

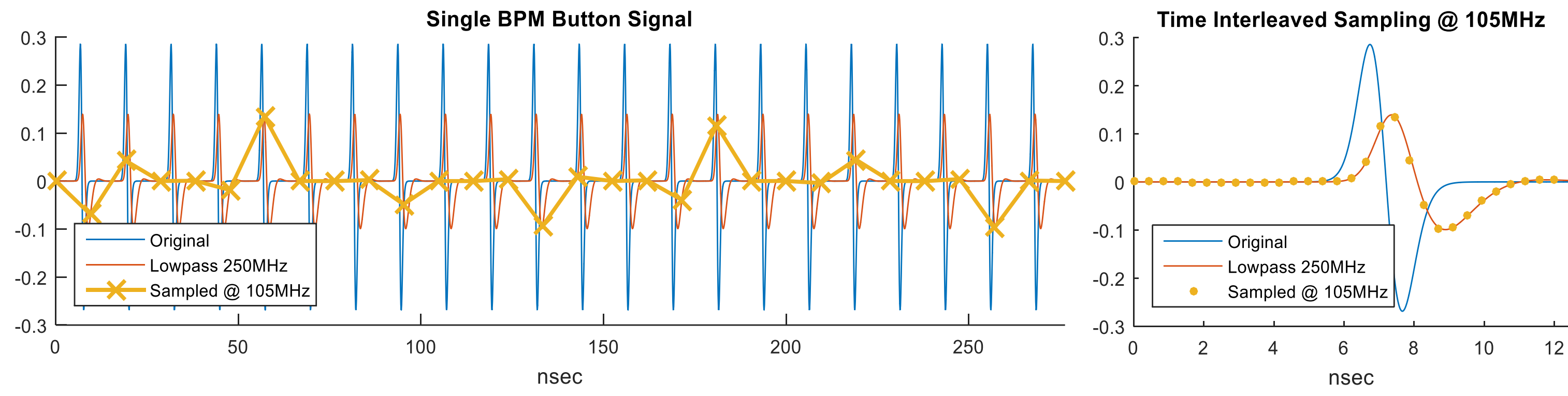
# Bunch Length Measurements Using Beam Position Monitors (BPMs)

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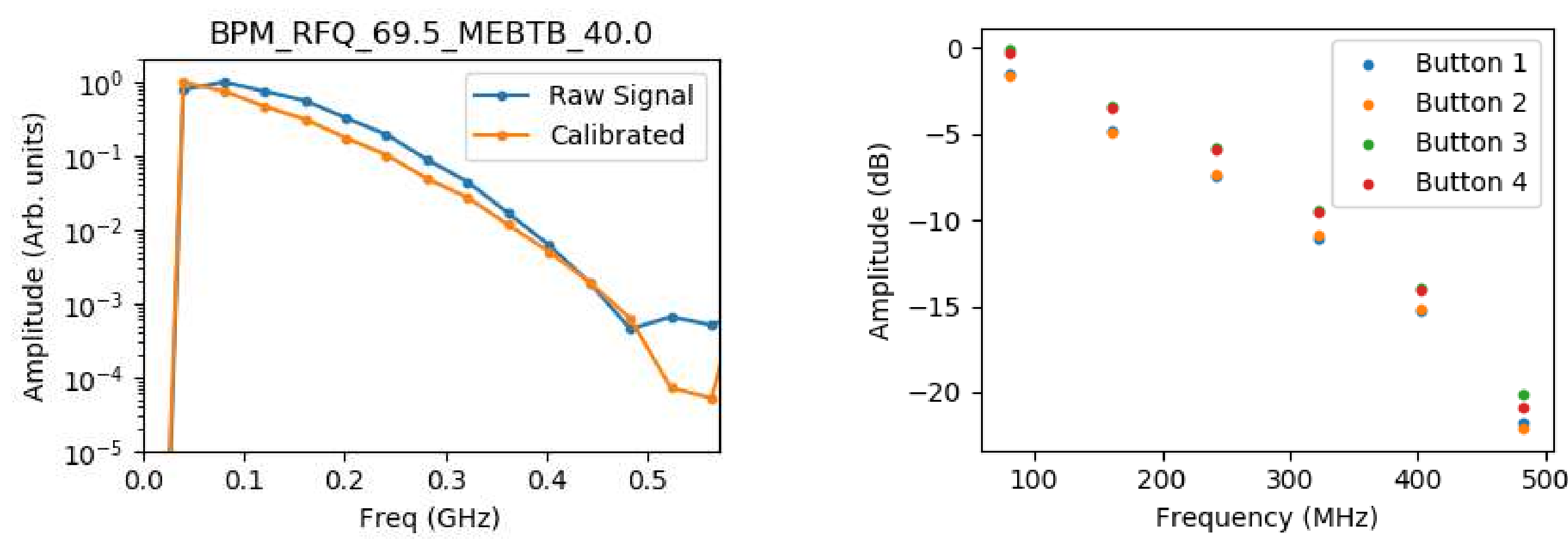
S. Cogan, S. Lidia, Facility for Rare Isotope Beams, East Lansing, MI, USA

## Signals Measured by BPMs

- Broad band signals measured using time interleaved sampling
  - 40.25 MHz signal is sampled at 119 MHz
  - Results in an effective sampling rate of 2.737 GHz



- The signals need to be calibrated for effects from the digitizer, 500 MHz low pass filtering, and dispersion from the cables connecting the pick ups to the digitizer
  - Harmonics of 80.5 MHz were input into the cables for each button on a BPM and measured with the digitizer
- The signals must also be corrected for the impedance of the buttons



- The calibrated signals represent the field distribution measured by the buttons, not the bunch distribution
  - For a transversely and longitudinally longitudinal bunch the field on the pipe wall is

$$\sigma_{wall}(\omega, z_m, \phi_m) = D_\omega \cos\left[\frac{\omega}{\beta c}(z_m - z_0)\right] \int dA_{beam} \sum_{n=0}^{\infty} \frac{I_n(g r/R_p)}{\pi N I_n(g)} \cos[n(\phi_m - \phi)] e^{-\frac{(x-x_0)^2}{2\sigma_x^2} - \frac{(y-y_0)^2}{2\sigma_y^2}} \quad g = \frac{\omega R_p}{\gamma \beta c}$$

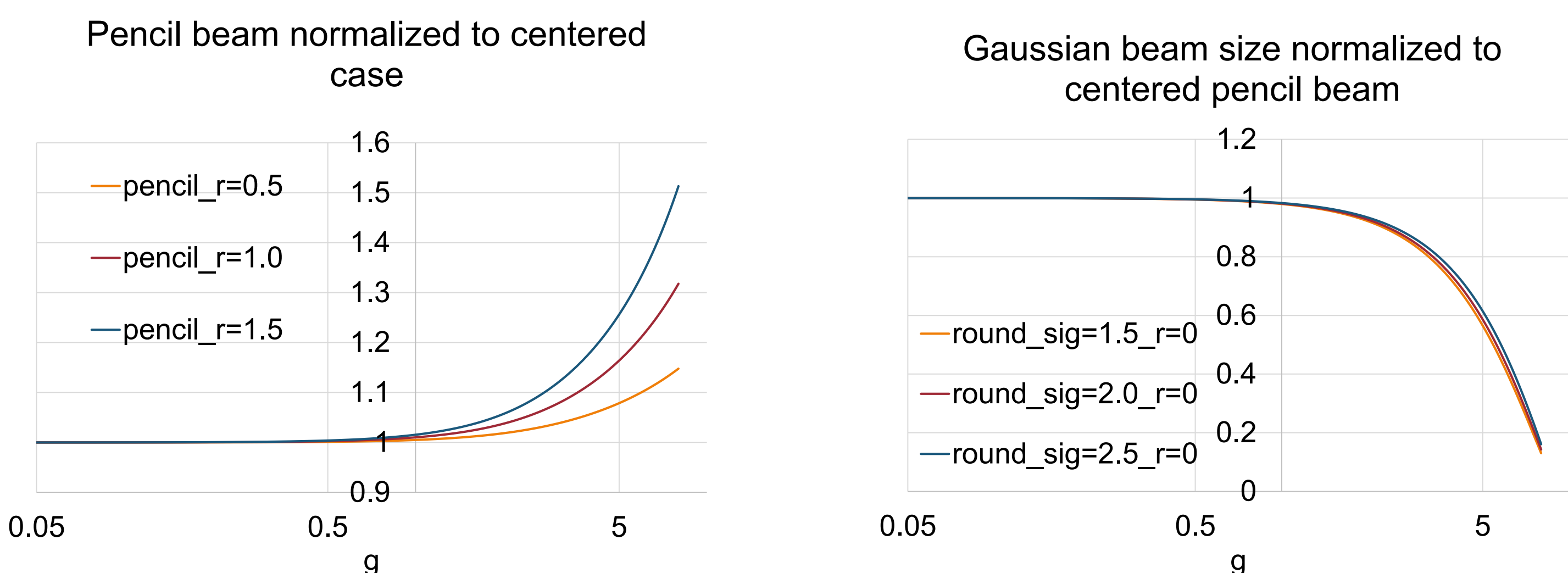
J. Cuperous, NIM, 1977

- The round button geometry is accounted for with a transit time factor
  - This factor is calculated for each azimuthal mode separately

$$T(\omega) = \frac{2}{n} \int_{-R_b}^{R_b} dz_m \cos\left[\frac{\omega}{\beta c}(z_m - z_0)\right] \sin\left[\frac{n}{R_p} \sqrt{R_b^2 - z_m^2}\right]$$

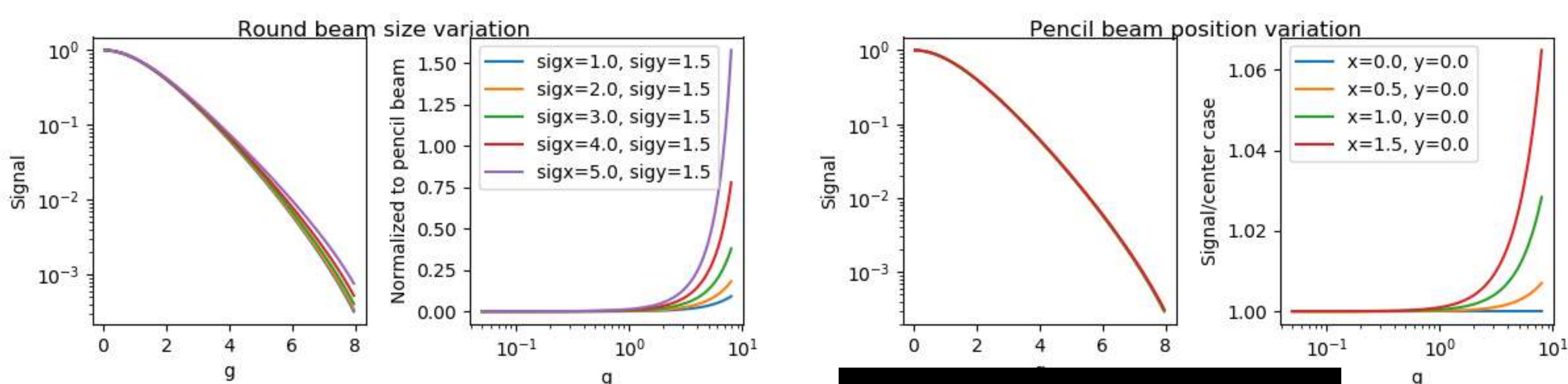
## Scaling with Transverse Properties

- Scalings with g
  - Need to account for transverse properties up to g~1
  - In FRIB MEBT,  $\beta=0.032$  corresponding to g~1-6 for measurable bandwidth



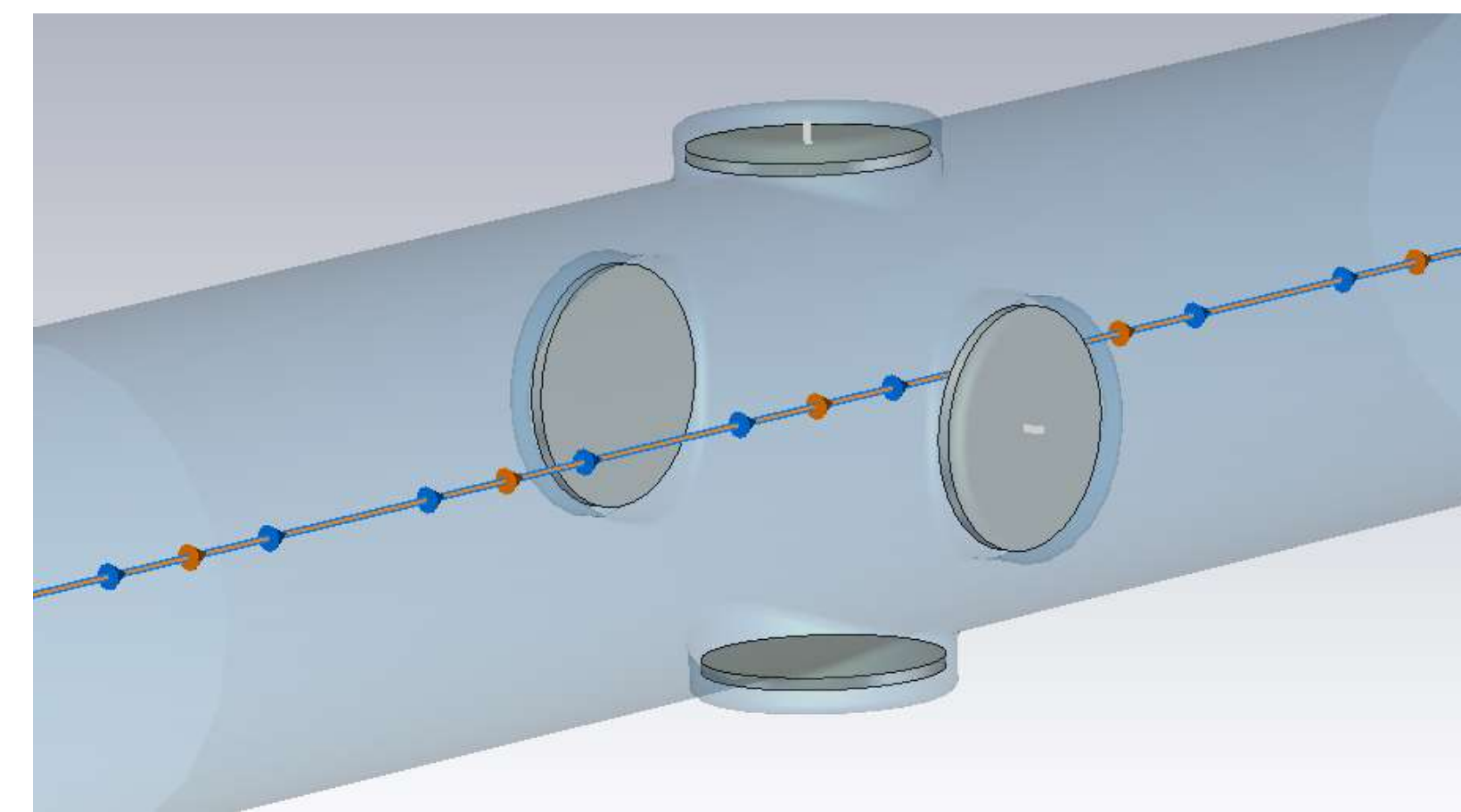
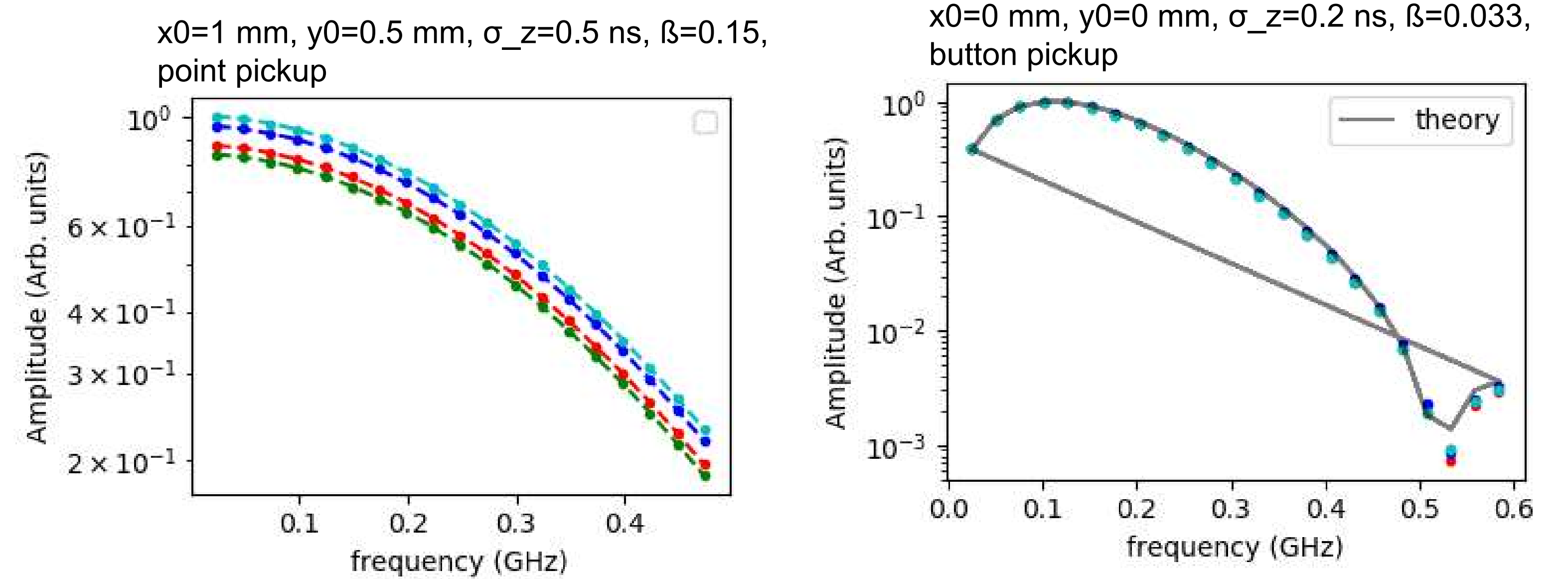
## Button Sum Scaling

- By adding the button signals, the measurements are less dependent of the transverse distribution
  - Offsetting a pencil beam 1.5 mm deviates by ~6% from centered case. For a single button the deviation is ~50%
- But, the beam position and transverse sizes cannot be uniquely determined with this method



## Simulations

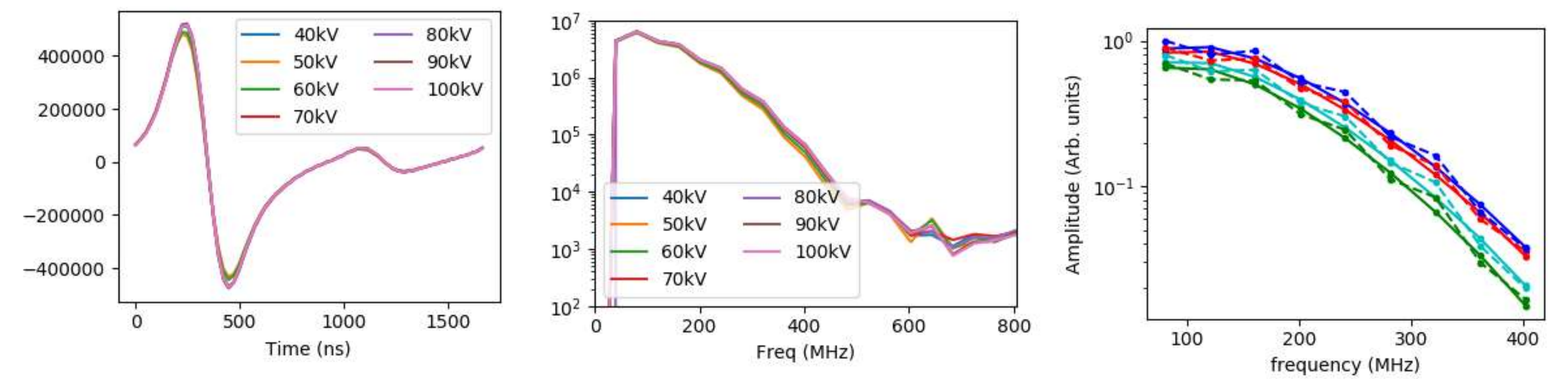
- CST Studio simulations confirm the analytic field distribution at the pipe wall
  - Simulated pencil beam and uniform beam distributions for different offsets, beam sizes, and velocities
  - Measured field at points on wall and with a BPM model



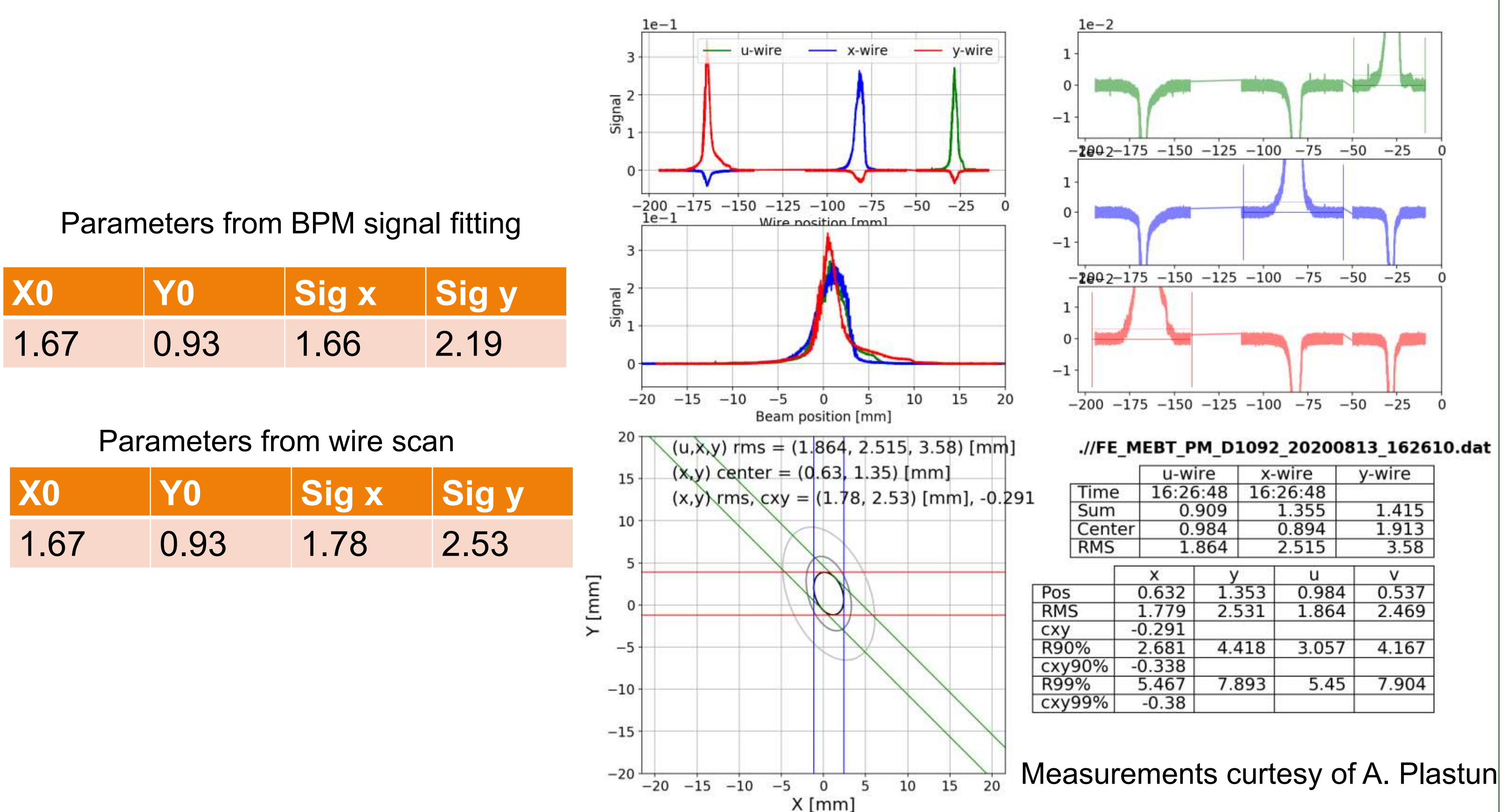
BPM model with pencil beam

## FRIB MEBT Measurements

- Fit the field equation with TTF to measured signals using seven fit parameters
  - Fit parameters: amplitude, noise offset,  $x_0$ ,  $y_0$ ,  $\sigma_x$ ,  $\sigma_y$ ,  $\sigma_z$



- Fitting the parameters needs improvements
  - The transverse position and beam size match measurements from the BPMs and wire profile scanner
  - Longitudinal beam size from fitting fails to follow trend of simulation when scanning the voltage of a buncher cavity



Measurements courtesy of A. Plastun

Bunch length at BPM3, Buncher scan

