

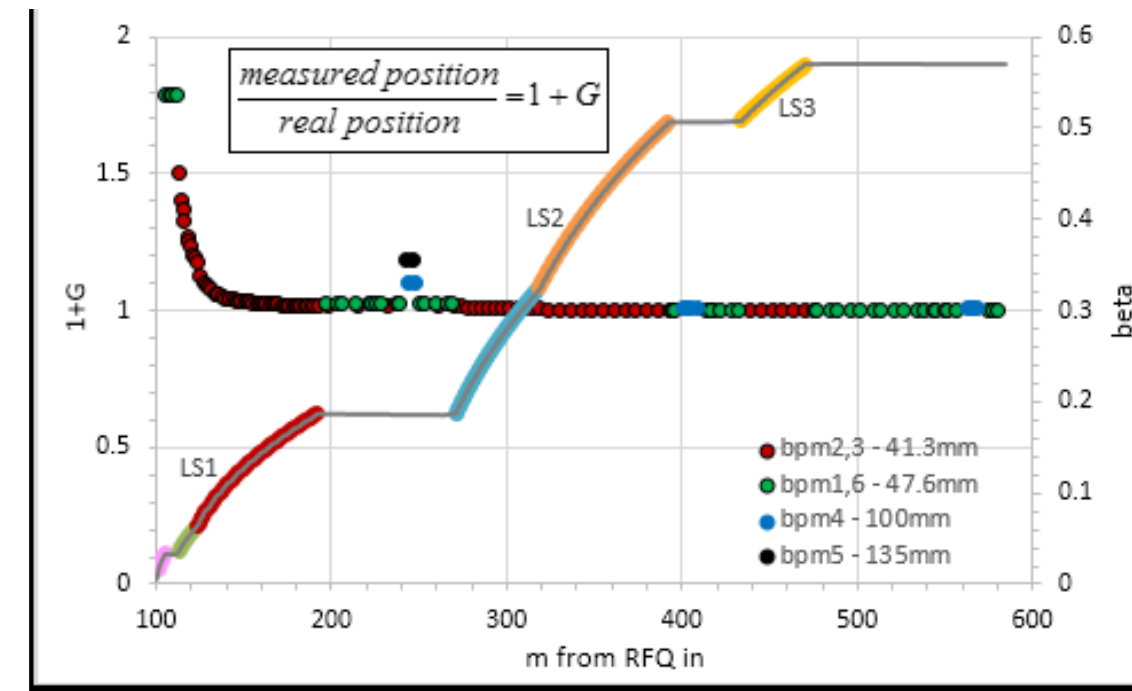
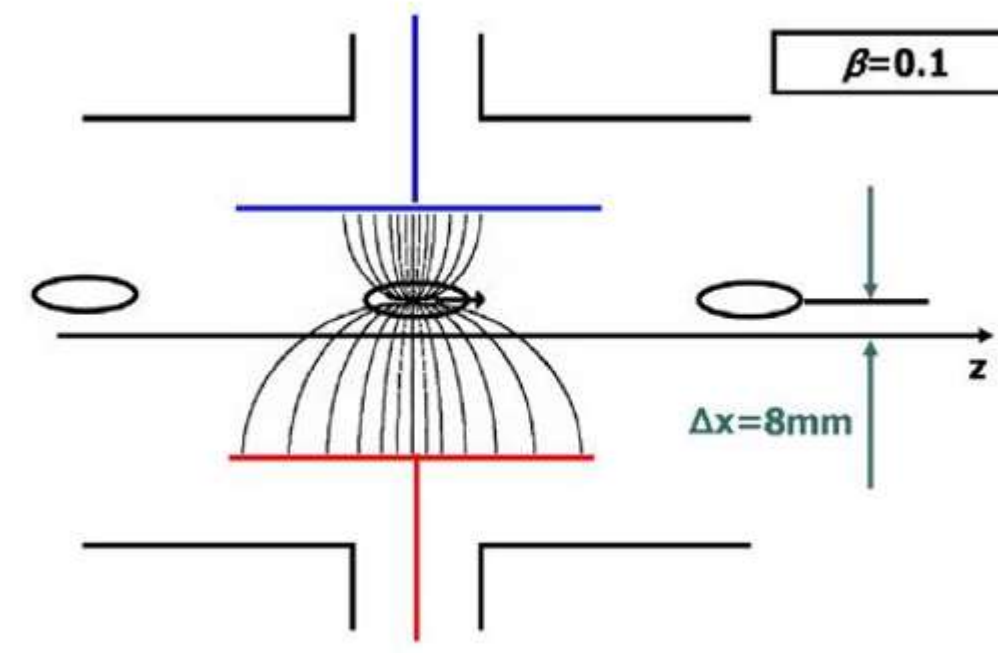
# BPM Low $\beta$ Calibration Test Stand

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If you wish to discuss,  
I will be at TUPP20

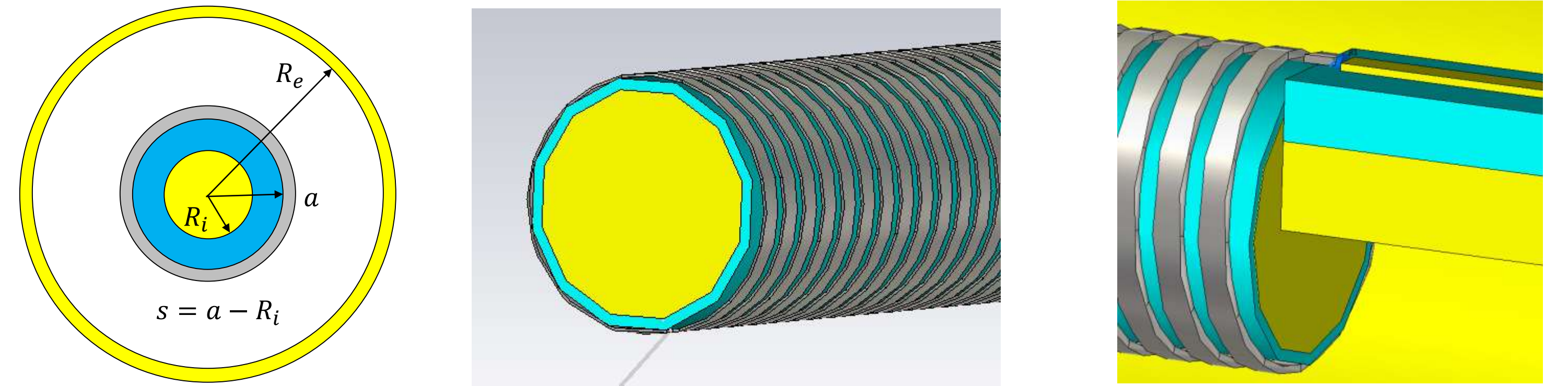
## Corrections for capacitive pick-ups for non-relativistic effects

- Non-relativistic beams are not pancaked longitudinally.
  - Standard analysis does not account for non-relativistic effects to simplify results.
  - The different field extents affect the measurements
- Corrections for non-relativistic effects
  - Analytic:  $x \propto \frac{1}{1+G} \frac{\Delta}{\Sigma}$ ,  $G = \frac{g I_0(g)}{2 I_1(g)}$ ,  $g = \frac{\omega D}{\beta \gamma c}$
  - Simulation: simulate response of device to non-relativistic beams
- Want benchtop test stand for measuring effects
  - Test stand must replicate field profile and velocity of beam
- Helical transmission lines can be used
  - They propagate pulses at low phase velocities



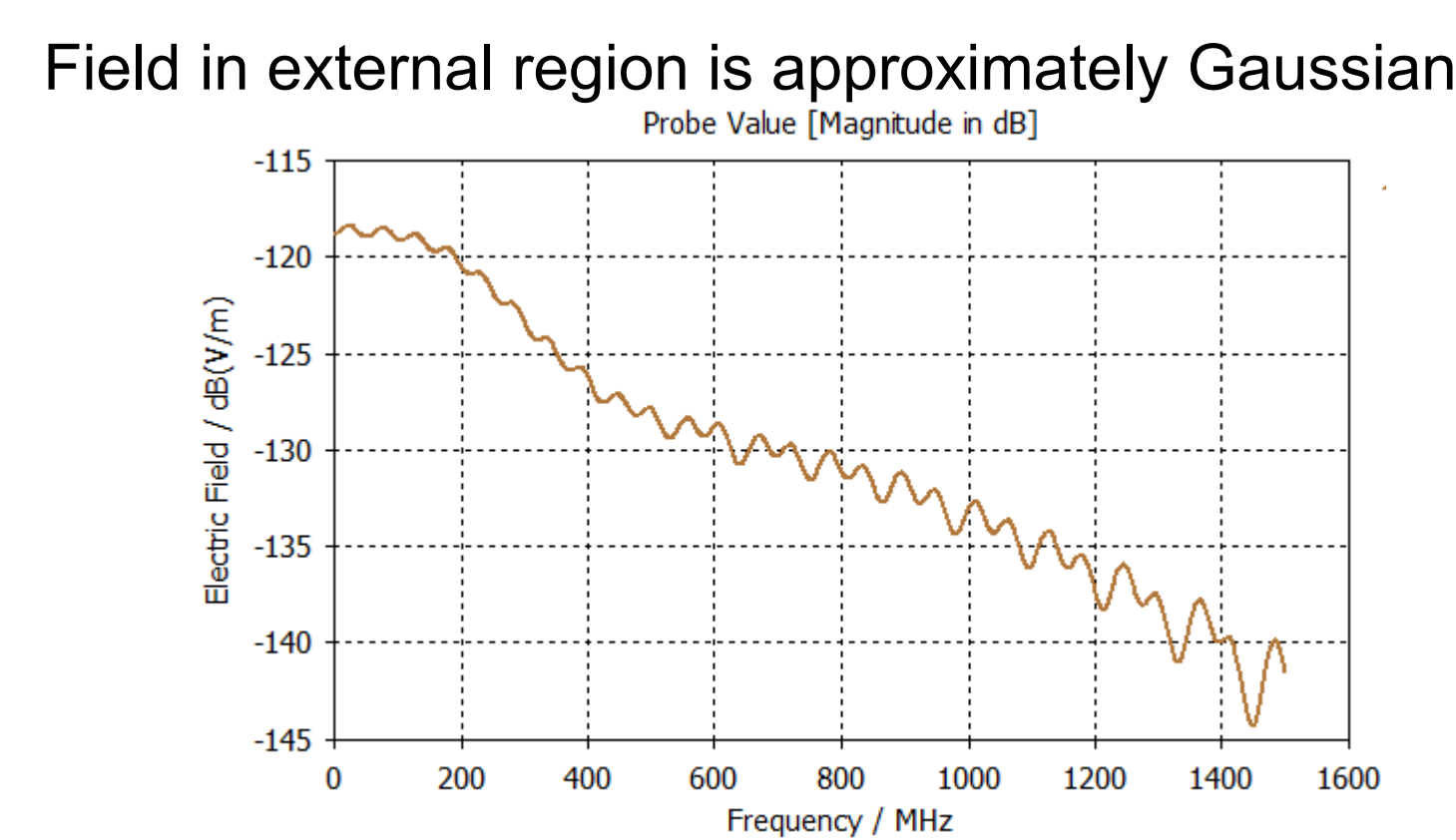
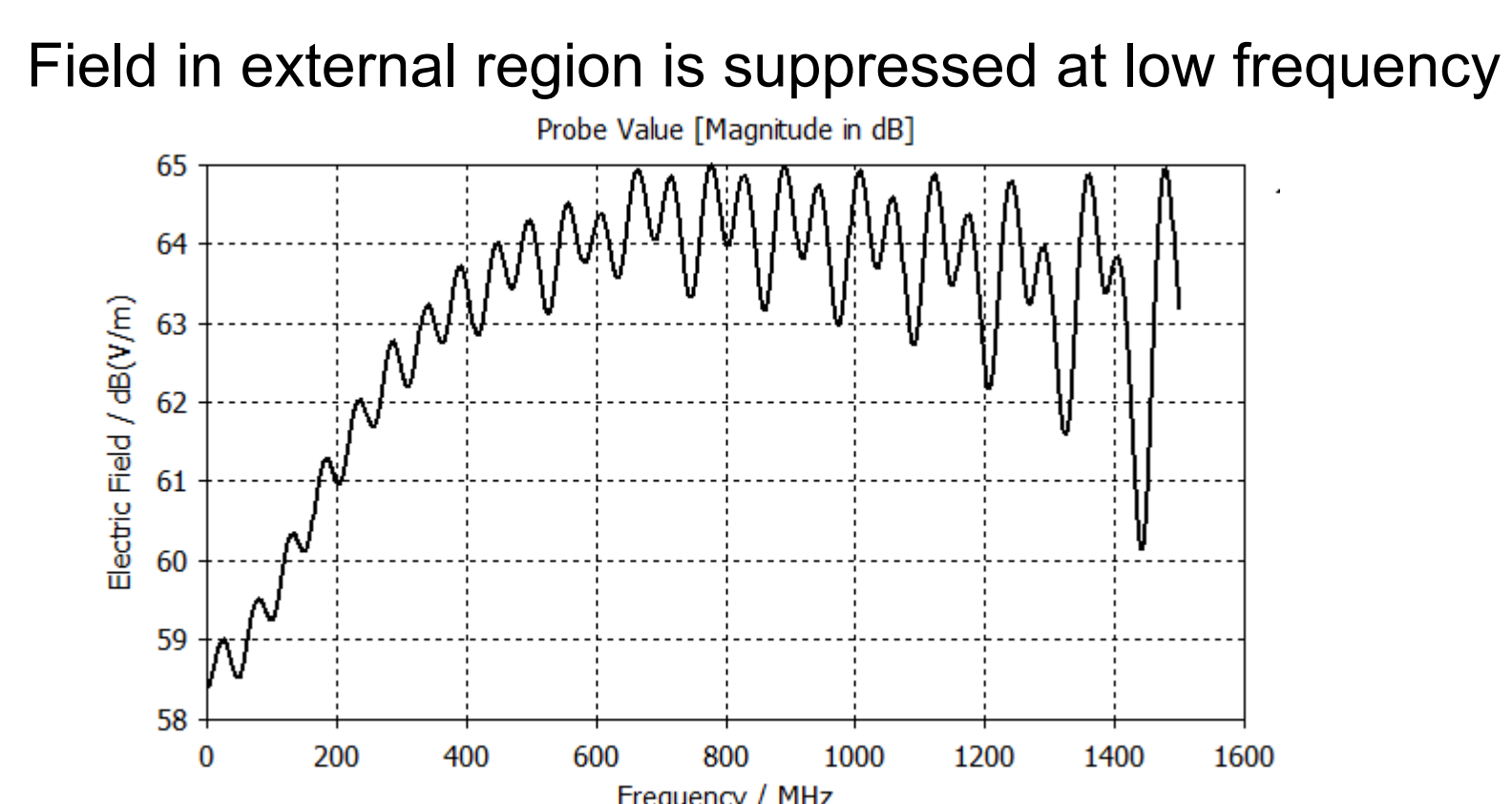
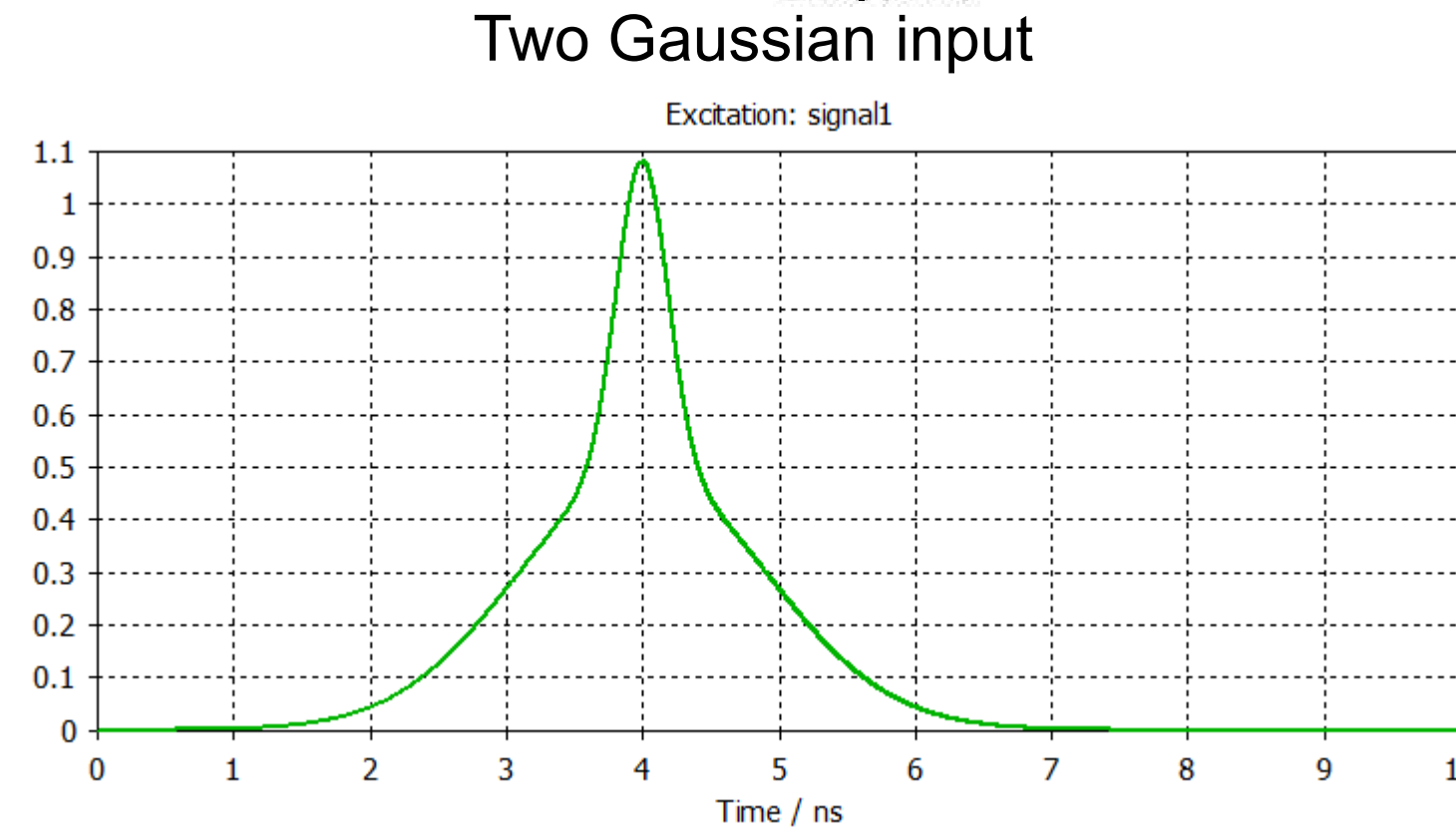
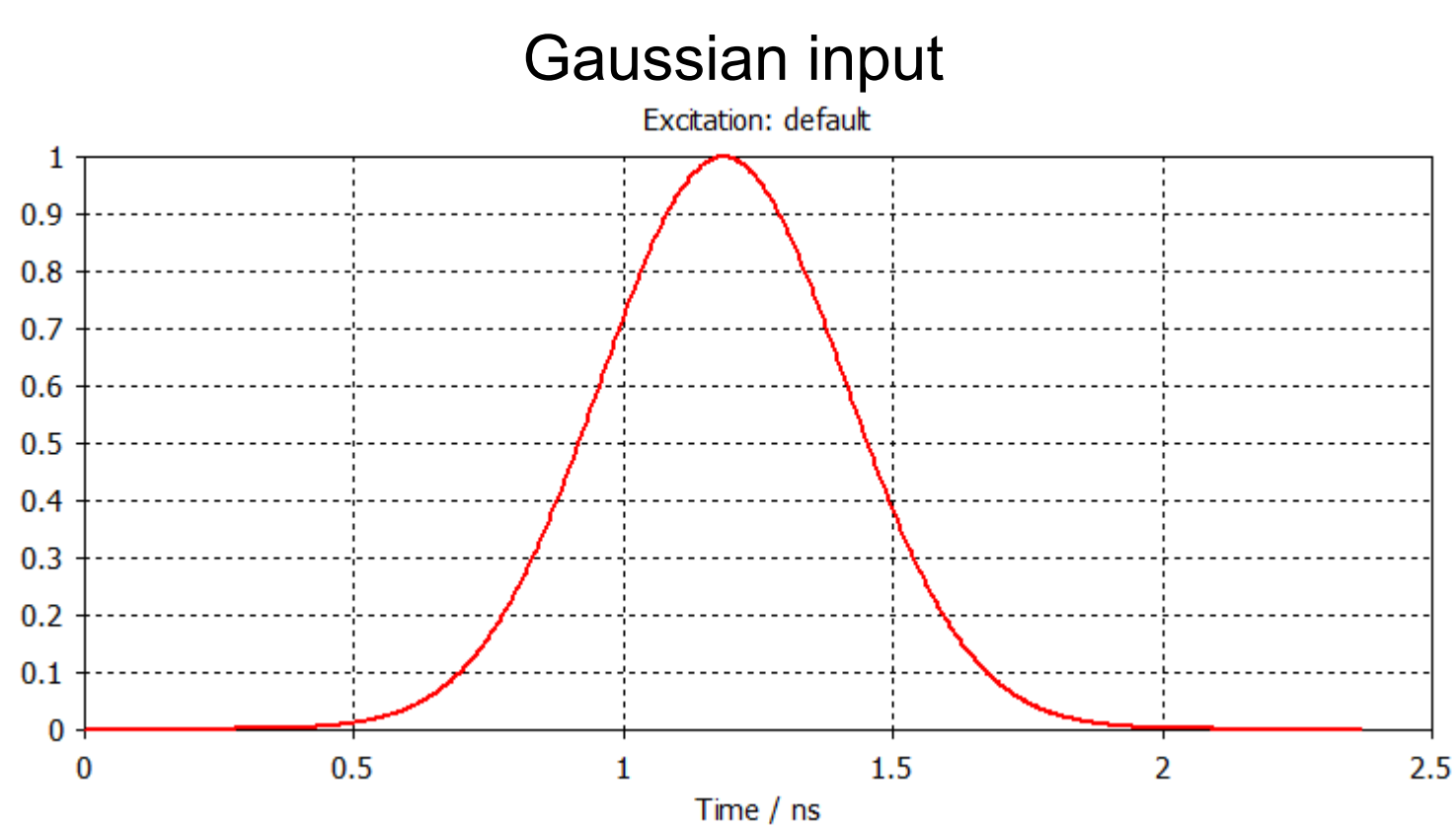
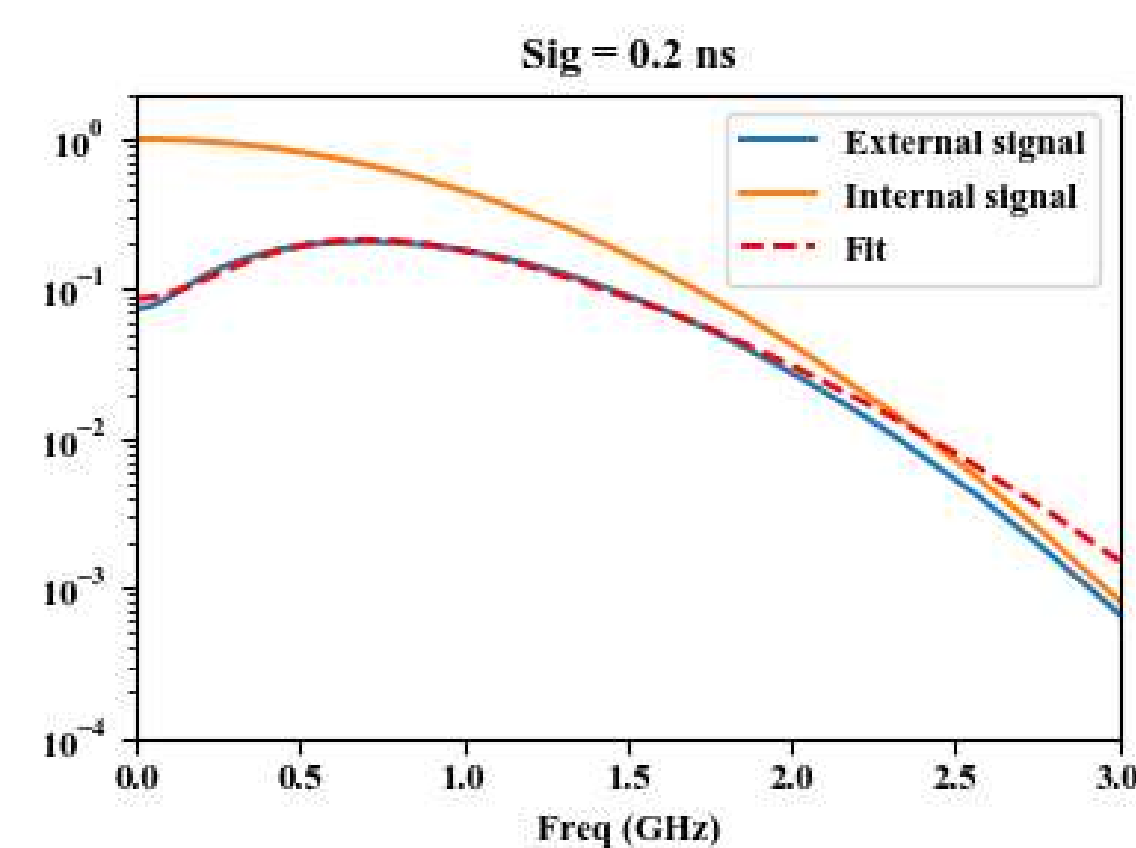
## Geometry

- The helix has pitch angle  $\psi$  and radius  $a$ . In simulations it has thickness  $\Delta a$
- Centered in the helix is a conducting rod of radius  $R_i$
- The inner conductor is covered in a dielectric of thickness  $s = a - R_i$  and dielectric constant  $\epsilon_r$ . This supports the helix
- The helix is inside a pipe with radius  $R_e$
- The signal is input into the internal region using a microstrip with the same impedance as the helix



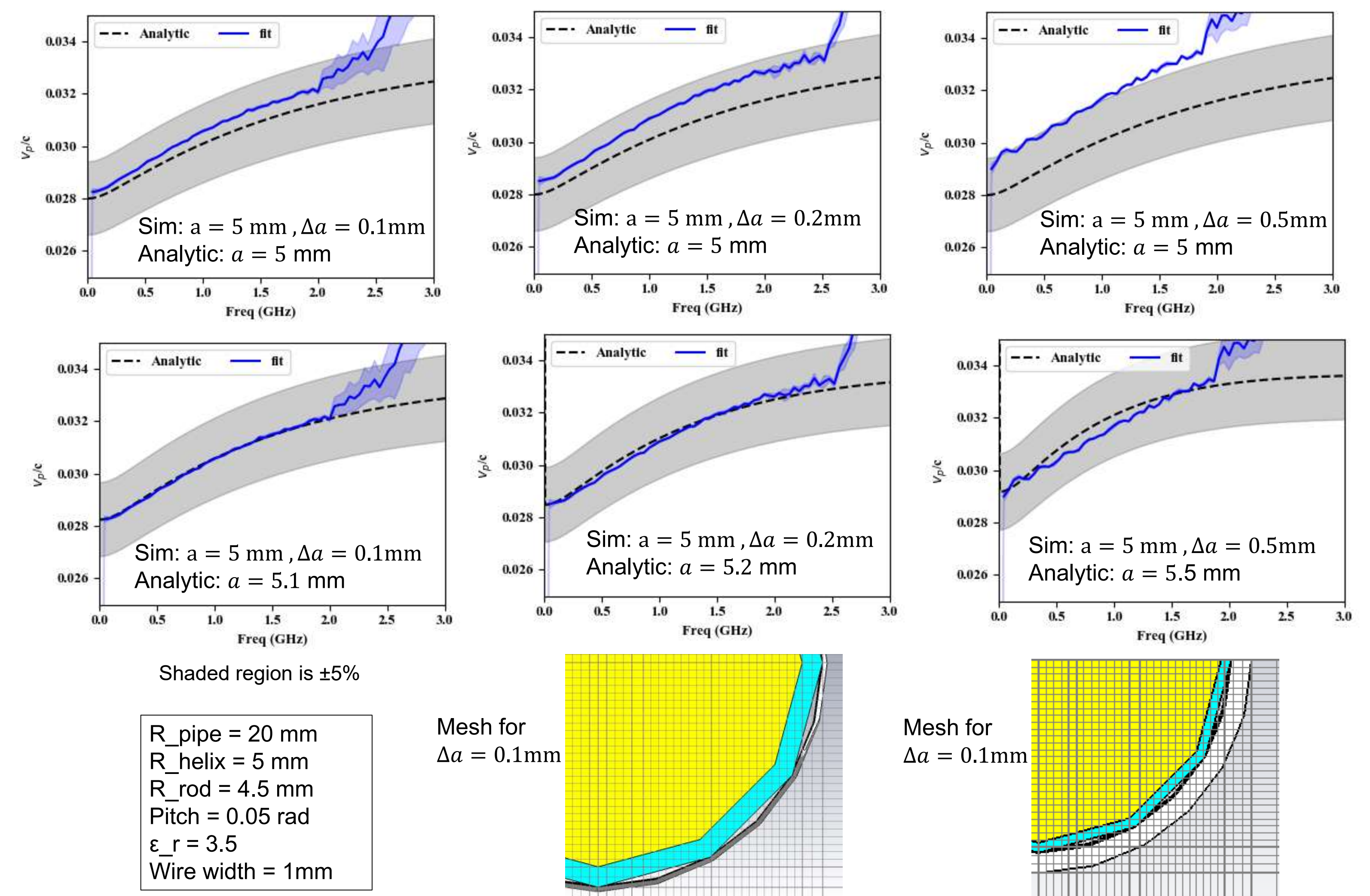
## Internal-External Coupling

- Signal is input into internal region, need field in external region to replicate a beam
  - The coupling suppresses low frequency components
- The signals are input in the internal region, therefore the input signal must be tailored to correct for this effect
  - The sum of two Gaussians can be used to approximate a Gaussian pulse in the external region



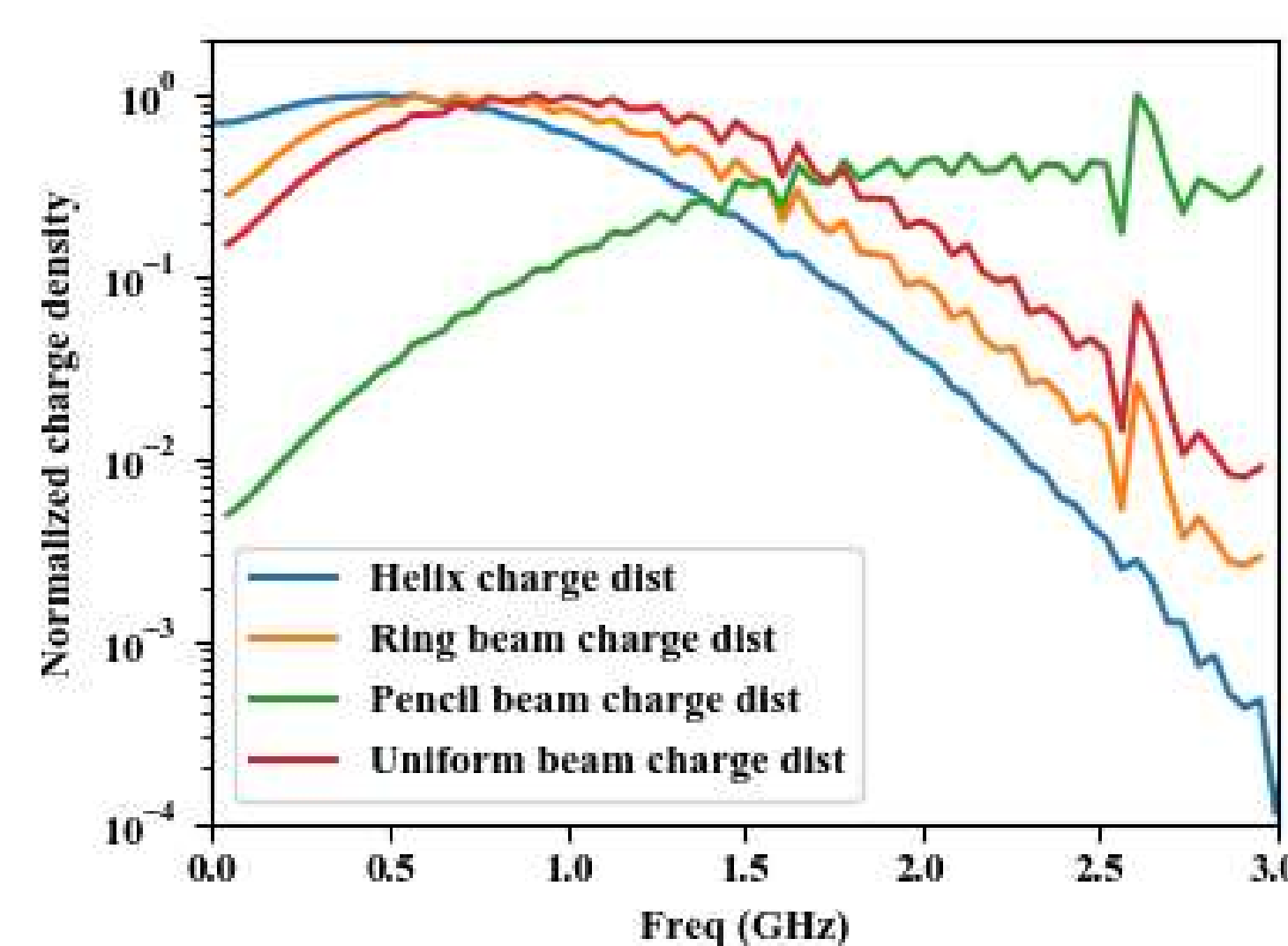
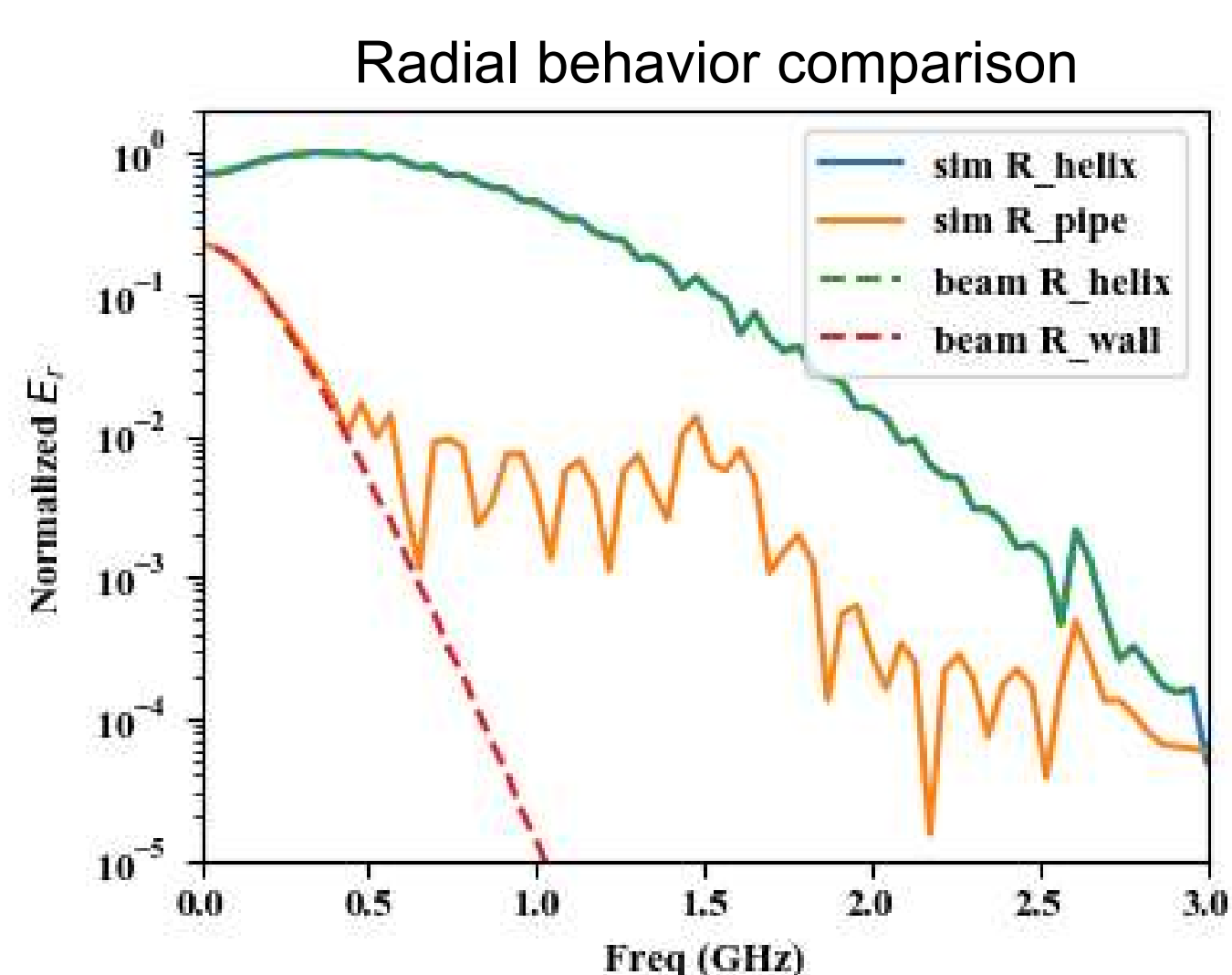
## Phase velocity

- The helical transmission line can theoretically support arbitrarily low phase velocities to match the velocities of non-relativistic beams
  - Simulations with the given parameters have  $v_p \approx 0.03c$  which is sufficiently low for the FRIB MEBT with beam velocity  $v_b = 0.032c$
- The phase velocity in simulations agree well with analytic results
  - However, better agreement can be achieved by assuming  $a \rightarrow a + \Delta a$  in the analytic solution. This works for a range of  $\Delta a$ . Currently, this phenomenon is not understood



## Beam Comparison

- An analytic beam profile was made to exactly match the electric field at the helix
  - The field from the beam at the pipe wall matches the helix simulations until the signal becomes noisy
- Different transverse profiles of the analytic beam were matched the helix field
  - The helix charge distribution best represents a ring beam



## Off Center Helices

- The helix needs to be offset to replicate the fields from offset beam.
- In simulations, the helix was offset in a grip up to 10 mm in 2 mm steps
  - No significant changes to dispersion or S11 are seen
  - Therefore no special considerations for the offset need to be made

