# Pulse Broadening of Ultraviolet Seed Laser Pulse Width Measurement using Ultrathin $\beta$-BBO Crystal* 

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## Abstract

- XFEL seed laser pulse duration is typically 100 200 fs with wavelengths in the 260 nm range.
- The Ultraviolet (UV) pulse width measurement was carried out with intensity cross-correlation.
- The output cross correlation pulse broadened due to group velocity mismatch between the 266.7 nm and 800 nm components. The broadening effect depends on the BBO crystal thickness.
- $0.015 \mathrm{~mm}, 0.055 \mathrm{~mm}$ and 0.1 mm thick BBO crystal samples are explored.
- To the best of our knowledge, this is the first time that $\beta$-BBO crystal with thickness of only 0.015 mm has been used to measure the UV seed laser pulse width.
- Experiment results show the measured pulse width broadens with increased BBO thickness in agreement with a theoretical model.


## XFEL Seed Laser System



Figure 1: Schematic of SXFEL seed laser system.


Figure 2: Schematic of the collinear cross-correlation diagnostic system. A prism was used to spatially separate the frequency components at the output stage.


Figure 3: Structure of third harmonic generation (THG) device. BS-beam splitter; DS-delay stage.


Figure 4: Refractive index $n(\theta)$ of the extraordinary wave $\theta$ is the angle between the optic axis and the direction of propagation. Vector $k$ shows beam propagation direction

## Theoretic Framework For the Cross Correlation Measurement

The frequency and phase matching conditions are expressed in Eqs. (1) and (2) which must be satisfied simultaneously[4].

$$
\begin{gather*}
\omega_{I R}+\omega_{D F G}=\omega_{U V}  \tag{1}\\
n_{I R} \omega_{I R}+n_{D F G} \omega_{D F G}=n_{U V} \omega_{U V} \tag{2}
\end{gather*}
$$

For an o-wave $n(\omega)=n_{o}(\omega)$; for an e wave $n(\omega)=$ $n_{e}(\theta, \omega)$ also depends on the angle $\theta$ between the direction of the wave and the optic axis of the crystal, which is shown in Fig.4. and expressed in Eq.(3) [4].

$$
\begin{equation*}
\frac{1}{n_{e}^{2}(\theta, \omega)}=\frac{\cos ^{2} \theta}{n_{o}^{2}(\omega)}+\frac{\sin ^{2} \theta}{n_{e}^{2}(\omega)} \tag{3}
\end{equation*}
$$

The cross-correlation overlap integral for intensity output can be expressed as Eq. (4).

$$
\begin{equation*}
I(\tau)_{c c}=\alpha \int_{-\infty}^{\infty} I_{u v}(t) I_{I R}(t-\tau) d t \tag{4}
\end{equation*}
$$

Assume pulses with Gaussian distribution along with negligible frequency chirp and negligible group velocity mismatch, the full width at half maximum (FWHM) $\tau_{c c}$ of the output envelope is

$$
\begin{equation*}
\tau_{c c}=\sqrt{\tau_{I R}^{2}+\tau_{U V}^{2}} \tag{5}
\end{equation*}
$$

UV input pulse width can be derived by deconvolution according to Eq. (6).
$I_{c c}(\tau) \approx \int_{-\infty}^{\infty}\left\{\exp \left[-2 \ln 2\left(\frac{t}{\tau_{U V}}\right)^{2}\right]\right\}^{2} \times\left\{\exp \left[-2 \ln 2\left(\frac{(t-\tau}{\tau_{I R}}\right)^{2}\right] \otimes \operatorname{sqr}\left[\frac{t}{\Delta\left(\overline{\left.v_{g}\right)^{\prime}}\right) c_{c}^{l c}}+\frac{1}{2}\right]\right\}^{2} d t(6)$
$\operatorname{sqr}(x)=\left\{\begin{array}{ll}1, & |x| \leq 1 / 2 \\ 0, & \text { otherwise }\end{array}, \quad \tau_{U V}\right.$ - UV beam FWHM, $\tau_{I R}$-IR beam FWHM. $\Delta\left(v_{g}^{-1}\right)_{c c}$-GVM between the UV and IR beams, $l_{c}$-BBO thickness and $\otimes$ denotes convolution.

The expression for group velocity and group velocity mismatch are given by in Eq. (7) and (8), respectively.

$$
\begin{gather*}
\mathrm{v}_{\mathrm{g}}=\frac{\mathrm{c}}{\mathrm{n}}\left(1+\frac{\lambda}{\mathrm{n}} \frac{\mathrm{dn}}{\mathrm{~d} \lambda}\right)  \tag{7}\\
\Delta\left(v_{g}^{-1}\right)_{c c}=\mathrm{GVM}=\frac{1}{V_{g}^{I R_{-} o}}-\frac{1}{V_{g}^{U V_{-} e}} \tag{8}
\end{gather*}
$$

The refraction indices for a 266.7 nm e-ray propagating through the BBO crystal with a cutting angle $\theta=44.4^{\circ}$ were calculated using Eqs. (3), (9) and (10)
$\mathrm{n}_{\mathrm{o}}(\lambda)=\sqrt{2.7405+\frac{0.0184}{\lambda^{2}-0.0179}-0.0155 \lambda^{2}}$
$n_{e}(\lambda)=\sqrt{2.3730+\frac{0.0128}{\lambda^{2}-0.0156}-0.0044 \lambda^{2}}$
$\frac{\mathrm{dn}_{\mathrm{o}}(\lambda)}{\mathrm{d} \lambda}=\frac{1}{2} * \frac{-\frac{0.0184}{\left(\lambda^{2}-0.0179\right)^{2}} * 2 \lambda-0.0155 * 2 \lambda}{\sqrt{2.7405+\frac{0.0184}{\lambda^{2}-0.0179}-0.0155 \lambda^{2}}}$
$\frac{\mathrm{dn}_{\mathrm{e}}(\lambda)}{\mathrm{d} \lambda}=\frac{1}{2} * \frac{-\frac{0.0128}{\left.\lambda^{2}-0.0156\right)^{2}} * 2 \lambda-0.0044 * 2 \lambda}{\sqrt{2.3730+\frac{0.0128}{\lambda^{2}-0.0156}-0.0044 \lambda^{2}}}$

## Results and discussion





Figure 5: Cross correlation data with error bars (blue line) and numerical fits (red line) using $0.015 \mathrm{~mm}, 0.055 \mathrm{~mm}$, and $0.1 \mathrm{~mm} \beta$-BBO crystal for DFG. All curves are fitted by Eq. (6) with $\tau_{I R}=57 \mathrm{fs}, \tau_{U V}=248 \mathrm{fs}$, and $\Delta\left(v_{g}^{-1}\right)_{c r}=671.5 \mathrm{fs} / \mathrm{mm}$.


Figure 6: FWHM of cross correlation signal from data in Fig 5. For these data Eq. (6) with $\tau_{I R}=57 \mathrm{fs}, \tau_{U V}=248 \mathrm{fs}$, and $\Delta\left(v_{g}^{-1}\right)_{c c}=671.5 \mathrm{fs} / \mathrm{mm}$.

## Summary

- pulse broadening of the 400 nm DFG cross-correlation signal was investigated in three different $\beta$-BBO crystal thicknesses. 0.015 mm BBO crystal thickness measurements for the first time to our knowledge.
- The results show that the 400 nm DFG pulse width increases as the BBO thickness increases as predicted.
- 0.055 mm crystal the measured $\sim 272$ fs FWHM pulse length is in very good agreement with theory and the two other measurements are within a about 4 percent.
- Results agree well with the theoretical model
- Further study are underway to explore influence from dispersion, spatial chirp and other nonlinear mechanisms.


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