Study of Field Ionization in the Charge Exchange Injection for the IPNS Upgrade

Yong-Chul Chae and Yanglai Cho
Argonne National Laboratory, 9700 So. Cass Ave., Argonne, Illinois 60439, U.S.A.

Abstract

The proposed 1-MW neutron spallation source is a rapid-cycling synchrotron (RCS) with a design intensity of $1.04 \times 10^{14}$ protons. A $H^-$ beam from the linac is injected into the synchrotron via the charge exchange process. Due to the high intensity of the beam, the minimization of beam loss is one of the primary concerns. In this paper, we study a possible beam loss associated with $\oplus$eld ionization, which includes estimates of the charge fraction and level distribution of the excited hydrogen atoms after stripping, and an estimate of lifetime of the excited hydrogen atoms in the transverse magnetic $\oplus$eld.

I. Introduction

Minimization of beam losses is one of the major goals at the proposed neutral spallation source at Argonne. Among the various injection-loss mechanisms, the beam loss due to $\oplus$eld ionization has recently received a great deal of attention after Hutson and Macek at Los Alamos reported that the measured 0.2-0.3% of beam loss at the Proton Storage Ring (PSR) [1] was attributed to $\oplus$eld ionization of the $n \geq 3$ excited hydrogen atoms in the 1.2-Tesla bending magnet located downstream of the stripping foil.

If the foil strips the electrons of injected $H^-$ ions completely, we will not have the $\oplus$eld-ionization loss. However, for a given foil thickness, the stripping efficiency is less than 100% resulting in the fraction of neutral hydrogen in the various excited states. It is these hydrogen atoms that will be ionized in the magnetic $\oplus$eld and, following a wrong orbit, eventually lost.

II. Field ionization

Let's consider an energetic hydrogen atom moving through the uniform magnetic $\oplus$eld $B$ whose direction is normal to the velocity $v$. Magnetic $\oplus$eld in the lab frame is transformed to mostly electric $\oplus$eld in the rest frame according to:

$$F(V/m) = \gamma \beta e B(T),$$

where $\gamma$ and $\beta$ are the usual relativistic quantities, $c$ is the speed of light, $B$ is the magnetic $\oplus$eld in the lab frame, and $F$ is the electric $\oplus$eld in the rest frame. This external electric $\oplus$eld puts the hydrogen atom in Stark states.

The Hamiltonian for the hydrogen atom in a Stark state may be written as

$$H = H_0 + H',$$

$$H_0 = \frac{p^2}{2m} - \frac{e^2}{r},$$

$$H' = -eFz = -eFr \cos \theta,$$

where $eFz$ is the external electric $\oplus$eld in the z-direction. Due to the external $\oplus$eld, the potential well of unperturbed hydrogen atoms is distorted in such a way that the width of the barrier becomes finite, which in turn allows the possibility of ionization via tunneling.

In order to include the effect of ionization in the solution of the Schrödinger equation, Landau [2] introduced the complex energy values de$\ominus$ned as

$$E = E_0 - \frac{i}{2} \Gamma,$$

where $E_0$ and $\Gamma$ are two constants, which are positive. The physical significance of the complex energy can be seen by writing the time factor in the wave function of the form

$$e^{- (i/\hbar) Et} = e^{- (i/\hbar) E_0 t} e^{- (\Gamma/\hbar) t/2}.$$

It can be seen that the probability of finding the electron inside the barrier decreases with time as $e^{- (\Gamma/\hbar) t}$. Thus $\Gamma$ determines the lifetime of the state de$\ominus$ned by $\tau = \hbar/\Gamma$, whose relation satisfies Heisenberg's uncertainty relation. If we measure the energy state, the spectrum will be centered at $E_0$ with width $\Gamma$. In the literature $E_0$ is commonly called Stark energy and $\Gamma$ is linewidth (of the spectrum).

Damburg and Kolosov [3] solved Schrödinger equation in the parabolic coordinate system for $E_0$ and $\Gamma$ using the perturbation method. They obtained the series in $F$ for the Stark energy and derived a semiempirical formula for $\Gamma$.

Damburg and Kolosov's formula was used to calculate the Stark energy and the lifetime of hydrogen atoms in excited states

Figure 1

Lifetime of Stark States ($n=5, 6$) of Hydrogen Atom in the Magnetic Field at 400 MeV. (The group of lines represents $n(n+1)/2$ energy states for a given $n$.)
The results for \( n \), the principal quantum number, equal to 5 and 6 are shown in Fig. 1, where the lifetimes of \( n(n + 1)/2 \) energy states for a given \( n \) are plotted as a function of magnetic \( \beta \) eld.

In the calculation, we assumed the injection energy of 400 MeV and considered the magnetic \( \beta \) eld strength up to 0.5 T. However, the ionization lifetime greater than \( 10^{-8} \) sec should be interpreted carefully, for the average radiation transition lifetime of a hydrogen atom is of the order of \( 10^{-8} \) sec or greater for \( n \geq 3 \) [6]

### III. Charge Fraction of \( H^- \) Ions

When \( H^- \) ions traverse a carbon foil, charge exchange processes occur. Assuming that the electron capturing process, governed by the \( E^{-3} \) law, is negligible, there are three important electron loss processes:

(i) \( H^- \rightarrow H^0 \), with cross section \( \sigma_{-10} \),

(ii) \( H^- \rightarrow H^+ \), with cross section \( \sigma_{-11} \),

(iii) \( H^0 \rightarrow H^+ \), with cross section \( \sigma_{01} \).

In terms of these cross sections, the charge fractions can be written as

\[
N_{H^-} = e^{-\sigma_{-10} x},
\]

\[
N_{H^0} = \frac{\sigma_{-11}}{(\sigma_{-11} + \sigma_{-10} - \sigma_{01})} \left[ e^{-\sigma_{01} x} - e^{-(\sigma_{01} x)} \right],
\]

\[
N_{H^+} = 1 - N_{H^-} - N_{H^0},
\]

where \( x \) is the foil thickness (the number of target atoms/cm\(^2\)), and \( N_{H^-} \), \( N_{H^0} \) and \( N_{H^+} \) are the three charge fractions in the beam.

Theoretical calculations for electron loss cross section have been worked out by several authors. One of these theories is due to Gillespie [7]. His results agreed well with the measurements in the wide range of energy including the measurements done at Fermilab with 200-MeV beam and the one at Los Alamos with 800-MeV beam. These measured cross sections are presented in Table 1, which indicates that cross section varies as \( \beta^{-3} \). Gillespie’s theory also shows such a scaling law \(^2\).

<table>
<thead>
<tr>
<th>Foil Thickness (( \mu g/cm^2 ))</th>
<th>( N_{H^-} ) (%)</th>
<th>( N_{H^0} ) (%)</th>
<th>( N_{H^+} ) (%)</th>
</tr>
</thead>
<tbody>
<tr>
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<td>98.3</td>
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<tr>
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<td>0.0002</td>
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<td>0.85</td>
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</tr>
<tr>
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</tr>
<tr>
<td>250</td>
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Table 2

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Figure 2

Charge Fractions vs. Foil Thickness at 400 MeV.

### IV. \( n \)-Distribution

After the foil, the neutral hydrogen atoms are distributed (or populated) in different states. At present no theory exists for excited-state production using the beam-foil method. However, we may mention the atomic-collision theory for radiative capture of free electrons by bare nuclei in the high velocity limit, which shows \( n^{-3} \) dependence on the principal quantum number of the capture cross section [6]. Even if it is not clear whether we can apply this approach to beam-foil interaction, the early measurement results at low energy (less than 1 MeV/au) showed such a dependence on principal quantum number\(^3\). An interesting theoretical analysis [11] of post-foil measurement of electromagnetic radiation and ion charge also suggests that the level populations decrease as \( n^{-3} \) and depend universally on the kinetic energy of the incoming beam. From these early studies we learn [11]:

- dependence of the level population on principal quantum number according to \( n^{-3} \) is observed frequently but not exclu-

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\(^2\)Stopping power of the foil is also governed by the same scaling law, which indicates that the two processes are similar. In fact, both processes are dominated by electron-electron elastic scattering.

\(^3\)J. Davidson [10] used neutral helium at 0.275 MeV in order to measure the absolute population in \( 3 \leq n \leq 6 \) after 6 \( \mu g/cm^2 \) carbon foil.
sively,
- dependence of the level population on foil thickness is unknown,
- dependence of the level population on kinetic energy of the incident beam was not observed.

Since the above studies are not conclusive enough to apply the findings to 400 MeV $^4$H ions passing the carbon foil as proposed for the neutral spallation source at Argonne, we pay attention to the recent experimental study on beam-foil interaction [12]. Assuming that the $n$ distribution is governed by a power law $n^{-p}$, the exponent of the power law $p$ is measured for a given foil at 800 MeV. The results are found to be:

For a given 25.0 $\mu g/cm^2$ carbon foil
\[
\begin{cases}
p = 3.41 & \text{for } n=2,\ldots,5 \\
p = 8.0 & \text{for } n=10,\ldots,14
\end{cases}
\]

For a given 198.0 $\mu g/cm^2$ carbon foil
\[
\begin{cases}
p = 1.29 & \text{for } n=2,\ldots,5 \\
p = 8.0 & \text{for } n=10,\ldots,14
\end{cases}
\]

It is interesting to note that a single power law is unable to characterize the $n$ distribution of excited states over a wide range of $n$ and the low-lying states become more evenly populated for the thicker foils.

**Application**

The injection orbit in the IPNS-Upgrade RCS [13] is shown in Fig. 3. With a 250-$\mu g/cm^2$ stripper foil, about 0.54% of the $^4$H beam emerges from the foil as partially stripped neutral hydrogen atoms, some of which are in the ground state and some of which are in excited states. If these particles are allowed to enter a normal bending magnet $\Theta$eld, they will become stripped and either hit the vacuum chamber wall or, if not lost, form a halo of large betatron oscillation around the normal proton beam.

Figure 3 shows that the neutrals pass through the center of one quadrupole (QD) and enter the next quadrupole (QF) at -11 cm, where the $\Theta$eld is 0.3 T, unless the $H^+$-catcher is installed. This $\Theta$eld over a length of 0.5 m is enough to strip all electrons with $n > 5$, or about 20% of the $H^+$ beam. In this estimation, we assumed that $n$-distribution follows $n^{-p}$ dependence, and, since the foil thickness is 250 $\mu g/cm^2$, we used $p = 1.29$ for the conservative estimate. The catcher, therefore, is placed upstream of this quadrupole (QF) as shown in Fig. 3.

The relatively short bumper magnets, B3 and B4 shown in Fig. 3, can also ionize the $H^+$ beam. However, the beam loss due to the $\Theta$eld ionization in these bumper magnets is negligible.

**Conclusion**

In order to minimize the beam loss in the proposed IPNS-Upgrade RCS due to $\Theta$eld ionization, we propose to use the relatively thick stripper foil with thickness of 250 $\mu g/cm^2$ and to install a $H^+$-catcher in the ring together with the careful trajectory control of the neutral hydrogen atoms.

**References**