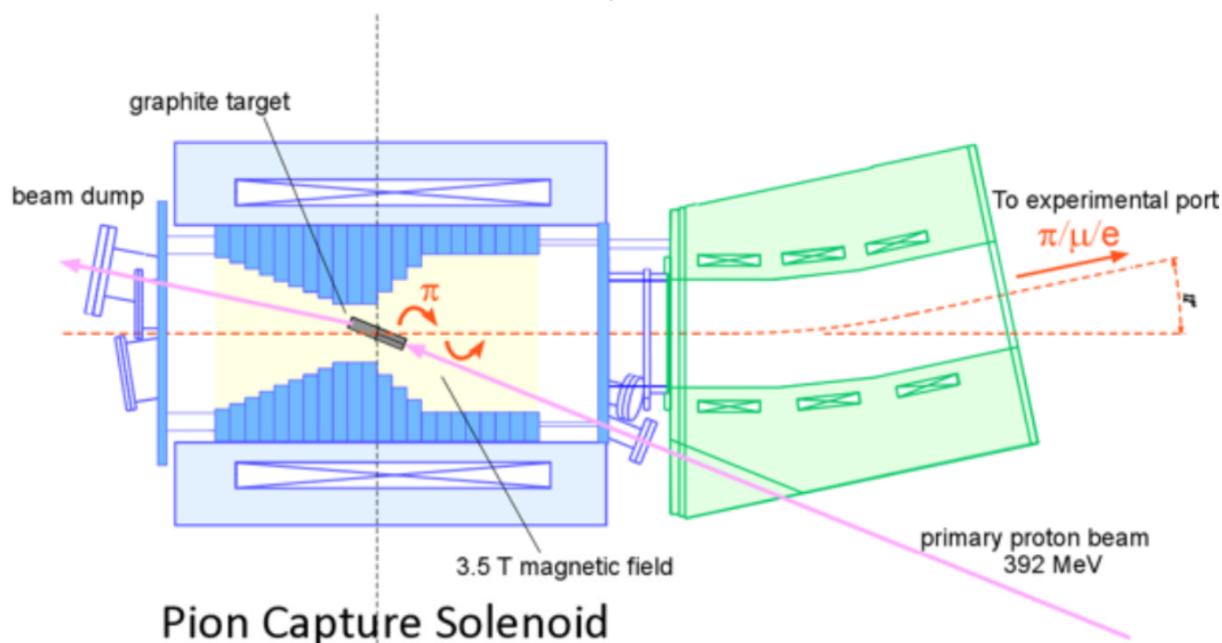
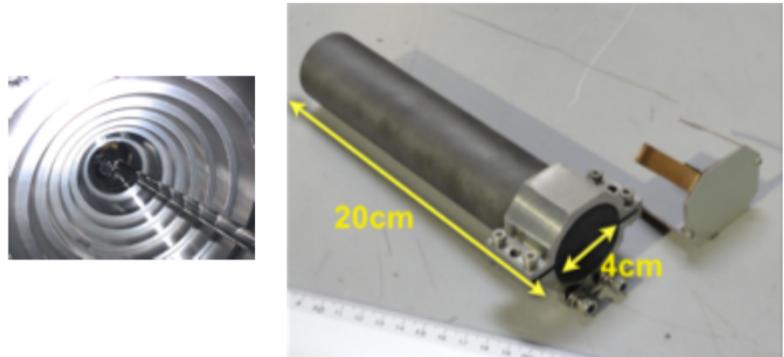


# Supplements

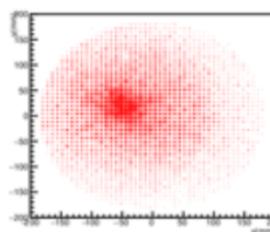
# A possible application of the hollow beam

## Pion capture solenoid & Pion transport solenoid

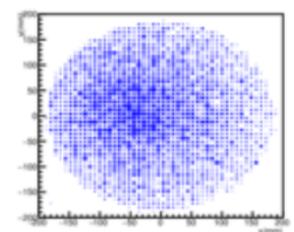
- Pion capture solenoid (3.5T)
  - pion production target inside (1.5 interaction length)
  - pion collection with large solid angles
- Pion transport solenoid (2.0T)
  - Curved solenoid to capture and transport pion/muon
  - Momentum selection with dipole collection field



Beam Profile by G4beamline simulation



Surface muon



Inflight-decay muon

Pion Capture Solenoid

exit of the 36° curved solenoid  
~  $3 \times 10^8$  positive muons  
~  $1 \times 10^8$  negative muons



~  $10^3$  pion production efficiency

# Previous studies of hollow beam formation

- Plasma lens (Z pinch discharge)
  - Short-pulsed heavy-ion beam ( $\sim 100\text{MeV/u}$ )
  - Beam diameter  $\sim 2\text{cm}$
  - Edge peak width  $\sim 5\text{mm}$
  - Contrast  $\sim 10$
  - Axisymmetric target irradiation for HED/HIF
- Hollowing due to space-charge effect
  - High-current heavy-ion beams from ECR ion source
  - Coexistence of ion beams with a different M/Q ratio
- Hollow electron gun
  - keV electron beams



FIG. 1. 10 mm radius ringlike light output from a scintillator situated perpendicular to the axis 0.3 m behind the plasma lens.

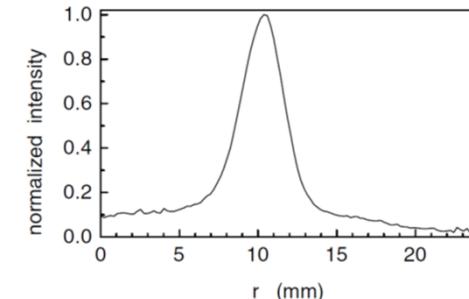


FIG. 6. Radial profile of the beam intensity distribution in the detection plane 0.3 m behind the plasma lens for the case of the optimum contrast of 10.

U. Neuner *et al.*, Phys. Rev. Lett. 85 (2000) p4518.

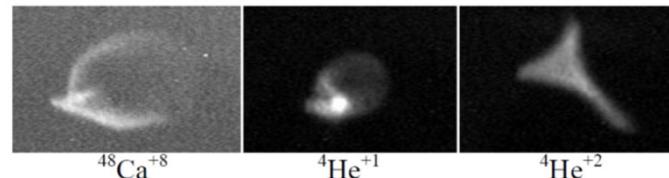


FIGURE 3. ECR is tuned to produce  $^{48}\text{Ca}$  of about 100 e $\mu\text{A}$  summed over all charge states. The support gas is helium of about 1200 e $\mu\text{A}$ . Here, the solenoid and analyzing magnet are set first to select  $^{48}\text{Ca}^{+8}$ , then  $^4\text{He}^{+1}$  and finally  $^4\text{He}^{+2}$ . Since the intensity of  $^{48}\text{Ca}$  in charge states higher than 8+ is low, the ring in the first picture is produced by short focusing of both helium charge states.

J. W. Stetson *et al.*, CYC(2004)p483.

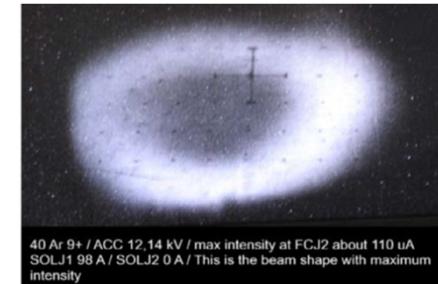


Figure 4: The beam profiles of Ar<sup>9+</sup> ion beam after the analysing magnet.

H. Koivisto *et al.*, ECR(2008)p18.

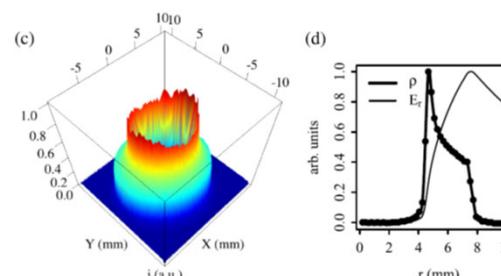


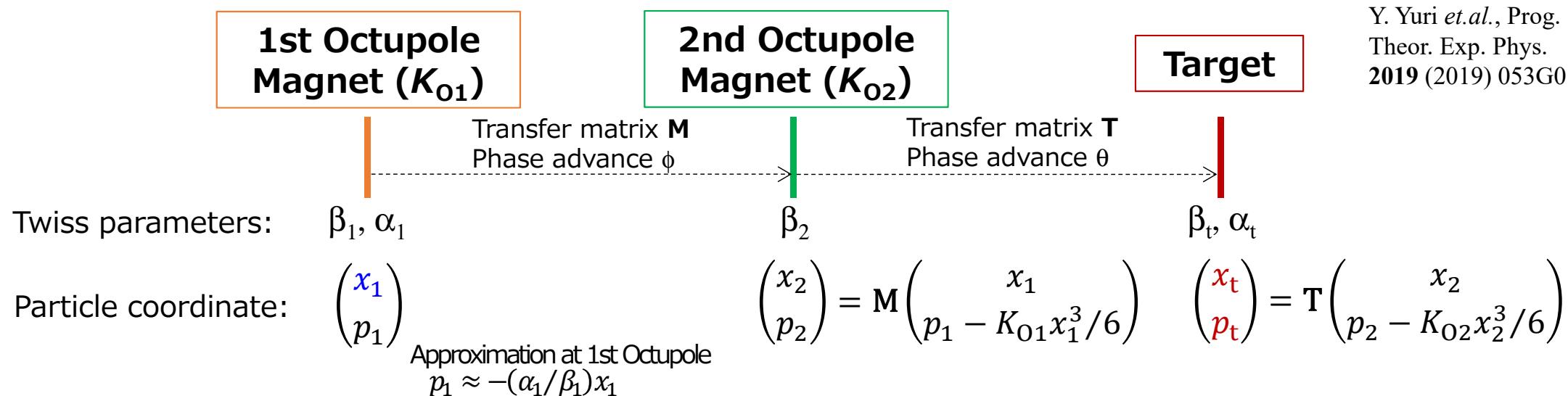
FIG. 2 (color online). Hollow electron gun: (a) top view; (b) side view; (c) measured current density profile; (d) measured charge density  $\rho$  and calculated radial electric field  $E_r$ .

G. Stancari *et al.*, Phys. Rev. Lett. 107 (2011) 084802.

The generation method and availability of hollow beams are limited.

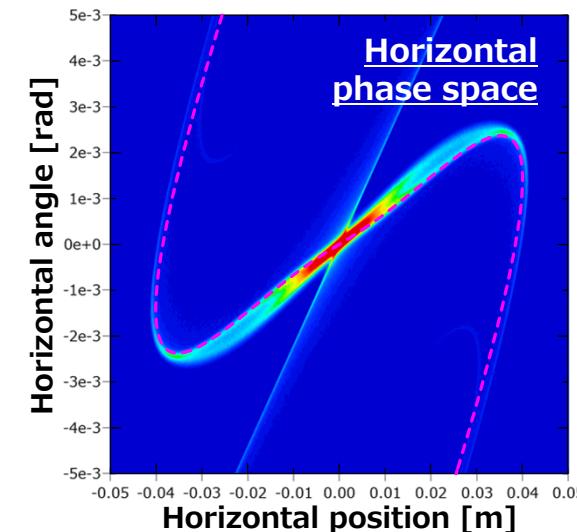
# Theoretical analysis (1D model)

Y. Yuri *et.al.*, Prog.  
Theor. Exp. Phys.  
2019 (2019) 053G01.



- ✓ The on-target phase-space shape can be approximately characterized by the Twiss parameters, the phase advance and the octupole strength:

$$\left\{ \begin{array}{l} x_t = \sqrt{\frac{\beta_t}{\beta_1}} \cos(\phi + \theta) x_1 - \frac{K_{O1}}{6} \sqrt{\beta_1 \beta_t} \sin(\phi + \theta) x_1^3 - \frac{K_{O2}}{6} \sqrt{\beta_2 \beta_t} \sin \theta \left( \sqrt{\frac{\beta_2}{\beta_1}} \cos \phi x_1 - \frac{K_{O1}}{6} \sqrt{\beta_1 \beta_2} \sin \phi x_1^3 \right)^3 \\ p_t = -\frac{1}{\sqrt{\beta_1 \beta_t}} \{ \sin(\phi + \theta) + \alpha_t \cos(\phi + \theta) \} x_1 - \frac{K_{O1}}{6} \sqrt{\frac{\beta_1}{\beta_t}} \{ \cos(\phi + \theta) - \alpha_t \sin(\phi + \theta) \} x_1^3 \\ \quad - \frac{K_{O2}}{6} \sqrt{\frac{\beta_2}{\beta_t}} (\cos \theta - \alpha_t \sin \theta) \left( \sqrt{\frac{\beta_2}{\beta_1}} \cos \phi x_1 - \frac{K_{O1}}{6} \sqrt{\beta_1 \beta_2} \sin \phi x_1^3 \right)^3 \end{array} \right.$$



The beam motion under nonlinear focusing has been theoretically predicted.