

## ROUND BEAM STUDIES AT NSLS-II\*

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### Abstract

Instead of typical flat beam, some synchrotron light users prefer round beam, i.e., with equal horizontal and vertical emittance, for various reasons (e.g., simplified optics, smaller fraction of photons getting discarded, better phase space match between photon and e-beam). Several future upgrade storage rings such as APS-U, ALS-U, and SLS-2 currently plan to operate in round beam mode. We report our beam study results on round beam operating at NSLS-II by driving linear difference coupling resonance.

### INTRODUCTION

Typical synchrotron light sources have been operating in horizontally elongated flat beam for decades. As newer light sources aim to further increase brightness, i.e., reduce emittance down to diffraction limit, beam lifetime becomes shorter and intrabeam scattering (IBS) effect becomes stronger. At some point, there will be no benefit to retain the traditional flat beam. Round beam is a natural choice for such advanced storage rings such as APS-U [1], ALS-U [2], and SLS-2 [3] to overcome these challenges. As another benefit of round beam, some beamline experiments like diffractive imaging utilize round pinholes that would discard many photons if not round [4]. Round beam is also advantageous in that it allows better photon-electron phase space matching, which results in brighter photon beam [5].

Round beam has been recently tested by operating at linear coupling resonance at APS [6]. We employed the same method to demonstrate round beam at NSLS-II, mostly focusing on lattice parameters that prevent beam from reaching full round state.

### EXPERIMENTAL RESULTS

All the tune scan experimental data presented in this paper were performed for the nominal NSLS-II bare lattice, i.e., with all insertion devices (IDs) opened, except for adjustment of tunes and chromaticities. The nominal parameters of the lattice are shown in Table 1.

For the purpose of scanning tunes around linear coupling resonance, we utilized special horizontal bumps generated by fast correctors. Unlike quadrupoles, these fast correctors are free from hysteresis effect, which makes the method very reproducible. However, because the fast correctors were not originally intended to be used for this purpose, and the maximum kick strength is only 15 urad, the range of tune change is limited to  $\sim \pm 5 \times 10^{-3}$ . The unperturbed (i.e., uncoupled) fractional tune

distance from resonance  $\Delta \equiv \nu_y - \nu_x - q$  with an integer  $q$  and unperturbed tunes  $\nu_x$  and  $\nu_y$  in all the experimental plots is estimated from the fast corrector setpoints and defined to be zero where vertical beam size becomes maximum.

Table 1: Nominal Parameters of NSLS-II Bare Lattice

Parameter	Value	Unit
Energy	3	GeV
Revolution period	2.64	$\mu\text{s}$
Ring tune $\nu_x, \nu_y$	33.22, 16.26	
Chromaticity $\xi_x, \xi_y$	+2, +2	
Transv. damping time $\tau_{x,y}$	55	ms
Horiz. natural emittance $\epsilon_0$	2.1	nm-rad
RMS energy spread $\delta$	$5 \times 10^{-4}$	

The common initial setup before starting each tune scan involves linear lattice correction, including minimization of coupling and vertical dispersion, using the software tool DTBLOC [7] developed at NSLS-II based on resonance driving terms derived from turn-by-turn (TbT) data.

To control (i.e., add) more coupling, the current of one of the skew quadrupoles in a non-dispersive section was adjusted from the state of minimized coupling. This change in normalized integrated strength of the skew quadrupole is denoted by  $\Delta a_2 L$ .

Note that  $\Delta a_2 L = 0$  does not mean no coupling, but rather the state with coupling minimized as much as possible by the lattice correction tool (typically the minimum tune distance between  $1 \times 10^{-4}$  and  $2 \times 10^{-4}$  can be achieved). In addition, machine drift between the completion of lattice correction and the start of tune scan sometimes resulted in loss of a well-corrected coupling state.

When the minimized coupling state has negligible coupling strength compared to the coupling added by the control skew quad, we can estimate the linear coupling driving term for difference resonance  $C$  [8]:

$$C = \frac{1}{2\pi} \oint ds \sqrt{\beta_x(s)\beta_y(s)} \cdot \Delta a_2 L(s) e^{i[\phi_x(s) - \phi_y(s) - \frac{\Delta \cdot 2\pi s}{L}]}$$

where  $L$  is the circumference, and  $\beta_{x,y}$  and  $\phi_{x,y}$  are the unperturbed beta functions and phases, respectively. Given the beta function values at the location of the selected skew quadrupole,  $|C| = 2.63 \times \Delta a_2 L [\text{m}^{-1}]$ .

The horizontal and vertical beam sizes measured at the pinhole camera for a three-pole wiggler (3PW) source [9], while varying the tune distance, for the nominal +2/+2 chromaticity lattice, are shown in Fig. 1(a). The corresponding ‘‘apparent’’ vertical emittance is shown in Fig. 1(b), defined as  $\mathbb{E}_y = \{\sigma_y^2 - (\eta_y \delta)^2\} / \beta_y$  [10], where  $\eta_y$ ,  $\delta$ , and  $\beta_y$  are the vertical dispersion, RMS energy spread, and the unperturbed vertical beta function

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at the 3PW, respectively. After lattice correction, these values are close to the design values:  $\eta_y = 0$  and  $\beta_y = 3.75$  m. Note that with a slight increase in coupling, the peak vertical emittance approaches  $1 \text{ nm} \sim \epsilon_0/2$ , i.e., round beam, but is much smaller with minimized coupling. TbT data also show incomplete x-y energy exchange for minimally coupled cases.

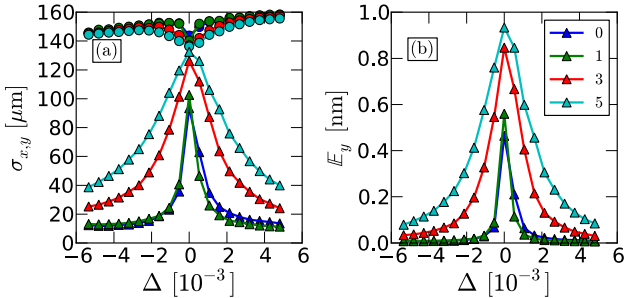


Figure 1: (a) Beam size and (b) apparent vertical emittance at x-ray pinhole camera (from a 3PW source) vs. tune distance from coupling resonance for different coupling strengths  $\Delta a_2 L = 0, 1, 3, 5 \times 10^{-4} \text{ m}^{-1}$ . Circles for horizontal and triangles for vertical beam quantities.  $\sim 2$  mA in 100 buckets.

One potential reason for this inability to achieve round beam is that simply the peak is missed due to finite tune distance steps. However, scanning around the resonance with very fine tune steps ruled out this possibility. Another possibility is due to tune jitter from magnet power supply noise. The RMS horizontal and vertical tune jitter was measured to be  $1.15 \times 10^{-4}$  and  $0.33 \times 10^{-4}$ , respectively.

However, even without tune jitter, this observation can be explained by a heuristic model of emittance exchange through linear coupling [11, 4] (corroborated by a multi-particle tracking study [12]):

$$\frac{d\epsilon_x}{dt} = -\alpha_c(\epsilon_x - \epsilon_y) - \alpha_x(\epsilon_x - \epsilon_0), \quad (1)$$

$$\frac{d\epsilon_y}{dt} = -\alpha_c(\epsilon_y - \epsilon_x) - \alpha_y\epsilon_y, \quad (2)$$

where  $\epsilon_0$  is the natural emittance, and  $\alpha_x$  and  $\alpha_y$  are the transverse damping rates ( $=1/55$  ms, always fixed in our experiments), while  $\alpha_c$  is an effective coupling exchange rate that increases with higher coupling. Setting the right-hand sides of Eqs. (1) and (2) to zero and solving for  $\epsilon_y$  and  $\epsilon_x$  yields the equilibrium emittances in the presence of coupling and damping:

$$\epsilon_y = \frac{\alpha_x \alpha_c}{\alpha_c(\alpha_x + \alpha_y) + \alpha_x \alpha_y} \epsilon_0,$$

$$\epsilon_x = \frac{\alpha_x(\alpha_c + \alpha_y)}{\alpha_c(\alpha_x + \alpha_y) + \alpha_x \alpha_y} \epsilon_0.$$

We can see that emittance ratio becomes

$$\frac{\epsilon_y}{\epsilon_x} = \frac{\alpha_c}{\alpha_c + \alpha_y}.$$

It is obvious then that round beam can be achieved only when  $\alpha_c \gg \alpha_y$ . Being heuristic, no formula exists for this effective rate  $\alpha_c$  to our best knowledge. However, it is known from a simple theory for weak betatron coupling

[13] that a particle exchanges oscillation energy between  $x$  and  $y$  planes at the period  $T$

$$T = \frac{1}{f_{\text{rev}} \sqrt{\Delta^2 + |C|^2}}$$

with  $f_{\text{rev}}$  being the revolution frequency, and achieves full energy modulation when  $\Delta = 0$ . Thus, we can assume  $\alpha_c$  to be on the same time scale as  $\alpha_{c0} \equiv 1/T_{\Delta=0} = f_{\text{rev}}|C|$ . Then we can represent  $\alpha_c = m\alpha_{c0}$  with  $m$  being an empirical factor. Figure 2 shows  $\epsilon_x$  and  $\epsilon_y$  vs.  $|C|$  for  $m = 1, 3, \text{ and } 10$ . At  $\Delta a_2 L = 1 \times 10^{-4} \text{ m}^{-1}$  (equivalent to  $|C| = 2.63 \times 10^{-4}$ ), the case of  $m = 10$  roughly agrees with the observed  $\epsilon_y$  of  $\sim 500$  pm. As coupling increases,  $\epsilon_y$  rapidly converges to  $\epsilon_0/2$ .

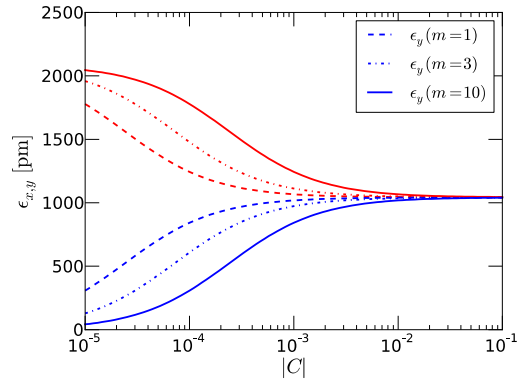


Figure 2: Emittance vs. coupling strength predicted from a heuristic model of transverse emittance sharing.

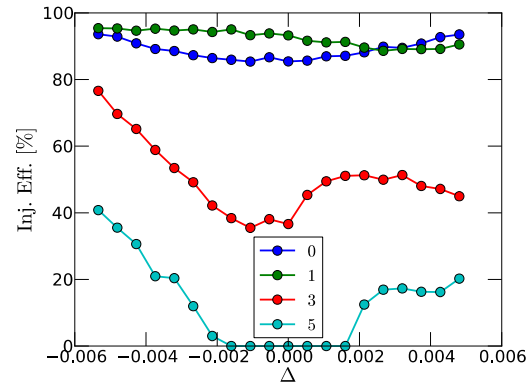


Figure 3: Injection efficiency vs. tune distance from coupling resonance for different coupling strengths  $\Delta a_2 L = 0, 1, 3, 5 \times 10^{-4} \text{ m}^{-1}$ .

From Fig. 1(b), to achieve  $>90\%$  of  $\epsilon_y$  for fully round beam for the nominal NSLS-II bare lattice, coupling strength of  $|C| = 1.3 \times 10^{-3}$  ( $\Delta a_2 L = 5 \times 10^{-4} \text{ m}^{-1}$ ) is required. However, injection efficiency drops rapidly with increased coupling, and to zero at the required coupling level, as shown in Fig. 3. For the NSLS-II damping wiggler lattice used for beamline operation, given its shorter transverse damping time of 24 ms, the required coupling will likely be higher, resulting potentially in worse injection. To avoid this issue, we may need to use the fast correctors to move away from coupling resonance temporarily, as done in the tune scan measurements presented here, during top off injection, although compatibility with

the fast orbit feedback, transient issues, and insufficient tune adjustment range will need to be addressed. Another solution would be to try a lattice with large amplitude-dependent tune shift, as suggested in [12].

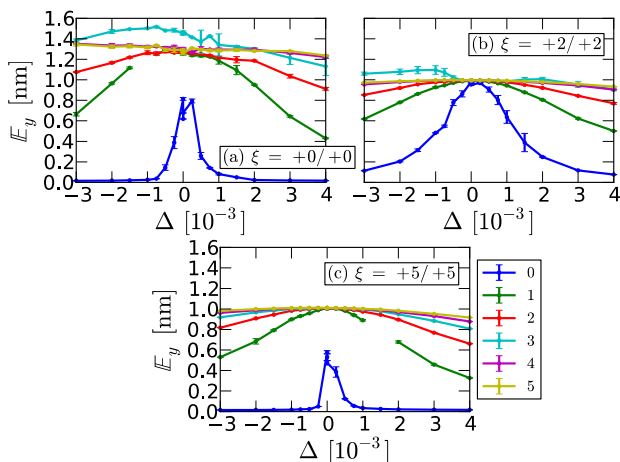


Figure 4: Measured vertical emittance vs.  $\Delta$  for different coupling strengths  $\Delta a_2 L = 0, 1, 2, 3, 4, 5 \times 10^{-3} \text{ m}^{-1}$  with (a)  $\xi = 0/0$ , (b)  $+2/+2$ , and (c)  $+5/+5$ .

We also investigated the effect of tune spread on round beam by adjusting linear chromaticities  $\xi_x/\xi_y$  (measured values shown in parentheses) to  $0/0$  ( $+0.11/+0.60$ ),  $+2/+2$  ( $+1.90/+2.25$ ), and  $+5/+5$  ( $+5.12/+5.11$ ) with  $\sim 4$  mA in 100 bunches. The experimental results are shown in Figs. 4-6. The RMS tune spread due to finite chromaticity is given by  $\sigma_v = \xi \delta$  where  $\delta = 5 \times 10^{-4}$ . With higher  $\xi$ , coupling resonance effect may be diluted due to more electrons oscillating at frequencies farther from resonance.

Unfortunately, for the  $+2/+2$  tune scan, a well-corrected coupling state was apparently lost before the scan was initiated, as can be seen from large vertical emittance with  $\Delta a_2 L = 0$  at  $\Delta = 0$  in Figs. 4(b) and 6(a). This makes it hard to draw a definitive conclusion that smaller vertical emittance with  $+5/+5$  compared to  $+2/+2$  at  $\Delta \neq 0$  is caused by larger chromatic tune spread (see Figs. 5(a)-(d)). Some or most of the emittance difference may be attributed to the initial residual coupling error.

Another complication in the obtained data is that the case of  $\xi = 0/0$  may be affected by collective effects, as the maximum vertical emittance in all the cases far exceeds the predicted maximum value of 1 nm. This conjecture is further supported by the fact that an attempt to bring  $\xi_y$  closer to 0 from  $+0.6$  during a scan setup resulted in sudden increase in beam size at the nominal fractional tunes (0.22, 0.26).

Nonetheless, one unexpected observation was that, for  $\xi = +5/+5$ , the coupling stopband width  $|C| = 2.6 \times 10^{-3}$  for  $\Delta a_2 L = 1 \times 10^{-3} \text{ m}^{-1}$  corresponds to mere  $\pm 0.5\sigma_v (= \pm 1.25 \times 10^{-3})$ . This means only  $\sim 38\%$  of the electrons (assuming Gaussian) at a given moment are within the stopband, and yet the measured vertical emittance at  $\Delta = 0$  shows that almost fully round beam is achieved. This suggests that round beam operation is

likely to be not so sensitive to the choice of linear chromaticity values.

Another surprise was that there appears to be unknown resonance or instability that increases both horizontal and vertical beam sizes with  $\Delta a_2 L = 3 \times 10^{-3} \text{ m}^{-1}$ , as seen in Fig. 6. This phenomenon is not observed for  $\xi = +5/+5$ , which implies the mechanism may be also related to collective effects.

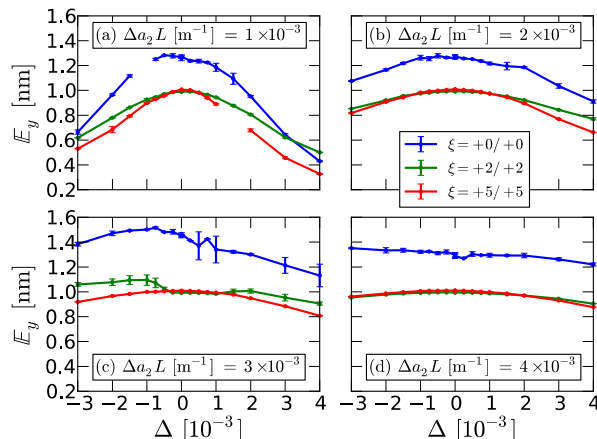


Figure 5: Measured vertical emittance vs.  $\Delta$  for  $\xi = 0/0, +2/+2, +5/+5$  with  $\Delta a_2 L =$  (a) 1, (b) 2, (c) 3, and (d)  $4 \times 10^{-3} \text{ m}^{-1}$ .

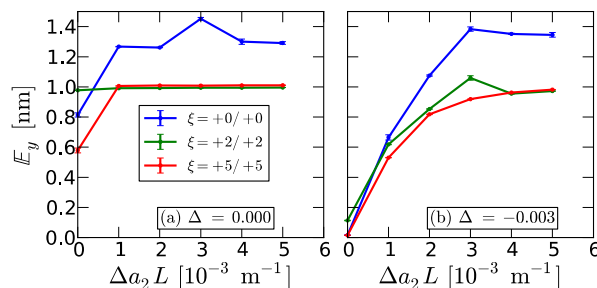


Figure 6: Measured vertical emittance vs.  $\Delta a_2 L$  for  $\xi = 0/0, +2/+2, +5/+5$  at (a)  $\Delta = 0$  and (b)  $\Delta = -0.003$ .

## CONCLUSION

We have demonstrated round beam at NSLS-II using the nominal bare lattice sitting on linear coupling resonance to obtain insights and potential pitfalls awaiting for future light sources planning to operate in round beam mode. To achieve round beam, coupling had to be increased to compete against damping effect to the point where injection became impossible if the tunes were set directly on resonance. To enable injection with this round beam scheme, other solutions such as temporary tune adjustment and a lattice with large tune shift with amplitude are likely needed. We also experimentally found that coupling resonance is not too sensitive to increased tune spread from higher linear chromaticities.

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