MITIGATION OF POWER LOSS DUE TO SKIN EFFECT BY THIN-LAYERED FILM*

Y. Iwashita, Kyoto University, Uji, Kyoto, JAPAN

Abstract

By investigating the skin effect on a metal film that is thinner than a skin depth, it was found that such a power loss can be mitigated by thin films with appropriate geometry. An experimental result on the reduction of the skin effect power loss with layered conductor films is reported and discussed.

INTRODUCTION

The AC current flows only on the metal surface, which is known as skin effect. The current concentration on the surface increases power loss. The skin effect on RF current is a main component of the transmission loss of cables or Q value in cavities. Reductions of power loss caused by the skin effect have been reported [1,2] in these years. The procedures, however, have some restrictions such as a narrow range of permittivity of insulation layer materials, in applying general RF objects. With a careful investigation, one simple method was found to be able to widen the application area. This paper presents a short review on the skin effect theory, and describes the new idea followed by an experimental result.

BRIEF REVIEW ON SKIN EFFECT

Let us consider a simple example as shown in Figure 1, where two layers of thin foils with thickness of just the skin depth $\delta$ are immersed in equally stepped RF fields. The total current in each layer is just the magnetic field difference between the front and backsides: the net currents of both the layers are the same. The total power loss is calculated as follows:

$$P_2 = \int_0^\delta \left( |j_1|^2 + |j_2|^2 \right) \sigma \, dx,$$

(1)

which shows 30% reduction from the bulk case. The effect can be enhanced when the number of layers is increased. The thicknesses that show minimum power loss decrease as the numbers of layers increase and shows $n^{0.5}$ dependence. Therefore, the RF power loss may be reduced by this geometry, if the current on each layer is well controlled. Figure 2 shows an example of the geometry to reduce the power loss for a dielectric resonator. Q enhancement factor for this dielectric cylindrical cavity is predicted to be up to 1.4 when $r_1$ and $r_2$ are optimized.

An important assumption in this configuration was that the permittivity of the inter layer dielectric material $\varepsilon_a$ is much lower than that of the resonator body $\varepsilon_b$. Since the distance $r_2 - r_1$ is the order of $\lambda/2$ in the resonator body, the inter layer spaces draw significant RF energy, otherwise. Figure 3 shows the Q enhancement factor as a function of $\varepsilon_a/\varepsilon_b$, which was obtained from axisymmetric calculation code. The Q enhancement is available only when a following condition is satisfied: $\varepsilon_a/\varepsilon_b \ll 0.5$. The ratio $\varepsilon_a/\varepsilon_b$ is desired to be less than 0.3 in this case. This condition is difficult to achieve when a resonator body is already a vacuum. Because the conductor films have to be supported by dielectric materials to make good insulation between layers, the situation becomes worse for such vacuum cavities. If there were such material, one could make a high Q accelerating cavity as shown in Figure 4.

In other words, an important restriction in applying this configuration to real RF objects is that the inter-layer space should not take extra energy with close resonance state even if the length is comparable to $\lambda/2$. 
LOCAL RESONANCE CONTROL

Figure 5(left) shows the schematic picture of such a local resonance model. This structure acts as a $\frac{\lambda}{2}$ mode resonator when a condition meets; electric and magnetic field distributions have a node and an antinode at the center, respectively. This can be described by an equivalent circuit model as shown in Figure 5(right). The local resonant frequency can be raised by reducing $L$ and/or $C$ as shown in Figure 6: to widen the gap at the edge areas and narrow the gap at the center area. Because these gap widths should be much smaller than the film length, the effect can be described by the gap stepping ratio $d_2/d_1$.

The effect of such an operation is evaluated by SUPERFISH calculations as a boundary condition problem as shown in Figure 7. The factor of the raised frequency is shown in Figure 8 as a function of the gap ratio $d_2/d_1$. Considering the resonator with the large gap ratio as two separate resonators (each of the length becomes a half), a large limiting value of the factor should be 2. This effect is equivalent to using a dielectric material with permittivity of 0.25. A practical limit of the frequency factor may be 1.8 since hundred times of 1$\mu$m narrower gap width is already 0.1mm and the slope is rather flat at the higher domain in Figure 8. This value corresponds to the permittivity of 0.3, which reaches the value stated above.

MEASUREMENT ON COAXIAL CAVITY

The effect was experimentally tested on a coaxial cavity, because it has a simple electromagnetic field distribution (see Figure 9). A thin film (5$\mu$m copper layer on 25$\mu$m polyimide [3]) was put on the inner conductor with its polyimide side down to form an insulation layer. Because the film has to be located at the high magnetic field region, the resonant mode for the measurement was the second lowest mode that has an antinode of its magnetic field at the center; other antinode regions are located at the ends and are difficult to put the films. The film locally covers the center inner region and the $Q$ values were measured while changing the length by cutting from its edges step by step. The length of the film can control the total current on the film that goes in and out as a displacement current.

The cavity has length of 2m to have its second lowest frequency 150MHz ($\lambda$=2m). The skin depth of the copper conductor at this frequency is 5.4$\mu$m. 80cm of the center region is initially wrapped around where the film was put directly on the inner most 30cm region while the outer areas have spacer layers by putting polyethylene meshes with 300$\mu$m thickness (see Figure 11). The $Q$-value was measured while the edges of the film were shortened. The measured result is shown in Figure 12. The ordinate shows a ratio $Q/Q_0$, where $Q_0$ is the measured $Q$-value when all the film was removed lastly. The abscissa shows a relative length of the covered length by film to $\lambda/2$. Because the observed frequency change was less than $10^{-3}$ and the volume under the conductor foil is very small.
compared with the cavity body, the electromagnetic field distribution should not have changed very much. The value of more than unity shows that the real power loss reduction was achieved with this scheme. The calculations were based on a configuration shown in Figure 13. In order to reduce the computation resources, the total system was scaled to 3GHz and the relative permittivity was set as $10^4$ instead of 1. The power losses in conductors are included by assigning complex permittivity. The value was chosen as $(1, 0.35 \times 10^9)$ considering following equation:

$$\text{rot} \mathbf{H} = \mathbf{D} + \sigma \mathbf{E} = (j \omega \varepsilon_0 \mathbf{E} + \sigma) \mathbf{E} = j \omega \varepsilon_0 \left( \varepsilon + \frac{\sigma}{j \omega \varepsilon_0} \right) \mathbf{E}$$

and $\varepsilon' = \sigma / j \omega \varepsilon_0$. Because the calculation only included power losses on the inner conductor and the conductor foil, the relative calculated values $Q/Q_0$ were compensated by following factors:
1) the outer conductor had 2.5 time larger radius than that of inner one, which gives factor 1.4 for total power loss.
2) it did not include the right most quarter area where the film was not put; this gives another factor 2.
Thus the differences were supposed to be diluted with this factor, which is denoted in the legend of the figure. Although the power losses at the endplate were not counted in this calculation, the results agreed with the measured data, considering the difficulty in setting the film on the inner conductor with the polyethylene mesh.

**DISCUSSIONS**

As one can already imagine, the stepped foil configuration can also be applied to a dielectric cavity with uniform permittivity (see Figure 14). Figure 15 shows the calculated enhancement factors of the Q-value, where the stepping ratio $d_2/d_1 = 8$. It also shows the case with no step while the permittivity of the spacer layer is set much smaller ($10^{-4}$) than that of resonator body. The effect of the step is close to use of the low permittivity material in this case. Although only the first quadrant is calculated using the symmetries, the values directly reflect the real case. The Q-value enhancement is also expected in this example. Because this resonator needs high permittivity and low loss dielectric material for its body, which is not easy, the experimental proof is a future subject.

Reducing RF losses of waveguide and accelerating cavity are one of the final goals of this study. Although the restriction on the permittivity can be reduced, only the stepping configuration is not enough to achieve the enhancement yet, because these RF objects have longer wall distances compared with the wavelength (see Figure 16). More sophisticated idea is needed for these kind of RF objects.

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**REFERENCES**